

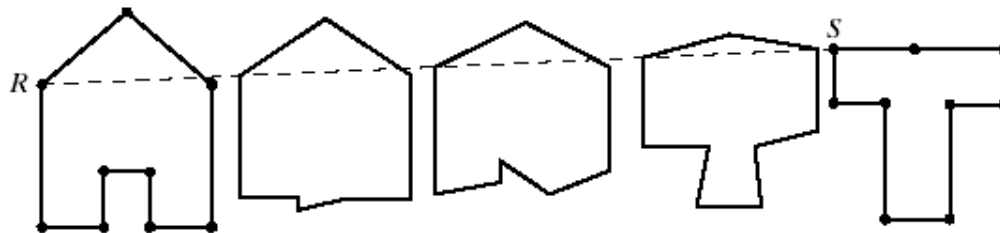
## Tweening

- In films, artists draw only the key frames of an animation sequence (usually the first and last).
- Tweening is used to generate the in-between frames

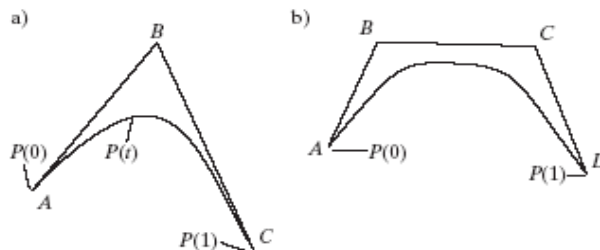


### How is it done?

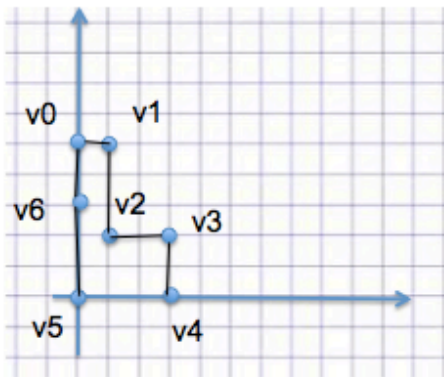
- $P = (1-t)A + tB$  is a linear interpolation (lerp or tween) of 2 points.
- Tweening takes 2 polylines and interpolates between them (using lerp) to make one turn into another (or vice versa).
  - $P(t)$  that is a fraction  $t$  of the way along the straight line (not to be drawn) from point A to point B.
  - $P_i(t) = (1-t)A_i + tB_i$ , for  $t = 0.0, 0.1, \dots, 1.0$  (or any other set of  $t$  in  $[0, 1]$ ), and draw the polyline for  $P_i$ .



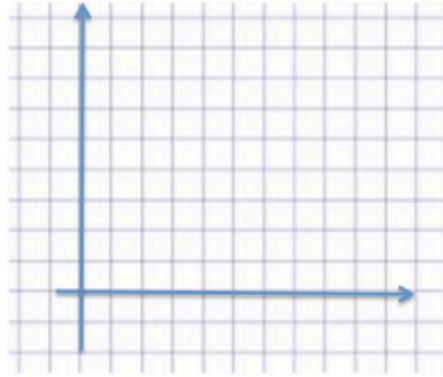
- Practice Question:
  - What is the effect of tweening when all of the points  $A_i$  in polyline A are the same? How is polyline B distorted in its appearance in each tween?
  - Polyline A is a square with vertices  $(1, 1)$ ,  $(-1, 1)$ ,  $(-1, -1)$ ,  $(1, -1)$  and polyline B is a wedge with vertices  $(4, 3)$ ,  $(5, -2)$ ,  $(4, 0)$ ,  $(3, -2)$ . Sketch the shape  $P(t)$  for  $t = -1, -0.5, 0.5$ , and  $1.5$ .
- Other uses of tweening:
  - Draw a smooth curve that passes through or near 3 points (A, B, and C). → expand  $((1-t) + t)^2$  and write:  $P(t) = (1-t)^2A + 2t(1-t)B + t^2C$ 
    - This is called the Bezier curve for points A, B, and C. It can be extended to 4 points by expanding  $((1-t) + t)^3$  and using each term as the coefficient of a point.



$t=0$

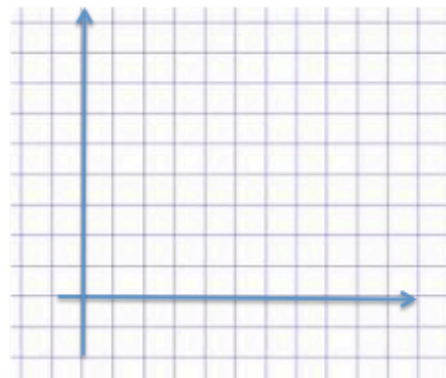


$t=0.3$

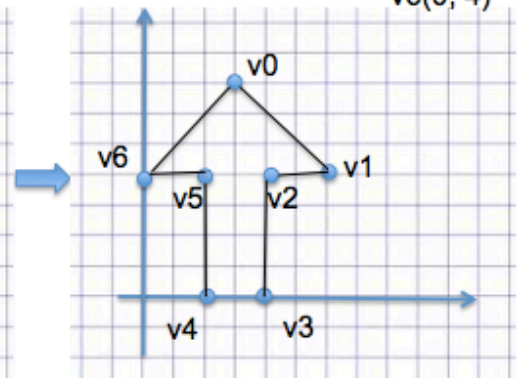


$v_0(0, 5)$   
 $v_1(1, 5)$   
 $v_2(1, 2)$   
 $v_3(3, 2)$   
 $v_4(3, 0)$   
 $v_5(0, 0)$   
 $v_6(0, 3)$

$v_0(3, 7)$   
 $v_1(6, 4)$   
 $v_2(4, 4)$   
 $v_3(4, 0)$   
 $v_4(2, 0)$   
 $v_5(2, 4)$   
 $v_6(0, 4)$



$t=0.6$



$t=1$