A Verified Garbage Collector for Gallina

Shengyi Wang[†], <u>Anshuman Mohan</u>[†], Qinxiang Cao[‡], Aquinas Hobor[†]





APLAS NIER December 1, 2019

Broad Problem

Verify graph-manipulating programs written in executable C with machine-checked correctness proofs

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Hard, but ubiquitous in critical areas

Broad Solution





Certifying Graph-Manipulating C Programs via Localizations within Data Structures

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VST + CompCert + 25000 LOC library

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[Wang et. al., PACMPL OOPSLA 2019]





Gallina \leadsto CompCert C \leadsto Assembly





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Gallina assumes infinite memory but CompCert C has a finite heap





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Solution: garbage collect the CompCert C code





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Gallina assumes infinite memory but CompCert C has a finite heap

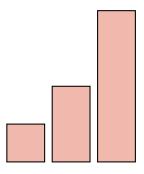
Solution: garbage collect the CompCert C code

New problem: verify the garbage collector

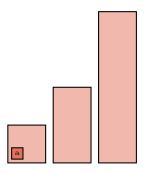
GC has jurisdiction over the heap



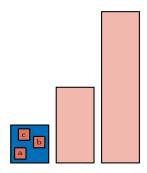
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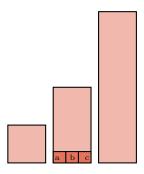
GC has jurisdiction over the heap Mutator allocs in special subheap



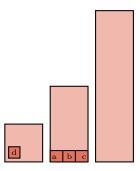
GC has jurisdiction over the heap Mutator allocs in special subheap If subheap is full



GC has jurisdiction over the heap Mutator allocs in special subheap If subheap is full call GC



GC has jurisdiction over the heap Mutator allocs in special subheap If subheap is full call GC and try again



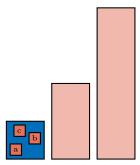
- 12 generations, doubling in size
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- 12 generations, doubling in size
- Functional mutator: no back pointers
- Cheney's mark-and-copy collects gen to next
- Potentially triggers cascade of pairwise collections
- Three key functions:
 - forward copies individual objects
 do_scan repairs copied objects
 forward_roots kick-starts the collection

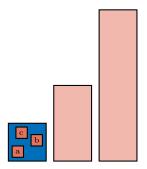
Intuitive Specification

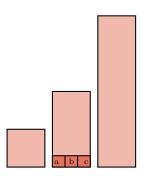
Primum non nocere: first, do no harm



Intuitive Specification

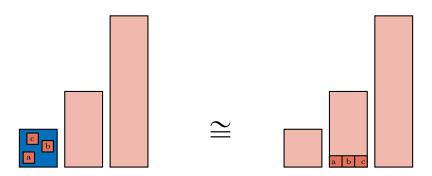
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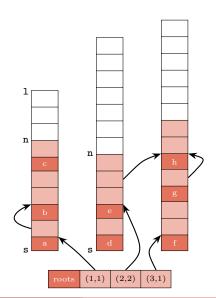


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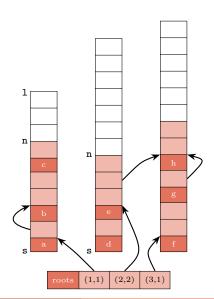
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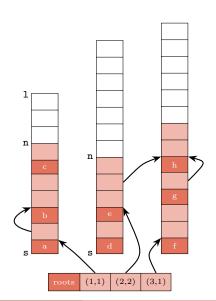
Nursery cannot fit alloc



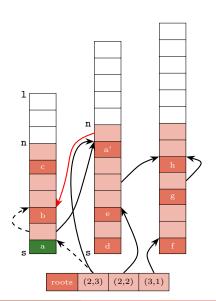
Nursery cannot fit alloc do_gen



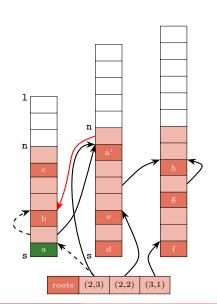
Nursery cannot fit alloc do_gen forward_roots



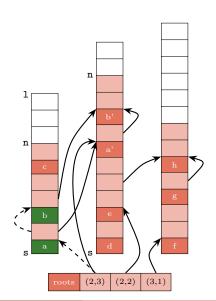
Nursery cannot fit alloc do_gen forward_roots forward



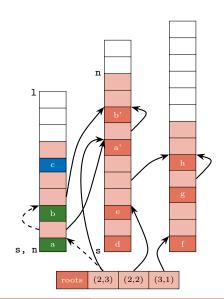
Nursery cannot fit alloc do_gen forward_roots forward do_scan



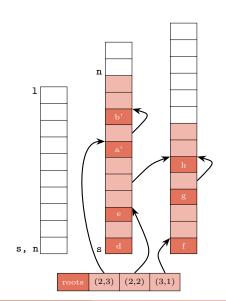
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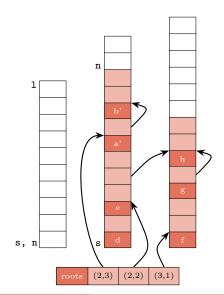
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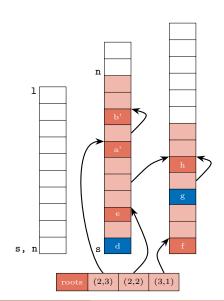
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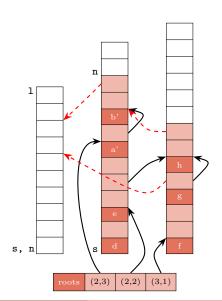
Non-Concerns



 $\begin{array}{c} \text{Non-Concerns} \\ \text{more garbage} \end{array}$

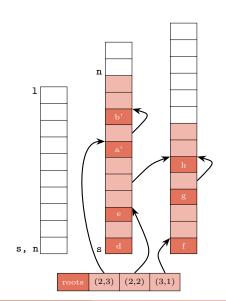


Non-Concerns more garbage backward pointers



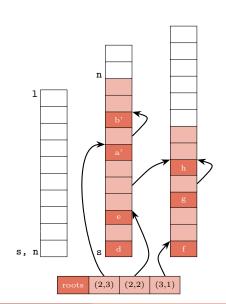
Non-Concerns more garbage backward pointers

Sources of Complexity



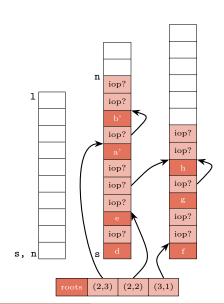
Non-Concerns more garbage backward pointers

Sources of Complexity variable-length objects



Non-Concerns more garbage backward pointers

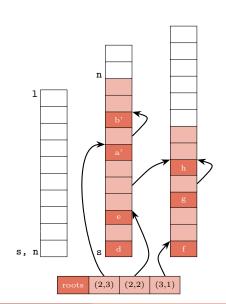
Sources of Complexity variable-length objects disambiguate int/ptr



Overview of Operations

Non-Concerns more garbage backward pointers

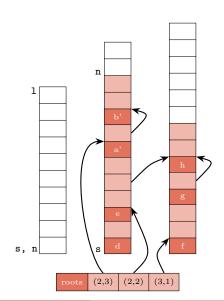
Sources of Complexity variable-length objects disambiguate int/ptr determine v's gen



Overview of Operations

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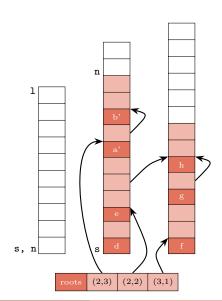
Sources of Complexity variable-length objects disambiguate int/ptr determine v's gen determine gen size



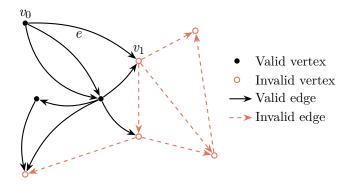
Overview of Operations

Non-Concerns more garbage backward pointers

Sources of Complexity variable-length objects disambiguate int/ptr determine v's gen determine gen size what if malloc fails?



A PreGraph is a hextuple (VType, EType, vvalid, evalid, src, dst)



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```
\begin{split} \mathbf{GC\_PreGraph:} \ & \mathtt{VType} \ := \ \mathtt{nat} \ * \ \mathtt{nat} \\ & \mathtt{EType} \ := \ \mathtt{VType} \ * \ \mathtt{nat} \\ & \mathtt{src} \ := \ \mathtt{fst} \\ & \mathtt{dst} \ := \ \mathit{unrestricted} \\ & \forall v. \ \mathtt{vvalid}(\gamma, v) \Leftrightarrow \mathtt{graph\_has\_v}(\gamma, v) \\ & \forall v. \ \mathit{out.} \ \mathtt{evalid}(\gamma, (v, \mathit{out})) \Leftrightarrow \\ & \mathtt{vvalid}(\gamma, v) \wedge \mathtt{In} \ \mathit{out} \ (\mathtt{get\_edges}(\gamma, v)) \end{split}
```

A LabeledGraph is a quadruple (PreGraph, VL, EL, GL)

GC_Graph: GC_PreGraph as shown

VL := raw_vert_block

EL := unit

GL := list gen_info

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```
GC Graph: GC PreGraph as shown
                         VL := raw_vert_block
                         EL := unit
                         GL := list gen info
Definition
raw fld := Z + GC Ptr.
                              Record gen_info :=
                              { s_addr: val;
Record raw vert block :=
                                s_ok: isptr s_addr;
{ raw mark: bool;
                                num_vert: nat;
                                (* elided *) }.
  copied_vertex: VType;
  raw flds: list raw fld;
  (* elided *) }.
```

forward is everywhere!

```
void forward (value *s, *l, **n, *p) {
  value * v; value va = *p;
  if(Is_block(va)) {
    v = (value*)iop2ptr(va);
    if(Is_from(s, l, v)) {
      header_t hd = Hd_val(v);
    if(hd == 0) {
      *p = Field(v,0);
    } else { /* elided */
```

```
forward is everywhere! forward is robust
```

```
void forward (value *s, *l, **n, *p) {
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              pointer?
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forward is robust
              pointer? in from space?
void forward (value *s, *l, **n, *p) {
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   header t hd = Hd val(v);
   if(hd == 0) {
    *p = Field(v,0);
   } else { /* elided */
```

```
void forward (value *s, *1, **n, *p) {
  value * v; value va = *p;
  if(Is_block(va)) {
    v = (value*)iop2ptr(va);
    if(Is_from(s, 1, v)) {
      header_t hd = Hd_val(v);
    if(hd == 0) {
      *p = Field(v,0);
    } else { /* elided */
```

```
forward is everywhere!
forward is robust
              pointer? in from space? already forwarded?
     and versatile
void forward (value *s, *l, **n, *p) {
value * v; value va = *p;
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forward is everywhere!
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void forward (value *s, *l, **n, *p) {
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   if(hd == 0) {
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   } else { /* elided */
```

```
\left\{ \begin{array}{l} \forall \gamma, from, to, v, n. \ \mathsf{gc\_graph}(\gamma) \land compat(\gamma, from, to) \land \\ \mathsf{s} = start(\gamma, from) \land 1 = \mathsf{s} + gensz(\gamma, from) \land \\ \mathsf{n} = nxtaddr(to) \land \mathsf{p} = vaddr(\gamma, v) + n \end{array} \right\} \stackrel{\mathrm{def}}{=} \phi_1
void forward (value *s, *l, **n, *p) {
    /* elided */
    if(hd == 0) {
       *p = Field(v,0);
\left\{\begin{array}{l} \phi_1 \wedge \exists \gamma'. \ \mathsf{gc\_graph}(\gamma') \wedge \gamma' = upd\_edge(\gamma, e, copy(\gamma, v)) \wedge \\ compat(\gamma', from, to) \wedge fwd\_relation(\gamma, \gamma', from, to, v, n) \end{array}\right\}
```

```
else {
  int i; int sz; value *new; sz = size(hd);
  new = *next+1; *next = new+sz; Hd_val(new) = hd;
  for(i = 0; i < sz; i++)
    Field(new, i) = Field(v, i);</pre>
```

```
else { int i; int sz; value *new; sz = size(hd); new = *next+1; *next = new+sz; Hd_val(new) = hd; for(i = 0; i < sz; i++) Field(new, i) = Field(v, i);  \left\{ \begin{array}{l} \phi_1 \wedge \exists \gamma', v'. \ \text{gc\_graph}(\gamma') \wedge v' = copied\_vertex(\gamma, to) \wedge \\ \gamma' = copy\_vertex(\gamma, to, v, v') \wedge compat(\gamma', from, to) \end{array} \right\} \stackrel{\text{def}}{=} \phi_2
```

```
else {
     int i; int sz; value *new; sz = size(hd);
    new = *next+1; *next = new+sz; Hd_val(new) = hd;
    for(i = 0: i < sz: i++)
         Field(new, i) = Field(v, i);
 \left\{ \begin{array}{l} \phi_1 \wedge \exists \gamma', v'. \ \mathsf{gc\_graph}(\gamma') \wedge v' = copied\_vertex(\gamma, to) \wedge \\ \gamma' = copy\_vertex(\gamma, to, v, v') \wedge compat(\gamma', from, to) \end{array} \right\} \stackrel{\mathrm{def}}{=} \phi_2 
    Hd val(v) = 0; Field(v, 0) = p2iop((void *)new);
    *p = p2iop((void *)new);
\left\{\begin{array}{l} \phi_2 \wedge \exists \gamma''. \ \mathsf{gc\_graph}(\gamma'') \wedge \gamma'' = upd\_edge(\gamma', e, v') \wedge \\ compat(\gamma'', from, to) \wedge fwd\_relation(\gamma, \gamma'', from, to, v, n) \end{array}\right\}
```

fwd_relation

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Inductive fwd_relation from to :
  forward_t -> LGraph -> Prop :=
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  forward_t -> LGraph -> LGraph -> Prop :=
| fr_v_not_in : forall v g,
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  fwd_relation from to (inl (inr v)) g g
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  forward_t -> LGraph -> LGraph -> Prop :=
| fr_v_not_in : forall v g,
  vgen v <> from ->
  fwd_relation from to (inl (inr v)) g g
| fr_e_to_fwded : forall e g,
  vgen (dst g e) = from ->
  raw_mark (vlabel g (dst g e)) = true ->
  let new_g := lgraph_gen_dst g e
    (copied vertex (vlabel g (dst g e))) in
  fwd_relation from to (inr e) g new_g
```

```
fr_e_to_not_fwded_Sn : forall e g g',
vgen (dst g e) = from ->
raw_mark (vlabel g (dst g e)) = false ->
let new_g :=
  lgraph_gen_dst (lgraph_copy1v g (dst g e) to)
        e (copy1v_new_v g to) in
fwd_loop from to
        (make_fields new_g (copy1v_new_v g to)) new_g g' ->
fwd_relation from to (inr e) g g'
```

Specification

Similar to forward_relation, we have forward_roots_relation do_scan_relation do_generation_relation garbage_collect_relation

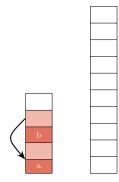
Specification

Similar to forward_relation, we have forward_roots_relation do_scan_relation do_generation_relation garbage_collect_relation

A composition of these gives us our isomorphism

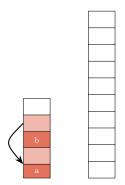
But the journey is far from easy!

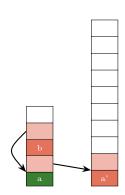
A brief look at semi_iso:



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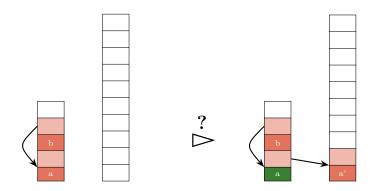
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A specific example:

```
Lemma semi_iso_refl: forall g from to,
  sound_gc_graph g -> semi_iso g g from to nil.
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   sound_gc_graph g -> semi_iso g g from to nil.

Lemma fwd_rel_semi_iso:
   forall from to p g1 g2 g3 roots,
      semi_iso g1 g2 from to l1 ->
      forward_relation from to p g2 g3 ->
      semi_iso g1 g3 from to
```

```
And eventually,
Theorem garbage_collect_iso: forall roots1 roots2 g1 g2,
...
garbage_collect_relation roots1 roots2 g1 g2 ->
gc_graph_iso g1 roots1 g2 roots2.
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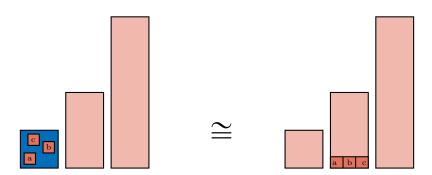
up to the vertices reachable from roots

The space between n and 1 is available for alloc

Note that we may still not achieve full isomorphism: the graph label may change to register new vertices and may even grow to accommodate new generations

Recap: Intuitive Specification

Primum non nocere: first, do no harm



 Cheney implemented too conservatively: only part of to space needs to be scanned during do_scan

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 Performance doubled

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    h->spaces[i].limit - h->spaces[i].start;
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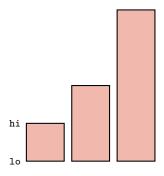
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if difference > 2<sup>31</sup>
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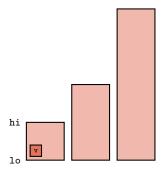
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int space_size =
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```

Fixed by adjusting nursery size

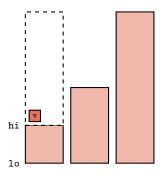
```
int Is_from(value * lo, value * hi, value * v) {
   return (lo <= v && v < hi); }</pre>
```



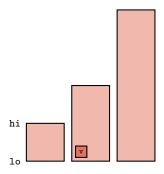
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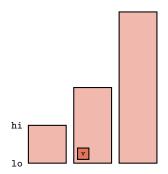


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Double-bounded pointer comparisons:

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Resolved using CompCert's extcall_properties

A classic OCaml trick to disambiguate int/ptr: int test_int_or_ptr (value x) { return (int)(((intnat)x)&1); }

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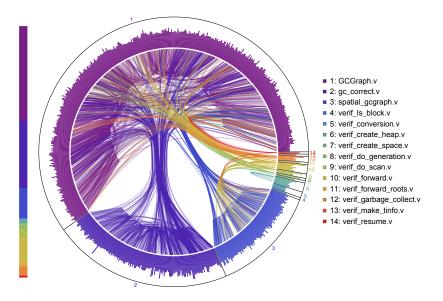
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Discussing char alignment issues with CompCert

Reusability: separation between pure and spatial reasoning



Problems of a similar shape

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Towards a verified GC for OCaml

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Further refinements required in C semantics before we can specify and verify OCaml's GC?