EGR 103L - Fall 2016

Laboratory 4 - Loops and Plots

CEMAL YAGCIOGLU (cy111) Lab Section EGR 103L9-05, WEDNESDAY 11.45 PM - 2.35 AM 2 OCTOBER, 2016

I understand and have adhered to all the tenets of the Duke Community Standard in completing every part of this assignment. I understand that a violation of any part of the Standard on any part of this assignment can result in failure of this assignment, failure of this course, and/or suspension from Duke University.

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1 Palm Figure 6.1-2

I gave x equally spaced values between 0 and 4 by using linspace code. Then I graphed [2, p. 265];

$$y = x^m \tag{1}$$

for different values of m(-0.5,0,0.5,1,2). I labeled each curve for different values of m with the m value, and gave title to the plot.

2 Chapra Problem 3.5

For the Chapra Problem 3.5, my program worked with different values of angle. With increasing number of N(number of steps used in Taylor Series), the accuracy for the given angle increased. On the other hand, with increasing angles, the accuracy of approximations decreased meaning the error increased. Even if the angles are actually are same, meaning two pi subtracted from the angle is same, bigger corresponding angle gave a higher error.

3 Chapra Problem 4.1

Table of Maclaurin series [1, p. 120] is;

$\begin{array}{c ccccccccccccccccccccccccccccccccccc$							
16 1e-02 12 4.000000000000051e+00 1.59e-05 7 16 1e-08 5 4.002257524798522e+00 3.36e+00 5 16 1e-08 12 4.00000000000000000e+00 1.27e-12 8 160 1e-02 5 1.482664109800340e+01 5.22e+01 5 160 1e-02 12 1.264911068004731e+01 7.89e-03 8 160 1e-08 5 1.482664109800340e+01 5.22e+01 5 160 1e-08 5 1.482664109800340e+01 5.22e+01 5 160 1e-08 5 1.264911064067352e+01 0.00e+00 10 1600 1e-08 12 1.052575377021292e+02 9.25e+01 5 1600 1e-02 12 4.00000000000000000e+01 1.52e-09 11 1600 1e-08 5 1.052575377021292e+02 9.25e+01 5 1600 1e-08 5 1.052575377021292e+02 9.25e+01 5 1600 1e-08 5 1.05264911064067374e+03 9.92e+01 5 <t< th=""><th></th><th>a</th><th>ϵ_s</th><th>maxit</th><th>\sqrt{a}</th><th>ϵ_a</th><th>iter</th></t<>		a	ϵ_s	maxit	\sqrt{a}	ϵ_a	iter
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16 1e-08 12 4.0000000000000000e+00 1.27e-12 8 160 1e-02 5 1.482664109800340e+01 5.22e+01 5 160 1e-02 12 1.264911068004731e+01 7.89e-03 8 160 1e-08 5 1.482664109800340e+01 5.22e+01 5 160 1e-08 12 1.264911064067352e+01 0.00e+00 10 1600 1e-02 5 1.052575377021292e+02 9.25e+01 5 1600 1e-02 12 4.000000000006651e+01 5.51e-04 10 1600 1e-08 5 1.052575377021292e+02 9.25e+01 5 1600 1e-08 5 1.052575377021292e+02 9.25e+01 5 1600 1e-08 5 1.052575377021292e+02 9.25e+01 5 1600 1e-08 5 1.0536930179416e+03 9.92e+01 5 16000 1e-02 5 1.005306930179416e+03 9.92e+01 5 16000		16	1e-02	12	4.00000000000051e+00	1.59e-05	7
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		160000	1e-02	12	4.000285706905372e+02	1.20e+00	12
160000 1e-08 12 4.000285706905372e+02 1.20e+00 12		160000	1e-08	5	1.000531194227066e+04	9.99e+01	5
		160000	1e-08	12	4.000285706905372e+02	1.20e+00	12

The quality of approximations increases as the iteration number increase. For the given iteration number, smaller values of a have higher quality of approximations. This can also be observed from increasing number of iterations as a increases. While for small values of a expected accuracy can be reached before iterations have reached to their maximum value, for higher values of a iterations reaches the maxvalue before they can reach to expected accuracy.

4 3D Projections

The figure and codes are in the appropriate appendices.

5 Data Logger

The diary, data file, and code are in the appropriate appendices.

A Codes

A.1 ExponentialsGraph.m

```
%[ExponentialsGraph.m]
 2
    %[Cemal Yagcioglu]
    %[October 2,2016]-
   % I have adhered to all the tenets of the
    % Duke Community Standard in creating this code.
   % Signed: [cy111]
7
    x = linspace(0,4);
8
    for m=[-0.5,0,0.5,1,2]
9
10
         axis([0,4,0,4])
11
         hold on
12
         y=x.^m;
13
         xticks([0 0.5 1 1.5 2 2.5 3 3.5 4])
14
         plot(x,y,'k')
15
16
17
    end
    hold off
18
    text(2.75,0.4,'\tmathbb{m} = -0.5')
19
     text(3.38,1.2,'\t m} = 0')
20
     text(3.3,2.1,'\t\{m\} = 0.5')
21
22
     text(2.75,3.2,'\t\{m\} = 1')
23
     text(1.5,3.25,'\t m} = 2')
24
     xlabel('\it{x}')
25
     ylabel('\it{y}')
26
     title('The Power Function \it{y = x^m} (cy111)')
27
28
     print -depsc ThePowerFunctionPlot
29
```

A.2 CosSeries.m

```
%[CosSeries.m]
 1
    %[Cemal Yagcioglu]
    %[October 2,2016]
    \% I have adhered to all the tenets of the
    % Duke Community Standard in creating this code.
5
    % Signed: [cy111]
6
7
    function [CosineApprox,Error] = CosSeries(x,N)
9
    CosineApprox(1) = 1
10
    for k=2:N %1 is defined, starting from 2
         CosineApprox(k) = CosineApprox(k-1) + (x.^{(2.*(k-1)).*((-1).^(k+1))./factorial(2.*(k-1)))}
11
12
    end
13
    CosineApprox(1)=1;
14
    Error=(((cos(x)-CosineApprox)./cos(x)).*100) %calculates error percent
15
    end
16
```

A.3 DivAvg.m

```
function [fx, ea, iter] = DivAvg(a, es, maxit)
```

```
\% DivAvg Use Divide and Average to find square root
3
        [fx, ea, iter] = DivAvg(a, es, maxit)
4
          a: number of which to take the square root
5
   %
          es: stopping error
6
          maxit: maximum number of iterations
7
          fx: approximation of square root of a
          ea: approximate relative error (%)
9
           iter: number of iterations
    % Based on IterMeth.m from Figure 4.2 on p. 94 of
    \% Applied Numerical Methods with MATLAB for
11
    % Scientists and Engineers
    % Steven C. Chapra, 3rd Edition
13
14
15
    %[DivAvg.m]
    %[Cemal Yagcioglu]
16
    %[October 2,2016]
17
    % I have adhered to all the tenets of the
18
    % Duke Community Standard in creating this code.
    % Signed: [cy111]
20
21
    %% defaults:
22
23
    if nargin<2||isempty(es),es=0.0001;end
24
    if nargin<3||isempty(maxit),maxit=50;end
25
    %% initialization
26
    iter = 1; sol = 1; ea = 100;
27
    %% iterative calculation
28
    while (1)
29
    solold = sol;
    sol = (sol + a./(sol))/(2);
31
    iter = iter + 1;
32
    if sol~=0
33
    ea=abs((sol - solold)/sol)*100; end
34
    if ea<=es || iter>=maxit,break,end
35
36
    fx = sol;
37
38
39
40
41
42
43
44
45
46
    end
```

A.4 ThreeDProjections.m

```
%[ThreeDProjections.m]
%[Cemal Yagcioglu]
%[October 2,2016]
% I have adhered to all the tenets of the
% Duke Community Standard in creating this code.
% Signed: [cy111]
t = linspace(-10,10,1000);
```

```
x = ((10.*exp(-0.5.*t)).*sin(3.*t+2));
 9
10
    y = (7.*exp(-0.4.*t)).*cos(5.*t-3);
11
    x=t.*cos(t)
    %y=t.*sin(t)
12
    z = ((8.*t./5)-8);
13
14
15
    subplot(2,2,1)
16
    plot(x,y)
17
18
    axis equal;
    axis([-10,10,-10,10])
19
20
    grid on
21
    xlabel('x')
22
    ylabel('y')
23
24
    subplot(2,2,2)
25
    plot3(x,y,z)
26
    axis equal;
27
    axis([-10,10,-10,10,-10,10])
    view(45, 35)
29
    grid on
    xlabel('x')
31
    ylabel('y')
32
    zlabel('z')
    title('Parametric Plots (cy111)')
33
    hold off
35
36
    subplot(2,2,3)
37
    plot(x,z)
    axis equal;
39
    axis([-10,10,-10,10])
40
    grid on
41
    ylabel('z')
42
    xlabel('x')
43
44
45
    subplot(2,2,4)
    plot(y,z)
46
47
    axis equal;
48
    axis([-10,10,-10,10])
49
    grid on
    ylabel('y')
50
51
    xlabel('z')
52
    print -deps ParametricPlots
```

A.5 DataLogger.m

```
1
2
      %delete('MyTemps.tex')
   Temp = [];
3
4
   i=1;
   Max=0;
5
   Min=999999;
7
   AvTemp=0;
   while i<99999999
```

```
9
         FID = fopen('MyTemps.txt', 'w');
10
         TempInput2 ='%4.2f';
11
         fprintf(FID,TempInput2,Temp);
12
         Temp(i) = input('Enter a Temperature: ');
         T=Temp(i);
13
14
         if T >= 0
15
         OldTemp = Temp;
16
         AvTemp = ((AvTemp*(i-1))+T)/(i);
17
         if T > Max
18
             Max = T;
19
         end
20
         if T < Min
21
             Min = T;
22
         end
    TempInput ='Enter a Temperature: %4.2f\n';
23
24
    fprintf(TempInput,T);
    fprintf('Readings Minimum Average Maximum\n');
25
26
    formatSpec = '
                          %0.0f %4.2f %4.2f %4.2f\n';
27
    fprintf(formatSpec,i,Min,AvTemp,Max);
28
         else
29
    %TempInput ='Enter a Temperature: %4.2f\n';
30
    %fprintf(TempInput,Temp);
31
             i=i+1000000000;
32
         end
33
         i=i+1;
34
         fprintf(FID, '\n');
35
36
37
38
39
    end
40
    save MyTemps.txt Temp -ascii
```

B Diary and Data Sets

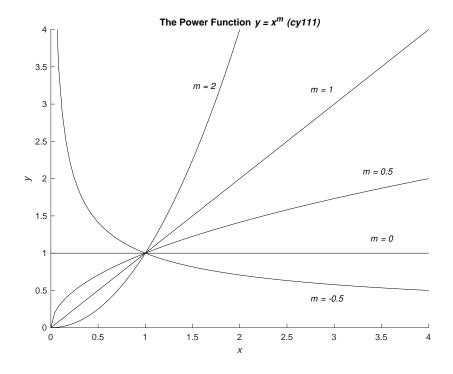
B.1 MyTemps.txt

```
1 3.0000000e+02 2.0000000e+02 2.5000000e+02 -1.0000000e+00
```

B.2 TempDiary.txt

```
1
    out =
 2
      259.0713
3
    Enter a Temperature: 259.07
    Readings Minimum Average Maximum
           1 259.07 259.07 259.07
5
6
    out =
    262.9039
7
   Enter a Temperature: 262.90
    Readings Minimum Average Maximum
9
10
           2 259.07 260.99 262.90
11
   out =
12
    254.2658
13
    Enter a Temperature: 254.27
14
    Readings Minimum Average Maximum
15
           3 254.27 258.75 262.90
16
    out =
     320.9484
17
   Enter a Temperature: 320.95
18
    Readings Minimum Average Maximum
           4 254.27 274.30 320.95
20
21
    out =
22
    256.4189
23
    Enter a Temperature: 256.42
24
    Readings Minimum Average Maximum
25
           5 254.27 270.72 320.95
26
    out =
27
     270.1800
    Enter a Temperature: 270.18
28
29
    Readings Minimum Average Maximum
30
           6 254.27 270.63 320.95
```

C Figures



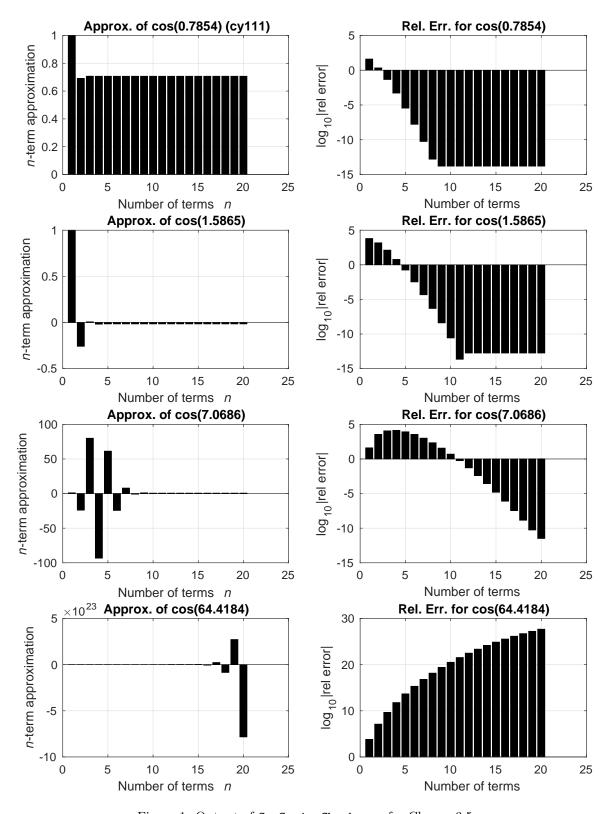


Figure 1: Output of ${\tt CosSeriesChecker.m}$ for Chapra 3.5

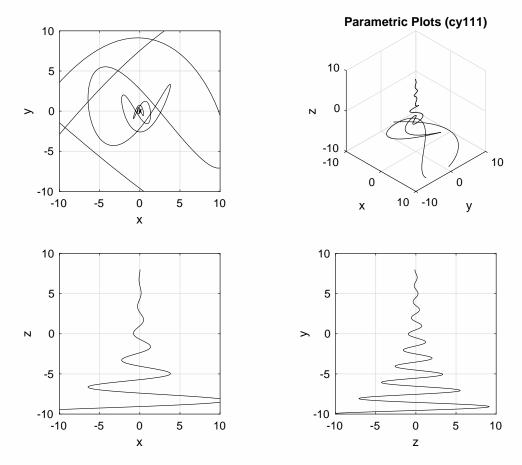


Figure 2: Output of ParametricPlots.m for Palm 5.15

References

- [1] Chapra, Steven C., Applied Numerical Methods with MATLAB for Engineering and Scientists. McGraw-Hill, New York, 3rd Edition, 2012.
- [2] Palm, William J., Introduction to MATLAB for Engineers. McGraw-Hill, New York, 3rd Edition, 2011.