

biobeam Documentation

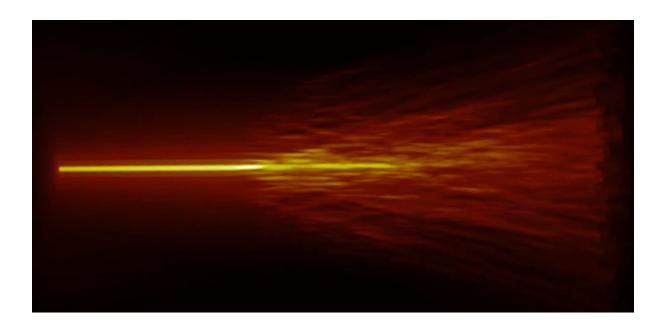
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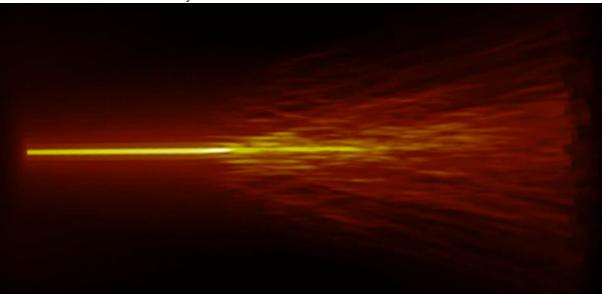
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1 Introduction

Biobeams is awesome. And so are you!



This is something I want to say that is not in the docstring.

2 Installation

To nicely render the 3d output it is advisible to install Spimagine, an OpenCL accelerated renderer Spimagine

pip install spimagine

After that you should be able to simple do

pip install biobeams

3 Basic Usage

3.1 Beam propagation

the main class for gpu accelerated bpm propagation

__init__ (size=None, shape=None, units=None, dn=None, lam=0.5, n0=1.0, simul_xy=None, simul_z=1, n_volumes=1, enforce_subsampled=False, fftplan_kwargs={})

Parameters

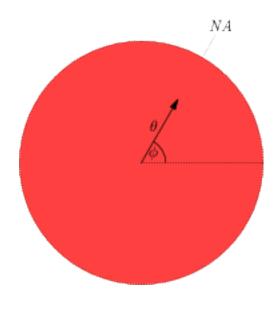
- size ((Sx, Sy, Sz)) the size of the geometry in microns (Sx,Sy,Sz)
- **shape** ((Nx, Ny, Nz)) the shape of the geometry in pixels (Nx, Ny, Nz)
- units ((dx, dy, dz)) the voxelsizes in microns (dx, dy, dz)
- **dn** (ndarray (float32|complex64)) refractive index distribution, dn.shape != (Nz,Ny,Nx)
- lam (float) the wavelength in microns
- n0 (float) the refractive index of the surrounding media
- **simul_xy** ((Nx, Ny, Nz), optional) the shape of the 2d computational geometry in pixels (Nx,Ny) (e.g. subsampling in xy)
- **simul_z** (*int*, *optional*) the subsampling factor along z
- n_volumes (int) splits the domain into chunks if GPU memory is not large enough (will be set automatically)

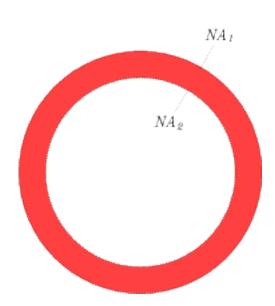
Example

4 Input Beam patterns

4.1 Gaussian/Bessel beams

Gaussian/Bessel beams





biobeam.focus_field_beam ($shape=(128,\ 128,\ 128)$, $units=(0.1,\ 0.1,\ 0.1)$, lam=0.5, NA=0.6, n0=1.0, $return_all_fields=False$, $n_integration_steps=200$) calculates the focus field for a perfect, aberration free optical system for x polzarized illumination via the vectorial debye diffraction integral (see 1). The pupil function is given by numerical aperture(s) NA (that can be a list to model bessel beams, see further below)

- **shape** (Nx, Ny, Nz) the shape of the geometry
- units (dx, dy, dz) the pixel sizes in microns
- lam (float) the wavelength of light used in microns
- NA (float/list) the numerical aperture(s) of the illumination objective that is either a single number (for gaussian beams) or an even length list of NAs (for bessel beams), e.g. NA = [0.5, 0.55] lets light through the annulus 0.5<0.55 (making a bessel beam) or NA = [0.1, 0.2, 0.5, 0.6] lets light through the annulus 0.1<0.2 and 0.5<0.6 making a beating double bessel beam...
- n0 (float) the refractive index of the medium
- n_integration_steps (int) number of integration steps to perform
- return_all_fields (boolean) if True returns also the complex vectorial field components

¹ Matthew R. Foreman, Peter Toeroek, Computational methods in vectorial imaging, Journal of Modern Optics, 2011, 58, 5-6, 339

- **u** (*ndarray*) the intensity of the focus field
- (u,ex,ey,ez) (list(ndarray)) the intensity of the focus field and the complex field components (if return_all_fields is True)

Example

```
>>> u = focus_field_beam((128,128,128), (0.1,0.1,.1), lam=.5, NA = .4)
```

References

biobeam.focus_field_beam_plane (shape=(128, 128), units=(0.1, 0.1), z=0.0, lam=0.5, NA=0.6, n0=1.0, $ex_g=None$, $n_integration_steps=200$) calculates the complex 2d input field at position -z of a perfect, aberration free optical system

Parameters

- **shape** (Nx, Ny) the 2d shape of the geometry
- units (dx, dy) the pixel sizes in microns
- **z** (float) defocus position in microns, such that the beam would focus at z e.g. an input field with z = 10. would hav its focus spot after 10 microns
- lam (float) the wavelength of light used in microns
- NA (float/list) the numerical aperture(s) of the illumination objective that is either a single number (for gaussian beams) or an even length list of NAs (for bessel beams), e.g. NA = [0.5,0.55] lets light through the annulus 0.5<0.55 (making a bessel beam) or NA = [0.1,0.2,0.5,0.6] lets light through the annulus 0.1<0.2 and 0.5<0.6 making a beating double bessel beam...
- **n0** (float) the refractive index of the medium
- n_integration_steps (int) number of integration steps to perform

Returns ex – the complex field

Return type ndarray

Example

```
>>> # the input pattern of a bessel beam that will focus after 4 microns
>>> ex = focus_field_beam_plane((256,256), (0.1,0.1), z = 4, lam=.5, NA = (.4,.5))
```

See also:

biobeam.focus_field_beam() the 3d function

4.2 Cylindrical Lens



```
biobeam.focus_field_cylindrical (shape=(128, 128, 128), units=(0.1, 0.1, 0.1), lam=0.5, NA=0.3, n0=1.0, return\_all\_fields=False, n\_integration\_steps=100)
```

calculates the focus field for a perfect, aberration free cylindrical lens after x polarized illumination via the vectorial debye diffraction integral (see ²). The pupil function is given by the numerical aperture NA

Parameters

- **shape** (Nx, Ny, Nz) the shape of the geometry
- units (dx, dy, dz) the pixel sizes in microns
- lam (float) the wavelength of light used in microns
- NA (float) the numerical aperture of the lens
- n0 (float) the refractive index of the medium
- return_all_fields (boolean) if True, returns u,ex,ey,ez where ex/ey/ez are the complex field components
- n_integration_steps (int) number of integration steps to perform
- return_all_fields if True returns also the complex vectorial field components

Returns

- **u** (*ndarray*) the intensity of the focus field
- (u,ex,ey,ez) (list(ndarray)) the intensity of the focus field and the complex field components (if return_all_fields is True)

Example

```
>>> u, ex, ey, ez = focus_field_cylindrical((128,128,128), (0.1,0.1,.1), lam=.5, NA = .4, ret
```

References

```
biobeam.focus_field_cylindrical_plane (shape=(128, 128), units=(0.1, 0.1), z=0.0, lam=0.5, NA=0.3, n0=1.0, ex\_g=None, n\_integration\_steps=200)
```

calculates the complex 2d input field at position -z of a perfect, aberration free optical system

Parameters

- **shape** (Nx, Ny) the 2d shape of the geometry
- units (dx, dy) the pixel sizes in microns
- **z** (float) defocus position in microns, such that the beam would focus at z e.g. an input field with z = 10. would hav its focus spot after 10 microns
- lam (float) the wavelength of light used in microns
- NA (float/list) the numerical aperture(s) of the illumination objective that is either a single number (for gaussian beams) or an even length list of NAs (for bessel beams), e.g. NA = [0.5,0.55] lets light through the annulus 0.5<0.55 (making a bessel beam) or NA = [0.1,0.2,0.5,0.6] lets light through the annulus 0.1<0.2 and 0.5<0.6 making a beating double bessel beam...
- n0 (float) the refractive index of the medium
- n_integration_steps (int) number of integration steps to perform

Returns ex – the complex field

² Colin J. R. Sheppard: Cylindrical lenses—focusing and imaging: a review, Appl. Opt. 52, 538-545 (2013)

Return type ndarray

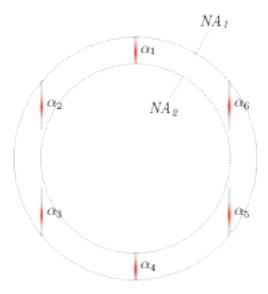
Example

```
>>> # the input pattern of a bessel beam that will focus after 4 microns
>>> ex = focus_field_cylindrical_plane((256,256), (0.1,0.1), z = 4., lam=.5, NA = (.4,.5))
```

See also:

biobeam.focus_field_cylindrical() the 3d function

4.3 Bessel Lattices



biobeam.focus_field_lattice (shape=(128,128,128), units=(0.1,0.1,0.1), lam=0.5, NA1=0.4, NA2=0.5, sigma=0.1, kpoints=6, $return_all_fields=False$, n0=1.0, $n_integration_steps=100$)

n0=1.0, $n_integration_steps=100$) Calculates the focus field for a bessel lattice. The pupil function consists out of discrete points (kpoints) superimposed on an annulus (NA1<NA2) which are smeared out by a 1d gaussian of given sigma creating an array of bessel beams in the focal plane (see 3).

- **shape** (Nx, Ny, Nz) the shape of the geometry
- units (dx, dy, dz) the pixel sizes in microns
- lam (float) the wavelength of light used in microns
- NA1 (float/list) the numerical aperture of the inner ring
- NA2 (float/list) the numerical aperture of the outer ring
- **sigma** (float) the standard deviation of the gaussian smear function applied to each point on the aperture (the bigger sigma, the tighter the sheet in y)
- **kpoints** (int/ (2, N) array) defines the set of points on the aperture that create the lattice, can be a (2,N) ndarray, such that kpoints[:,i] are the coordinates of the ith point a single int, defining points on a regular polygon (e.g. 4 for a square lattice, 6 for a hex lattice) $k_i = \arcsin\frac{NA_1+NA_2}{2n_0} \begin{pmatrix} \cos\phi_i \\ \sin\phi_i \end{pmatrix}$, $\phi_i = \frac{\pi}{2} + \frac{2i}{N}$
- **n0** (float) the refractive index of the medium

³ Chen et al. Lattice light-sheet microscopy: imaging molecules to embryos at high spatiotemporal resolution. Science 346, (2014).

- n_integration_steps (int) number of integration steps to perform
- return_all_fields (boolean) if True, returns u,ex,ey,ez where ex/ey/ez are the complex vector field components

- **u** (ndarray) the intensity of the focus field
- (u,ex,ey,ez) (list(ndarray)) the intensity of the focus field and the complex field components (if return all fields is True)

Example

```
>>> u = focus_field_lattice((128,128,128), (0.1,0.1,.1), lam=.5, NA1 = .44, NA2 = .55, kpoint
```

References

biobeam.focus_field_lattice_plane (shape=(256, 256), units=(0.1, 0.1), z=0.0, lam=0.5, NA1=0.4, NA2=0.5, sigma=0.1, kpoints=6, n0=1.0, $apodization_bound=10$, $ex_g=None$, $n_integration_steps=100$)

calculates the complex 2d input field at position -z of a for a bessel lattice beam.

Parameters

- **shape** (Nx, Ny) the shape of the geometry
- units (dx, dy) the pixel sizes in microns
- \mathbf{z} (float) defocus position in microns, such that the beam would focus at z e.g. an input field with z = 10. would have its focal spot after 10 microns
- lam (float) the wavelength of light used in microns
- NA1 (float/list) the numerical aperture of the inner ring
- NA2 (float/list) the numerical aperture of the outer ring
- **sigma** (float) the standard deviation of the gaussian smear function applied to each point on the aperture (the bigger sigma, the tighter the sheet in y)
- **kpoints** (int/ (2, N) array) defines the set of points on the aperture that create the lattice, can be a (2,N) ndarray, such that kpoints[:,i] are the coordinates of the ith point a single int, defining points on a regular polygon (e.g. 4 for a square lattice, 6 for a hex lattice) $k_i = \arcsin \frac{NA_1 + NA_2}{2n_0} \begin{pmatrix} \cos \phi_i \\ \sin \phi_i \end{pmatrix}$, $\phi_i = \frac{\pi}{2} + \frac{2i}{N}$
- n0 (float) the refractive index of the medium
- **apodization_bound** (*int*) width of the region where the input field is tapered to zero (with a hamming window) on the +/- x borders
- n_integration_steps (int) number of integration steps to perform
- return_all_fields (boolean) if True, returns u,ex,ey,ez where ex/ey/ez are the complex vector field components

Returns \mathbf{u} – the 2d complex field

Return type ndarray

```
>>> u = focus_field_lattice_plane((128,128), (0.1,0.1), z = 2., lam=.5, NA1 = .44, NA2 = .55,
```

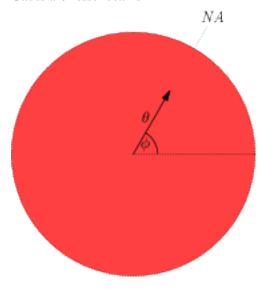
See also:

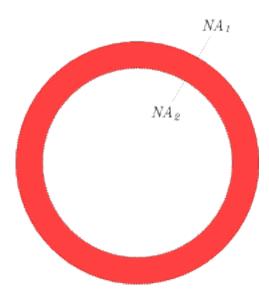
biobeam.focus_field_lattice() the corresponding 3d function

5 Focus field calculations

5.1 Gaussian/Bessel beams

Gaussian/Bessel beams





biobeam.focus_field_beam ($shape=(128,\ 128,\ 128)$, $units=(0.1,\ 0.1,\ 0.1)$, $lam=0.5,\ NA=0.6$, n0=1.0, $return_all_fields=False$, $n_integration_steps=200$) calculates the focus field for a perfect, aberration free optical system for x polzarized illumination via the vectorial debye diffraction integral (see 1). The pupil function is given by numerical aperture(s) NA (that can be a list to model bessel beams, see further below)

¹ Matthew R. Foreman, Peter Toeroek, Computational methods in vectorial imaging, Journal of Modern Optics, 2011, 58, 5-6, 339

- **shape** (Nx, Ny, Nz) the shape of the geometry
- units (dx, dy, dz) the pixel sizes in microns
- lam (float) the wavelength of light used in microns
- NA (float/list) the numerical aperture(s) of the illumination objective that is either a single number (for gaussian beams) or an even length list of NAs (for bessel beams), e.g. NA = [0.5, 0.55] lets light through the annulus 0.5<0.55 (making a bessel beam) or NA = [0.1, 0.2, 0.5, 0.6] lets light through the annulus 0.1<0.2 and 0.5<0.6 making a beating double bessel beam...
- **n0** (float) the refractive index of the medium
- n_integration_steps (int) number of integration steps to perform
- return_all_fields (boolean) if True returns also the complex vectorial field components

- **u** (*ndarray*) the intensity of the focus field
- (u,ex,ey,ez) (list(ndarray)) the intensity of the focus field and the complex field components (if return_all_fields is True)

Example

```
>>> u = focus_field_beam((128,128,128), (0.1,0.1,.1), lam=.5, NA = .4)
```

References

biobeam.focus_field_beam_plane (shape=(128, 128), units=(0.1, 0.1), z=0.0, lam=0.5, NA=0.6, n0=1.0, $ex_g=None$, $n_integration_steps=200$) calculates the complex 2d input field at position -z of a perfect, aberration free optical system

Parameters

- **shape** (Nx, Ny) the 2d shape of the geometry
- units (dx, dy) the pixel sizes in microns
- \mathbf{z} (float) defocus position in microns, such that the beam would focus at z e.g. an input field with z = 10. would hav its focus spot after 10 microns
- lam (float) the wavelength of light used in microns
- NA (float/list) the numerical aperture(s) of the illumination objective that is either a single number (for gaussian beams) or an even length list of NAs (for bessel beams), e.g. NA = [0.5,0.55] lets light through the annulus 0.5<0.55 (making a bessel beam) or NA = [0.1,0.2,0.5,0.6] lets light through the annulus 0.1<0.2 and 0.5<0.6 making a beating double bessel beam...
- n0 (float) the refractive index of the medium
- n_integration_steps (int) number of integration steps to perform

Returns ex – the complex field

Return type ndarray

Example

```
>>> # the input pattern of a bessel beam that will focus after 4 microns
>>> ex = focus_field_beam_plane((256,256), (0.1,0.1), z = 4, lam=.5, NA = (.4,.5))
```

See also:

biobeam.focus_field_beam() the 3d function

5.2 Cylindrical Lens



biobeam.focus_field_cylindrical(shape=(128, 128, 128), units=(0.1, 0.1, 0.1), $lam=0.5, NA=0.3, n0=1.0, return_all_fields=False$, $n_integration_steps=100$)

calculates the focus field for a perfect, aberration free cylindrical lens after x polarized illumination via the vectorial debye diffraction integral (see ²). The pupil function is given by the numerical aperture NA

Parameters

- **shape** (Nx, Ny, Nz) the shape of the geometry
- units (dx, dy, dz) the pixel sizes in microns
- lam (float) the wavelength of light used in microns
- NA (float) the numerical aperture of the lens
- **n0** (float) the refractive index of the medium
- return_all_fields (boolean) if True, returns u,ex,ey,ez where ex/ey/ez are the complex field components
- n_integration_steps (int) number of integration steps to perform
- return_all_fields if True returns also the complex vectorial field components

Returns

- **u** (*ndarray*) the intensity of the focus field
- (**u,ex,ey,ez**) (*list(ndarray)*) the intensity of the focus field and the complex field components (if return_all_fields is True)

Example

```
>>> u, ex, ey, ez = focus_field_cylindrical((128,128,128), (0.1,0.1,.1), lam=.5, NA = .4, ret
```

References

biobeam.focus_field_cylindrical_plane ($shape=(128,\ 128),\ units=(0.1,\ 0.1),\ z=0.0,\ lam=0.5,\ NA=0.3,\ n0=1.0,\ ex_g=None,\ n_integration_steps=200)$

calculates the complex 2d input field at position -z of a perfect, aberration free optical system

² Colin J. R. Sheppard: Cylindrical lenses—focusing and imaging: a review, Appl. Opt. 52, 538-545 (2013)

- **shape** (Nx, Ny) the 2d shape of the geometry
- units (dx, dy) the pixel sizes in microns
- **z** (float) defocus position in microns, such that the beam would focus at z e.g. an input field with z = 10. would hav its focus spot after 10 microns
- lam (float) the wavelength of light used in microns
- NA (float/list) the numerical aperture(s) of the illumination objective that is either a single number (for gaussian beams) or an even length list of NAs (for bessel beams), e.g. NA = [0.5,0.55] lets light through the annulus 0.5<0.55 (making a bessel beam) or NA = [0.1,0.2,0.5,0.6] lets light through the annulus 0.1<0.2 and 0.5<0.6 making a beating double bessel beam...
- n0 (float) the refractive index of the medium
- n_integration_steps (int) number of integration steps to perform

Returns ex – the complex field

Return type ndarray

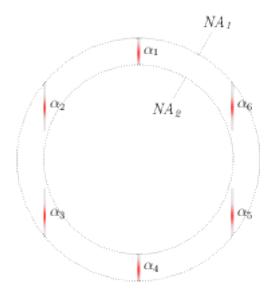
Example

```
>>> # the input pattern of a bessel beam that will focus after 4 microns
>>> ex = focus_field_cylindrical_plane((256,256), (0.1,0.1), z = 4., lam=.5, NA = (.4,.5))
```

See also:

biobeam.focus_field_cylindrical() the 3d function

5.3 Bessel Lattices



biobeam.focus_field_lattice (shape=(128,128,128), units=(0.1,0.1,0.1), lam=0.5, NA1=0.4, NA2=0.5, sigma=0.1, kpoints=6, $return_all_fields=False$, n0=1.0, $n_integration_steps=100$)

Calculates the focus field for a bessel lattice. The pupil function consists out of discrete points (kpoints) superimposed on an annulus (NA1<NA2) which are smeared out by a 1d gaussian of given sigma creating an array of bessel beams in the focal plane (see ³).

³ Chen et al. Lattice light-sheet microscopy: imaging molecules to embryos at high spatiotemporal resolution. Science 346, (2014).

- **shape** (Nx, Ny, Nz) the shape of the geometry
- units (dx, dy, dz) the pixel sizes in microns
- lam (float) the wavelength of light used in microns
- NA1 (float/list) the numerical aperture of the inner ring
- NA2 (float/list) the numerical aperture of the outer ring
- **sigma** (float) the standard deviation of the gaussian smear function applied to each point on the aperture (the bigger sigma, the tighter the sheet in y)
- **kpoints** (int/ (2, N) array) defines the set of points on the aperture that create the lattice, can be a (2,N) ndarray, such that kpoints[:,i] are the coordinates of the ith point a single int, defining points on a regular polygon (e.g. 4 for a square lattice, 6 for a hex lattice) $k_i = \arcsin\frac{NA_1 + NA_2}{2n_0} \begin{pmatrix} \cos\phi_i \\ \sin\phi_i \end{pmatrix}$, $\phi_i = \frac{\pi}{2} + \frac{2i}{N}$
- n0 (float) the refractive index of the medium
- n_integration_steps (int) number of integration steps to perform
- return_all_fields (boolean) if True, returns u,ex,ey,ez where ex/ey/ez are the complex vector field components

- **u** (*ndarray*) the intensity of the focus field
- (u,ex,ey,ez) (list(ndarray)) the intensity of the focus field and the complex field components (if return_all_fields is True)

Example

```
>>> u = focus_field_lattice((128,128,128), (0.1,0.1,.1), lam=.5, NA1 = .44, NA2 = .55, kpoint
```

References

biobeam.focus_field_lattice_plane (shape=(256, 256), units=(0.1, 0.1), z=0.0, lam=0.5, NA1=0.4, NA2=0.5, sigma=0.1, kpoints=6, n0=1.0, $apodization_bound=10$, $ex_g=None$, $n_integration_steps=100$)

calculates the complex 2d input field at position -z of a for a bessel lattice beam.

- **shape** (Nx, Ny) the shape of the geometry
- units (dx, dy) the pixel sizes in microns
- \mathbf{z} (float) defocus position in microns, such that the beam would focus at z e.g. an input field with z = 10. would have its focal spot after 10 microns
- lam (float) the wavelength of light used in microns
- NA1 (float/list) the numerical aperture of the inner ring
- NA2 (float/list) the numerical aperture of the outer ring
- **sigma** (float) the standard deviation of the gaussian smear function applied to each point on the aperture (the bigger sigma, the tighter the sheet in y)
- **kpoints** (*int*/ (2, N) array) defines the set of points on the aperture that create the lattice, can be a (2,N) ndarray, such that kpoints[:,i] are the coordinates of

the ith point - a single int, defining points on a regular polygon (e.g. 4 for a square lattice, 6 for a hex lattice) $k_i = \arcsin\frac{NA_1+NA_2}{2n_0} \begin{pmatrix} \cos\phi_i \\ \sin\phi_i \end{pmatrix}$, $\phi_i = \frac{\pi}{2} + \frac{2i}{N}$

- n0 (float) the refractive index of the medium
- **apodization_bound** (*int*) width of the region where the input field is tapered to zero (with a hamming window) on the +/- x borders
- n_integration_steps (int) number of integration steps to perform
- return_all_fields (boolean) if True, returns u,ex,ey,ez where ex/ey/ez are the complex vector field components

Returns \mathbf{u} – the 2d complex field

Return type ndarray

Example

```
>>> u = focus_field_lattice_plane((128,128), (0.1,0.1), z = 2., lam=.5, NA1 = .44, NA2 = .55,
```

See also:

biobeam.focus_field_lattice() the corresponding 3d function

6 Simulating light sheet microscopy

7 Aberrations

8 Examples

8.1 Plane wave scattered by sphere

```
# create the refractive index difference
x = 0.1 * np.arange(-128, 128)
Z, Y, X = np.meshgrid(x, x, x, indexing = "ij")
R = np.sqrt(X**1+Y**2+Z**2)
dn = 0.05 * (R<2.)
# create the computational geometry
m = Bpm3d(dn = dn, units = (0.1, 0.1, 0.1), lam = 0.5)
# propagate a plane wave and return the intensity
u = m._propagate()
# vizualize
import matplotlib.pyplot as plt
plt.subplot(1,2,1)
plt.imshow(u[...,128], cmap = "hot")
plt.title("zy slice")
plt.subplot(1,2,2)
plt.imshow(u[128,...], cmap = "hot")
plt.title("xy slice")
```

- 8.2 Light sheet through cell phantom
- 8.3 Computing the psf inside a cell phantom
- 8.4 Aberration from sphere

9 Some Examples

or not?

print "huhu"
huhu

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