

Data Mining



Feed Forward Neural Networks

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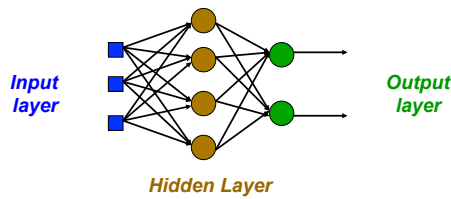
Outline

- Multi-layer Neural Networks
- Feedforward Neural Networks
 - FF NN model
 - Backpropagation (BP) Algorithm
 - Practical Issues of FFNN

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Multi-layer NN

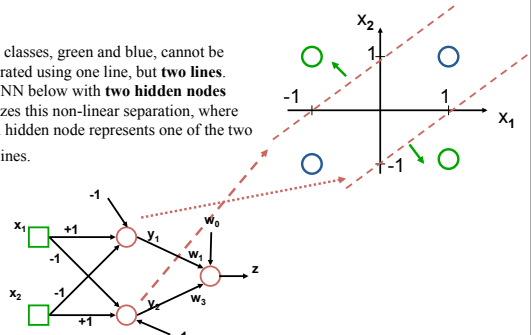
- Between the input and output layers there are hidden layers, as illustrated below.
 - Hidden nodes do not directly send outputs to the external environment.
- Multi-layer NN overcome the limitation of a single-layer NN
 - they can handle non-linearly separable learning tasks.



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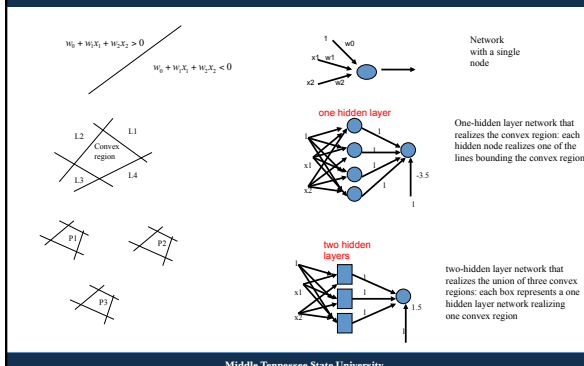
XOR problem

Two classes, green and blue, cannot be separated using one line, but **two lines**. The NN below with **two hidden nodes** realizes this non-linear separation, where each hidden node represents one of the two red lines.



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Types of decision regions



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Types of decision regions

Structure	Types of Decision Regions	Exclusive-OR Problem	Class Separation	Most General Region Shapes
Single-Layer	Half Plane Bounded By Hyperplane			
Two-Layer	Convex Open Or Closed Regions			
Three-Layer	Arbitrary (Complexity Limited by No. of Nodes)			

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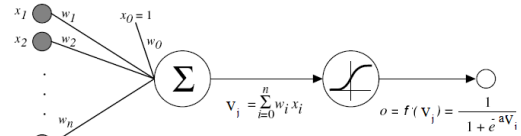
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- Multi-layer Neural Networks
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 - BP rules derivation
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FFNN NEURON MODEL

- The classical learning algorithm of FFNN is based on the gradient descent method.
- The activation function used in FFNN are continuous functions of the weights, differentiable everywhere.
 - A typical activation function is the Sigmoid Function



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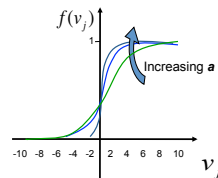
Activation Function

- A typical activation function is the Sigmoid Function:

$$f(v_j) = \frac{1}{1 + e^{-av_j}} \quad \text{with } a > 0$$

$$\text{where } v_j = \sum_i w_{ji} y_i$$

with w_{ji} weight of link from node i to node j and y_i output of node i



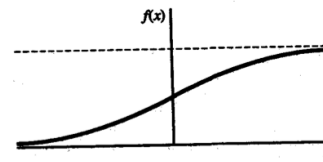
- when a approaches to 0, f tends to a linear function
- when a tends to infinity then f tends to the step function

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Binary Sigmoid Activation Function

$$f(x) = \frac{1}{1 + e^{(-x)}}$$

$$f'(x) = f(x)[1 - f(x)]$$



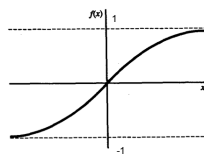
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Bipolar Sigmoid Activation Function

$$f(x) = \frac{2}{1 + e^{(-x)}} - 1$$

Preferred

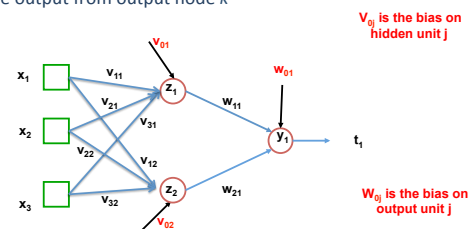
$$f'(x) = \frac{1}{2} [1 + f(x)][1 - f(x)]$$



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FFNN MODEL

- v_{ij} : The weight from input node i to hidden layer node j
 - Δv_{ij} : The weight updating amount from node i to node j
- w_{kj} : The weight from hidden layer node j to output node k
 - Δw_{kj} : The weight updating amount from node j to node k
- t_k : The output from output node k



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The objective of multi-layer NN

- The **error of output neuron j** after the activation of the network on the n -th training example $(x(n), d(n))$ is:

$$e_j(n) = d_j(n) - o_j(n)$$

- The **network error** is the sum of the squared errors of the output neurons:

$$E(n) = \frac{1}{2} \sum_{j \text{ output node}} e_j^2(n)$$

- The **total mean squared error** is the average of the network errors over the training examples.

$$E(W) = \frac{1}{N} \sum_{n=1}^N E(n)$$

$$E(W) = \frac{1}{2N} \sum_n \sum_j (d_j(n) - o_j(n))^2$$

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Feed Forward NN

Idea: Credit assignment problem

- Problem of assigning 'credit' or 'blame' to individual elements involving in forming overall response of a learning system (hidden units)
- In neural networks, problem relates to distributing the network error to the weights.

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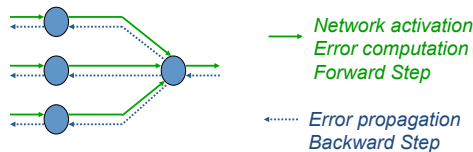
Training: Backprop algorithm

- Searches for weight values that **minimize the total error of the network** over the set of training examples.
- Repeated** procedures of the following two passes:
 - Forward pass:** Compute the **outputs** of all units in the network, and the **error** of the output layers.
 - Backward pass:** The network error is used for updating the weights (**credit assignment problem**).
 - Starting at the output layer, **the error is propagated backwards through the network, layer by layer**. This is done by recursively computing the local gradient of each neuron.

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Backprop

- Back-propagation training algorithm illustrated:



- Backprop adjusts the weights of the NN in order to minimize the network total mean squared error.

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Back Propagation

Initialize all weights to small random numbers.

While (E(W) **unsatisfactory** & **Itera** < **Max_Iteration**)

- For each training example, Do

- Input the training example to the network and compute the network outputs
- For each output unit k

$$\delta_k \leftarrow o_k(1 - o_k)(d_k - o_k)$$

- For each hidden unit h

$$\delta_h \leftarrow o_h(1 - o_h) \sum_{k \in \text{outputs}} w_{h,k} \delta_k$$

- Update each network weight $w_{i,j}$

$$w_{i,j} \leftarrow w_{i,j} + \Delta w_{i,j}$$

where

$$\Delta w_{i,j} = \eta \delta_j x_{i,j}$$

EndFor

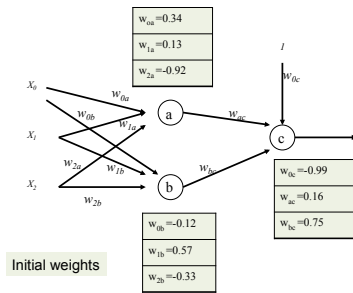
EndWhile

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Back Propagation Example

• XOR

X_0	X_1	X_2	Y
1	0	0	0
1	0	1	1
1	1	0	1
1	1	1	0



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Back Propagation Example

 $\eta=0.5$; $\sigma_x = 1/(1 + e^{-x})$; For instance $\{(1, 0, 0), 0\}$

Neuro a		Neuro b		Neuro c	
$w_{0a}=0.34$	$v_a=0.34$	$w_{0b}=-0.12$	$v_b=-0.12$	$w_{0c}=-0.99$	$v_c=-0.54$
$w_{1a}=0.13$	$\sigma_a=0.58$	$w_{1b}=0.57$	$\sigma_b=0.47$	$w_{1c}=0.16$	$\sigma_c=0.37$
$w_{2a}=-0.92$		$w_{2b}=-0.33$		$w_{2c}=0.75$	
$\delta_a = \sigma_a(1-\sigma_a) \sum w_{ac} \delta_c$ $= 0.58 * (1-0.58) * 0.16 * (-0.085)$ $= -0.003$				$\delta_c = \sigma_c(1-\sigma_c) y(d_c - \sigma_c)$ $= 0.37 * (1-0.37) * (0-0.37)$ $= -0.085$	
$\Delta w_{0a} = \eta \delta_a x_0 = 0.5 * (-0.003) * 1$ $= -0.015$				$\Delta w_{0c} = \eta \delta_c x_0 = 0.5 * (-0.085) * 1$ $= -0.043$	

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Back Propagation Example

Neuro a	Neuro b	Neuro c
$w_{0a} = w_{0a} + \Delta w_{0a} = 0.34 - 0.015$ $= 0.325$		
$w_{1a} = w_{1a} + \Delta w_{1a} = 0.13 + 0$		
$w_{2a} = w_{2a} + \Delta w_{2a} = -0.92 + 0$		
$\Delta w_{0a} = \eta \delta_a x_0 = 0.5 * (-0.003) * 1$ $= -0.015$		$\Delta w_{0c} = \eta \delta_c x_0 = 0.5 * (-0.085) * 1$ $= -0.043$
$\Delta w_{1a} = \eta \delta_a x_1 = 0.5 * (-0.003) * 0 = 0$		
$\Delta w_{2a} = \eta \delta_a x_2 = 0.5 * (-0.003) * 0 = 0$		

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Network training:

- Two types of training:
 - **Incremental mode** (on-line, stochastic, or per-observation) Weights updated after each instance is presented
 - **Batch mode** (off-line or per -epoch) Weights updated after all the patterns are presented

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Stopping criterions

- **Sensible stopping criterions:**
 - **total mean squared error change:** Back-prop is considered to have converged when the absolute rate of change in the average squared error per epoch is sufficiently small (in the range [0.01, 0.1]).
 - **generalization based criterion:** After each epoch the NN is tested for generalization using a different set of examples (validation set). If the generalization performance is adequate then stop.

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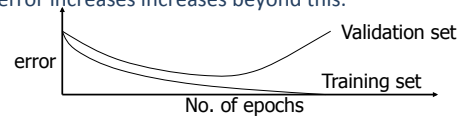
Use of Available Data Set for Training

- The available data set is normally split into three sets as follows:
 - Training set** – use to update the weights. Patterns in this set are repeatedly in random order. The weight update equation are applied after a certain number of patterns.
 - Validation set** – use to decide when to stop training only by monitoring the error.
 - Test set** – Use to test the performance of the neural network. It should not be used as part of the neural network development cycle.

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Earlier Stopping - Good Generalization

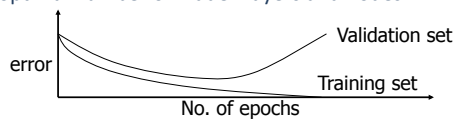
- Running too many epochs may **overtrain** the network and result in **overfitting** and perform poorly in generalization.
- Keep a hold-out validation set and test accuracy after every epoch. Maintain weights for best performing network on the validation set and stop training when error increases beyond this.



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Model Selection by Cross-validation

- Too few hidden units** prevent the network from learning adequately fitting the data and learning the concept.
- Too many hidden units** leads to overfitting.
- Similar **cross-validation methods** can be used to determine an appropriate number of hidden units by using the optimal test error to select the model with optimal number of hidden layers and nodes.



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NN DESIGN

- Data representation**
- Network Topology**
- Network Parameters**
- Training**

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Data Representation

- Data representation **depends on the problem**. In general NNs work on **continuous (real valued) attributes**. Therefore symbolic attributes are encoded into continuous ones.
- Attributes of different types may have different ranges of values which affect the training process. **Normalization** may be used, like the following one which scales each attribute to assume values between 0 and 1.

$$x_i = \frac{x_i - \min_i}{\max_i - \min_i}$$

for each value x_i of attribute i , where \min_i and \max_i are the minimum and maximum value of that attribute over the training set.

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Network Topology

- The number of layers and neurons depend on the specific task**. In practice this issue is solved by trial and error.
- Two types of adaptive algorithms can be used:**
 - start from a large network and successively remove some neurons and links until network performance degrades.
 - begin with a small network and introduce new neurons until performance is satisfactory.

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Network parameters

- How are the weights initialized?
- How is the learning rate chosen?
- How many hidden layers and how many neurons?
- How many examples in the training set?

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Initialization of weights

- In general, initial weights are randomly chosen, with typical values between -1.0 and 1.0 or -0.5 and 0.5.
- If some inputs are much larger than others, random initialization may bias the network to give much more importance to larger inputs. In such a case, weights can be initialized as follows:

$$w_{ij} = \pm \frac{1}{2m} \sum_{l=1, \dots, m} \frac{1}{|x_l|}$$

For weights from the input to the first layer

$$w_{jk} = \pm \frac{1}{2n} \sum_{l=1, \dots, n} \frac{1}{q(\sum_i w_{ij} x_l)}$$

For weights from the first to the second layer

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Choice of learning rate

- The right value of η depends on the application. Values between 0.1 and 0.9 have been used in many applications.

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Size of Training set

- **Rule of thumb:**
 - the number of training examples should be at least five to ten times the number of weights of the network.
- **Other rule:**

$$N > \frac{|W|}{(1-a)}$$

$|W|$ = number of weights
 a = expected accuracy

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Applications of FFNN

Classification, pattern recognition:

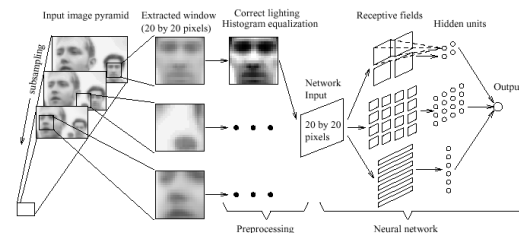
- FFNN can be applied to tackle non-linearly separable learning tasks.
 - Recognizing printed or handwritten characters
 - Face recognition
 - Classification of loan applications into credit-worthy and non-credit-worthy groups
 - Analysis of sonar radar to determine the nature of the source of a signal
 - Speech Recognition

Regression and forecasting:

- FFNN can be applied to learn non-linear functions (regression) and in particular functions whose inputs is a sequence of measurements over time (time series).

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Neural Net Based Face Detection



- Large training set of faces and small set of non-faces
- Training set of non-faces automatically built up:
 - Set of images with no faces
 - Every 'face' detected is added to the non-face training set.

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