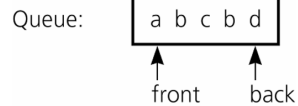


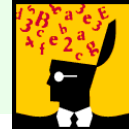
Queue

- ❑ FIFO: first in first out
- ❑ Operations on a queue occur only at its two ends: front and back (rear)
- ❑ Application:
 - Waiting line
 - Simulations



What is coming

- ❑ Queue applications
- ❑ Implementation of Queue
 - Pointer-based Q
 - Array-based Q



UML diagram for the class Queue

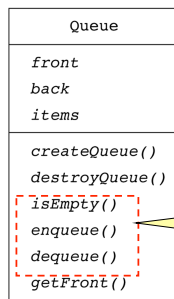


Figure 7-2: Some queue operations

Operation	Queue after operation
aQueue.createQueue()	front
aQueue.enqueue(5)	5
aQueue.enqueue(2)	5 2
aQueue.enqueue(7)	5 2 7
aQueue.getFront(queueFront)	5 2 7 (queueFront is 5)
aQueue.dequeue(queueFront)	5 2 7 (queueFront is 5)
aQueue.dequeue(queueFront)	2 7 (queueFront is 2)

```

class Queue {
public:
    Queue(); // default constructor
    Queue(const Queue& Q); // copy constructor
    ~Queue(); // destructor
    bool isEmpty() const;
    void enqueue(QueueItemType newItem);
    void dequeue();
    void dequeue(QueueItemType& queueFront);
    void getFront(QueueItemType& queueFront) const;
private:
    struct QueueNode {
        QueueItemType item;
        QueueNode *next;
    }; // end struct
    QueueNode *frontPtr;
    QueueNode *backPtr;
}; // end class
  
```

Application of Queue

- ❑ Reading String of characters
- ❑ Recognizing palindromes

Example 1: Reading String of characters

```

□ Converts digits in a queue into a decimal integer result
Queue may store leading whitespaces
// 247 = 2*100 + 4*10 + 7 = 10*(10*2 + 4) + 7
do { // skip leading blanks
    aQueue.dequeue(ch)
} while (ch is blank)
result = 0 // result to be stored
done = false
do {
    result = 10*result + int(ch-'0')
    if (!aQueue.isEmpty())
        aQueue.dequeue(ch)
    else
        done = true
} while (!done and ch is a digit)

```

Example 2: Recognizing palindrome

Use both a queue and a stack

```

isPal (in str:string): boolean
aQ.createQueue ()
aStack.createStack ()
length = length of str
for (i=1 though length) {
    aQ.enqueue(ith character of str)
    aStack.push(ith character of str)
}
isEqual = true
while (!aQ.isEmpty() and isEqual) {
    aQ.getFront(qFront)
    aStack.getTop(stackTop)
    if (qFront equals stackTop) {
        aQ.dequeue ()
        aStack.pop ()
    } else
        isEqual = false
}
return isEqual

```

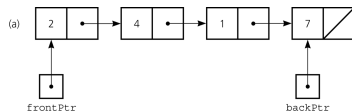
String: abcbd

Queue: a b c b d
front back

Stack: d b c b a
top

Pointer-based implementation

- Linear linked list with two external pointer
- Insert at the back and delete from the front

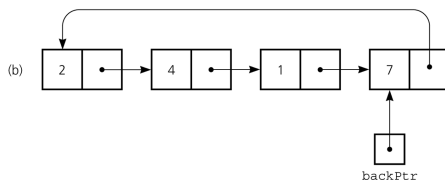


```

class Queue {
public:
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    void dequeue(QueueItemType& queueFront);
    void getFront(QueueItemType& queueFront) const;
private:
    struct QueueNode {
        QueueItemType item;
        QueueNode *next;
    }; // end struct
    QueueNode *frontPtr;
    QueueNode *backPtr;
}; // end class

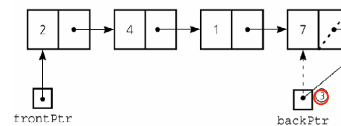
```

A pointer-based implementation of a queue:
a circular linear linked list with one external pointer



Back is backPtr
Front is backPtr->next

Inserting an item into a nonempty queue



1. newPtr->next = NULL;
2. backPtr->next = newPtr;
3. backPtr = newPtr;

Inserting an item into an empty queue:
 (a) before insertion;
 — (b) after insertion

(a)

frontPtr

backPtr

Deleting an item from a queue of more than one item

1. tempPtr = frontPtr;
2. frontPtr = frontPtr->next;
3. tempPtr->next = NULL;
4. Delete tempPtr;

Queue: array-based implementation

- If fixed sized queue is not a problem → array
- A naive array-based implementation of a queue
- Rightward drift can cause the queue to appear full

Queue: array-based Q

- Naïve array-based implementation
 - front = 0; back = -1; when empty
 - enQ :
 - back++;
 - items[back];
 - deQ : front++;
 - if (back < front) → empty
 - if (back == maxQ - 1) → full
 - → right drift

Queue: array-based Q

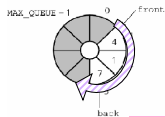
- Solution 1:
 - shift array element
 - Too expensive: it would dominate the cost of the implementation

Queue: array-based Q

- Solution 2: use circular array
 - deQ → $(++front) \% \text{maxQ}$
 - enQ → $(++back) \% \text{maxQ}$

How do we detect Q empty or full?

The effect of some operations of the queue



dequeue

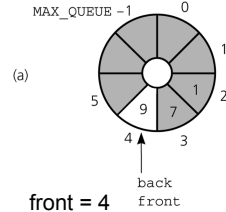
Enqueue 9

front = 1
back = 3

front = 2
back = 3

front = 2
back = 4

Queue with single item



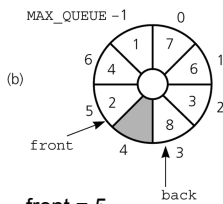
front = 4
back = 4

front passes back when the queue becomes empty
front = 5 and back = 4

Is this full or empty?



Queue with single empty slot



front = 5
back = 3

back catches up to front when the queue becomes full
front = 5 and back = 4

Array-based Q (Circular array)

If front is one slot ahead of back, is Q full or empty?

- Keep a count of the number of items in the Q

- new empty Q: front = 0; back = maxQ - 1; size = 0;
- Check the size before deleting or inserting an item

- Enqueue:

if (size < maxQ) { // not full

back = (back + 1) % maxQ;

items[back] = newItem;

++size;

}

- Dequeue:

if (size > 0) { // not empty

front = (front + 1) % maxQ;

--size;

}

Array-based Q (Circular array)

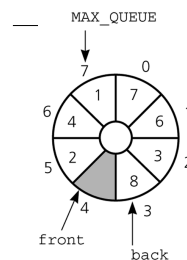
If front is one slot ahead of back, is Q full or empty?

- Use only maxQ element with maxQ+1 size array

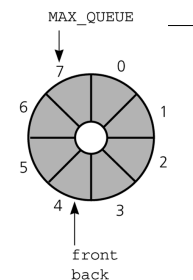
- Sacrifice one element and make front (actual front-1)
- full : if front == (back+1) % (maxQ+1)
- empty : if front == back

- No need for keeping track of queue size

Use MAX_QUEUE-1 number of elements in the array.
Sacrifice one element, front is (actual front-1)



A full queue



An empty queue