Computer Graphics

Transformations of Objects
Ch5 Sec 6

Drawing 3D Shapes in OpenGL

- GLUT provides several 3D objects: a sphere, a cone, a torus, the five Platonic solids, and the teapot.
- Each is available as a **wireframe** model (one appearing as a collection of wires connected end to end) and as a solid model with faces that can be shaded.
- All are drawn by default centered at the origin.
- To use the solid version, replace Wire by Solid in the functions.

Drawing 3D Shapes in OpenGL (2)

- **cube:** glutWireCube (GLdouble size);
  - Each side is of length size.
- **sphere:** glutWireSphere (GLdouble radius, GLint nSlices, GLint nStacks);
  - nSlices is the number of "orange sections" and nStacks is the number of disks.
  - Alternately, nSlices boundaries are longitude lines and nStacks boundaries are latitude lines.

Drawing 3D Shapes in OpenGL (3)

- **torus:** glutWireTorus (GLdouble inRad, GLdouble outRad, GLint nSlices, GLint nStacks);
- **teapot:** glutWireTeapot (GLdouble size);
  - Why teapots? A standard graphics challenge for a long time was both making a teapot look realistic and drawing it quickly.

Drawing 3D Shapes in OpenGL (4)

- **tetrahedron:** glutWireTetrahedron ();
- **octahedron:** glutWireOctahedron ();
- **dodecahedron:** glutWireDodecahedron ();
- **icosahedron:** glutWireIcosahedron ();
- **cone:** glutWireCone (GLdouble baseRad, GLdouble height, GLint nSlices, GLint nStacks);

Drawing 3D Shapes in OpenGL (5)

- **tapered cylinder:** gluCylinder (GLUquadricObj * qobj, GLdouble baseRad, GLdouble topRad, GLdouble height, GLint nSlices, GLint nStacks);
- The **tapered cylinder** is actually a *family* of shapes, distinguished by the value of topRad.
  - When topRad is 1, there is no taper; this is the classic **cylinder**.
  - When topRad is 0, the tapered cylinder is identical to the **cone**.

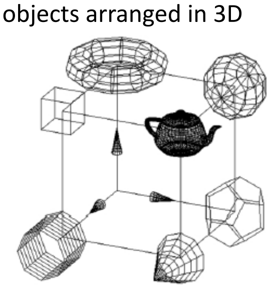
Drawing 3D Shapes in OpenGL (6)

- To draw the tapered cylinder in OpenGL, you must
  1. define a new quadric object,
  2. set the drawing style (GLU_LINE: wireframe, GLU_FILL: solid), and
  3. draw the object:

```
GLUquadricObj * qobj = gluNewQuadric ();
   // make a quadric object
gluQuadricDrawStyle (qobj,GLU_LINE);
   // set style to wireframe
gluCylinder (qobj, baseRad, topRad, nSlices, nStacks);
 // draw the cylinder
```

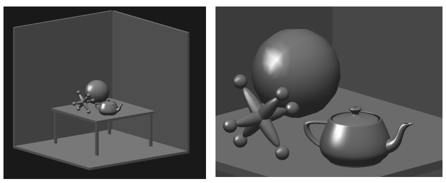

Demo Example

- Quadric objects with display list
- glu objects arranged in 3D



Demo
Solid 3D Drawing in OpenGL

- A solid object scene is rendered with shading. The light produces highlights on the sphere, teapot, and jack.



Solid 3D Drawing in OpenGL (2)

- The scene contains three objects resting on a table in the corner of a room.
- The three walls are made by flattening a cube into a thin sheet and moving it into position.
- The jack is composed of three stretched spheres oriented at right angles plus six small spheres at their ends.

Solid 3D Drawing in OpenGL (3)

- The table consists of a table top and four legs.
- Each of the table's five pieces is a cube that has been scaled to the desired size and shape (next slide).
- The table is based on four parameters that characterize the size of its parts: topWidth, topThick, legLen, and legThick.

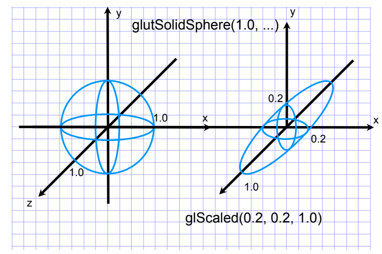
Solid 3D Drawing in OpenGL (4)

- A routine tableLeg() draws each leg and is called four times within the routine table() to draw the legs in the four different locations.
- The different parameters used produce different modeling transformations within tableLeg(). As always, a glPushMatrix(), glPopMatrix() pair surrounds the modeling functions to isolate their effect.

Code for the Solid Example

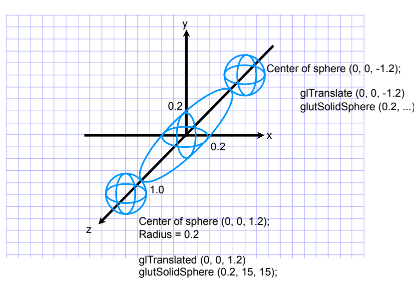
- The solid version of each shape, such as glutSolidSphere(), is used.
- To create shaded images, the position and properties of a light source and certain properties of the objects' surfaces must be specified, in order to describe how they reflect light (Ch. 8).
- We just present the various function calls here; using them as shown will generate shading.

Jack on Table Example

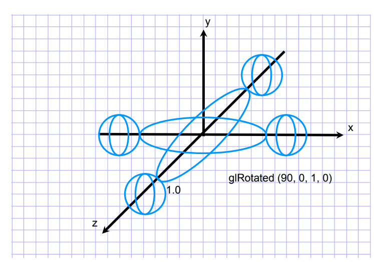


Solid sphere centered at origin

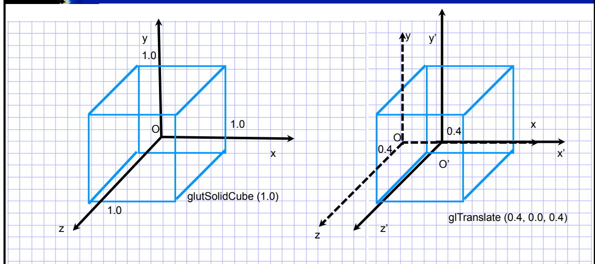
Jack on Table Example



Jack on Table Example



Jack on Table Example



Solid cube centered at origin

Draw Table Top

Jack on Table Example

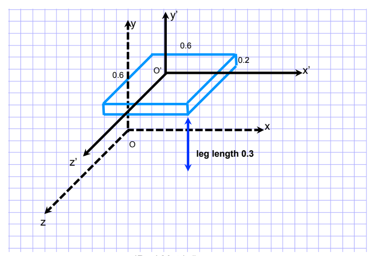


Table Width = 0.6
Table Thickness = 0.02

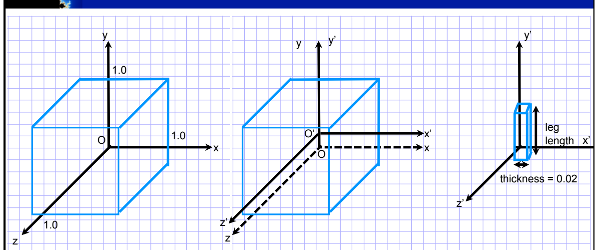
Table Top

```
glPushMatrix()

glTranslated (0, 0.3, 0)  // O' raised 0.3 from 0 along y
glScaled(0.6, 0.02, 0.6)  // O' (0.4, 0.3, 0.4)
glutSolidCube (1.0)

glPopMatrix()
```


Jack on Table Example



glSolidCube (1.0)

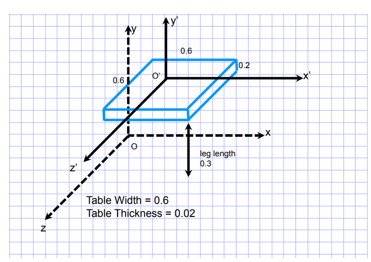
glTranslate(0, len/2, 0)

glScaled(0.02, 0.3, 0.02)

Leg Thickness = 0.02
Leg Length = 0.3

Draw Table Leg

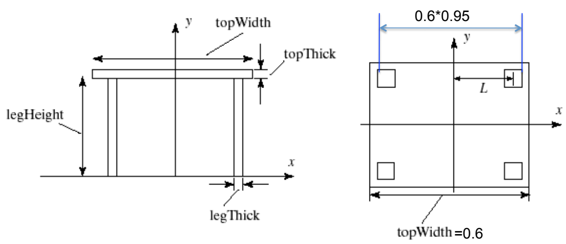
Jack on Table Example



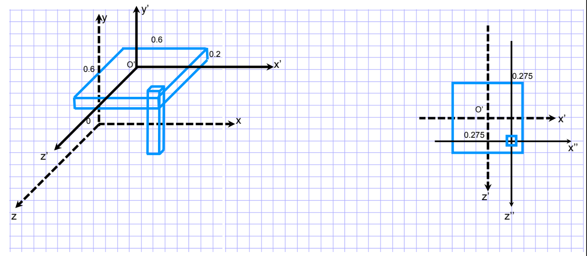

```
pushMatrix
glTranslated (0, 0.3, 0)
glScaled(0.6, 0.02, 0.6)
glutSolidCube (1.0)
popMatrix
```

Assemble The Table (draw table)

Table Construction



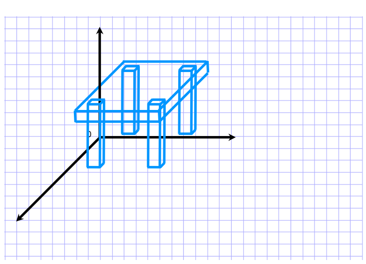
Jack on Table Example



pushMatrix
dist = 0.6 * 0.95 / 2 - 0.02 / 2.0 = 0.275
glTranslated (0.275, 0, 0.275)
DrawTableLeg(0.02, 3.0)

pushMatrix
glTranslated(0, len/2, 0)
glScaled(0.02, len, 0.02)
glutSolidCube(1.0)
popMatrix

Jack on Table Example



Assembled Table

dist = 0.275

glTranslated(0, 0, -2*dist)
DrawTableLeg(0.02, 0.3)

glTranslated(-2*dist, 0, 2*dist)
DrawTableLeg(0.02, 0.3)

glTranslated(0, 0, -2*dist)
DrawTableLeg(0.02, 0.3)

Scene Description Language (SDL)

- Previous scenes were described through specific OpenGL calls that transform and draw each object, as in the following code:
  - glTranslated (0.25, 0.42, 0.35);
  - glutSolidSphere (0.1, 15, 15);
  - // draw a sphere
- The objects were “hard-wired” into the program. This method is cumbersome and error-prone.

SDL (2)

- We want the designer to be able to specify the objects in a scene using a simple language and place the description in a file.
- The drawing program becomes a general-purpose program:
  - It reads a scene file at run-time and draws whatever objects are encountered in the file.

Example SDL Scene

```
! example.dat: simple scene: 1 light and 4 shapes
! beginning ! is a comment; extends to end of line
background 0 0 1        ! create a blue background
light 2 9 8 1 1 1       ! put a white light at (2, 9, 8)
diffuse .9 .1 .1        ! make following objects reddish
translate 3 5 –2 sphere    ! put a sphere at 3 5 –2
translate –4 –6 8  cone    ! put a cone in the scene
translate  1 1 1 cube            ! add a cube
diffuse 0 1 0           ! make following objects green
translate 40 5 2 scale .2 .2 .2 sphere   ! tiny sphere
```


The SDL Scene

- The scene has a bright blue background color (*red*, *green*, *blue*) = (0, 0, 1), a bright white (1, 1, 1) light situated at (2, 9, 8), and four objects: two spheres, a cone and a cube.
- The light field points to the list of light sources, and the obj field points to the object list.
- Each shape object has its own affine transformation *M* that describes how it is scaled, rotated, and positioned in the scene. It also contains various data fields that specify its material properties. Only the diffuse field is shown in the example.

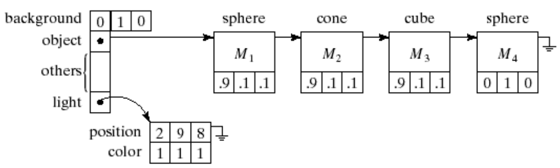
Using SDL

- The **Scene Description Language (SDL)**, provides a Scene class that supports the reading of an SDL file and the drawing of the objects described in the file.
- A <u>global</u> Scene object is created:

  `Scene scn; // create a scene object`
- Read in a scene file using the read method of the class:

  `scn.read("example.dat");  // read the scene file & build an object list`

SDL Data Structure



The SDL Scene (2)

- Once the light list and object list have been built, the application can render the scene:
  scn.makeLightsOpenGL(),
  scn.drawSceneOpenGL(); // render scene with OpenGL
- The first instruction passes a description of the light sources to OpenGL. The second uses the method drawSceneOpenGL() to draw each object in the object list.
- The code for this method is very simple:

```
void Scene :: drawSceneOpenGL()
{
    for(GeomObj* p = obj; p ; p = p->next)
        p->drawOpenGL(); // draw it
}
```


The SDL Scene (3)

- The function moves a pointer through the object list, calling drawOpenGL() for each object in turn.
- Each different shape can draw itself; it has a method drawOpenGL() that calls the appropriate routine for that shape.
- Each first passes the object's material properties to OpenGL, then updates the modelview matrix with the object's specific affine transformation.
- The original modelview matrix is pushed and later restored to protect it from being affected after this object has been drawn.

Examples of Objects which can Draw Themselves

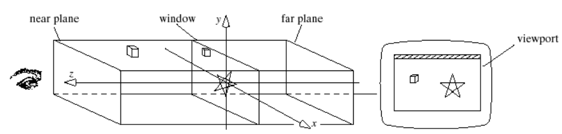
```
void Sphere :: drawOpenGL()
{
  tellMaterialsGL();  //pass material data to OpenGL
  glPushMatrix();
  glMultMatrixf(transf.m); // load this object's matrix
  glutSolidSphere(1.0,10,12); // draw a sphere
  glPopMatrix();
}
void Cone :: drawOpenGL()
{
  tellMaterialsGL();//pass material data to OpenGL
  glPushMatrix();
  glMultMatrixf(transf.m); // load this object's matrix
  glutSolidCone(1.0,1.0, 10,12); // draw a cone
  glPopMatrix();
}
```

Drawing 3D Scenes in OpenGL

- We want to transform objects in order to orient and position them as desired in a 3D scene.
- OpenGL provides the necessary functions to build and use the required matrices.
- The matrix stacks maintained by OpenGL make it easy to set up a transformation for one object, and then return to a previous transformation, in preparation for transforming another object.

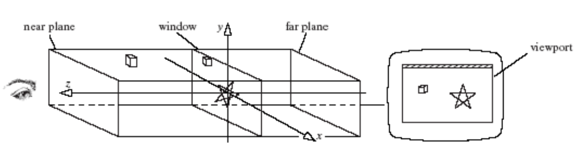
The Viewing Process and the Graphics Pipeline

- The 2D drawing so far is a special case of 3D viewing, based on a simple parallel projection.
- The eye is looking along the z-axis at the world window, a rectangle in the *xy*-plane.



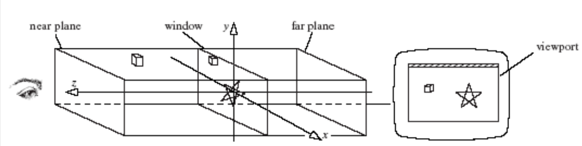
The Viewing Process and the Graphics Pipeline (2)

- *Eye* is simply a point in 3D space.
- The "orientation" of the eye ensures that the view volume is in front of the eye.
- Objects closer than *near* or farther than *far* are too blurred to see.



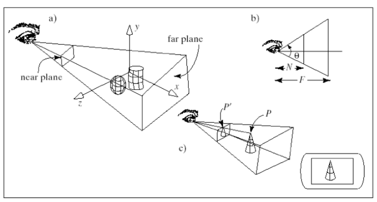
The Viewing Process and the Graphics Pipeline (3)

- The **view volume** of the camera is a rectangular parallelepiped (Orthographic Projection)
- Its side walls are fixed by the window edges; its other two walls are fixed by a **near plane** and a **far plane**.



The Viewing Process and the Graphics Pipeline (4)

- The **view volume** of the camera using Perspective Projection (to be discussed later)
- Its side walls are fixed by the window edges; its other two walls are fixed by a **near plane** and a **far plane**.

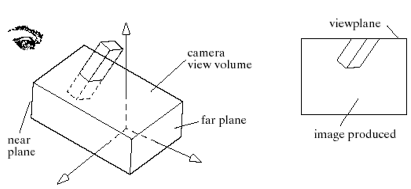


The Viewing Process and the Graphics Pipeline (5)

- Points inside the view volume are projected onto the window along lines parallel to the z-axis.
- We ignore their z-component, so that the 3D point (x_1 y_1, z_1) projects to (x_1, y_1, 0).
- Points lying outside the view volume are clipped off.
- A separate **viewport transformation** maps the projected points from the window to the viewport on the display device.

The Viewing Process and the Graphics Pipeline (6)

- In 3D, the only change we make is to allow the camera (eye) to have a more general position and orientation in the scene in order to produce better views of the scene.

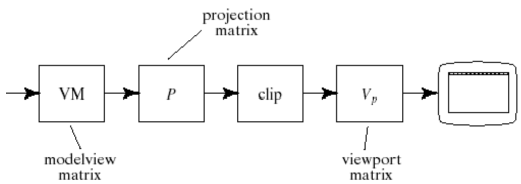


The Viewing Process and the Graphics Pipeline (7)

- The z axis points *toward* the eye. X and y point to the viewer's right and up, respectively.
- Everything outside the view volume is clipped.
- Everything inside it is projected along lines parallel to the axes onto the window plane (parallel projection).

The Viewing Process and the Graphics Pipeline (8)

- OpenGL provides functions for defining the view volume and its position in the scene, using matrices in the graphics pipeline.



The Viewing Process and the Graphics Pipeline (9)

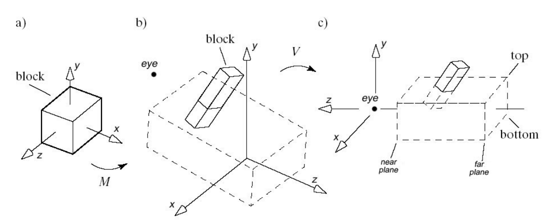
- Each vertex of an object is passed through this pipeline using glVertex3d(x, y, z).
- The vertex is multiplied by the various matrices, clipped if necessary, and if it survives, it is mapped onto the viewport.
- Each vertex encounters three matrices:
  - The **modelview matrix;**
  - The **projection matrix;**
  - The **viewport matrix;**

The Modelview Matrix

- The **modelview matrix** is the *CT* (current transformation).
- It combines modeling transformations on objects and the transformation that orients and positions the camera in space (hence *modelview*).
- It is a single matrix in the actual pipeline.
  - For ease of use, we will think of it as the product of two matrices: a modeling matrix *M*, and a viewing matrix *V*. The modeling matrix is applied first, and then the viewing matrix, so the modelview matrix is in fact the product *VM.*

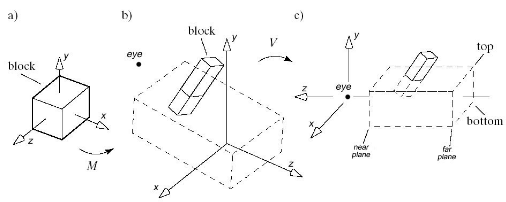
The Modelview Matrix

- A modeling transformation *M* scales, rotates, and translates the cube into the block.



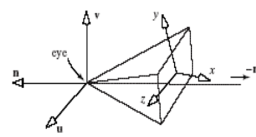
The Modelview Matrix (V)

- The camera moves from its position in the scene to its generic position (eye at the origin and the view volume aligned with the *z*-axis).
- The coordinates of the block's vertices are changed so that projecting them onto a plane (e.g., the near plane) displays the projected image properly.



The Modelview Matrix (V)

- The matrix *V* changes the coordinates of the scene vertices into the **camera's coordinate system,** or into **eye coordinates**.
- To inform OpenGL that we wish it to operate on the modelview matrix we call glMatrixMode(GL_MODELVIEW);



Setting Up the Scene

```
glMatrixMode (GL_MODELVIEW);
   // set up the modelview matrix
glLoadIdentity ();
   // initialize modelview matrix
   // set up the view part of the matrix
   // do any modeling transformations on the scene
```

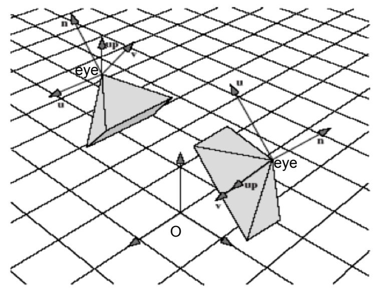

Setting Up the Camera (View Matrix)

```
glMatrixMode (GL_MODELVIEW);
   // make the modelview matrix current
glLoadIdentity();
   // start with identity matrix
   // position and aim the camera
gluLookAt (eye.x, eye.y, eye.z,    // eye position
   look.x, look.y, look.z,     // the "look at" point
    0, 1, 0)   // approximation to true up direction
   // Now do the modeling transformations
```

Setting Up the Camera (2)

- What gluLookAt does is create a camera coordinate system of three mutually orthogonal unit vectors: **u**, **v**, and **n.**
- **n** = eye - look; **u** = **up** x **n**; **v** = **n** x **u**
- Normalize **n**, **u**, **v** (in the camera system) and
- let **e** = eye - O in the camera system, where O is the origin.

The effect of gluLookAt



Setting Up the Camera (3)

- Then gluLookAt () sets up the view matrix

$$V = \begin{pmatrix} u_x & u_y & u_z & d_x \\ v_x & v_y & v_z & d_y \\ n_x & n_y & n_z & d_z \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

where **d** = (-**e**·**u**, -**e**·**v**, -**e**·**n**)

- **up** is usually (0, 1, 0) (along the y-axis), *look* is frequently the middle of the window, and *eye* frequently looks down on the scene.

Practice Question

- Given: gluLookAt (4, 4, 4, 0, 1, 0, 0, 1, 0);

What is the View matrix V?

Steps:

1. Compute vectors n, u, v
2. Normalize n, u, v
3. Compute vector: **e** = eye – O

   d = (-**e**·**u**, -**e**·**v**, -**e**·**n**)
4. Put the view matrix together

Practice Question

$$\mathbf{n} = eye - look = (4, 3, 4)$$

$$\mathbf{u} = \mathbf{up} \times \mathbf{n} = \begin{vmatrix} \mathbf{i} & \mathbf{j} & \mathbf{k} \\ 0 & 1 & 0 \\ 4 & 3 & 4 \end{vmatrix} = (4, 0, -4)$$

$$\mathbf{v} = \mathbf{n} \times \mathbf{u} = (-12, 32, -12)$$

Normalize **u**, **v**, and **n**,

$\mathbf{n} = (0.6247, 0.4685, 0.6247)$

$\mathbf{u} = (0.70711, 0, -0.70711)$

$\mathbf{v} = (-0.3313, 0.8834, -0.3313)$

$dx = -\mathbf{eye}.\mathbf{u} = (-4, -4, -4) . (0.70711, 0, -0.70711) = 0$

$dy = -\mathbf{eye}.\mathbf{v} = (-4, -4, -4) . (-0.3313, 0.8834, -0.3313) = -0.88345$

$dz = -\mathbf{eye}.\mathbf{n} = (-4, -4, -4) . (0.6247, 0.4685, 0.6247) = -6.872$

So that,

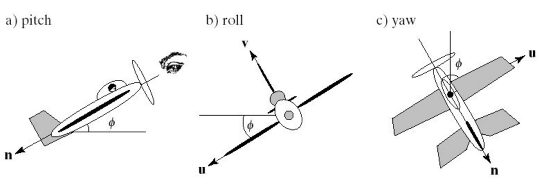
$$V = \begin{pmatrix} .70711 & 0 & -.70711 & 0 \\ -.3313 & .88345 & -.3313 & -.88345 \\ .6247 & .4685 & .6247 & -6.872 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

Setting Up the Camera

- We shall use a **jib camera**.
- The photographer rides at the top of the tripod.
- The camera moves through the scene bobbing up and down to get the desired shots.

Changing Camera Orientation

- We can think of the jib camera as behaving like an airplane.
  - It can pitch, roll, or yaw from its position.



Changing Camera Orientation (2)

- **Pitch** – the angle between the longitudinal axis and world horizontal.
- **Roll –** the angle between the transverse axis and the world.
- **Yaw –** motion of the longitudinal axis causing a change in the direction of the plane's flight.

The Viewing Process and the Graphics Pipeline

- OpenGL provides functions for defining the view volume and its position in the scene, using matrices in the graphics pipeline.