

ISCA '25



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Genesisⁱ: A Hybrid CV-DV Compiler for Hamiltonian Simulation

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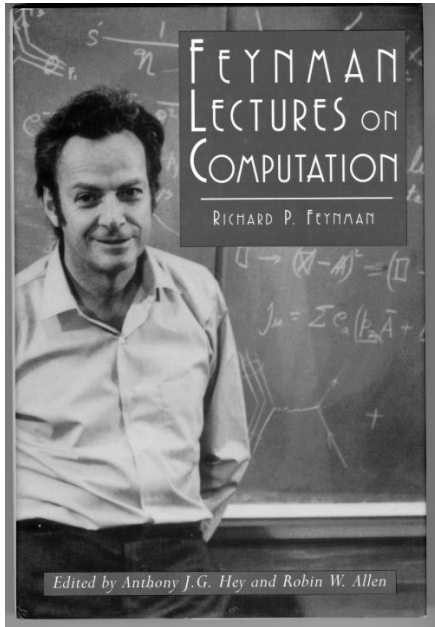
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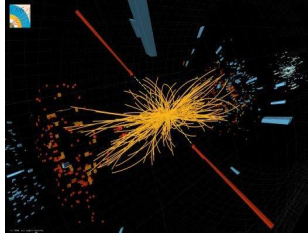
Introduction - Simulation of Nature



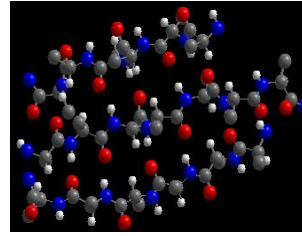
“Nature isn’t classical, dammit, and if you want to make a simulation of Nature, you’d better make it quantum mechanical, and by golly it’s a wonderful problem because it doesn’t look so easy.”

R. P. Feynman, 1981

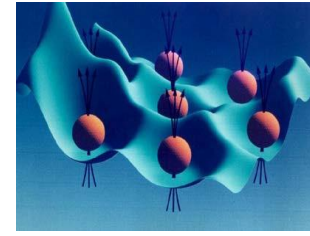
Introduction- Capability of Quantum Computer



particle
collision



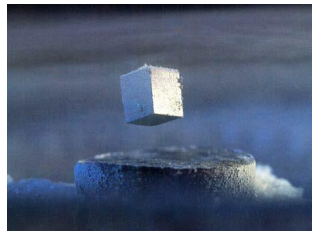
molecular
chemistry



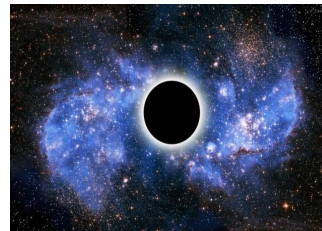
entangled
electrons

A quantum computer can simulate efficiently any physical process that occurs in Nature.

(Maybe. We don't actually know for sure.) - John Preskill



superconductor

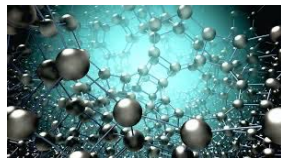
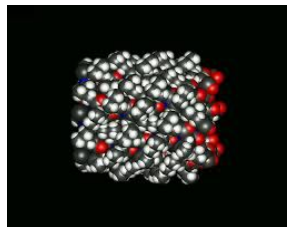


black hole

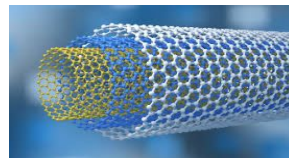


early universe

Hamiltonian Simulation



Quantum Chemistry



Material Science



High-Energy Physics

Hamiltonian Simulation

$$e^{-iHt}$$

Molecular Biology



Drug Discovery



- Hamiltonian Simulation is a “killer” quantum computing application currently

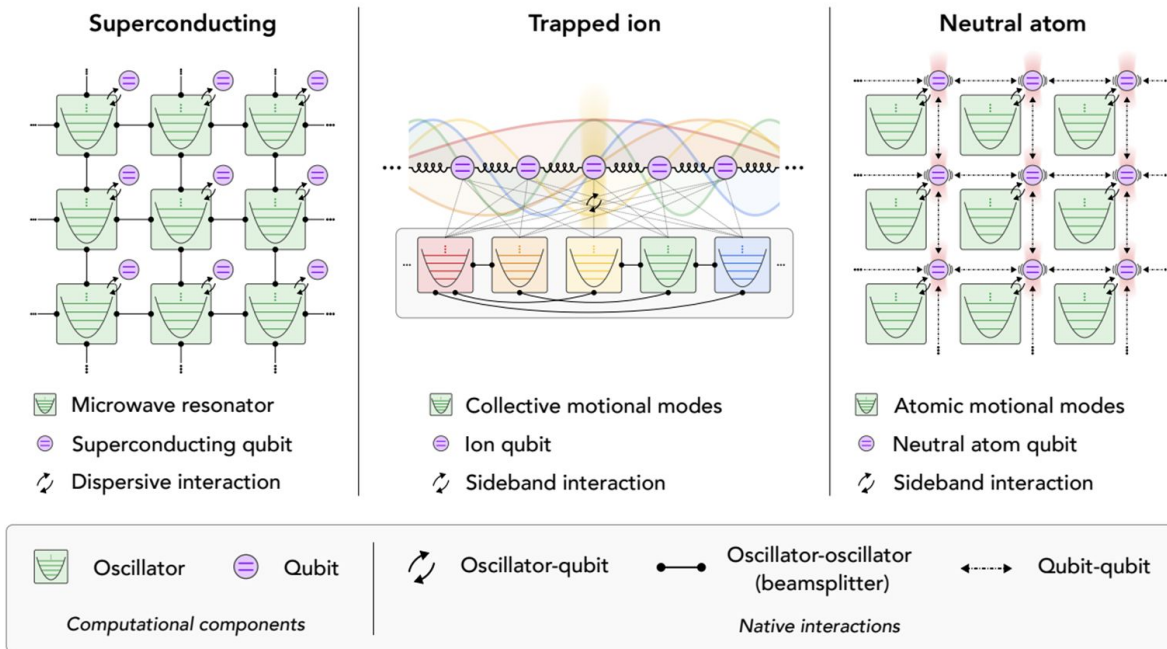
Hybrid CVDV Background

- Most current quantum machines use qubits that are **discrete-variable (DV)** systems – which is quite fit to simulate the Fermions with Discrete states .
- In contrast, Bosons have continuous/infinite states, and a **continuous-variable (CV)** quantum system (qumode) which has a spectrum of many possible states, is fit to simulate the Bosonic system. It can retain more robust quantum states and has the potential to achieve excellent quantum error correction.
- **CV-only** hardware is challenging to have non-Gaussian resources.
- **DV-only** hardware needs truncation for simulating CV states, also it is difficult to simulate native bosonic operators.
- **Hybrid CV-DV** hardware takes the best of both system and is well-suited for the physical simulation with fermion-boson mixtures

Hybrid CVDV Background

(a)

Hybrid CV-DV Quantum Processors

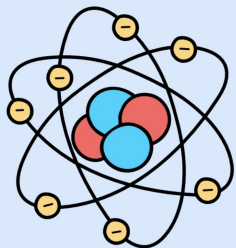


Source: “Hybrid Oscillator-Qubit Quantum Processors: Instruction Set Architectures, Abstract Machine Models, and Applications.” Liu et al. arXiv 2407.10381v2

Hybrid CVDV Background

Hamiltonian

$$e^{-iHt}$$



- Hybrid CV-DV hardware takes the best of both system and is well-suited for the physical simulation with fermion-boson mixtures
- However, compiler and programming systems are largely undeveloped for hybrid CV-DV systems.
- Fermion-Boson mixtures interactions have not been thoroughly investigated, Genesis tries to bridge this gap and offers a complete end-to-end hamiltonian simulation compilation support!

Challenges and Motivation

1. Complex Cross-Domain Problem

- Domain Specific Language (DSL) Hamiltonian Grammar and Multi-level Compilation

2. Qumode-centric Gate Synthesis

- Rule-Based Recursive Template Matching

3. Multi-qubit Pauli-string Synthesis

- Traveling Ancilla Qumode

4. Limited Connectivity Constraints

- Hybrid CVDV Hardware Mapping and Routing

Hamiltonian Grammar DSL Representation

Hamiltonian Model Example:

$$H = -t \sum_{i,j,\sigma} c_{i\sigma}^\dagger c_{j\sigma} + U \sum_i b_i^\dagger b_i + g \sum_{i,\sigma} \hat{n}_{i\sigma} (b_i^\dagger + b_i)$$

Corresponding Example Hamiltonian Grammar Representation:


```
Const t = 1;
Const U = 1;
Const g = 1;

Range i = [0, 10, 1];
Range j = [0, 10, 1];
Range sigma = [0, 2, 1];

Result = - t *Sum_over(i, j, sigma){FC[i][sigma]* FA[j][sigma]}
        + U *Sum_over(i){BC[i]* BA[i]}
        + g * Sum_over(i, sigma){TensorProd(FN[i][sigma], BC[i] + BA[i])};
```

CVDVQASM and Multi-level Compilation

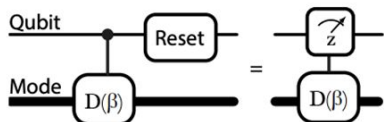
1. Hamiltonian Formula

$$H = -t \sum_{i,j,\sigma} c_{i\sigma}^\dagger c_{j\sigma} + U \sum_i b_i^\dagger b_i + g \sum_{i,\sigma} \hat{n}_{i\sigma} (b_i^\dagger + b_i)$$


2. Hamiltonian Grammar


```
- t *Sum_over(i, j, sigma){FC[i][sigma]* FA[j][sigma]}
+ U *Sum_over(i){BC[i]* BA[i]}
+ g * Sum_over(i, sigma){TensorProd(FN[i][sigma], BC[i] + BA[i])};
```

5. Physical CVDVQASM file




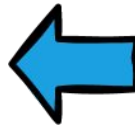
4. Logical CVDVQASM file

```
// Pauli String with Parameter
pauli(pi/4) YIYZXXIIIIIIII;
pauli(pi/4) XZYZYIIIIIIII;
// Phase Space Rotation Gate
R(pi/4) qm[1];
R(pi/4) qm[2];
// Control Displacement Gate
CD(pi/4) q[2], qm[1];
CD(pi/4) q[3], qm[1];
// Displacement Gate
D(pi/4) qm[2];
D(pi/4) qm[2];
```



3. Intermediate Representation

```
pauli(0.392699075j): IXIZIVII;
pauli(0.392699075j): IIVIXIII;
bosonic: exp(prod((-1j),dagger(b(0)),b(0)));
bosonic: exp(prod((-1j),dagger(b(1)),b(1)));
hybrid: exp(prod((-0.78539815j),sigma(0, 0),sum(dagger(b(0)),b(0))));
hybrid: exp(prod((0.78539815j),sigma(3, 0),sum(dagger(b(0)),b(0))));
```

Direct Qumode-centric Gate Synthesis

Type	Gate Name	Definition
Qubit	x, y Rotation	$r_\varphi(\theta) = \exp \left[-i\frac{\theta}{2} (\cos \varphi \sigma_x + \sin \varphi \sigma_y) \right]$
	z Rotation	$r_z(\theta) = \exp \left(-i\frac{\theta}{2} \sigma_z \right)$
Qumode	Phase-Space Rotation	$R(\theta) = \exp \left[-i\theta a^\dagger a \right]$
	Displacement	$D(\alpha) = \exp \left[\left(\alpha a^\dagger - \alpha^* a \right) \right]$
	Beam-Splitter	$BS(\theta, \varphi) = \exp \left[-i\frac{\theta}{2} \left(e^{i\varphi} a^\dagger b + e^{-i\varphi} ab^\dagger \right) \right]$
Hybrid	Conditional Phase-Space Rotation	$CR(\theta) = \exp \left[-i\frac{\theta}{2} \sigma_z a^\dagger a \right]$
	Conditional Parity	$CP = \exp \left[-i\frac{\pi}{2} \sigma_z a^\dagger a \right]$
	Conditional Displacement	$CD(\alpha) = \exp \left[\sigma_z \left(\alpha a^\dagger - \alpha^* a \right) \right]$
	Conditional Beam-Splitter	$CBS(\theta, \varphi) = \exp \left[-i\frac{\theta}{2} \sigma_z \left(e^{i\varphi} a^\dagger b + e^{-i\varphi} ab^\dagger \right) \right]$
	Rabi Interaction	$RB(\theta) = \exp \left[-i\sigma_x \left(\theta a^\dagger - \theta^* a \right) \right]$

Quantum Algorithms Define Compiler Rules: Operator Decomposition in CV-DV Systems

- Trotterization(Trotter-Suzuki formula)

$$e^{(M+N)t} \approx \left(e^{Mt'} e^{Nt'} \right)^n$$

- BCH(Baker Campbell Hausdorff formula)

$$e^{[M,N]t^2} \approx e^{Mt} e^{Nt} e^{-Mt} e^{-Nt}.$$

- Block Encoding

$$O = \begin{pmatrix} A & B \\ C & D \end{pmatrix}$$

$$O = |0\rangle \langle 0| \otimes A + |0\rangle \langle 1| \otimes B + |1\rangle \langle 0| \otimes C + |1\rangle \langle 1| \otimes D.$$

- Commutator $\sigma_z[A, B]$ and anticommutator $\sigma_z\{A, B\}$ implementation in CVDV architecture

Rule-Based Recursive Template Matching

Rules	Operator Template	Conditions	Decomposition Output	Reference	Precision
1	$\exp(Mt + Nt) \approx \text{Trotter}(Mt, Nt)$		$(\exp(Mt/k)\exp(Nt/k))^k$	Trotterization	Approx
2	$\exp([Mt, Nt]) \approx \text{BCH}(Mt, Nt)$		$\exp(Mt)\exp(Nt)\exp(-Mt)\exp(-Nt)$	BCH	Approx
3	$\exp(t^2[M, N])$	M, N Hermitian	$\exp([it\sigma_I N, it\sigma_I M])$	[20]	Exact
4	$\exp(-it^2\sigma_I\{M, N\})$	M, N Hermitian	$\exp([it\sigma_J M, it\sigma_K N])$	[20]	Exact
5	$\exp(-it^2\sigma_z[M, N])$		$\exp([itN, it\sigma_z M])$	This paper	Exact
6	$\exp(t^2\sigma_z((MN - (MN)^\dagger)))$	$[M, N] = 0$	$\exp([X \cdot it\mathcal{B}_N \cdot X, it\mathcal{B}_M])$	[20]	Exact
7	$\exp(it^2\sigma_z((MN + (MN)^\dagger)))$	$[M, N] = 0$	$\exp([S \cdot it\mathcal{B}_M \cdot S^\dagger, X \cdot it\mathcal{B}_N \cdot X])$	[20]	Exact
8	$\exp\left(-2it\begin{pmatrix} MN & 0 \\ 0 & -MN \end{pmatrix}\right)$	M, N Hermitian	$\exp(-it\sigma_z[M, N] - it\sigma_z\{M, N\})$	This paper	Exact
9	$\exp\left(2it^2\begin{pmatrix} MN & 0 \\ 0 & -MN \end{pmatrix}\right)$	$[M, N] = 0$ $MN = (MN)^\dagger$	$\exp([S \cdot it\mathcal{B}_M \cdot S^\dagger, X \cdot it\mathcal{B}_N \cdot X])$	[20]	Exact
10	$\exp(2it\mathcal{B}_{MN})$	$[M, N] = 0$	$X \cdot \exp(t\sigma_y(MN - (MN)^\dagger) + it\sigma_x(MN + (MN)^\dagger)) \cdot X$	[20]	Exact
11	$\exp\left(it\begin{pmatrix} 2MN & 0 \\ 0 & -NM - (NM)^\dagger \end{pmatrix}\right)$	$MN = (MN)^\dagger$	$\exp([S \cdot it\mathcal{B}_M \cdot S^\dagger, X \cdot it\mathcal{B}_N \cdot X])$	[20]	Exact
12	$\mathcal{B}_a = \exp\left(2i\alpha\begin{pmatrix} 0 & a \\ a^\dagger & 0 \end{pmatrix}\right)$	$\alpha = \alpha^*$	$\exp(i(\pi/2)a^\dagger a)\exp(i(\alpha(a^\dagger + a)) \otimes \sigma_y)\exp(-i(\pi/2)a^\dagger a)\exp(i(\alpha(a^\dagger + a)) \otimes \sigma_x)$	[20]	Approx
13	$\mathcal{B}_{a^\dagger} = \exp\left(2i\alpha\begin{pmatrix} 0 & a^\dagger \\ a & 0 \end{pmatrix}\right)$	$\alpha = \alpha^*$	$\exp(i(\pi/2)a^\dagger a)\exp(i(\alpha(a^\dagger + a)) \otimes \sigma_y)\exp(-i(\pi/2)a^\dagger a)\exp(-i(\alpha(a^\dagger + a)) \otimes \sigma_x)$	This paper	Approx
14	$e^{(P_1 P_2 \dots P_n)(\alpha a_k^\dagger - \alpha^* a_k)}$		Multi-qubit-controlled displacement: Right hand side (RHS) of Equation (11) first line	[28]	Exact
15	$e^{2i\alpha^2 P_1 P_2 \dots P_n}$		Multi-Pauli Exponential: Right hand side (RHS) of Equation (9) first line	This Paper	Exact
16	All Native Gates RHS in Table 2		All Native Gates Left Hand Side (LHS) Table 2	[28]	Exact

[20] "Leveraging Hamiltonian Simulation Techniques to Compile Operations on Bosonic Devices." Kang, Christopher, et al. arXiv:2303.15542

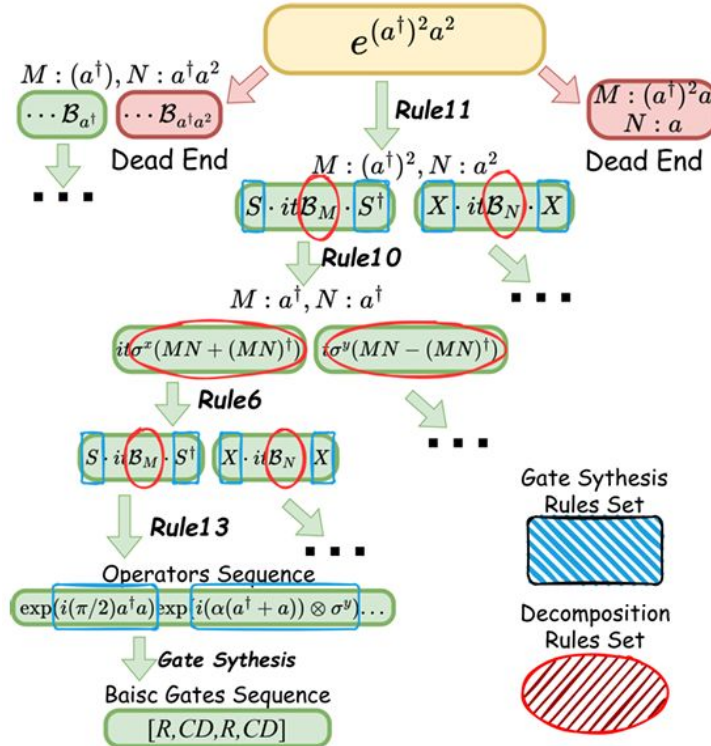
Rule-Based Recursive Template Matching

Basic Gates Set

Type	Gate Name	Definition
Qubit	x, y Rotation	$r_\theta(\theta) = \exp\left[-\frac{i\theta}{2}(\cos\varphi\sigma_x + \sin\varphi\sigma_y)\right]$
	z Rotation	$r_z(\theta) = \exp\left[-\frac{i\theta}{2}\sigma_z\right]$
Qumode	Phase-Space Rotation	$R(\theta) = \exp\left[-i\theta a^\dagger a\right]$
	Displacement	$D(\alpha) = \exp\left[\alpha a^\dagger - \alpha^* a\right]$
	Beam-Splitter	$BS(\theta, \varphi) = \exp\left[-\frac{i\theta}{2}\left\{e^{i\varphi}a^\dagger b + e^{-i\varphi}ab^\dagger\right\}\right]$
Hybrid	Conditional Phase-Space Rotation	$CR(\theta) = \exp\left[-\frac{i\theta}{2}\sigma_z a^\dagger a\right]$
	Conditional Parity	$CP = \exp\left[-\frac{i\pi}{2}\sigma_z a^\dagger a\right]$
	Conditional Displacement	$CD(\alpha) = \exp\left[\sigma_z \left(\alpha a^\dagger - \alpha^* a\right)\right]$
	Conditional Beam-Splitter	$CRBS(\theta, \varphi) = \exp\left[-\frac{i\theta}{2}\sigma_z \left\{e^{i\varphi}a^\dagger b + e^{-i\varphi}ab^\dagger\right\}\right]$
	Rabi Interaction	$RB(\theta) = \exp\left[-i\theta\sigma_x \left(a^\dagger a^\dagger - b^\dagger b\right)\right]$

Decomposition Rules Set

Rule	Operator Template	Conditions	Decomposition Output	Reference	Precision
1	$\exp(Ma + N^\dagger) \rightarrow \text{Toffoli}(M, N)$		$\exp(M) \exp(N^\dagger)$	Toffoli gates	Approx
2	$\exp\left[\frac{1}{2}(M, N)\right] \rightarrow \text{BCR}(M, N)$		$\exp(M) \exp(N) \exp(-M) \exp(-N)$	BCR	Approx
3	$\exp(i\pi a^\dagger a)$	M, N Hermitian	$\exp(i\pi a^\dagger a) \exp(i\pi a^\dagger a)$	[10]	Exact
4	$\exp(-i\pi a^\dagger a)$	M, N Hermitian	$\exp(-i\pi a^\dagger a) \exp(-i\pi a^\dagger a)$	[10]	Exact
5	$\exp(-i\pi a^\dagger a)$	M, N Hermitian	$\exp(-i\pi a^\dagger a) \exp(-i\pi a^\dagger a)$	This paper	Exact
6	$\exp(i\pi a^\dagger a)$	M, N Hermitian	$\exp(i\pi a^\dagger a) \exp(i\pi a^\dagger a)$	[10]	Exact
7	$\exp(i\pi a^\dagger a)$	M, N Hermitian	$\exp(i\pi a^\dagger a) \exp(i\pi a^\dagger a)$	[10]	Exact
8	$\exp\left(-i\pi \begin{pmatrix} M & 0 \\ 0 & -M \end{pmatrix} \begin{pmatrix} a^\dagger \\ a \end{pmatrix}\right)$	M, N Hermitian	$\exp(-i\pi a^\dagger a) \exp(-i\pi a^\dagger a)$	This paper	Exact
9	$\exp\left(-i\pi \begin{pmatrix} M & 0 \\ 0 & -M \end{pmatrix} \begin{pmatrix} a^\dagger \\ a \end{pmatrix}\right)$	M, N Hermitian	$\exp(-i\pi a^\dagger a) \exp(-i\pi a^\dagger a)$	[10]	Exact
10	$\exp(i\pi a^\dagger a)$	M, N Hermitian	$\exp(i\pi a^\dagger a) \exp(i\pi a^\dagger a)$	[10]	Exact
11	$\exp\left(i\pi \begin{pmatrix} M & 0 \\ 0 & -M \end{pmatrix} \begin{pmatrix} a^\dagger \\ a \end{pmatrix}\right)$	M, N Hermitian	$\exp(i\pi a^\dagger a) \exp(i\pi a^\dagger a)$	[10]	Exact
12	$B_a = \exp\left(i\pi \begin{pmatrix} M & 0 \\ 0 & -M \end{pmatrix} \begin{pmatrix} a^\dagger \\ a \end{pmatrix}\right)$	M, N Hermitian	$\exp(i\pi a^\dagger a) \exp(i\pi a^\dagger a)$	[10]	Approx
13	$B_a = \exp\left(i\pi \begin{pmatrix} M & 0 \\ 0 & -M \end{pmatrix} \begin{pmatrix} a^\dagger \\ a \end{pmatrix}\right)$	M, N Hermitian	$\exp(i\pi a^\dagger a) \exp(i\pi a^\dagger a)$	This paper	Approx
14	$\mu^{(M)}(a^\dagger, a) \mu^{(N)}(a^\dagger, a)$	Multi-qubit controlled displacement. Right hand side (RHS) of Equation (1) first line	$\exp(i\pi a^\dagger a) \exp(i\pi a^\dagger a)$	[10]	Exact
15	$\mu^{(M)}(a^\dagger, a) \mu^{(N)}(a^\dagger, a)$	Multi-qubit controlled displacement. Right hand side (RHS) of Equation (1) first line	$\exp(i\pi a^\dagger a) \exp(i\pi a^\dagger a)$	This paper	Exact
16	All Native Gates (RHS in Table 1)		All Native Gates (RHS in Table 1)	[10]	Exact



$$e^{(a^\dagger)^2 a^2}$$



Basic Gates Sequence
(Logical CVDVQASM Circuit)

Gate Synthesis
Rules Set



Decomposition
Rules Set



Repeat the rewrite
process until it
produces only
basis gates

Multi-qubit Pauli-string Synthesis

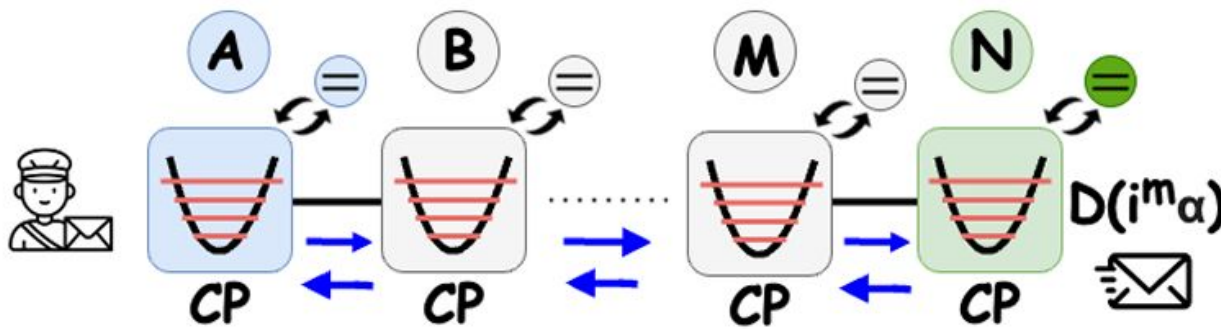
- Qubits are not directly connected with each other, we propose a scheme to synthesize an arbitrary multi-qubit Pauli-string on Hybrid CV-DV platforms.
- It is inspired by phase kickback in DV systems, where the phase of the control qubit is influenced by the operation on the target qubits.

$$\begin{aligned} U &= D^k(i\alpha) CD^{(k, P_1 \dots P_n)}(-\alpha) D^k(-i\alpha) CD^{(k, P_1 \dots P_n)}(\alpha) \\ &= e^{2i\alpha^2 P_1 P_2 \dots P_n} \end{aligned}$$

Multi-qubit Pauli-string Synthesis

- Our final multi-Pauli exponential decomposition makes use of a multi-qubit controlled CD gate proposed by Liu et al., as below:

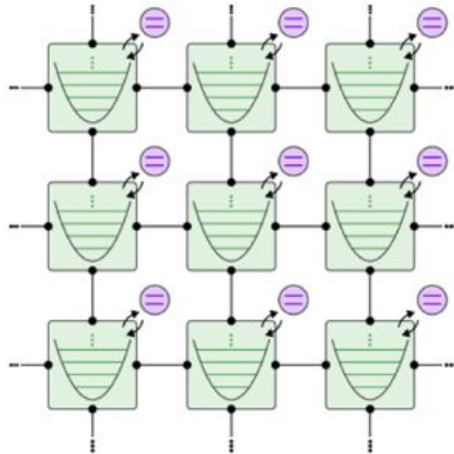
$$\begin{aligned} \text{CD}^{(k, P_1 P_2 \cdots P_n)}(\alpha) &= U_{\text{seq}}^\dagger D(i^n \alpha) U_{\text{seq}} \\ &= e^{(P_1 P_2 \cdots P_n)(\alpha a_k^\dagger - \alpha^* a_k)} \end{aligned}$$






Source: “Hybrid Oscillator-Qubit Quantum Processors: Instruction Set Architectures, Abstract Machine Models, and Applications.” Liu et al. arXiv 2407.10381v2

Limited Hardware Connectivity

Superconducting



-  Microwave resonator
-  Superconducting qubit
-  Dispersive interaction

- Qumode-qumode Mapping.

Interactions are limited to adjacent qumodes. For non-adjacent qumodes, qumode SWAP gates are used, with routing optimized to minimize such SWAPs.

- Qubit-qumode Mapping.

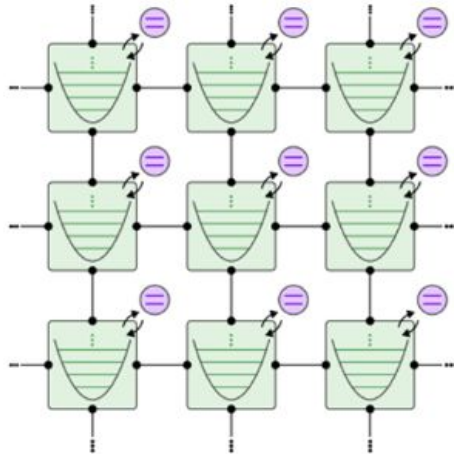
Each qumode interacts only with its associated qubit. For interactions with other qumodes, adjacency is established by moving qumodes, similar to qumode-qumode mapping.




- Qubit-qubit Mapping.

Qubits interact indirectly via an ancilla qumode, which is moved between qubits to mediate interactions and complete gate operations.

Limited Hardware Connectivity

Superconducting



-  Microwave resonator
-  Superconducting qubit
-  Dispersive interaction

- Qumode-qumode Mapping.

Interactions are limited to adjacent qumodes. For non-adjacent qumodes, qumode SWAP gates are used, with routing optimized to minimize such SWAPs.

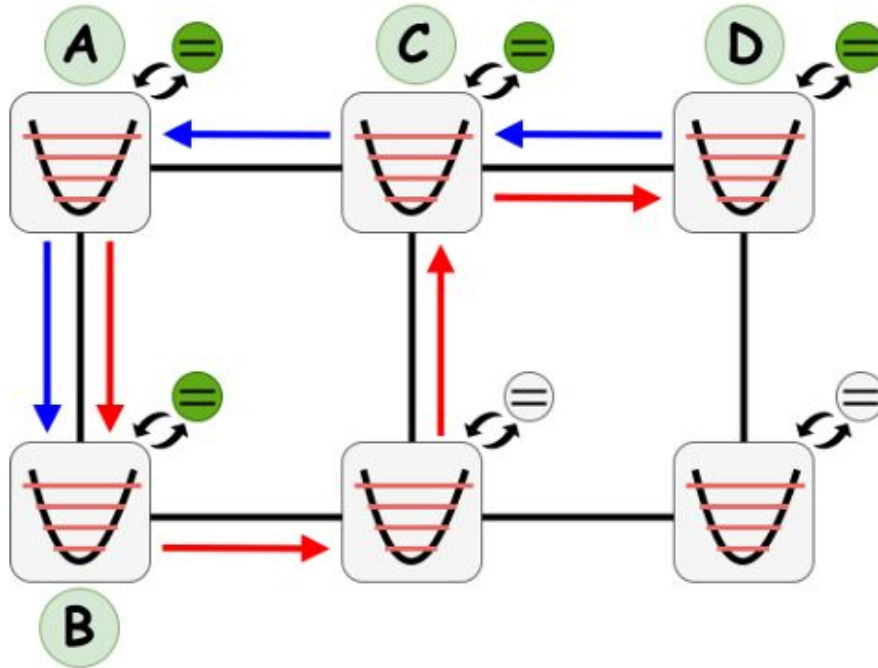
- Qubit-qumode Mapping.

Each qumode interacts only with its associated qubit. For interactions with other qumodes, adjacency is established by moving qumodes, similar to qumode-qumode mapping.

Working Frontier: all unresolved gates whose dependence has been resolved

Using a Qiskit Sabre-like reward function to execute gate from the frontier and update it.

Optimized Ancilla Qumode Routing



$A \rightarrow B \rightarrow (A) \rightarrow C \rightarrow D$: **4** BS gates

$D \rightarrow C \rightarrow A \rightarrow B$: **3** BS gates

The Optimized Ancilla Qumode Routing Problem can be reformulated as a relaxed **Hamiltonian Path Problem**, similar to a modified Traveling Salesman Problem (TSP). Unlike the closed-path TSP, this problem allows revisiting vertices and does not require returning to the starting vertex.

Optimized Ancilla Qumode Routing

Qumode-SWAP

1 Beam-Splitter gate
(20x depth/duration)

Qubit-SWAP

(in CVDV System)

12 control displacement gates

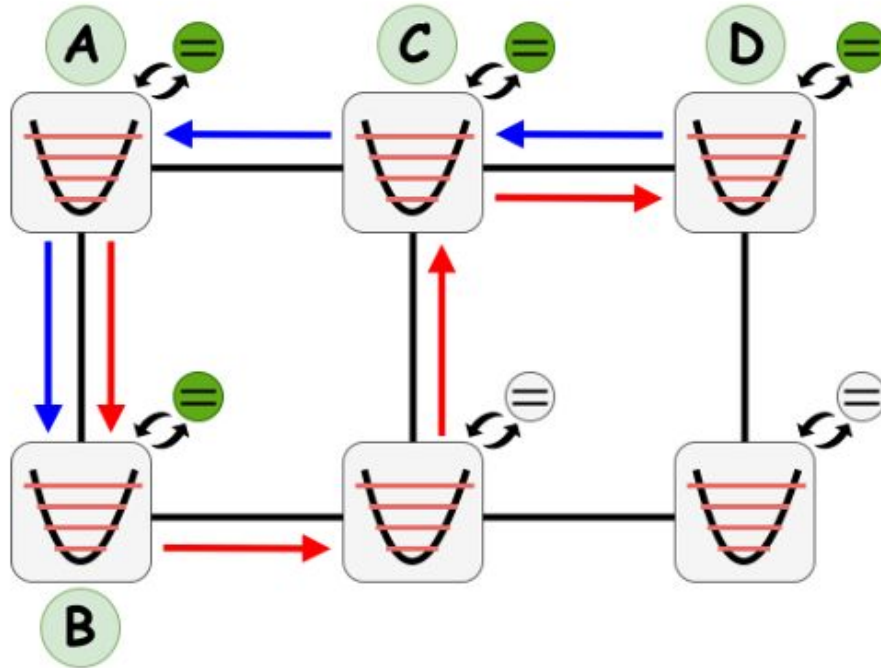
12 Qumode-SWAPs

(480x depth/duration)

- **Dynamic Qubit Floating**

Relocation strategy, when a qubit-qubit pair distance in a specific multi-qubit exponential is too far, and this qubit-qubit pair appear often in the following multi-qubit exponential, we will try to relocate the qubit using Qubit-SWAP to cluster them.

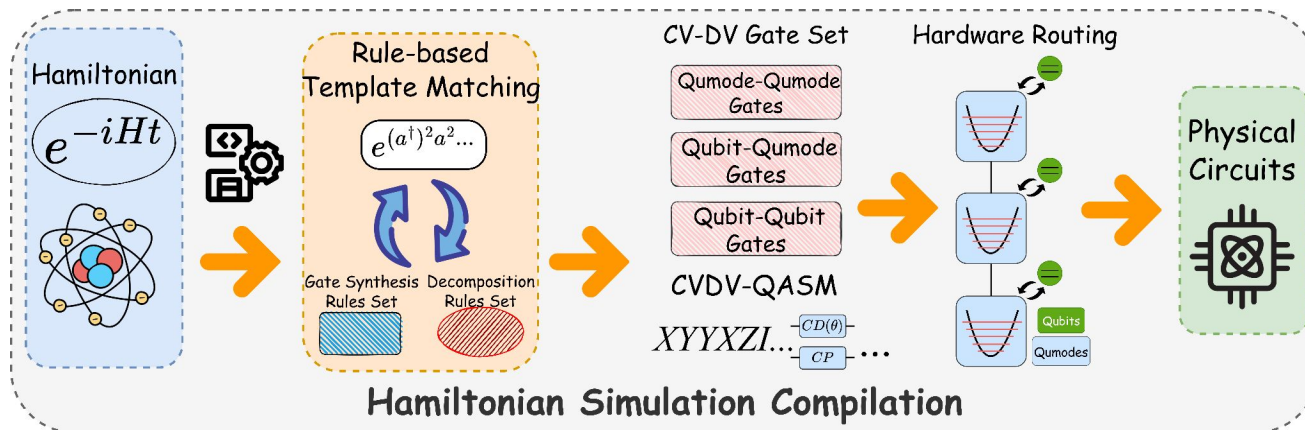
Optimized Ancilla Qumode Routing



- Christofides Algorithm
Baseline
- Threshold Accepting Algorithm
3-7% better duration time, 4.8% in avg
- Dynamic Qubit Floating
6% worse duration time in avg
4/20 better than baseline and 2/20 better than Threshold Accepting

End to End Implementation

1. **Hamiltonian Parsing:** Translates a Hamiltonian from mathematical form into a DSL-based representation.
2. **Intermediate Representation (IR):** Converts the DSL into an IR consisting of Pauli strings and operator expressions(bosonic, hybrid).
3. **Pattern Matching and Gate Synthesis:** Matches fermionic and bosonic operator terms and synthesizes them into logical CV-DV circuits in CVDVQASM format.
4. **Physical Mapping:** Maps logical circuits and Pauli terms to hardware-compliant physical circuits, and outputs the final(physical) CVDVQASM program(s).



Software access:

<https://github.com/ruadapt/Genesis-CVDV-Compiler>

GitHub QR Code:



End to End Implementation

- Evaluation 1. Multi Pauli-String Synthesis

- 20 Qubit Hamiltonian such as LiH(4,12), BeH2(6,14) ...
- # Pauli Strings from 631 to 1884
- JW and BK encoding

- Evaluation 2. General Hamiltonian Simulation Compilation

- 6 Hamiltonian Models such as Hubbard-Holstein Model, Bose-Hubbard Model ... At most 60 Qubits and 120 Qumodes

End to End Implementation-in the future

- Intermediate Tools 1. CVDV Mapping and Routing

- Support more architecture(neutral atom)
- Better relocate strategy when compile multi pauli-strings

- Intermediate Tools 2. Operator Pattern Matching

- Flexible customize rules and multiple decomposition perspectives
- Better compilation efficiency and robustness
- Error analysis and unitary verification

Codes Available

Welcome to give it a try!

Software access:

<https://github.com/ruadapt/Genesis-CVDV-Compiler>

GitHub Link:





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Thank You!