



# biobeam Documentation

*Release 0.1.0*

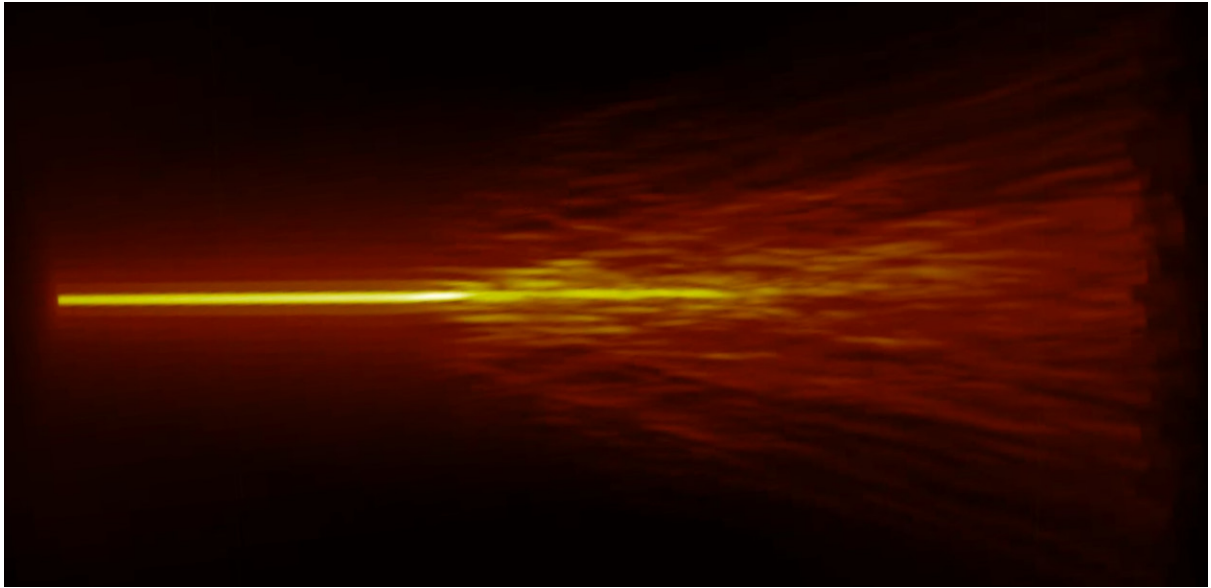
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## Contents

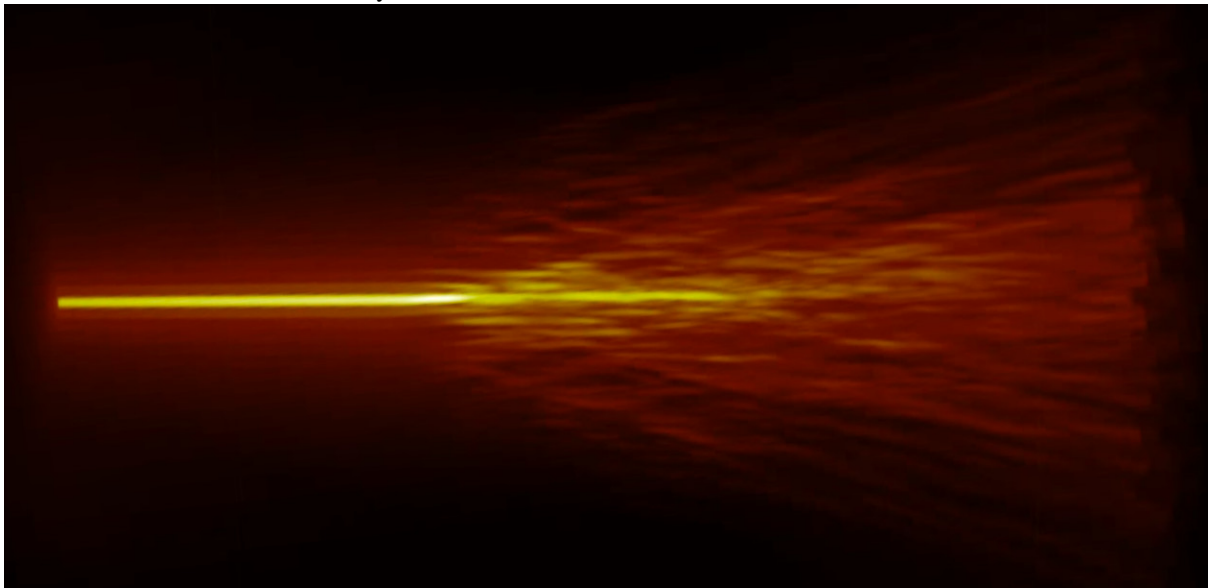
<b>1</b>	<b>Introduction</b>	<b>2</b>
<b>2</b>	<b>Installation</b>	<b>2</b>
<b>3</b>	<b>Basic Usage</b>	<b>3</b>
3.1	Beam propagation . . . . .	3
<b>4</b>	<b>Input Beam patterns</b>	<b>3</b>
4.1	Gaussian/Bessel beams . . . . .	3
4.2	Cylindrical Lens . . . . .	5
4.3	Bessel Lattices . . . . .	7
<b>5</b>	<b>Focus field calculations</b>	<b>8</b>
5.1	Gaussian/Bessel beams . . . . .	8
5.2	Cylindrical Lens . . . . .	10
5.3	Bessel Lattices . . . . .	12
<b>6</b>	<b>Simulating light sheet microscopy</b>	<b>13</b>
<b>7</b>	<b>Aberrations</b>	<b>13</b>
<b>8</b>	<b>Examples</b>	<b>13</b>
8.1	Plane wave scattered by sphere . . . . .	13
8.2	Light sheet through cell phantom . . . . .	13
8.3	Computing the psf inside a cell phantom . . . . .	13
8.4	Aberration from sphere . . . . .	13
<b>9</b>	<b>Some Examples</b>	<b>13</b>
	<b>Index</b>	<b>15</b>

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## 1 Introduction

Biobeams is awesome. And so are you!



This is something I want to say that is not in the docstring.

## 2 Installation

To nicely render the 3d output it is advisable to install *Spimagine*, an OpenCL accelerated renderer [Spimagine](#)

```
pip install spimagine
```

After that you should be able to simply do

```
pip install biobeams
```

## 3 Basic Usage

### 3.1 Beam propagation

`class biobeam.Bpm3d` (*size=None, shape=None, units=None, dn=None, lam=0.5, n0=1.0, simul\_xy=None, simul\_z=1, n\_volumes=1, enforce\_subsampling=False, fftplan\_kwargs={}*)

the main class for gpu accelerated bpm propagation

`__init__` (*size=None, shape=None, units=None, dn=None, lam=0.5, n0=1.0, simul\_xy=None, simul\_z=1, n\_volumes=1, enforce\_subsampling=False, fftplan\_kwargs={}*)

#### Parameters

- **size** (*(Sx, Sy, Sz)*) – the size of the geometry in microns (Sx,Sy,Sz)
- **shape** (*(Nx, Ny, Nz)*) – the shape of the geometry in pixels (Nx,Ny,Nz)
- **units** (*(dx, dy, dz)*) – the voxelsizes in microns (dx,dy,dz)
- **dn** (*ndarray (float32|complex64)*) – refractive index distribution, `dn.shape != (Nz,Ny,Nx)`
- **lam** (*float*) – the wavelength in microns
- **n0** (*float*) – the refractive index of the surrounding media
- **simul\_xy** (*(Nx, Ny, Nz), optional*) – the shape of the 2d computational geometry in pixels (Nx,Ny) (e.g. subsampling in xy)
- **simul\_z** (*int, optional*) – the subsampling factor along z
- **n\_volumes** (*int*) – splits the domain into chunks if GPU memory is not large enough (will be set automatically)

#### Example

```
>>> m = Bpm3d(size = (10,10,10), shape = (256,256,256), units = (0.1,0.1,0.1), lam = 0.488, n0 = 1.0)
```

**aberr\_at** (*NA=0.4, center=(0, 0, 0), n\_zern=20, n\_integration\_steps=200*)

*c = (cx,cy,cz)* in realtive pixel coordinates wrt the center

returns phi, zern

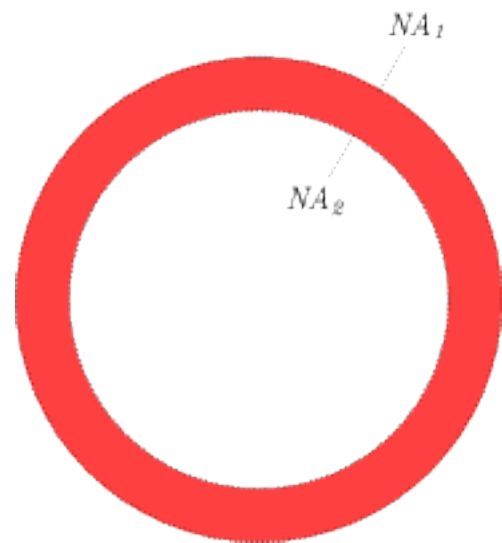
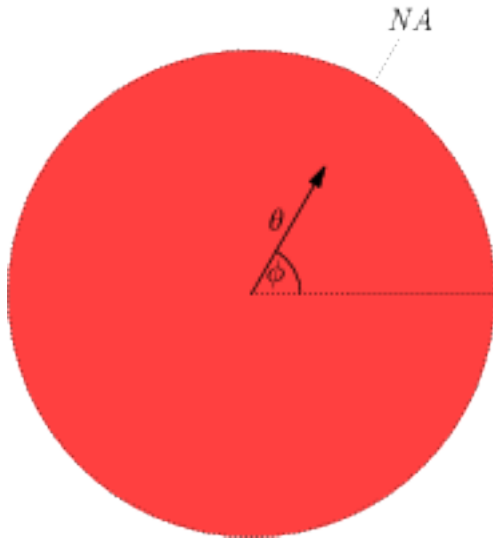
**aberr\_field\_grid** (*NA, cxs, cys, cz, n\_zern=20, n\_integration\_steps=200*)

*cxs, cys* are equally spaced 1d arrays defining the grid

## 4 Input Beam patterns

### 4.1 Gaussian/Bessel beams

Gaussian/Bessel beams



`biobeam.focus_field_beam(shape, units, lam=0.5, NA=0.6, n0=1.0, return_all_fields=False, n_integration_steps=200)`

calculates the focus field for a perfect, aberration free optical system for x polarized illumination via the vectorial debye diffraction integral (see <sup>1</sup>). The pupil function is given by numerical aperture(s) NA (that can be a list to model bessel beams, see further below)

#### Parameters

- **shape** ( $N_x, N_y, N_z$ ) – the shape of the geometry
- **units** ( $dx, dy, dz$ ) – the pixel sizes in microns
- **lam** (*float*) – the wavelength of light used in microns
- **NA** (*float/list*) – the numerical aperture(s) of the illumination objective that is either a single number (for gaussian beams) or an even length list of NAs (for bessel beams), e.g.  $NA = [0.5, 0.55]$  lets light through the annulus  $0.5 < 0.55$  (making a bessel beam ) or  $NA = [0.1, 0.2, 0.5, 0.6]$  lets light through the annulus  $0.1 < 0.2$  and  $0.5 < 0.6$  making a beating double bessel beam...
- **n0** (*float*) – the refractive index of the medium
- **n\_integration\_steps** (*int*) – number of integration steps to perform
- **return\_all\_fields** (*boolean*) – if True returns also the complex vectorial field components

<sup>1</sup> Matthew R. Foreman, Peter Toeroek, *Computational methods in vectorial imaging*, Journal of Modern Optics, 2011, 58, 5-6, 339

### Returns

- **u** (*ndarray*) – the intensity of the focus field
- **(u,ex,ey,ez)** (*list(ndarray)*) – the intensity of the focus field and the complex field components (if `return_all_fields` is `True`)

### Example

```
>>> u = focus_field_beam((128,128,128), (0.1,0.1,.1), lam=.5, NA = .4)
```

### References

`biobeam.focus_field_beam_plane(shape=(128, 128), units=(0.1, 0.1), z=0.0, lam=0.5, NA=0.6, n0=1.0, ex_g=None, n_integration_steps=200)`  
calculates the complex 2d input field at position -z of a perfect, aberration free optical system

### Parameters

- **shape** (*Nx, Ny*) – the 2d shape of the geometry
- **units** (*dx, dy*) – the pixel sizes in microns
- **z** (*float*) – defocus position in microns, such that the beam would focus at z e.g. an input field with  $z = 10$ . would hav its focus spot after 10 microns
- **lam** (*float*) – the wavelength of light used in microns
- **NA** (*float/list*) – the numerical aperture(s) of the illumination objective that is either a single number (for gaussian beams) or an even length list of NAs (for bessell beams), e.g.  $NA = [0.5, 0.55]$  lets light through the annulus  $0.5 < 0.55$  (making a bessell beam ) or  $NA = [0.1, 0.2, 0.5, 0.6]$  lets light through the annulus  $0.1 < 0.2$  and  $0.5 < 0.6$  making a beating double bessell beam...
- **n0** (*float*) – the refractive index of the medium
- **n\_integration\_steps** (*int*) – number of integration steps to perform

**Returns** **ex** – the complex field

**Return type** *ndarray*

### Example

```
>>> # the input pattern of a bessell beam that will focus after 4 microns
>>> ex = focus_field_beam_plane((256,256), (0.1,0.1), z = 4, lam=.5, NA = (.4,.5))
```

See also:

`biobeam.focus_field_beam()` the 3d function

## 4.2 Cylindrical Lens



`biobeam.focus_field_cylindrical` (*shape*, *units*, *lam*=0.5, *NA*=0.3, *n0*=1.0, *return\_all\_field*=False, *n\_integration\_steps*=100)

calculates the focus field for a perfect, aberration free cylindrical lens after x polarized illumination via the vectorial debye diffraction integral (see <sup>2</sup>). The pupil function is given by the numerical aperture NA

#### Parameters

- **shape** (*Nx, Ny, Nz*) – the shape of the geometry
- **units** (*dx, dy, dz*) – the pixel sizes in microns
- **lam** (*float*) – the wavelength of light used in microns
- **NA** (*float*) – the numerical aperture of the lens
- **n0** (*float*) – the refractive index of the medium
- **return\_all\_fields** (*boolean*) – if True, returns u,ex,ey,ez where ex/ey/ez are the complex field components
- **n\_integration\_steps** (*int*) – number of integration steps to perform
- **return\_all\_fields** – if True returns also the complex vectorial field components

#### Returns

- **u** (*ndarray*) – the intensity of the focus field
- **(u,ex,ey,ez)** (*list(ndarray)*) – the intensity of the focus field and the complex field components (if return\_all\_fields is True)

#### Example

```
>>> u, ex, ey, ez = focus_field_cylindrical((128,128,128), (0.1,0.1,.1), lam=.5, NA = .4, ret
```

#### References

`biobeam.focus_field_cylindrical_plane` (*shape*=(128, 128), *units*=(0.1, 0.1), *z*=0.0, *lam*=0.5, *NA*=0.6, *n0*=1.0, *ex\_g*=None, *n\_integration\_steps*=200)

calculates the complex 2d input field at position -z of a perfect, aberration free optical system

#### Parameters

- **shape** (*Nx, Ny*) – the 2d shape of the geometry
- **units** (*dx, dy*) – the pixel sizes in microns
- **z** (*float*) – defocus position in microns, such that the beam would focus at z e.g. an input field with z = 10. would hav its focus spot after 10 microns
- **lam** (*float*) – the wavelength of light used in microns
- **NA** (*float/list*) – the numerical aperture(s) of the illumination objective that is either a single number (for gaussian beams) or an even length list of NAs (for bessell beams), e.g. NA = [0.5,0.55] lets light through the annulus 0.5<0.55 (making a bessell beam ) or NA = [0.1,0.2,0.5,0.6] lets light through the annulus 0.1<0.2 and 0.5<0.6 making a beating double bessell beam...
- **n0** (*float*) – the refractive index of the medium
- **n\_integration\_steps** (*int*) – number of integration steps to perform

**Returns** **ex** – the complex field

**Return type** ndarray

<sup>2</sup> Colin J. R. Sheppard: Cylindrical lenses—focusing and imaging: a review, Appl. Opt. 52, 538-545 (2013)

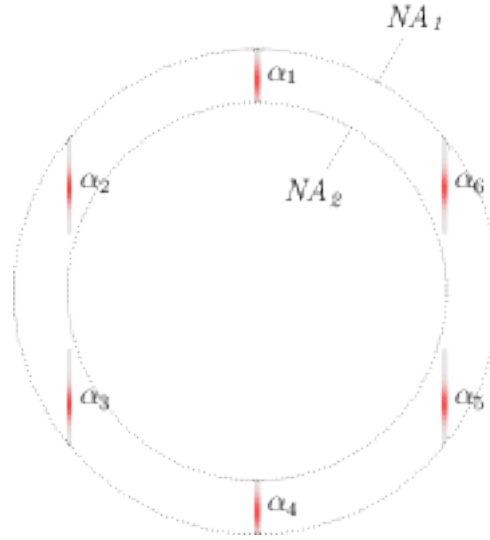
### Example

```
>>> # the input pattern of a bessel beam that will focus after 4 microns
>>> ex = focus_field_cylindrical_plane((256,256), (0.1,0.1), z = 4., lam=.5, NA = (.4,.5))
```

See also:

`biobeam.focus_field_cylindrical()` the 3d function

## 4.3 Bessel Lattices



`biobeam.focus_field_lattice(shape, units, lam=0.5, NA1=0.4, NA2=0.5, sigma=0.1, kpoints=6, n0=1.0, n_integration_steps=100)`  
calculates the focus field for a bessel lattice. The pupil function consists out of discrete points (kpoints) superimposed on an annulus ( $NA1 < NA2$ ) which are smeared out by a 1d gaussian of given sigma creating an array of bessel beams in the focal plane (see <sup>3</sup>).

### Parameters

- **shape** ( $N_x, N_y, N_z$ ) – the shape of the geometry
- **units** ( $dx, dy, dz$ ) – the pixel sizes in microns
- **lam** (*float*) – the wavelength of light used in microns
- **NA1** (*float/list*) – the numerical aperture of the inner ring
- **NA2** (*float/list*) – the numerical aperture of the outer ring
- **sigma** (*float*) – the standard deviation of the gaussian smear function applied to each point on the aperture (the bigger sigma, the tighter the sheet in y)
- **kpoints** (*int/ (2,N) array*) – defines the set of points on the aperture that create the lattice, can be - a (2,N) ndarray, such that `kpoints[:,i]` are the coordinates of the *i*th point - a single int, defining points on a regular polygon (e.g. 4 for a square lattice, 6 for a hex lattice)  $k_i = \arcsin \frac{NA_1 + NA_2}{2n_0} \begin{pmatrix} \cos \phi_i \\ \sin \phi_i \end{pmatrix}$ ,  $\phi_i = \frac{\pi}{2} + \frac{2i}{N}$
- **n0** (*float*) – the refractive index of the medium
- **n\_integration\_steps** (*int*) – number of integration steps to perform
- **return\_all\_fields** (*boolean*) – if True, returns `u, ex, ey, ez` where `ex/ey/ez` are the complex vector field components

<sup>3</sup> Chen et al. Lattice light-sheet microscopy: imaging molecules to embryos at high spatiotemporal resolution. Science 346, (2014).

## Returns

- **u** (*ndarray*) – the intensity of the focus field
- **(u,ex,ey,ez)** (*list(ndarray)*) – the intensity of the focus field and the complex field components (if `return_all_fields` is `True`)

## Example

```
>>> u = focus_field_lattice((128,128,128), (0.1,0.1,.1), lam=.5, NA1 = .44, NA2 = .55, kpoint
```

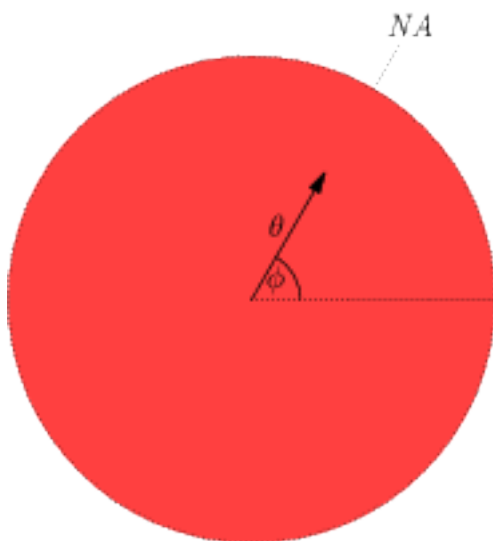
## References

```
biobeam.focus_field_lattice_plane(shape=(256, 256), units=(0.1, 0.1), z=0.0,  
lam=0.5, NA1=0.4, NA2=0.5, sigma=0.1, Npoly=6,  
n0=1.0, apodization_bound=10, ex_g=None,  
n_integration_steps=100)
```

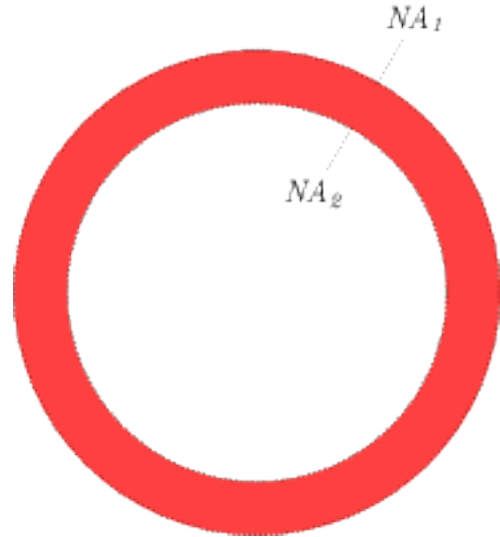
# 5 Focus field calculations

## 5.1 Gaussian/Bessel beams

### Gaussian/Bessel beams







`biobeam.focus_field_beam(shape, units, lam=0.5, NA=0.6, n0=1.0, return_all_fields=False, n_integration_steps=200)`

calculates the focus field for a perfect, aberration free optical system for x polarized illumination via the vectorial debye diffraction integral (see <sup>1</sup>). The pupil function is given by numerical aperture(s) NA (that can be a list to model bessell beams, see further below)

#### Parameters

- **shape** ( $N_x, N_y, N_z$ ) – the shape of the geometry
- **units** ( $dx, dy, dz$ ) – the pixel sizes in microns
- **lam** (*float*) – the wavelength of light used in microns
- **NA** (*float/list*) – the numerical aperture(s) of the illumination objective that is either a single number (for gaussian beams) or an even length list of NAs (for bessell beams), e.g.  $NA = [0.5, 0.55]$  lets light through the annulus  $0.5 < 0.55$  (making a bessell beam ) or  $NA = [0.1, 0.2, 0.5, 0.6]$  lets light through the annulus  $0.1 < 0.2$  and  $0.5 < 0.6$  making a beating double bessell beam...
- **n0** (*float*) – the refractive index of the medium
- **n\_integration\_steps** (*int*) – number of integration steps to perform
- **return\_all\_fields** (*boolean*) – if True returns also the complex vectorial field components

#### Returns

- **u** (*ndarray*) – the intensity of the focus field
- **(u,ex,ey,ez)** (*list(ndarray)*) – the intensity of the focus field and the complex field components (if `return_all_fields` is True)

#### Example

```
>>> u = focus_field_beam((128,128,128), (0.1,0.1,.1), lam=.5, NA = .4)
```

#### References

`biobeam.focus_field_beam_plane(shape=(128, 128), units=(0.1, 0.1), z=0.0, lam=0.5, NA=0.6, n0=1.0, ex_g=None, n_integration_steps=200)`  
calculates the complex 2d input field at position -z of a perfect, aberration free optical system

<sup>1</sup> Matthew R. Foreman, Peter Toeroek, *Computational methods in vectorial imaging*, Journal of Modern Optics, 2011, 58, 5-6, 339

### Parameters

- **shape** ( $N_x, N_y$ ) – the 2d shape of the geometry
- **units** ( $dx, dy$ ) – the pixel sizes in microns
- **z** (*float*) – defocus position in microns, such that the beam would focus at z e.g. an input field with  $z = 10$ . would hav its focus spot after 10 microns
- **lam** (*float*) – the wavelength of light used in microns
- **NA** (*float/list*) – the numerical aperture(s) of the illumination objective that is either a single number (for gaussian beams) or an even length list of NAs (for bessell beams), e.g.  $NA = [0.5, 0.55]$  lets light through the annulus  $0.5 < 0.55$  (making a bessell beam ) or  $NA = [0.1, 0.2, 0.5, 0.6]$  lets light through the annulus  $0.1 < 0.2$  and  $0.5 < 0.6$  making a beating double bessell beam...
- **n0** (*float*) – the refractive index of the medium
- **n\_integration\_steps** (*int*) – number of integration steps to perform

**Returns** **ex** – the complex field

**Return type** ndarray

### Example

```
>>> # the input pattern of a bessell beam that will focus after 4 microns
>>> ex = focus_field_beam_plane((256,256), (0.1,0.1), z = 4, lam=.5, NA = (.4,.5))
```

See also:

`biobeam.focus_field_beam()` the 3d function

## 5.2 Cylindrical Lens



`biobeam.focus_field_cylindrical` (*shape, units, lam=0.5, NA=0.3, n0=1.0, return\_all\_field=False, n\_integration\_steps=100*)

calculates the focus field for a perfect, aberration free cylindrical lens after x polarized illumination via the vectorial debye diffraction integral (see <sup>2</sup>). The pupil function is given by the numerical aperture NA

### Parameters

- **shape** ( $N_x, N_y, N_z$ ) – the shape of the geometry
- **units** ( $dx, dy, dz$ ) – the pixel sizes in microns
- **lam** (*float*) – the wavelength of light used in microns
- **NA** (*float*) – the numerical aperture of the lens
- **n0** (*float*) – the refractive index of the medium
- **return\_all\_fields** (*boolean*) – if True, returns u,ex,ey,ez where ex/ey/ez are the complex field components
- **n\_integration\_steps** (*int*) – number of integration steps to perform
- **return\_all\_fields** – if True returns also the complex vectorial field components

<sup>2</sup> Colin J. R. Sheppard: Cylindrical lenses—focusing and imaging: a review, Appl. Opt. 52, 538-545 (2013)

## Returns

- **u** (*ndarray*) – the intensity of the focus field
- **(u,ex,ey,ez)** (*list(ndarray)*) – the intensity of the focus field and the complex field components (if `return_all_fields` is `True`)

## Example

```
>>> u, ex, ey, ez = focus_field_cylindrical((128,128,128), (0.1,0.1,.1), lam=.5, NA = .4, ret
```

## References

`biobeam.focus_field_cylindrical_plane` (*shape=(128, 128), units=(0.1, 0.1), z=0.0, lam=0.5, NA=0.6, n0=1.0, ex\_g=None, n\_integration\_steps=200*)

calculates the complex 2d input field at position -z of a perfect, aberration free optical system

## Parameters

- **shape** (*Nx, Ny*) – the 2d shape of the geometry
- **units** (*dx, dy*) – the pixel sizes in microns
- **z** (*float*) – defocus position in microns, such that the beam would focus at z e.g. an input field with  $z = 10$ . would hav its focus spot after 10 microns
- **lam** (*float*) – the wavelength of light used in microns
- **NA** (*float/list*) – the numerical aperture(s) of the illumination objective that is either a single number (for gaussian beams) or an even length list of NAs (for bessell beams), e.g.  $NA = [0.5, 0.55]$  lets light through the annulus  $0.5 < 0.55$  (making a bessell beam ) or  $NA = [0.1, 0.2, 0.5, 0.6]$  lets light through the annulus  $0.1 < 0.2$  and  $0.5 < 0.6$  making a beating double bessell beam...
- **n0** (*float*) – the refractive index of the medium
- **n\_integration\_steps** (*int*) – number of integration steps to perform

**Returns** **ex** – the complex field

**Return type** `ndarray`

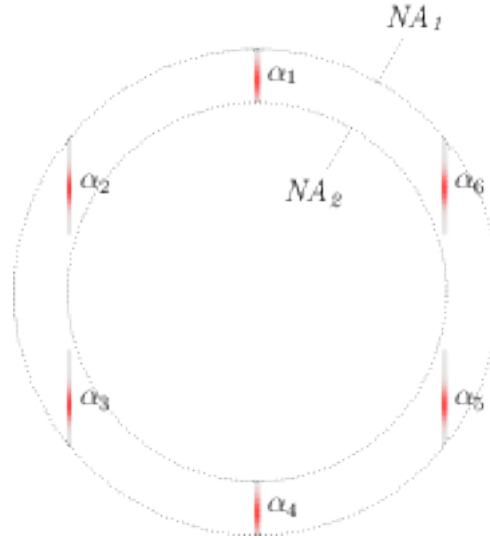
## Example

```
>>> # the input pattern of a bessell beam that will focus after 4 microns
>>> ex = focus_field_cylindrical_plane((256,256), (0.1,0.1), z = 4., lam=.5, NA = (.4,.5))
```

**See also:**

`biobeam.focus_field_cylindrical()` the 3d function

### 5.3 Bessel Lattices



`biobeam.focus_field_lattice(shape, units, lam=0.5, NA1=0.4, NA2=0.5, sigma=0.1, kpoints=6, n0=1.0, n_integration_steps=100)`  
calculates the focus field for a bessel lattice. The pupil function consists out of discrete points (kpoints) superimposed on an annulus ( $NA1 < NA2$ ) which are smeared out by a 1d gaussian of given sigma creating an array of bessel beams in the focal plane (see <sup>3</sup>).

#### Parameters

- **shape** ( $N_x, N_y, N_z$ ) – the shape of the geometry
- **units** ( $dx, dy, dz$ ) – the pixel sizes in microns
- **lam** (*float*) – the wavelength of light used in microns
- **NA1** (*float/list*) – the numerical aperture of the inner ring
- **NA2** (*float/list*) – the numerical aperture of the outer ring
- **sigma** (*float*) – the standard deviation of the gaussian smear function applied to each point on the aperture (the bigger sigma, the tighter the sheet in y)
- **kpoints** (*int/ (2,N) array*) – defines the set of points on the aperture that create the lattice, can be - a (2,N) ndarray, such that  $kpoints[:,i]$  are the coordinates of the  $i$ th point - a single int, defining points on a regular polygon (e.g. 4 for a square lattice, 6 for a hex lattice)  $k_i = \arcsin \frac{NA_1 + NA_2}{2n_0} \begin{pmatrix} \cos \phi_i \\ \sin \phi_i \end{pmatrix}$ ,  $\phi_i = \frac{\pi}{2} + \frac{2i}{N}$
- **n0** (*float*) – the refractive index of the medium
- **n\_integration\_steps** (*int*) – number of integration steps to perform
- **return\_all\_fields** (*boolean*) – if True, returns  $u, ex, ey, ez$  where  $ex/ey/ez$  are the complex vector field components

#### Returns

- **u** (*ndarray*) – the intensity of the focus field
- **(u,ex,ey,ez)** (*list(ndarray)*) – the intensity of the focus field and the complex field components (if `return_all_fields` is True)

<sup>3</sup> Chen et al. Lattice light-sheet microscopy: imaging molecules to embryos at high spatiotemporal resolution. Science 346, (2014).

## Example

```
>>> u = focus_field_lattice((128,128,128), (0.1,0.1,.1), lam=.5, NA1 = .44, NA2 = .55, kpoint
```

## References

```
biobeam.focus_field_lattice_plane(shape=(256, 256), units=(0.1, 0.1), z=0.0,  
                                lam=0.5, NA1=0.4, NA2=0.5, sigma=0.1, Npoly=6,  
                                n0=1.0, apodization_bound=10, ex_g=None,  
                                n_integration_steps=100)
```

## 6 Simulating light sheet microscopy

## 7 Aberrations

## 8 Examples

### 8.1 Plane wave scattered by sphere

```
# create the refractive index difference  
x = 0.1 * np.arange(-128,128)  
Z, Y, X = np.meshgrid(x,x,x,indexing = "ij")  
R = np.sqrt(X**2+Y**2+Z**2)  
dn = 0.05*(R<2.)  
  
# create the computational geometry  
m = Bpm3d(dn = dn, units = (0.1,0.1,0.1), lam = 0.5)  
  
# propagate a plane wave and return the intensity  
u = m._propagate()  
  
# vizualize  
import matplotlib.pyplot as plt  
plt.subplot(1,2,1)  
plt.imshow(u[...],128], cmap = "hot")  
plt.title("zy slice")  
plt.subplot(1,2,2)  
plt.imshow(u[128,...],128], cmap = "hot")  
plt.title("xy slice")
```

### 8.2 Light sheet through cell phantom

### 8.3 Computing the psf inside a cell phantom

### 8.4 Aberration from sphere

## 9 Some Examples

or not?

```
print "huhu"
```

huhu

## Index

### Symbols

`__init__()` (biobeam.Bpm3d method), 3

### A

`aberr_at()` (biobeam.Bpm3d method), 3

`aberr_field_grid()` (biobeam.Bpm3d method), 3

### B

Bpm3d (class in biobeam), 3

### F

`focus_field_beam()` (in module biobeam), 4, 9

`focus_field_beam_plane()` (in module biobeam), 5, 9

`focus_field_cylindrical()` (in module biobeam), 5, 10

`focus_field_cylindrical_plane()` (in module biobeam),  
6, 11

`focus_field_lattice()` (in module biobeam), 7, 12

`focus_field_lattice_plane()` (in module biobeam), 8, 13