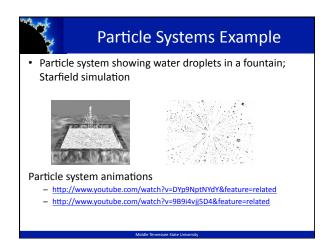


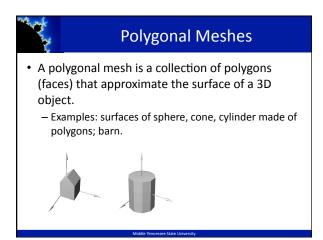


3D Modeling

- Polygonal meshes capture the shape of complex 3D objects in simple data structures.
 - Platonic solids, the Buckyball, geodesic domes, prisms.
 - Extruded or swept shapes, and surfaces of revolution.
- Solids with smoothly curved surfaces.
- Animated Particle systems: each particle responds to conditions.
- Physically based systems: the various objects in a scene are modeled as connected by springs, gears, electrostatic forces, gravity, or other mechanisms.

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Polygonal Meshes (2)

- Polygons are easy to represent (by a sequence of vertices) and transform.
- They have simple properties (a single normal vector, a well-defined inside and outside, etc.).
- They are easy to draw (using a polygon-fill routine, or by mapping texture onto the polygon).

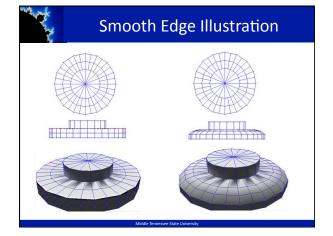
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Polygonal Meshes (3)

- Meshes are a standard way of representing 3D objects in graphics.
- A mesh can approximate the surface to any degree of accuracy by making the mesh finer or coarser.
- We can also smooth the polygon edges using rendering techniques.

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Polygonal Meshes (4)

- Meshes can model both solid shapes and thin skins.
 - The object is solid if the polygonal faces fit together to enclose space.
 - In other cases, the faces fit together without enclosing space, and so they represent an infinitesimally thin surface.
- In both cases we call the collection of polygons a **polygonal mesh** (or simply a **mesh**).



Polygonal Meshes (5)

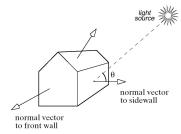
- A polygonal mesh is described by a list of polygons, along with information about the direction in which each polygon is facing.
- If the mesh represents a solid, each face has an inside and an outside relative to the rest of the mesh.
- In such a case, the directional information is often simply the outward pointing normal vector to the plane of the face used in the shading process.

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Polygonal Meshes (6)

• The normal direction to a face determines its brightness.



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Polygonal Meshes (7)

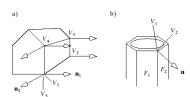
- For some objects, we associate a normal vector to each vertex of a face rather than one vector to an entire face.
 - We use meshes, which represent objects with smoothly curved faces such as a sphere or cylinder.
 We will refer to the faces of such objects, but with the idea that there is a "smooth-underlying surface".
 - When we display such an object, we will want to deemphasize the individual faces of the object in order to make the object look smooth.

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Polygonal Meshes (8)

- Each vertex V_1 , V_2 , V_3 , and V_4 defining the side wall of the barn has the same normal \mathbf{n}_1 , the normal vector to the side wall.
- But vertices of the front wall, such as V₅, will use normal n₂. (Note that vertices V₁ and V₅ are located at the same point in space, but use different normals.)





Defining a Polygonal Mesh

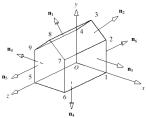
- A mesh consists of 3 lists: the vertices of the mesh, the outside normal at each vertex, and the faces of the mesh.
- Example: the cube has 6 polygonal faces and 8 vertices
 - Mesh notes
- Example: the basic barn has 7 polygonal faces and 10 vertices (each shared by 3 faces).
 - Code example

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Defining a Polygonal Mesh (2)

- It has a square floor one unit on a side.
- Because the barn has flat walls, there are only 7 distinct normal vectors involved, the normal to each face as shown.



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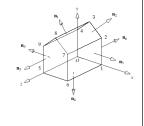
Defining a Polygonal Mesh (3)

- The vertex list reports the locations of the distinct vertices in the mesh.
- The list of normals reports the directions of the distinct normal vectors that occur in the model.
- The face list indexes into the vertex and normal lists.

Mary S

Vertex List for the Barn

vertex	Х	У	Z
0	0	0	0
1	1	0	0
2	1	1	0
3	0.5	1.5	0
4	0	1	0
5	0	0	1
6	1	0	1
7	1	1	1
8	0.5	1.5	10
9	0	1	1

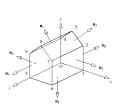


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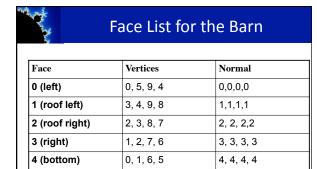
Normal List for the Barn

The normal list (as unit vectors, to the 7 basic planes or polygons).



0
0
0
0
0
1
-1

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5, 6, 7, 8, 9

0, 4, 3, 2, 1



Defining a Polygonal Mesh (4)

- Only the indices of the vertices and normals are used.
- The list of vertices for a face begins with any vertex in the face, and then proceeds around the face vertex by vertex until a complete circuit has been made.
 - There are two ways to traverse a polygon: clockwise and counterclockwise. For instance, face #5 above could be listed as (5, 6, 7, 8, 9) or (9, 8, 7, 6, 5).
 - Convention: Traverse the polygon counterclockwise as seen from outside the object.
 - Traverse the vertex so that the interior of the face lies to the left
 - Using the convention allows algorithms to distinguish with ease the front from the back of a face.

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5 (front)

6 (back)

3D File Formats

- There is no standard file format.
- Some formats have been found to be efficient and easy to use: for example, the .qs file format developed by the Stanford University Computer Graphics Laboratory. This particular mesh model has 2,748,318 points (about 5,500,000 triangles) and is based on 566,098 vertices.
 - http://lodbook.com/models/







5, 5, 5, 5, 5

6, 6, 6, 6, 6



3D File Formats (2)

 OpenGL has the capability to load a variety of 3D model formats such as (but not limited to) 3DS, VRML, PLY, MS3D, ASE and OBJ. ply format ascii 1.0 comment generated by ply_writer element vertex 543652 property float x property float y property float z element face 1087716 property list uchar int vertex_indices end _header - 0.00709887 0.064825 - 0.0472725 - 0.0046435 0.064825 - 0.0472725 - 0.0078784 0.0665075 - 0.0066075 - 0.0065075 - 0.006

-0.0076435 0.0650297 -0.0472725

3 543641 543645 543651 3 543641 543651 543650 3 543651 543645 543602 3 543645 543595 543601 3 543646 543645 543613 3 543649 543650 543625

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Calculating Normals

- Take any three non-collinear points on the face, V₁, V₂, and V₃, and compute the normal as their cross product m = (V₁ V₂) × (V₃ V₂) and normalize it to unit length.
 - If the two vectors V₁ V₂ and V₃ V₂ are nearly parallel, the cross product will be very small and numerical inaccuracies may result.
 - The polygon may not be perfectly planar. Thus the surface represented by the vertices cannot be truly flat. We need to form some average value for the normal to the polygon, one that takes into consideration all of the vertices.
 - Newell's Method for Normal

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Newell's Method for Normals

- Given N vertices, define next(i) = n_i = (i+1) mod N.
- Traverse the vertices for the face in counter-clockwise order from the outside.
- The normal computed points to the outside (front) of the face:

$$n_{x} = \sum_{i=0}^{N-1} (y_{i} - y_{ni})(z_{i} + z_{ni})$$

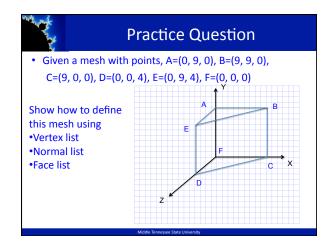
$$n_{y} = \sum_{i=0}^{N-1} (z_{i} - z_{ni})(x_{i} + x_{ni})$$

$$n_{z} = \sum_{i=0}^{N-1} (x_{i} - x_{ni})(y_{i} + y_{ni})$$



Practice Question

- · For the following polygons,
 - Are they planar?
 - What is its normal computed based on cross product method?
 - What is the normal computed using the Newell's method?
- 1. $P_0(6, 1, 4)$, $P_1=(7, 0, 9)$, and $P_2=(1, 1, 2)$ 2. $P_0(0, 0, 3)$, $P_1=(-3, 1, 3)$, $P_2=(0, 0, 5)$, and $P_3=(3, 0, 0)$

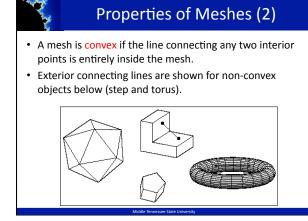




Properties of Meshes

- A closed mesh represents a solid object (which encloses a volume).
- A mesh is connected if there is an unbroken path along the edges of the mesh between any two vertices.
- A mesh is simple if it has no holes. Example: a sphere is simple; a torus is not.
- A mesh is planar if every face is a plane polygon.
 Triangular meshes are frequently used to enforce planarity.

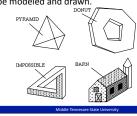
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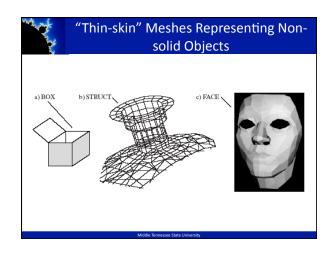




Meshes for Drawing Non-physical Objects

- $\bullet \ \ \, \text{The figure labeled IMPOSSIBLE looks impossible but is not}.$
- This object can be represented by a mesh.
- Gershon Elber's web site
 (http://www.cs.technion.ac.il/~gershon/EscherForReal/) presents a collection of physically impossible objects, and describes how they can be modeled and drawn.







Working with Meshes in a Program

- We want an efficient Mesh class that makes it easy to create (in terms of reading mesh data into special data structure) and draw the object.
- Since mesh data is frequently stored in a file, we also need simple ways to read and write mesh files.
 - Refer to Mesh notes on cube

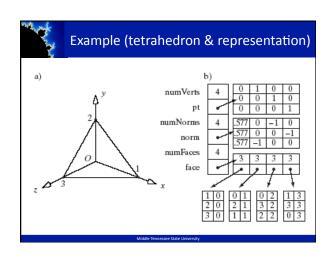
ARABA Tarana Cara III.



Meshes in a Program (2)

- The Face data type is a list of vertices and the normal vector associated with each vertex in the face.
- It is an array of index pairs; the normal to the vth vertex of the fth face has value norm[face[f].vert[v].normIndex].
- This indexing scheme is quite orderly and easy to manage, and it allows rapid random access indexing into the pt[] array.

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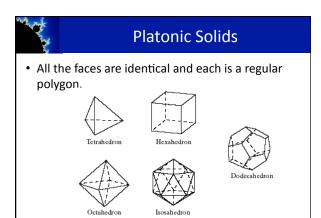


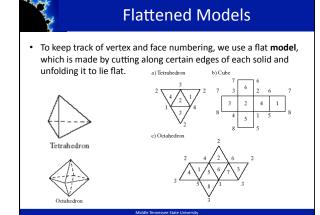


Drawing the Mesh Object

- Mesh::draw() traverses the array of faces in the mesh object, and for each face sends the list of vertices and their normals down the graphics pipeline.
- In OpenGL, to specify that subsequent vertices are associated with normal vector m, execute glNormal3f (m.x, m.y, m.z).
- For proper shading, these vectors must be normalized. Otherwise, place glEnable(GL_NORMALIZE) in the init() function. This requests that OpenGL automatically normalize all normal vectors.

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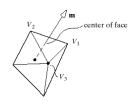


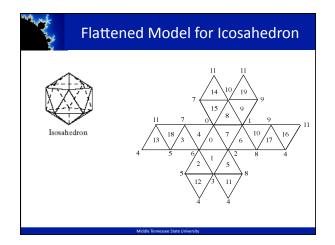


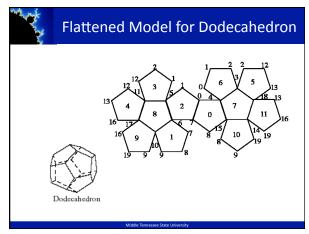


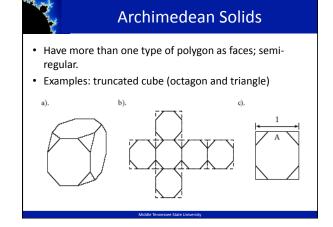
Normal Vectors for the Platonic Solids

- Normals can be found using Newell's method.
- Also, because of the high degree of symmetry of a Platonic solid, if the solid is centered at the origin, the normal vector to each face is the vector from the origin to the center of the face (the average of the vertices of the face).











Truncated Cube

- Each edge of the cube is divided into three parts; the middle part of length and the middle portion of each edge is joined to its neighbors.
- Thus if an edge of the cube has endpoints C and D, two new vertices, V and W, are formed as the

$$V = \frac{1+A}{2}C + \frac{1-A}{2}D \qquad W = \frac{1-A}{2}C + \frac{1+A}{2}D$$

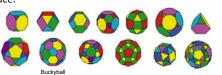
$$W = \frac{1 - A}{2}C + \frac{1 + A}{2}D$$

$$A = \sqrt{2} - 1$$



Number of Archimedean Solids

- Given the constraints that faces must be regular polygons, and that they must occur in the same arrangement about each vertex, there are only 13 possible Archimedean solids.
- Archimedean solids have sufficient symmetry that the normal vector to each face is found using the center of the face.

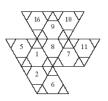




Truncated Icosahedron

- The truncated icosahedron (soccer ball) consists of regular hexagons and pentagons.
- More recently this shape has been named the Buckyball after Buckminster Fuller, because of his interest in geodesic structures similar to this.





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Prisms

- A prism is formed by moving a regular polygon along a straight line.
- When the line is perpendicular to the polygon, the prism is a right prism.







