

CSCI 3110

Algorithm Efficiency

Measuring the Efficiency of Algorithms

Algorithm Growth Rates

Keeping Your Perspective

Recursion?

Examples

Iteration vs. Recursion

Towers of Hanoi

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Recursion



What's recursion?

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What's recursion

- A powerful problem solving technique
- A special case of divide-and-conquer technique
 - Sub-problems have the exact type of the original type, with smaller size
- A function of accomplishing a task by invoking itself



How to construct recursive solution?

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STL Sorting Algorithms Four questions for constructing recursive solutions

- How can you define the problem in terms of a smaller problem of the same type?
- How does each recursive call diminish the size of the problem?
- What instance of the problem can serve as the base case?
- As the problem size diminishes, will you reach this base case?



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The Factorial of n

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■ Problem

- Compute the factorial of an integer n
- An iterative definition of factorial(n) factorial(n) = n * (n-1) * (n-2) * ... * 1 for any integer n > 0 factorial(0) = 1
- A recursive definition of factorial(n)

The Factorial of n: two versions

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■ version 1:

```
int factorial( int n )
{
    if ( n == 0 )
        return 1;
    else
        return n * factorial( n-1 );
}
```

version 2:



Box trace: the way to understand recursion

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■ Box trace

- A systematic way to trace the actions of a recursive method
- Each box roughly corresponds to an activation record
- Contains a function's local environment at the time of and as a result of the call to the method



Box trace: Procedure

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Box trace

- Label each recursive call in the function body
- Represent each call to the function by a new box containing local environment of the function.
 - parameters
 - local variables
 - placeholder for return value
 - the value of the function itself
- Draw an arrow from the box that makes the call to the newly created box, and label each arrow
- Start executing the function body corresponding to new created box
- On exiting the function, cross off the current box and follow its arrow back to the box that called the function

Box trace factorial function

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Summary STL Sorting Algorithms The initial call is made, and method fact begins execution:

At point A a recursive call is made, and the new invocation of the method fact begins execution:

$$n = 3$$
A: fact(n-1)=?

return ?

A

 $n = 2$
A: fact(n-1)=?

return ?

At point A a recursive call is made, and the new invocation of the method fact begins execution:

$$\begin{array}{c} n = 3 \\ A: \ \text{fact(n-1)=?} \\ \text{return?} \end{array} \qquad \begin{array}{c} A \\ A: \ \text{fact(n-1)=?} \\ \text{return?} \end{array} \qquad \begin{array}{c} A \\ A: \ \text{fact(n-1)=?} \\ \text{return?} \end{array}$$

Box trace factorial function

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At point A a recursive call is made, and the new invocation of the method fact begins execution:

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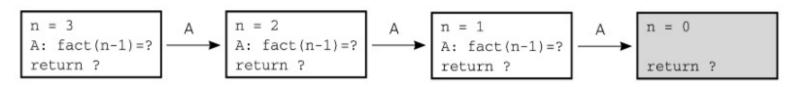
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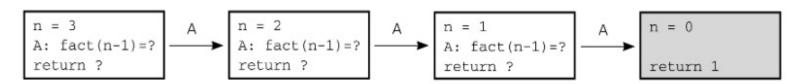
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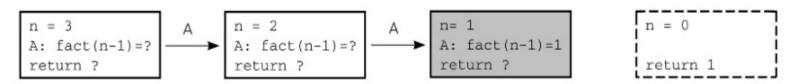
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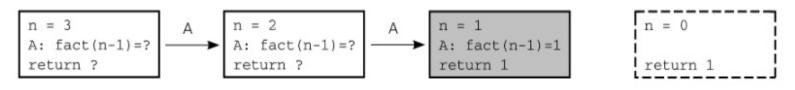
This is the base case, so this invocation of fact completes:



The method value is returned to the calling box, which continues execution:



The current invocation of fact completes:



Box trace factorial function

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The method value is returned to the calling box, which continues execution:

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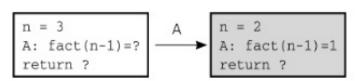
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The current invocation of fact completes:

$$\begin{array}{c} n = 3 \\ A: fact(n-1) = ? \\ return ? \end{array} \longrightarrow \begin{array}{c} A \\ A: fact(n-1) = 1 \\ return 2 \end{array}$$

The method value is returned to the calling box, which continues execution:

The current invocation fact completes:

The value 6 is returned to the initial call.



String Backward

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■ Problem

■ Given a string of characters, write it in reverse order

Recursive solution

- Each recursive step of the solution diminishes by 1 the length of the string to be written backward
- Base case: write the empty string backward



Recursive Solutions

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- Using StrBackward(a[0...n]) to indicate the solution to write string a[0...n] backward
- Solution 1
 StrBackward(a[0...n]) = output a[n] + StrBackward(a[0...n-1])
- Solution 2
 StrBackward(a[0...n]) = StrBackward(a[1...n]) + output a[0]

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```
void writeBackward1( string s )
 if (s.size() > 0)
    string subs = s.substr(0, s.size()-1);
    cout \ll s[s.size()-1];
    writeBackward1( subs );
void writeBackward2( string s )
 if (s.size() > 0)
    string subs = s.substr(1, s.size()-1);
    writeBackward2( subs );
    cout \ll s[0];
```



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■ Problem

- How many different choices are there for exploring k planets out of n planets in a solar system?
- Pay attention to the problem size and base cases



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- Let c(n, k) be the number of groups of k planets chosen from n
- In terms of Planet X:

```
c(n, k) = the number of groups of k planets
that include Planet X
```

+

the number of groups of k planets that do not include Planet X

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- The number of ways to choose k out of n things is the sum of
 - the number of ways to choose k-1 out of n-1 things
 - the number of ways to choose k out of n-1 things
- c(n, k) = c(n-1, k-1) + c(n-1, k)

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Base Cases

- There is one group of everything c(k, k) = 1
- There is one group of nothing c(n, 0) = 1
- $\mathbf{c}(n,k) = 0 \text{ if } k > n$

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Recursive solution

$$c(n, k) =$$

1 if $k = 0$

1 if $k = n$

0 if $k > n$
 $c(n-1, k-1) + c(n-1, k)$ if $0 < k < n$

if
$$k = 0$$

if $k = n$
if $k > n$



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■ Problem

■ Given a number x, and an array of ascent sorted integers with size n, give an efficient algorithm to find if x appears in the array.



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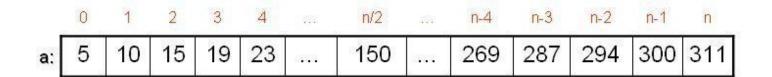
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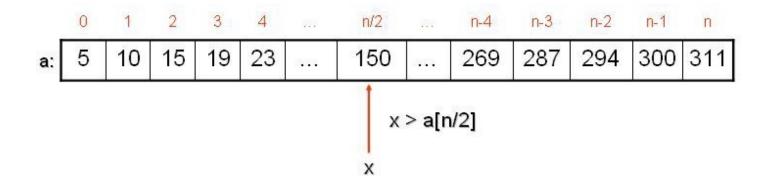
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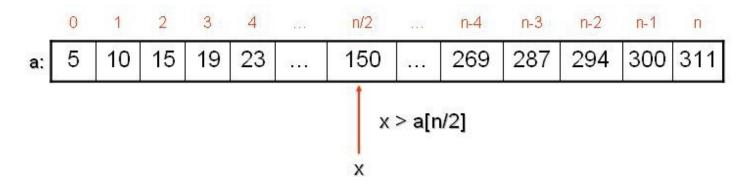
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■ x > a[n/2]: search x in a[n/2..n]



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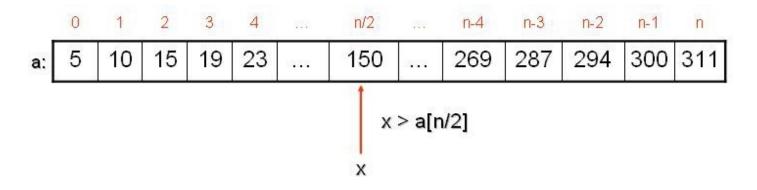
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- x > a[n/2]: search x in a[n/2..n]
- \blacksquare x == a[n/2]: return true



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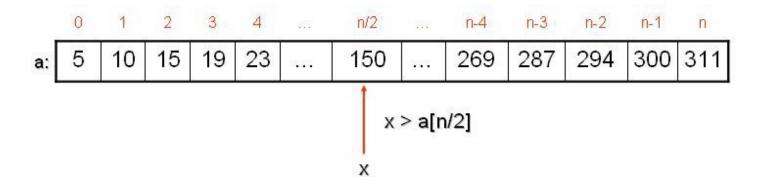
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- x > a[n/2]: search x in a[n/2..n]
- $\mathbf{x} == a[n/2]$: return true
- \blacksquare x < a[n/2]: search x in a[0..n/2]



Recursive Solution

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Let **BinarySearch**(a[0...n],x) be the solution to the problem of checking if x is in the array a[0...n]

BinarySearch(a[0...n], x) =

BinarySearch(a[0...n/2-1], x)

n/2

BinarySearch(a[n/2+1...n], x)

Base cases:

- array has no elements, which indicates x is not in this array
- $\mathbf{x} == \operatorname{array}[\operatorname{arraySize}/2]$, which indicates x is in the array with index arraySize/2



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```
int BinarySearch(int array[], int first, int last, int key)
  int mid;
  if (first > last)
     return -1;
  else {
       mid = (first + last) / 2;
       if (key == array[mid])
          return mid;
        else if (value < array[mid])
          return BinarySearch(array, first, mid - 1, key);
        else if (value > array[mid])
          return BinarySearch(array, mid + 1, last, key);
```



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Costs

- Recursion: calling the same function over and over
- Iteration: 'jumps back' to the beginning of the loop.
- Iteration is more efficient
 - A function call is often more expensive than a jump.
 - Space: Every function call may require space for parameters and local variables. A recursive algorithm may need space proportional to the number of nested calls.
 - Time: Allocating and later releasing local memory, copying values into the local memory for the parameters, branching to/returning from the function.
 - "Clever" compilers may produce machine code that incurs minimal or no overhead for recursion.
 - Most recursive solution can be rewritten as iteration



Iteration vs. Recursion

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- Recursion is easier to maintain
 - clearer, simpler, shorter, and easier to understand than their non-recursive counterparts.
 - reflects the abstract solution strategy (algorithm).
- Recursion provides an elegant solution to some kind of problems, sometimes, the only solution.



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What's the Towers of Hanoi problem?

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Towers of Hanoi Puzzle



b) move n - 1 disks from A to C

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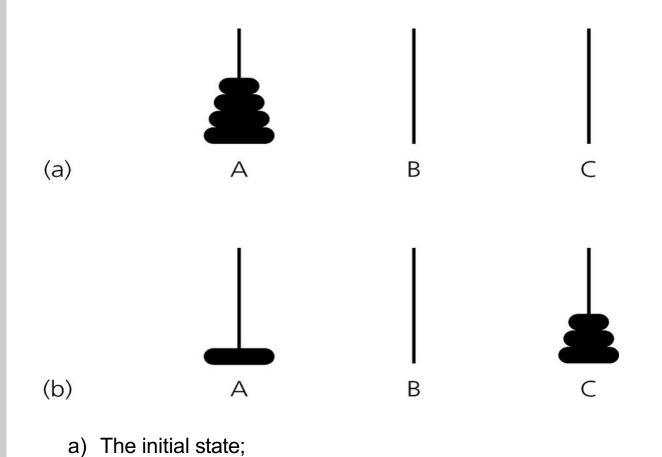
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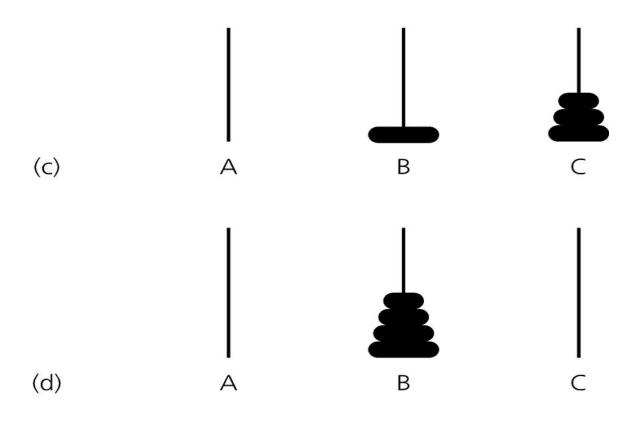
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- c) move one disk from A to B;
- d) move n 1 disks from C to B



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```
void SolveTowers(int count, char source, char destination, char spare)
{
    if (count ==1)
        cout << "moving disk from " << source << " to " << destination << endl;
    else
    {
        SolveTowers(count-1, source, spare, destination);
        SolveTowers(1, source, destination, spare);
        SolveTowers(count-1, spare, destination, source);
    }
}</pre>
```



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STL Sorting Algorithms When N=3, i.e., solve SolveTowers(3, A, B, C) Trace of program execution

SolveTowers(3, A, B, C)

SolveTowers(2, A, C, B) \rightarrow SolveTowers(1, A, B, C) A \rightarrow B

SolveTowers(1, A, C, B) $A \rightarrow C$

SolveTowers(1, B, C, A) $B \rightarrow C$

SolveTowers(1, A, B, C) \rightarrow A \rightarrow B

SolveTowers(2, C, B, A) \rightarrow SolveTowers(1, C, A, B) \rightarrow A

 \rightarrow SolveTowers(1, C, B, A) $C \rightarrow B$

 \rightarrow SolveTowers(1, A, B, C) A \rightarrow B



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Summary

- Recursion is a technique that solves a problem by solving smaller problems of the same type
- When constructing a recursive solution, keep the following 4 questions in mind
 - How to define the problem in terms of a smaller problem of the same type?
 - How does each recursive call diminish the size of the problem?
 - What instance of the problem can serve as the base case(s)?
 - As the problem size diminishes, will you reach this base case?
- You can use the box method to trace the actions of a recursive functions. Each box represents a activation record.



Summary

CSCI 3110

Algorithm Efficiency

Measuring the Efficiency of Algorithms

Algorithm Growth Rates

Keeping Your Perspective

Recursion?

Examples

Iteration vs. Recursion

Towers of Hanoi

Summary

Sorting Algorithms

Selection Sort

Bubble Sort

Insertion Sort

Mergesort

Quick Sort

Radix Sort

Summary

- Recursion allow you to solve problems such as the Towers of Hanoi whose iterative solution are difficult to conceptualize. Even the most complex problems often have straightforward recursive solutions. Such solutions can be easier to understand, describe, and implement than iterative solutions.
- Some recursive solutions are much less efficient than a corresponding iterative solution due to their inherently inefficient algorithms and the overhead of function calls.
- If you can easily, clearly, and efficiently solve a problem by using iteration, you should do so.