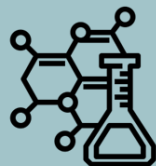


Genesis*i*: A Hybrid CV-DV Compiler for Hamiltonian Simulation

Zihan Chen
May 21, 2025

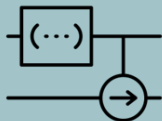
Genesis*is*



Hamiltonian



Intermediate
Representation(s)



Logical Circuits



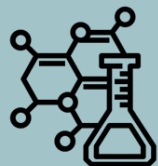
Physical Circuits

Genesis: A Compiler for Hamiltonian Simulation on Hybrid CV-DV Quantum Computers

Genesis is a compiler framework for Hamiltonian simulation targeting hybrid continuous-variable (CV) and discrete-variable (DV) quantum systems.

It supports multi-level logical circuit compilation, Hybrid CV-DV domain-specific language (DSL), and hardware circuit mapping and routing.

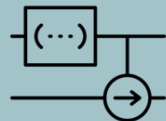
Genesisⁱ



Hamiltonian



Intermediate
Representation(s)



Logical Circuits



Physical Circuits

Collaborative Work(Rutgers & NCSU)

- To appear in **ISCA '25**: Zihan Chen*, Jiakang Li*, Minghao Guo*, Henry Chen, Zirui Li, Joel Bierman, Yipeng Huang, Huiyang Zhou, Yuan Liu, and Eddy Z. Zhang. 2025. Genesis: A Compiler for Hamiltonian Simulation on Hybrid CV-DV Quantum Computers. In *Proceedings of the 52nd Annual International Symposium on Computer Architecture (ISCA '25)*, June 21–25, 2025, Tokyo, Japan. ACM, New York, NY, USA, 15 pages.

<https://doi.org/10.1145/3695053.3731065>

- **arXiv preprint**:2505.13683, 2025
- Software access:

<https://github.com/ruadapt/Genesis-CVDV-Compiler>

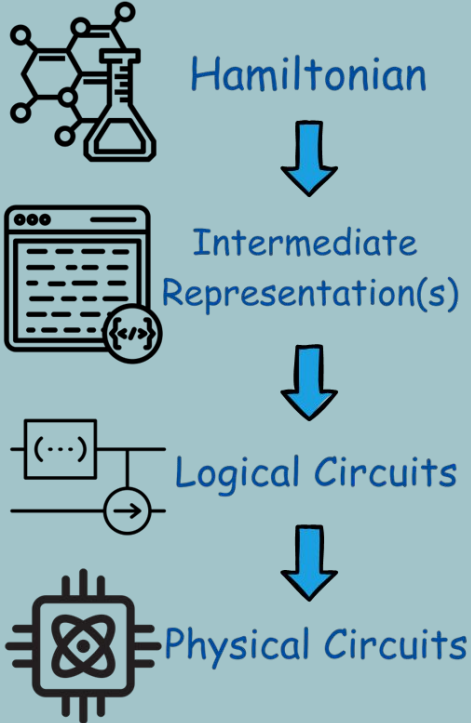
Preprint:



Code:



Genesis^{is}



1. Background and Motivation
2. Domain Specific Language Design
3. Logical Circuit Synthesis
4. Physical Circuit Mapping
5. End-to-end Implementation

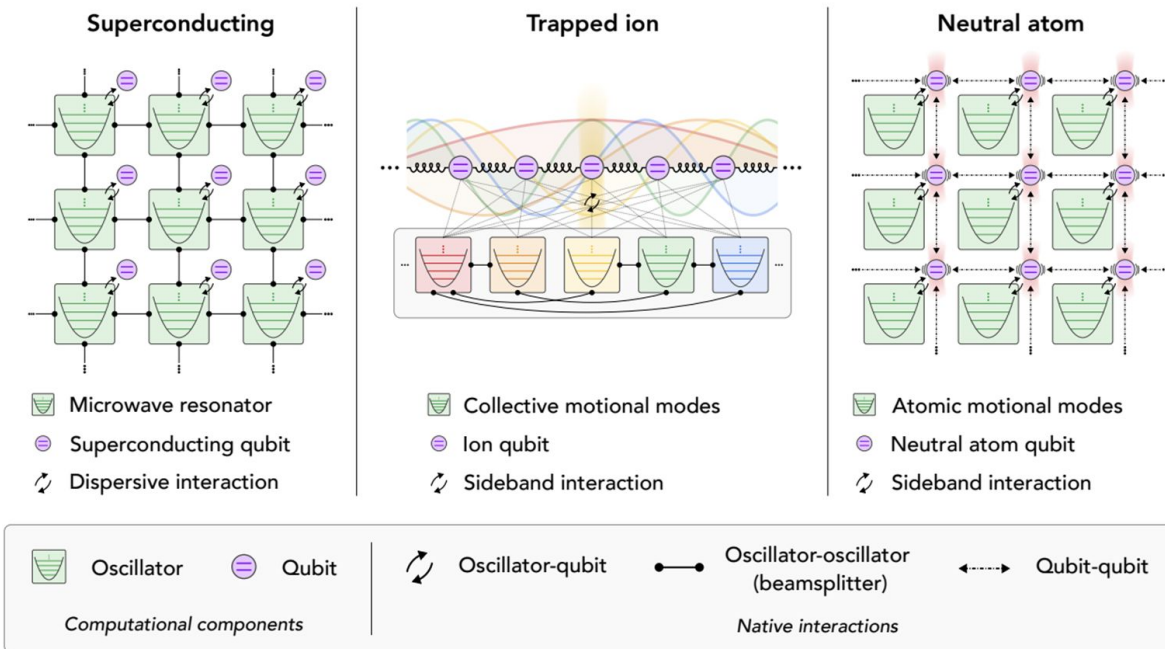
1.1 Hybrid CV-DV Background

- Most current quantum machines use qubits that are **discrete-variable (DV)** systems – essentially two-state quantum systems.
- In contrast, a **continuous-variable (CV)** quantum system (qumode) has a spectrum of many possible states, theoretically an infinite continuum of states. It can retain more robust quantum states and has the potential to achieve excellent quantum error correction.
- **CV-only** hardware is limited to generate non-Gaussian resources.
- **DV-only** hardware needs truncation for simulating CV states, also it is difficult to simulate native bosonic operators.
- **Hybrid CV-DV** hardware takes the best of both system and is well-suited for the physical simulation with fermion-boson mixtures

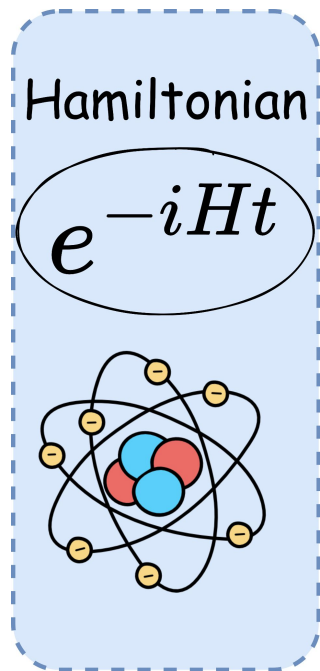
1.1 Hybrid CV-DV Background

(a)

Hybrid CV-DV Quantum Processors



1.2 Hamiltonian Simulation Background

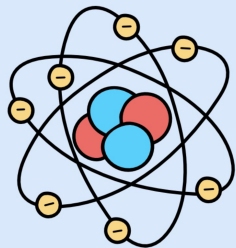


- Hamiltonian Simulation is a “killer” quantum computing application currently
- Hamiltonian Simulation could unlock insights into chemistry, physics, and materials science.
- Fermions \rightarrow discrete states \rightarrow qubits (DV)
- Bosons \rightarrow continuous/infinite states \rightarrow qumodes (CV)

1.2 Hamiltonian Simulation Background

Hamiltonian

$$e^{-iHt}$$



- Hybrid CV-DV hardware takes the best of both system and is well-suited for the physical simulation with fermion-boson mixtures
- However, compiler and programming systems are largely undeveloped for hybrid CV-DV systems.
- Fermion-Boson mixtures interactions have not been thoroughly investigated, Genesis tries to bridge this gap and offers a complete end-to-end hamiltonian simulation compilation support!

1.3 Challenges and Motivation

1. Complex Cross-Domain Problem

- Hamiltonian Grammar(DSL) and Multi-level Compilation

2. Qumode-centric Gate Synthesis

- Rule-Based Recursive Template Matching

3. Multi-qubit Pauli-string Synthesis

- Traveling Ancilla Qumode

4. Limited Connectivity Constraints

- Hybrid CVDV Hardware Mapping and Routing

2.1 Hamiltonian Grammar

Hamiltonian Model Example:

$$H = -t \sum_{i,j,\sigma} c_{i\sigma}^\dagger c_{j\sigma} + U \sum_i b_i^\dagger b_i + g \sum_{i,\sigma} \hat{n}_{i\sigma} (b_i^\dagger + b_i)$$

Corresponds Hamiltonian Grammar Representation:

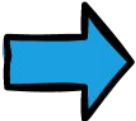
```
Const t = 1;
Const U = 1;
Const g = 1;

Range i = [0, 10, 1];
Range j = [0, 10, 1];
Range sigma = [0, 2, 1];

Result = - t *Sum_over(i, j, sigma){FC[i][sigma]* FA[j][sigma]}
        + U *Sum_over(i){BC[i]* BA[i]}
        + g * Sum_over(i, sigma){TensorProd(FN[i][sigma], BC[i] + BA[i])};
```


2.2 CVDVQASM and Multi-level Compilation

1. Hamiltonian Formula

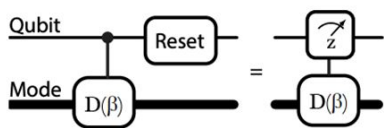
$$H = -t \sum_{i,j,\sigma} c_{i\sigma}^\dagger c_{j\sigma} + U \sum_i b_i^\dagger b_i + g \sum_{i,\sigma} \hat{n}_{i\sigma} (b_i^\dagger + b_i)$$


2. Hamiltonian Grammar

```
- t *Sum_over(i, j, sigma){FC[i][sigma]* FA[j][sigma]}
+ U *Sum_over(i){BC[i]* BA[i]}
+ g * Sum_over(i, sigma){TensorProd(FN[i][sigma], BC[i] + BA[i])};
```




5. Physical CVDVQASM file




4. Logical CVDVQASM file

```
// Pauli String with Parameter
pauli(pi/4) YIYZXXIIIIIIII;
pauli(pi/4) XZYXYYIIIIIIII;
// Phase Space Rotation Gate
R(pi/4) qm[1];
R(pi/4) qm[2];
// Control Displacement Gate
CD(pi/4) q[2], qm[1];
CD(pi/4) q[3], qm[1];
// Displacement Gate
D(pi/4) qm[2];
D(pi/4) qm[2];
```



3. Intermediate Representation

```
pauli(0.392699075j): IXIZIYII;
pauli(0.392699075j): IIVIXIII;
bosonic: exp(prod((-1j),dagger(b(0)),b(0)));
bosonic: exp(prod((-1j),dagger(b(1)),b(1)));
hybrid: exp(prod((-0.78539815j),sigma(0, 0),sum(dagger(b(0)),b(0))));
hybrid: exp(prod((0.78539815j),sigma(3, 0),sum(dagger(b(0)),b(0))));
```



3.1 Direct Qumode-centric Gate Synthesis

Type	Gate Name	Definition
Qubit	x, y Rotation	$r_\varphi(\theta) = \exp \left[-i\frac{\theta}{2} (\cos \varphi \sigma_x + \sin \varphi \sigma_y) \right]$
	z Rotation	$r_z(\theta) = \exp \left(-i\frac{\theta}{2} \sigma_z \right)$
Qumode	Phase-Space Rotation	$R(\theta) = \exp \left[-i\theta a^\dagger a \right]$
	Displacement	$D(\alpha) = \exp \left[\left(\alpha a^\dagger - \alpha^* a \right) \right]$
	Beam-Splitter	$BS(\theta, \varphi) = \exp \left[-i\frac{\theta}{2} \left(e^{i\varphi} a^\dagger b + e^{-i\varphi} ab^\dagger \right) \right]$
Hybrid	Conditional Phase-Space Rotation	$CR(\theta) = \exp \left[-i\frac{\theta}{2} \sigma_z a^\dagger a \right]$
	Conditional Parity	$CP = \exp \left[-i\frac{\pi}{2} \sigma_z a^\dagger a \right]$
	Conditional Displacement	$CD(\alpha) = \exp \left[\sigma_z \left(\alpha a^\dagger - \alpha^* a \right) \right]$
	Conditional Beam-Splitter	$CBS(\theta, \varphi) = \exp \left[-i\frac{\theta}{2} \sigma_z \left(e^{i\varphi} a^\dagger b + e^{-i\varphi} ab^\dagger \right) \right]$
	Rabi Interaction	$RB(\theta) = \exp \left[-i\sigma_x \left(\theta a^\dagger - \theta^* a \right) \right]$

3.2 Product Formula and Block Encoding

- Trotterization(Trotter-Suzuki formula)

$$e^{(M+N)t} \approx \left(e^{Mt'} e^{Nt'} \right)^n$$

- BCH(Baker Campbell Hausdorff formula)

$$e^{[M,N]t^2} \approx e^{Mt} e^{Nt} e^{-Mt} e^{-Nt}.$$

- Block Encoding

$$O = \begin{pmatrix} A & B \\ C & D \end{pmatrix}$$

$$O = |0\rangle\langle 0| \otimes A + |0\rangle\langle 1| \otimes B + |1\rangle\langle 0| \otimes C + |1\rangle\langle 1| \otimes D.$$

- Commutator $[A, B]$ and anticommutator $\sigma_z\{A, B\}$ implementation in CVDV architecture

3.3 Rule-Based Recursive Template Matching

Rules	Operator Template	Conditions	Decomposition Output	Reference	Precision
1	$\exp(Mt + Nt) \approx \text{Trotter}(Mt, Nt)$		$(\exp(Mt/k)\exp(Nt/k))^k$	Trotterization	Approx
2	$\exp([Mt, Nt]) \approx \text{BCH}(Mt, Nt)$		$\exp(Mt)\exp(Nt)\exp(-Mt)\exp(-Nt)$	BCH	Approx
3	$\exp(t^2[M, N])$	M, N Hermitian	$\exp([it\sigma_I N, it\sigma_I M])$	[20]	Exact
4	$\exp(-it^2\sigma_I\{M, N\})$	M, N Hermitian	$\exp([it\sigma_J M, it\sigma_K N])$	[20]	Exact
5	$\exp(-it^2\sigma_Z[M, N])$		$\exp([itN, it\sigma_Z M])$	This paper	Exact
6	$\exp(t^2\sigma_Z((MN - (MN)^\dagger)))$	$[M, N] = 0$	$\exp([X \cdot it\mathcal{B}_N \cdot X, it\mathcal{B}_M])$	[20]	Exact
7	$\exp(it^2\sigma_Z((MN + (MN)^\dagger)))$	$[M, N] = 0$	$\exp([S \cdot it\mathcal{B}_M \cdot S^\dagger, X \cdot it\mathcal{B}_N \cdot X])$	[20]	Exact
8	$\exp\left(-2it\begin{pmatrix} MN & 0 \\ 0 & -MN \end{pmatrix}\right)$	M, N Hermitian	$\exp(-it\sigma_Z[M, N] - it\sigma_Z\{M, N\})$	This paper	Exact
9	$\exp\left(2it^2\begin{pmatrix} MN & 0 \\ 0 & -MN \end{pmatrix}\right)$	$[M, N] = 0$ $MN = (MN)^\dagger$	$\exp([S \cdot it\mathcal{B}_M \cdot S^\dagger, X \cdot it\mathcal{B}_N \cdot X])$	[20]	Exact
10	$\exp(2it\mathcal{B}_{MN})$	$[M, N] = 0$	$X \cdot \exp(t\sigma_Y(MN - (MN)^\dagger) + it\sigma_X(MN + (MN)^\dagger)) \cdot X$	[20]	Exact
11	$\exp\left(it\begin{pmatrix} 2MN & 0 \\ 0 & -NM - (NM)^\dagger \end{pmatrix}\right)$	$MN = (MN)^\dagger$	$\exp([S \cdot it\mathcal{B}_M \cdot S^\dagger, X \cdot it\mathcal{B}_N \cdot X])$	[20]	Exact
12	$\mathcal{B}_a = \exp\left(2i\alpha\begin{pmatrix} 0 & a \\ a^\dagger & 0 \end{pmatrix}\right)$	$\alpha = \alpha^*$	$\exp(i(\pi/2)a^\dagger a)\exp(i(\alpha(a^\dagger + a)) \otimes \sigma_Y)\exp(-i(\pi/2)a^\dagger a)\exp(i(\alpha(a^\dagger + a)) \otimes \sigma_X)$	[20]	Approx
13	$\mathcal{B}_{a^\dagger} = \exp\left(2i\alpha\begin{pmatrix} 0 & a^\dagger \\ a & 0 \end{pmatrix}\right)$	$\alpha = \alpha^*$	$\exp(i(\pi/2)a^\dagger a)\exp(i(\alpha(a^\dagger + a)) \otimes \sigma_Y)\exp(-i(\pi/2)a^\dagger a)\exp(-i(\alpha(a^\dagger + a)) \otimes \sigma_X)$	This paper	Approx
14	$e^{(P_1 P_2 \dots P_n)(\alpha a_k^\dagger - \alpha^* a_k)}$		Multi-qubit-controlled displacement: Right hand side (RHS) of Equation (11) first line	[28]	Exact
15	$e^{2i\alpha^2 P_1 P_2 \dots P_n}$		Multi-Pauli Exponential: Right hand side (RHS) of Equation (9) first line	This Paper	Exact
16	All Native Gates RHS in Table 2		All Native Gates Left Hand Side (LHS) Table 2	[28]	Exact

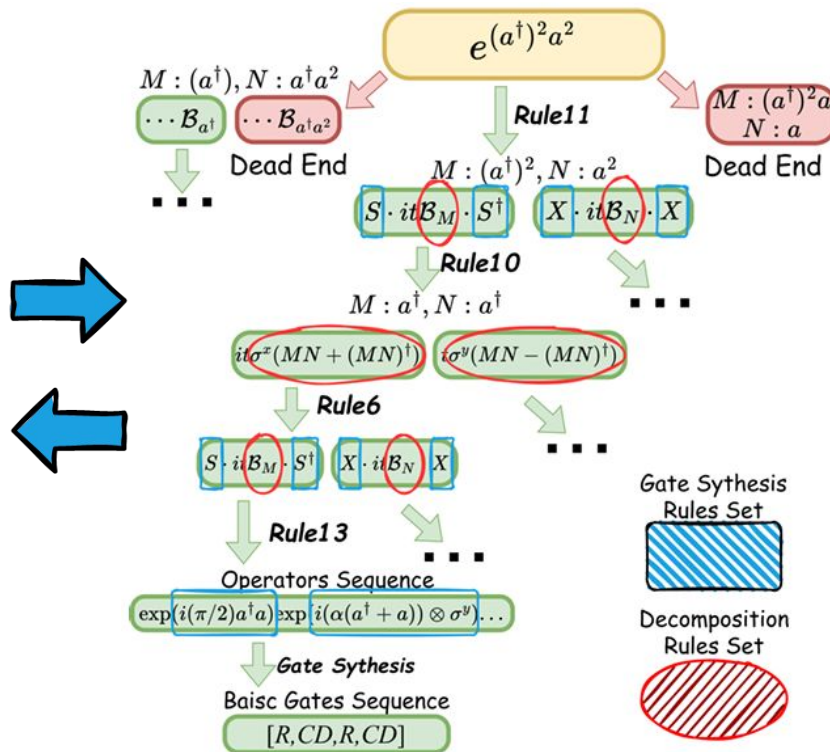
3.3 Rule-Based Recursive Template Matching

Basic Gates Set

Type	Gate Name	Definition
Qubit	x, y Rotation	$r_{\theta}(\theta) = \exp\left[-i\frac{\theta}{2}(\cos\sigma\sigma_x + \sin\sigma\sigma_y)\right]$
	z Rotation	$r_z(\theta) = \exp\left[-i\frac{\theta}{2}\sigma_z\right]$
Qumode	Phase-Space Rotation	$R(\theta) = \exp\left[-i\theta\hat{a}^\dagger\hat{a}\right]$
	Displacement	$D(\alpha) = \exp\left[\alpha\hat{a}^\dagger - \alpha^*\hat{a}\right]$
	Beam-Splitter	$BS(\theta, \varphi) = \exp\left[-i\frac{\theta}{2}(\hat{a}^\dagger\hat{a}^\dagger + \hat{a}\hat{a} + e^{-i\varphi}\hat{a}\hat{b}^\dagger)\right]$
	Conditional Phase-Space Rotation	$CR(\theta) = \exp\left[-i\frac{\theta}{2}\sigma_z\hat{a}^\dagger\hat{a}\right]$
Hybrid	Conditional Parity	$CP = \exp\left[-i\frac{\pi}{2}\sigma_z\hat{a}^\dagger\hat{a}\right]$
	Conditional Displacement	$CD(\alpha) = \exp\left[\sigma_z(\alpha\hat{a}^\dagger - \alpha^*\hat{a})\right]$
	Conditional Beam Splitter	$CBS(\theta, \varphi) = \exp\left[-i\frac{\theta}{2}\sigma_z(\hat{a}^\dagger\hat{a}^\dagger + \hat{a}\hat{a} + e^{-i\varphi}\hat{a}\hat{b}^\dagger)\right]$
	Rabi Interaction	$RI(\theta) = \exp\left[-i\sigma_z(\hat{b}^\dagger - \hat{b}^*)\hat{a}\right]$

Decomposition Rules Set

Rules	Operator Template	Conditions	Decomposition Output	Reference	Precision
1	$\exp(M\hat{a} + N\hat{a}^\dagger) \rightarrow \text{Toffoli}(M, N)$		$\exp(M)\exp(N)\exp(N^\dagger)$	Toffoli	Approx
2	$\exp\left[\frac{i}{2}(\hat{a}^\dagger + \hat{a})^2\right] \rightarrow \text{BCR}(\hat{a}, \hat{a})$		$\exp(M)\exp(N)\exp(-i\pi/4)\exp(N)$	BCR	Approx
3	$\exp(i\hat{a}^\dagger\hat{a})$	M, N Hermitian	$\exp(i\hat{a}^\dagger\hat{a})\exp(M)\exp(N)$	[10]	Exact
4	$\exp(-i\hat{a}^\dagger\hat{a})$	M, N Hermitian	$\exp(-i\hat{a}^\dagger\hat{a})\exp(M)\exp(N)$	[10]	Exact
5	$\exp(-i\hat{a}^\dagger\hat{a})$	M, N Hermitian	$\exp(-i\hat{a}^\dagger\hat{a})\exp(M)\exp(N)$	This paper	Exact
6	$\exp(i\hat{a}^\dagger\hat{a})\exp(MN + (MN)^\dagger)$	$[M, N] = 0$	$\exp(i\hat{a}^\dagger\hat{a})\exp(M)\exp(N)$	[10]	Exact
7	$\exp(i\hat{a}^\dagger\hat{a})\exp(MN - (MN)^\dagger)$	$[M, N] = 0$	$\exp(i\hat{a}^\dagger\hat{a})\exp(M)\exp(N)$	[10]	Exact
8	$\exp\left(-i\frac{\pi}{4}\left(\frac{\hat{a}^\dagger + \hat{a}}{2}\right)^2\right)$	M, N Hermitian	$\exp(-i\hat{a}^\dagger\hat{a})\exp(M)\exp(N)$	This paper	Exact
9	$\exp\left(-i\frac{\pi}{4}\left(\frac{\hat{a}^\dagger - \hat{a}}{2}\right)^2\right)$	$[M, N] = 0$ $RS = (RS)^\dagger$	$\exp(i\hat{a}^\dagger\hat{a})\exp(M)\exp(N)$	[10]	Exact
10	$\exp(i\hat{a}^\dagger\hat{a})\exp(MN + (MN)^\dagger)$	$X = \exp(i\hat{a}^\dagger\hat{a})\exp(MN + (MN)^\dagger) \in \text{SU}(2)$	$\exp(i\hat{a}^\dagger\hat{a})\exp(M)\exp(N)$	[10]	Exact
11	$\exp\left(-i\frac{\pi}{4}\left(\frac{\hat{a}^\dagger + \hat{a}}{2}\right)^2\right)$	$RS = (RS)^\dagger$	$\exp(i\hat{a}^\dagger\hat{a})\exp(M)\exp(N)$	[10]	Exact
12	$\exp\left(-i\frac{\pi}{4}\left(\frac{\hat{a}^\dagger - \hat{a}}{2}\right)^2\right)$	$\alpha = \alpha^*$	$\exp(i\hat{a}^\dagger\hat{a})\exp(MN + (MN)^\dagger) \in \text{SU}(2)$	[10]	Approx
13	$\exp\left(-i\frac{\pi}{4}\left(\frac{\hat{a}^\dagger + \hat{a}}{2}\right)^2\right)$	$\alpha = \alpha^*$	$\exp(i\hat{a}^\dagger\hat{a})\exp(MN + (MN)^\dagger) \in \text{SU}(2)$	This paper	Approx
14	$\exp(i\hat{a}^\dagger\hat{a})\exp(MN + (MN)^\dagger)$	Multi-qubit controlled Displacement: Right hand side (RHS) of Equation (1) first line	$\exp(i\hat{a}^\dagger\hat{a})\exp(MN + (MN)^\dagger) \in \text{SU}(2)$	This Paper	Exact
15	$\exp(i\hat{a}^\dagger\hat{a})\exp(MN - (MN)^\dagger)$	Multi-qubit controlled Displacement: Right hand side (RHS) of Equation (1) first line	$\exp(i\hat{a}^\dagger\hat{a})\exp(MN - (MN)^\dagger) \in \text{SU}(2)$	This Paper	Exact
16	All Native Gates (BGR in Table 1)		All Native Gates (BGR in Table 1)	[20] Table 1	Exact



Basic Gates Sequence
(Logical CVDVQASM Circuit)

Repeat the rewrite
process until it
produces only
basis gates

3.4 Multi-qubit Pauli-string Synthesis

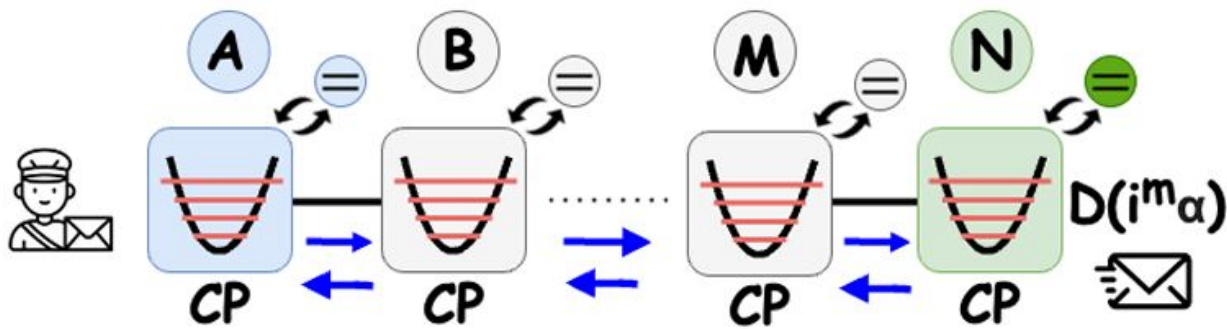
- Qubits are not directly connected with each other, we propose a scheme to synthesize an arbitrary multi-qubit Pauli-string on Hybrid CV-DV platforms.
- It is inspired by phase kickback in DV systems, where the phase of the control qubit is influenced by the operation on the target qubits.

$$\begin{aligned} U &= D^k(i\alpha) CD^{(k, P_1 \dots P_n)}(-\alpha) D^k(-i\alpha) CD^{(k, P_1 \dots P_n)}(\alpha) \\ &= e^{2i\alpha^2 P_1 P_2 \dots P_n} \end{aligned}$$

3.4 Multi-qubit Pauli-string Synthesis

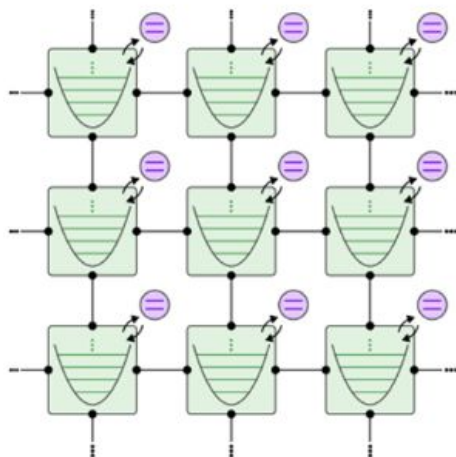
- Our final multi-Pauli exponential decomposition makes use of a multi-qubit controlled CD gate proposed by Liu et al., as below:




$$\begin{aligned} \text{CD}^{(k, P_1 P_2 \cdots P_n)}(\alpha) &= U_{\text{seq}}^\dagger D(i^n \alpha) U_{\text{seq}} \\ &= e^{(P_1 P_2 \cdots P_n)(\alpha a_k^\dagger - \alpha^* a_k)} \end{aligned}$$



4.1 Limited Hardware Connectivity

Superconducting



-  Microwave resonator
-  Superconducting qubit
-  Dispersive interaction

- Qumode-qumode Mapping.

Interactions are limited to adjacent qumodes. For non-adjacent qumodes, qumode SWAP gates are used, with routing optimized to minimize such SWAPs.

- Qubit-qumode Mapping.

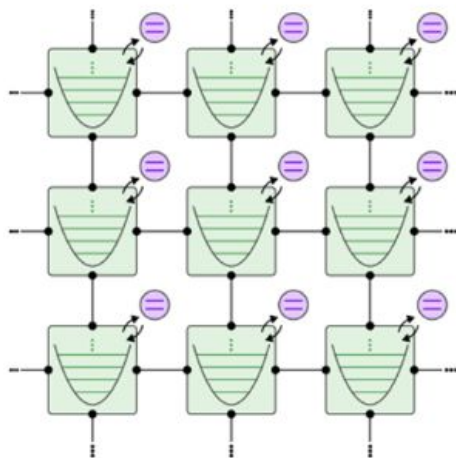
Each qumode interacts only with its associated qubit. For interactions with other qumodes, adjacency is established by moving qumodes, similar to qumode-qumode mapping.




- Qubit-qubit Mapping.

Qubits interact indirectly via an ancilla qumode, which is moved between qubits to mediate interactions and complete gate operations.

4.1 Limited Hardware Connectivity

Superconducting



-  Microwave resonator
-  Superconducting qubit
-  Dispersive interaction

- **Qumode-qumode Mapping.**

Interactions are limited to adjacent qumodes. For non-adjacent qumodes, qumode SWAP gates are used, with routing optimized to minimize such SWAPs.

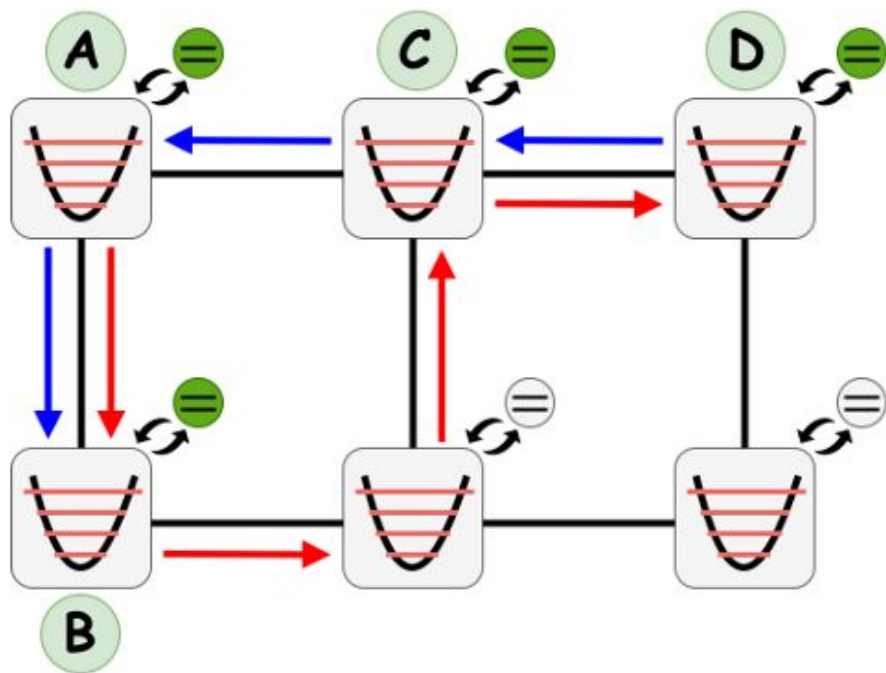
- **Qubit-qumode Mapping.**

Each qumode interacts only with its associated qubit. For interactions with other qumodes, adjacency is established by moving qumodes, similar to qumode-qumode mapping.

Working Frontier: all unresolved gates whose dependence has been resolved

Using a Qiskit Sabre-like reward function to execute gate from the frontier and update it.

4.2 Optimized Ancilla Qumode Routing



$A \rightarrow B \rightarrow V \rightarrow D$: **4** BS gates

$D \rightarrow C \rightarrow A \rightarrow B$: **3** BS gates

The Optimized Ancilla Qumode Routing Problem can be reformulated as a relaxed **Hamiltonian Path Problem**, similar to a modified Traveling Salesman Problem (TSP). Unlike the closed-path TSP, this problem allows revisiting vertices and does not require returning to the starting vertex.

4.2 Optimized Ancilla Qumode Routing

Qumode-SWAP

1 Beam-Splitter gate
(20x depth/duration)

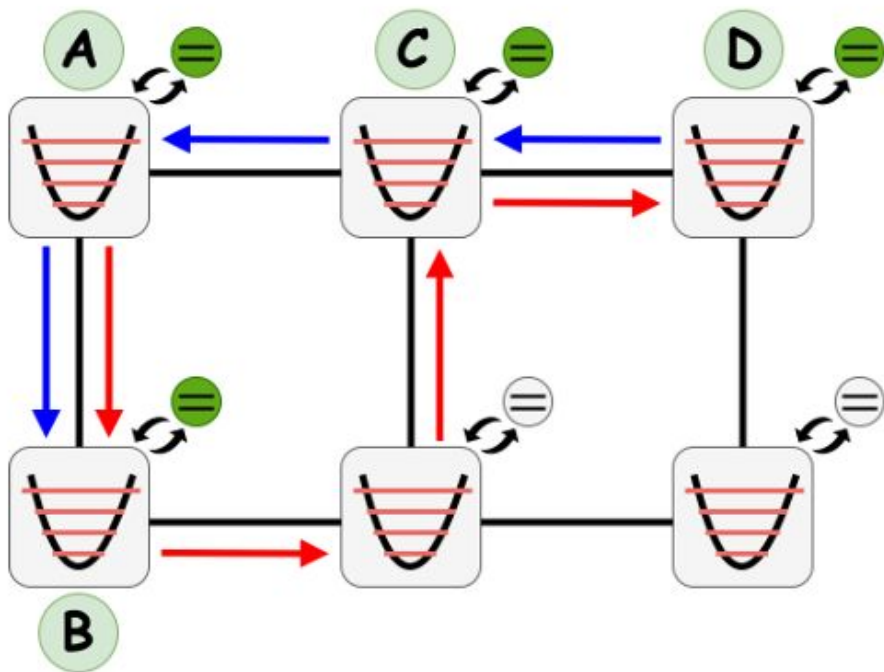
Qubit-SWAP (in CVDV System)

12 control displacement gates
12 Qumode-SWAPs
(480x depth/duration)

- **Dynamic Qubit Floating**

Relocation strategy, when a qubit-qubit pair distance in a specific multi-qubit exponential is too far, and this qubit-qubit pair appear often in the following multi-qubit exponential, we will try to relocate the qubit using Qubit-SWAP to cluster them.

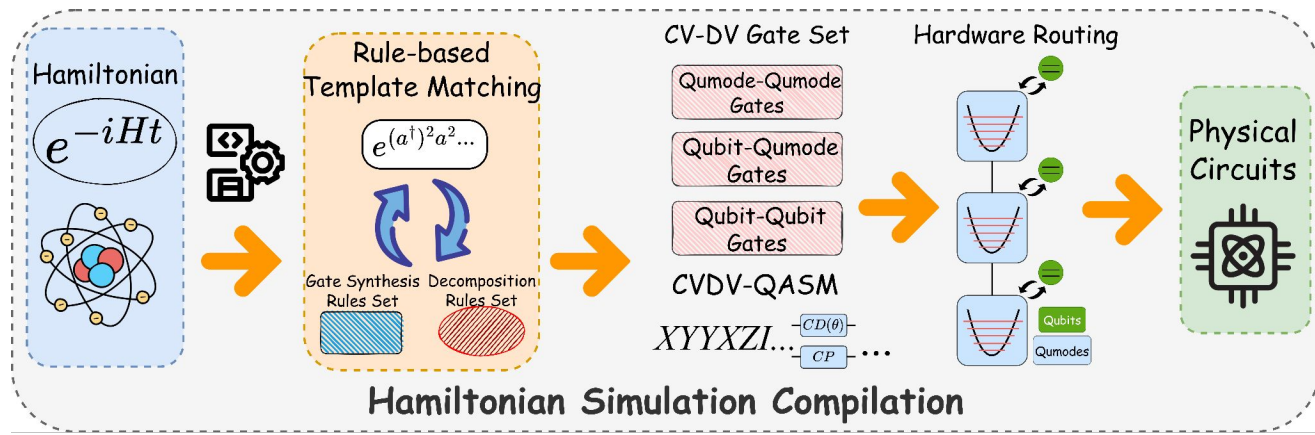
4.2 Optimized Ancilla Qumode Routing



- Christofides Algorithm
Baseline
- Threshold Accepting Algorithm
3-7% better duration time, 4.8% in avg
- Dynamic Qubit Floating
6% worse duration time in avg
4/20 better than baseline and 2/20 better than Threshold Accepting

5. End-to-end Implementation

1. **Hamiltonian Parsing:** Translates a Hamiltonian from mathematical form into a DSL-based representation.
2. **Intermediate Representation (IR):** Converts the DSL into an IR consisting of Pauli strings and operator expressions(bosonic, hybrid).
3. **Pattern Matching and Gate Synthesis:** Matches fermionic and bosonic operator terms and synthesizes them into logical CV-DV circuits in CVDVQASM format.
4. **Physical Mapping:** Maps logical circuits and Pauli terms to hardware-compliant physical circuits, and outputs the final(physical) CVDVQASM program(s).



5. End-to-end Implementation

- Evaluation 1. Multi Pauli-String Synthesis
 - 20 Qubit Hamiltonian such as LiH(4,12), BeH2(6,14) ...
 - # Pauli Strings from 631 to 1884
 - JW and BK encoding
- Evaluation 2. General Hamiltonian Simulation Compilation
 - 6 Hamiltonian Models such as Hubbard-Holstein Model, Bose-Hubbard Model ... At most 60 Qubits and 120 Qumodes

5. End-to-end Implementation

- Intermediate Tools 1. CVDV Mapping and Routing
 - Support more architecture(neutral atom)
 - Better relocate strategy when compile multi pauli-strings
- Intermediate Tools 2. Operator Pattern Matching
 - Flexible customize rules and multiple decomposition perspectives
 - Better compilation efficiency and robustness
 - Error analysis and unitary verification

Thank You!