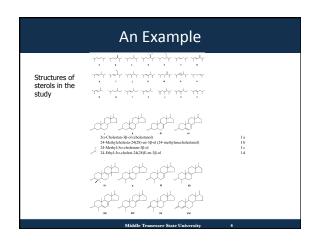


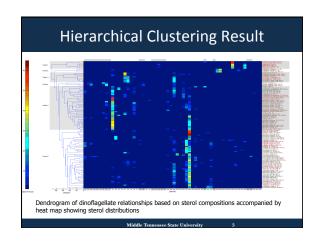
An Example

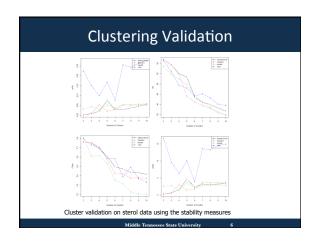
- Study: How different species of Dinoflagellates (Algae) relates to each other by studying their sterol composition
 - identify the relationships via sterol composition similarity amongst dinoflagellates
 - investigate the correspondences between the dinoflagellates sharing a similar sterol compositions and their evolutionary histories.
- Data:
 - Sterol composition of 102 dinoflagellates

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An Example Data: 58 named sterols and steroidal ketones 102 dinoflagellate species Analysis method Hierarchical Clustering based on Sterol composition data Clustering validation using multiple clustering schemes and clustering criteria





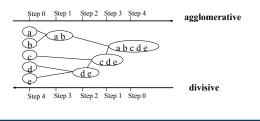


An Example

- · Conclusion of the Study:
 - Our results indicated that several, but not all, dinoflagellate genera share similar sterol compositions
 - sterol composition of dinoflagellates has been determined, to a certain extent, by the evolutionary diversification of this lineage.

Agglomerative vs. Divisive Clustering

• Use distance matrix as clustering criteria. This method does not require the number of clusters k as an input, but needs a termination condition



Single-link vs. Complete-link

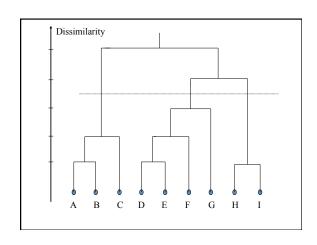
- · Difference: the way to characterize the similarity between a pair of clusters
 - single link: minimum of the distances between all pairs of patterns drawn from the two clusters
 - complete link: maximum of the distances between all pairs of patterns drawn from the two clusters
 - average link: average of the distances between all pairs of
 - patterns drawn from the two clusters
 UPGMA (Unweighted Pair Group Method with Arithmetic Mean)
- · All use agglomerative clustering control structure

Agglomerative clustering

- Step 1: place each pattern in its own cluster construct a list of inter-pattern distances for all distinct unordered pairs of patterns, and sort this list in ascending order
- Step through the sorted list of distances, forming for each distinct dissimilarity value dk, a graph on the patterns where pairs of patterns closer than d_k are connected by a graph edge.
- If all patterns are members of a completely connected graph, stop.

Dendrogram

- A Dendrogram Shows How the Clusters are Merged Hierarchically:
- Decompose data objects into several levels of nested partitioning (tree of clusters), called a dendrogram.
- A <u>clustering</u> of the data objects is obtained by <u>cutting</u> the dendrogram at the desired level, then each connected component forms a cluster.



Practice Question

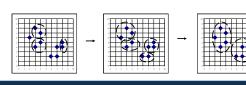
 Cluster the following six objects, using single-link and complete link agglomerative clustering methods:

	Gender	Age	Time	Fever	Cough
Obj1	F	2	2	Υ	N
Obj2	M	2	0.5	N	N
Obj3	F	15	3	Υ	Υ
Obj4	F	18	0.5	Υ	N
Obj5	M	58	4	N	Υ
Obj6	F	44	14	N	Υ

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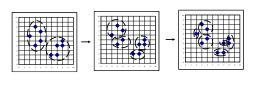
AGNES (Agglomerative Nesting)

- Implemented in statistical analysis packages, e.g., Splus
- Use the Single-Link method and the dissimilarity matrix.
- · Merge nodes that have the least dissimilarity
- Go on in a non-descending fashion
- Eventually all nodes belong to the same cluster



DIANA (Divisive Analysis)

- · Inverse order of AGNES
- Eventually each node forms a cluster on its own



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More on Hierarchical Clustering Methods

- Major weakness of agglomerative clustering methods
 - <u>do not scale</u> well: time complexity of at least $O(n^2)$, where n is the number of total objects
 - can never undo what was done previously
- · Integration of hierarchical with distance-based clustering
 - BIRCH (1996) (Balanced Iterative Reducing and Clustering using Hierarchies): uses CF-tree and incrementally adjusts the quality of sub-clusters
 - <u>CURE (1998</u>): selects well-scattered points from the cluster and then shrinks them towards the center of the cluster by a specified fraction

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• Only works with "metric" attributes

- Must have Euclidean coordinates
- Designed for very large data sets
- Time and memory constraints are explicit
- Treats dense regions of data points as sub-clusters
 - Not all data points are important for clustering
- Only one scan of data is necessary

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• Incremental, distance-based approach

- Does not need the whole data set in advance
- Unique approach: distance based algorithms generally need all the data points to work
- Does not assume that the probability distributions on attributes is independent

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3

Balanced Iterative Reducing and Clustering using Hierarchies (BIRCH)

- Incrementally construct a CF (Clustering Feature) tree, a hierarchical data structure for multiphase clustering
 - Phase 1: scan DB to build an initial in-memory CF tree (a multilevel compression of the data that tries to preserve the inherent clustering structure of the data)
 - Phase 2: use an arbitrary clustering algorithm to cluster the leaf nodes of the CF-tree
- Scales linearly: finds a good clustering with a single scan and improves the quality with a few additional scans
- Weakness: handles only numeric data, and sensitive to the order of the data record.

Clustering Feature Vector

Clustering Feature: CF = (N, LS, SS)

N: Number of data points

LS:
$$\sum_{i=1}^{N} = \overrightarrow{X_i}$$

SS: $\sum_{i=1}^{N} = \overrightarrow{X_i^2}$



CF = (5, (16,30),(54,190))

(3, 4)

(2, 6)(4, 5)

(4, 7)

(3, 8)

Given a cluster of instances $\{\vec{X}_i\}$, we define the centroid, the radius, and the diameter:

$$\begin{split} \vec{X0} &= \frac{\sum_{i=1}^{N} \vec{X}_i}{N} \\ R &= (\frac{\sum_{i=1}^{N} (\vec{X}_i - \vec{X0})^2}{N})^{\frac{1}{2}} \\ D &= (\frac{\sum_{i=1}^{N} \sum_{j=1}^{N} (\vec{X}_i - \vec{X_j})^2}{N(N-1)})^{\frac{1}{2}} \end{split}$$

We define the Euclidean and Manhattan distance between any two clusters as:

$$D0 = ((\vec{X0}_1 - \vec{X0}_2)^2)^{\frac{1}{2}}$$

$$D1 = |\vec{X0}_1 - \vec{X0}_2| = \sum_{i=1}^{d} |\vec{X0}_1^{(i)} - \vec{X0}_1^{(i)}|$$

We define the average inter-cluster, the average intra-cluster, and the variance increase distances as:

$$D2 = (\frac{\sum_{i=1}^{N_1} \sum_{j=N_1+1}^{N_1+N_2} (\vec{X}_i - \vec{X_j})^2}{N_1 N_2})^{\frac{1}{2}}$$

$$D3 = (\frac{\sum_{i=1}^{N_1+N_2} \sum_{j=1}^{N_1+N_2} (\vec{X_i} - \vec{X_j})^2}{(N_1+N_2)(N_1+N_2-1)})^{\frac{1}{2}}$$

$$\begin{array}{c} D4 = & (\sum_{k=1}^{N_1+N_2} (\vec{X_k} - \sum_{i=1}^{j_{N_1}+N_2} \vec{X_i})^2 \\ & - \sum_{i=1}^{N_1} (\vec{X_i} - \frac{\sum_{i=1}^{N_1} \vec{X_i}}{N_1})^2 - \sum_{j=N_1+1}^{N_1+N_2} (\vec{X_j} - \frac{\sum_{i=N_1+1}^{N_1+N_2} \vec{X_i}}{N_2})^2)^{\frac{1}{2}} \end{array}$$

The algorithm: CF

A Clustering Feature (CF) summarizes a sub-cluster of data points.

Given a cluster $\{\vec{X_1}, \vec{X_2}, \dots, \vec{X_N}\}$

$$\mathbf{CF} = (N, \vec{LS}, SS)$$

N is the number of data points $\vec{LS} = \sum_{i=1}^{N} \vec{X}_i$ $SS = \sum_{i=1}^{N} \vec{X}_i^2$

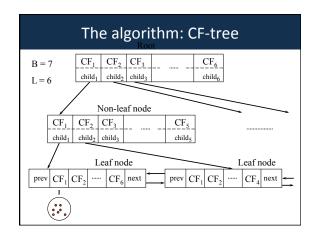
$$LS = \sum_{i=1}^{N} X_i$$

$$SS = \sum_{i=1}^{N} \vec{X}_i$$

$$\mathbf{CF_1} + \mathbf{CF_2} = (N_1 + N_2, \vec{LS}_1 + \vec{LS}_2, SS_1 + SS_2)$$



- Stores significantly less then all of the data points in the sub-cluster
- A CF entry has enough information to calculate D0-D4
- · Additivity theorem allows us to incrementally merge sub-clusters



· Each non-leaf node has at most B entries CF ² CF Each leaf node has at most L CF entries which each satisfy CF CF ...BCF threshold T Node size is determined by dimensionality of data points and input parameter P (page size)

• Recurse down from root Choose the "closest" CF and go to that node Modify the leaf – If the closest CF in the leaf can not absorb, make a new CF entry. If there is no room, split the node • Traverse back up Modifying CFs or splitting nodes

• If we run out of space, increase T

- By increasing the threshold, CFs absorb more data
- Rebuilding "pushes" CFs over
 - The larger T allows different CFs to group together
- Reducibility theorem
 - Increasing T will result in a CF-tree as small or smaller then the original

Phase 1: Load data into memory

- Build a CF-tree with the data
- Phase 2: Condense data
- Rebuild the CF-tree with a larger T
- Condensing is optional

· Phase 3: Global clustering

- Use existing clustering algorithm on CF entries
- Helps fix problem where natural clusters span nodes

· Phase 4: Cluster refining

- Do additional passes over the data set and reassign data points to the closest centroid from phase 3
- Refining is optional

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Why have optional phases?

- Phase 2 allows us to resize the data set so Phase 3 runs on an optimally sized data set
- Phase 4 fixes a problem with CF-trees where some data points may be assigned to different leaf entries
- Phase 4 will always converge to a minimum
- Phase 4 allows us to discard outliers

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· Input parameters:

- Memory (M): 5% of data set

- Disk space (R): 20% of M

Distance equation: D2

- Quality equation: weighted average diameter (D)

- Initial threshold (T): 0.0

- Page size (P): 1024 bytes

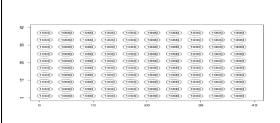
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· Create 3 synthetic data sets for testing

- Also create an ordered copy for testing input order
- KMEANS and CLARANS require entire data set to be in memory
 - Initial scan is from disk, subsequent scans are in memory

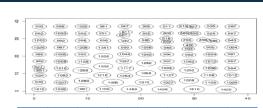
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Intended clustering



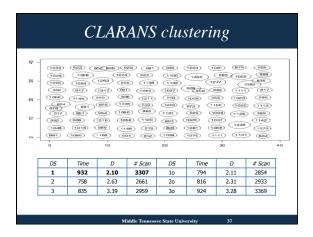
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Kmeans Clustering

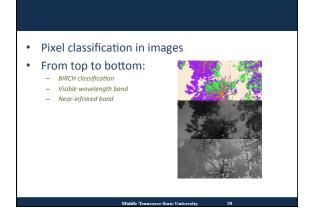


0	10		20		30		40
DS	Time	D	# Scan	DS	Time	D	# Scan
1	43.9	2.09	289	10	33.8	1.97	197
2	13.2	4.43	51	20	12.7	4.20	29
3	32.9	3.66	187	Зо	36.0	4.35	241

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- BIRCH works with very large data sets
 BIRCH performs faster then CLARANS or LBG, while getting better compression and nearly as
- Explicitly bounded by computational resources
 - Runs with specified amount of memory (P)
- Superior to CLARANS and KMEANS

good quality

- Quality, speed, stability and scalability

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