

# Reward Function

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# Reward Function - Part 1

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The reward function is defined as:

$$\xi_j = S_j P_j e^{\left(\frac{(t_j^E) - t_j^R}{\sigma}\right)^2} + (P_j^D)(d_j)(g(k))$$

**Where:**

- $S_j$  indicates if task  $j$  is performed (1) or not (0).
- $P_j$  indicates if task  $j$  is downloaded (1) or not (0).
- $t_j^E$  is the task  $j$  actual execution time.
- $t_j^R$  is the task  $j$  requested time.

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# Reward Function - Part 2

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Continuing with the reward function parameters:

- $\alpha$  is the weight factor for SoC (State of Charge) goodness w.r.t task execution, where:

$\alpha < 1 \Rightarrow$  more weight to performance and battery health

$\alpha = 1 \Rightarrow$  same weight to  $P_j$  and  $R$

$\alpha > 1 \Rightarrow$  more weight to  $R$

- $E_{max}$  is the maximum charge (safety limit).

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# Reward Function - Part 3

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$E_L$  is the minimum charge (safety limit).

$N$  is the number of sampling points between ground station power.

$\delta$  is the dispersion in time from requested of execution (gaussian weight).

The modification for the function  $g(k)$  is as follows:

$$g(k) = \begin{cases} 1 & \text{if } k = 1 \\ 0.5 & \text{if } k = 2 \\ 0.25 & \text{if } k = 3 \\ 0 & \text{if } k \geq 4 \end{cases}$$



# Overall Performance Metric

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$$\xi = \sum_{j=1}^J \xi_j + \frac{\alpha}{N} \sum_{i=1}^N \left( \frac{E_i - E_L}{E_{max} - E_L} \right)$$

This equation defines the overall performance metric ( $\xi$ ) for a nanosatellite, which may include considerations of energy efficiency, task management, and operational longevity.



# Task Efficiency

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$$\sum_{j=1}^J \xi_j$$

The first term sums the efficiencies ( $\xi_j$ ) of individual tasks or subsystems ( $j$ ) within the nanosatellite, reflecting how well each task performs relative to its energy consumption and operational objectives.



# Energy Efficiency

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$$\frac{\alpha}{N} \sum_{i=1}^N \left( \frac{E_i - E_L}{E_{max} - E_L} \right)$$

The second term represents the average, normalized measure of the battery's state of charge, weighted by  $\alpha$ . It assesses the energy efficiency by considering the battery charge levels ( $E_i$ ) at  $N$  different sampling points, bounded by the safety limits ( $E_{max}$  and  $E_L$ ).





# Notebook

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