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# Solving the Jigsaw Puzzle via Various Learning Approaches

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## Abstract

1       The jigsaw puzzle is a game dating back to the 1760s and despite years of develop-  
2       ments in both game and technology, there is a lack of literature utilizing various  
3       machine learning (ML) techniques to solve this game. To tackle this issue, we  
4       developed a learning-based solver which leverages multiple existing ML architec-  
5       tures involving computer vision. Through analyses of each model’s performance  
6       of solving the puzzle, we then determine whether certain model architectures are  
7       preferred over others for this task and hypothesize on the models’ interpretability.

## 8   1   Introduction

9       A square jigsaw is a subset of jigsaw puzzles where each puzzle tile is a square and the correct  
10      configuration of the tiles displays an  $n$ -by- $n$  grid. To solve a square jigsaw, the user must first  
11      determine the correct tile configuration (position and orientation). In this project, we focus on using  
12      computer vision techniques in machine learning (ie. convolutional neural networks (CNNs)) to  
13      identify the correct tile configuration. We will then compare the solving performance of various Deep  
14      CNN (DCNN) architectures. The motivation for this project follows from the lack of diverse machine  
15      learning-based literature surrounding jigsaw DCNN solvers. We hope that our conclusions may be  
16      used to better select models for similar tasks and increase model explainability.

## 17   2   Related Works

18      There are 2 general approaches to solving square jigsaws.

19      Firstly, one can solve the board in an iterative process. This is done by computing an edge compati-  
20      bility metric between sub-image pairs, and using this information to prune possibilities. Zanoci and  
21      Andress computed an edge compatibility metric using non-ML neighboring pixel information and the  
22      color gradients [1]. This was done between all possible sub-image pairs ( $n^2 * 4^2$  total comparisons,  
23      where  $n$  = number of sub-images). Then, treating pieces as vertices and compatibility scores as  
24      edges, they utilized the minimum spanning tree algorithm to recreate the original board using the  
25      most likely edges. Only 80% of edges were correctly matched, using board sizes of hundreds of  
26      pieces. A downfall of non-ML methods is the deterministic nature of the solver, and its difficulty  
27      to adapt to simple perturbations such as eroded edges. A simpler method proposed by Bhaskhar,  
28      uses a fine-tuned ResNet to compute edge compatibilities between puzzle tiles. Then the grid is  
29      iteratively filled in, using the most probable tile at each time step. As a result, over 80% of pieces  
30      were rearranged into their correct position/orientation [2].

31 The second approach is for one to attempt to solve the entire board at one time. Noroozi separately  
 32 fed each sub-piece into a siamese-enned CNN, then combined these encodings in a fully connected  
 33 layer to predict the original permutation [3]. Accuracy in terms of solving entire board was low  
 34 at only 67% with a board size of 3x3. Given that 9! permutations exist, solving at once may be  
 35 too complex for current architectures. A similar method by Kulharia [4] used a many to one long  
 36 short-term memory (LSTM) to output a one-hot encoding of the permutation. Input at each time-step  
 37 was a collapsed sub-image. It only achieved 80% accuracy per complete board solve despite a small  
 38 board size of 2x2. We will expand on the first approach in our project.

### 39 3 Method

#### 40 3.1 Image Data Source

41 We will create the dataset for our report using the Caltech-UCSD Birds 200 (CUB\_200) 2011 dataset  
 42 [5]. CUB-200 2011 is an image dataset containing 11,788 images of 200 different bird species. Using  
 43 a 70/30 split, we will partition these images into training and validation datasets, with 8,252 images  
 44 in the training set and 3,536 in the validation set.

#### 45 3.2 Edge Compatibility Train Data

46 Our DCNN's input is a square concatenation of 2 subimages, and the output is whether they are  
 47 left-right adjacent, which we will now refer to as adjacent. To generate these input output pairings we  
 48 make use of Bhaskhar's `Checking_adjacency_dataset` repository [2], which will generate edge  
 49 concatenations between the images' various edges (See Fig 4). For each n-by-n grid, there are  $n^2$   
 50 puzzle pieces and  $C(n^2, 2)$  possible pairs of square concatenations. The repository will then randomly  
 51 choose from these pairs to create our train data that has a roughly equal number of adjacent labels,  
 52 and non-adjacent labels, and will output our newly formed data.

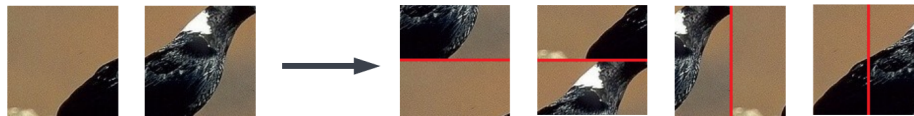


Figure 1: 2 sub-images can generate 4 different concatenations.

#### 53 3.3 Adjacency Classifier

54 The goal of this classifier is to determine whether an input image, consisting of two puzzle pieces,  
 55 (P,Q), is left-right adjacent. Drawing inspiration from the work of [2], we will finetune different image  
 56 classification models (listed below) on a custom adjacency dataset to create the adjacency classifier.  
 57 Furthermore, we want to compare the performance of these models both in terms of their prediction  
 58 accuracy as adjacency classifiers, and how well they work in combination with the downstream solver  
 59 to complete the puzzle. In the following sections we will briefly describe the architecture of each  
 60 CNN used, and how we have adapted the model to fit our finetuning process.

##### 61 3.3.1 ResNet Architecture

62 The ResNet models were first proposed in [6]. There are currently five versions of ResNet (ResNet18,  
 63 ResNet34, ResNet50, ResNet101, ResNet152) trained on the ImageNet dataset available for fine  
 64 tuning in the `torchvision` library in PyTorch. In general, the ResNet models contain convolutional  
 65 kernels of size 3x3, and the number of filter layers increases along with the depth of the network.  
 66 Thus, different versions of the ResNets correspond to the total number of filter layers in the network  
 67 (see Fig. 5 for architecture detail). The defining feature for ResNets are the residual blocks which  
 68 exist between pairs/triplets of the convolutional layers with residual connections that propagate the

69 unaltered input to the output (see Fig. 6). This innovation was introduced in order to prevent the  
70 vanishing gradient problem.

71

72 To adapt ResNets for our finetuning process, we modified the final fully connected layer originally  
73 meant for a larger classification task to one meant for binary classification. Note that when we  
74 finetuned on all the ResNets, the weights/bias parameters that are affected belong to this final  
75 classification layer.

### 76 3.3.2 VGG Architecture

77 The VGG models were first proposed in [7]. There are 4 versions of VGG (VGG11, VGG13, VGG16,  
78 VGG19) with batch normalization implemented in the `torchvision` library in PyTorch. Similar  
79 to ResNets, the VGGs contain only 3x3 convolution filters; however, they are considerably more  
80 shallow (the deepest VGG has 19 total layers, while the deepest ResNet has 152) (see. Fig. 7). The  
81 limitation on the VGGs' depth is due to the vanishing gradient problem, where more layers lead to  
82 issues with weight updates during training.

83 To adapt the VGGs for our finetuning process, we have to again modify the final classification layer  
84 to fit our binary classification task.

### 85 3.3.3 ResNeXt Architecture

86 The ResNeXt models were first proposed in [8](See Fig. 8). What sets the ResNeXts apart from  
87 ResNets are the structure of the residual blocks. Instead of applying convolution filters to the block's  
88 entire input feature map, a series of convolutions are applied to parts of the the input and then the  
89 output is then grouped back together(see Fig. 9). This parallel structure allows specialization to  
90 occur among groups where different characteristics are learned (ie. edges, corners etc).

91

92 To adapt the ResNeXts for our finetuning process, we modified the final fully connected layer exactly  
93 like how we had done for the ResNets.

### 94 3.3.4 Setup

95 For the sake of fair comparison, all CNN models were tested on control hyper parameters (see Table  
96 1).

## 97 3.4 Configuration Solver

98 The configuration solver takes as input a randomly scrambled n-by-n board (see Fig. 10 - 12). Due  
99 to time constraints, this portion of the implementation leveraged existing functions from [2]. At  
100 each time step the solver receives a board that is partially filled in, and outputs a new board with 1  
101 additional piece adjacent to a piece already filled in. To decide on the next piece, the solver will try  
102 every single combination of (open spot, remaining piece, orientation). That is if there are S open  
103 spots, R remaining pieces, and 4 orientations, our solver will attempt  $S \cdot R \cdot 4$  combinations, and pick  
104 the most probable one according to the average edge compatibility scores of all its edges. The validity  
105 of an edge of 2 pieces stacked vertically can be checked by simply cutting out the edge, rotating the  
106 edge 90 degrees, and then passing it in to the left-right adjacent CNN classifier. The solver process is  
107 visualized in Figure 2 of the appendix.

## 108 4 Results and Discussion

### 109 4.1 Adjacency Classifier Performance

110 Overall all, we see that all models achieved their highest validation accuracy between 0.90 and 0.94,  
111 and their lowest validation loss between  $<0.15$  and 0.36. In general, we see that deeper, more complex

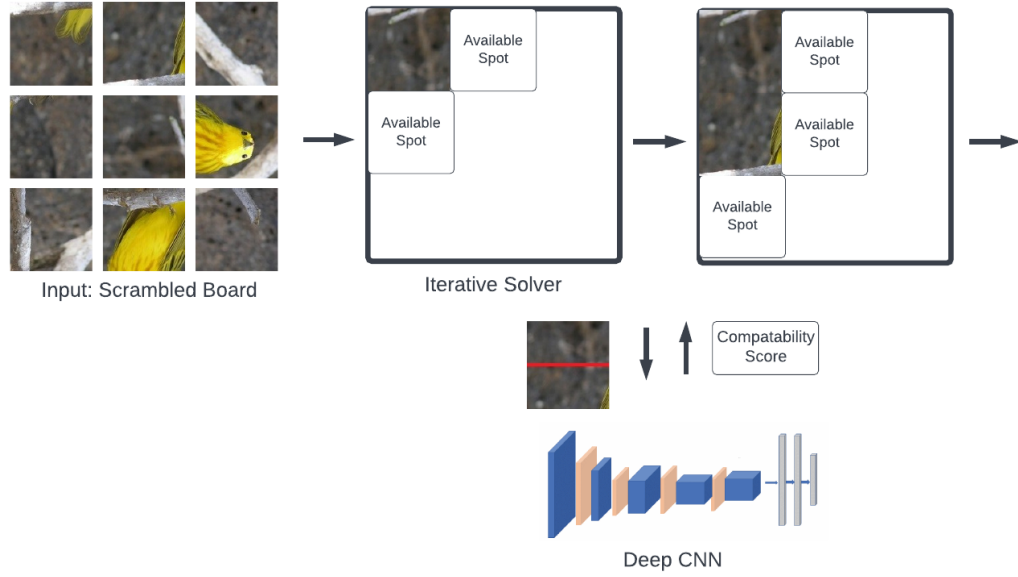


Figure 2: Architecture of Solving Process

models do not offer better generalizability for our problem, instead, shallower, simpler models are more capable.

In terms of individual model performances, we achieved the highest training accuracy of 0.99 and lowest training loss of 0.05 on VGG13, and highest validation accuracy of 0.94 and lowest validation loss of  $<0.15$  on VGG16.

## 4.2 Final Solver

To test how well our adjacency classifier works in combination with the downstream configuration solver, we run the entire pipeline (ie. adjacency classifier + configuration solver) on two test images (see Fig. 10-12 for sample input/output). In the interest of time we did not run a complete performance study with more samples. However, what we observe from our limited test set is that VGG16 performed the best (ie. only model to give a correct complete solution) in terms of solving a 3x3 board, and a 2x2 board. This result corroborates with our adjacency classification tests as VGG16 also gave the best validation loss/accuracy (see Table. 4 -5).

## 4.3 Discussion

As for our training processes, we observe that the bigger ResNet models (ie. ResNet101 and ResNet152) suffer overfitting before the training runs end (refer to figure in Appendix). We see the training accuracy improving whilst the validation accuracy worsens (the same can be seen for the loss curves). This is reasonable as the size of our entire dataset is rather small which means that more complex models will easy overfit to the training data and perform suboptimally in validation.

For the VGG curves, however, training is unstable with noisy and significant jumps in valid accuracy and loss. This suggest to us that the learning rate for the model is set too high - the gradient descent algorithm has trouble stabilizing near the local minimum because the step size for updates are too large which causes large oscillations. In the interest of time we did not remedy this issue but trained all models on the same control settings.

Importantly, all Deep CNNs hit an adjacency classification accuracy cap near 94%. We speculate that this issue may be due to the nature of the dataset itself. Our dataset contains images of birds

138 with natural landscapes that include the sky and water. Unlike in commercial puzzles, our pieces  
 139 were never checked to maintain a good balance of distinguishing features across all sub images.  
 140 It is possible that many sub images contained the same generic background (Refer to Figure 3 in  
 141 Appendix) lacking in major features. Here, we require our CNN to pay strong attention to pixel level  
 142 details. This might be challenging to Deep CNNs pretrained on object recognition, where localized  
 143 pixel level information is lost in its deeper later layers, especially since we only fine tuned the final  
 144 classification layer.

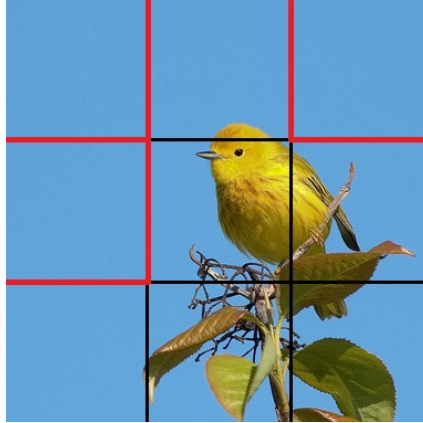


Figure 3: The edges marked in red do not have defining features. This imbalance across puzzle tiles could have yielded the accuracy cap of 95%.

145 Finally, we want to observe the effect of using different CNNs for adjacency classification has on  
 146 the downstream solver. From our limited results, we see that the overall solver performance can be  
 147 improved (only VGG16 + solver gave a completely correct solution for both test samples).

## 148 5 Conclusion and Next Steps

149 In this report, we expanded on existing methods by showing that various pretrained Deep CNNs can  
 150 be successfully fine-tuned to generate working adjacency scoring metrics. Importantly, we concluded  
 151 that smaller, wider CNNs (such as VGGs) may obtain higher accuracies by paying finer attention  
 152 to details than longer, narrower models (such as ResNets), especially when pretrained for object  
 153 classification.

### 154 5.1 Future Work - Train Data

155 In real life, jigsaw tile edges are eroded inwards anywhere from 1% to 5%, which would be a perfect  
 156 challenge for machine learning. In future works, we can test and explore the effects of various degrees  
 157 of erosion on edge adjacency classification performance.

### 158 5.2 Future Work - Solver

159 As well, in the future we can tackle the issue of the propagation of errors downstream. Incorrectly  
 160 placed pieces cannot be readjusted, as well some pieces are placed with only 1 neighboring edge  
 161 information which introduces significant uncertainty. To remedy this, we propose solving in batches.  
 162 That is, we can simultaneously solve divisions of 2x2 at a time by brute forcing  $4^4 \times 4!$  combinations  
 163 per  $C(n, 4)$  subsets, taking the most likely combination according to chained edge compatibility  
 164 scores. Finally, we can have a top-down double check by having a CNN take in a subdivision and  
 165 output its validity, then backtracking if necessary.

## References

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## Appendix

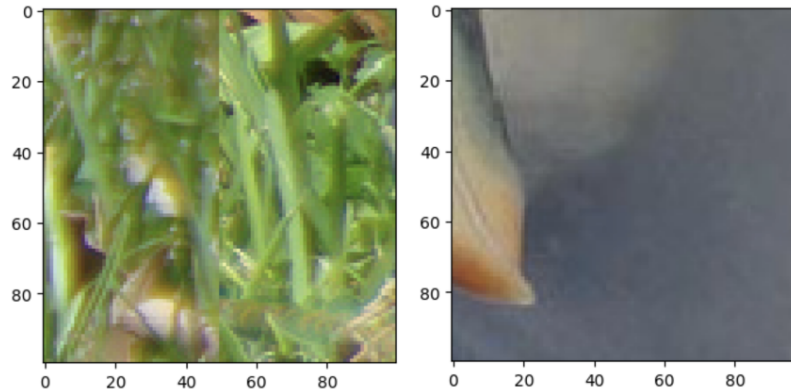


Figure 4: Two square concatenations of puzzle piece edges. On the left, we see that the edges are not left-right adjacent and thus they will have label 0. Whereas on the right we see that the edges are left-right adjacent, and thus they will have label 1.

Hyperparameter	Value
learning rate	0.001
momentum	0.9
examples per epoch	500
optimizer	optim.SGD

Table 1: Hyperparameters for all CNN Models

layer name	output size	18-layer	34-layer	50-layer	101-layer	152-layer
conv1	112×112	7×7, 64, stride 2				
conv2_x	56×56	3×3 max pool, stride 2				
		$\begin{bmatrix} 3 \times 3, 64 \\ 3 \times 3, 64 \end{bmatrix} \times 2$	$\begin{bmatrix} 3 \times 3, 64 \\ 3 \times 3, 64 \end{bmatrix} \times 3$	$\begin{bmatrix} 1 \times 1, 64 \\ 3 \times 3, 64 \\ 1 \times 1, 256 \end{bmatrix} \times 3$	$\begin{bmatrix} 1 \times 1, 64 \\ 3 \times 3, 64 \\ 1 \times 1, 256 \end{bmatrix} \times 3$	$\begin{bmatrix} 1 \times 1, 64 \\ 3 \times 3, 64 \\ 1 \times 1, 256 \end{bmatrix} \times 3$
conv3_x	28×28	$\begin{bmatrix} 3 \times 3, 128 \\ 3 \times 3, 128 \end{bmatrix} \times 2$	$\begin{bmatrix} 3 \times 3, 128 \\ 3 \times 3, 128 \end{bmatrix} \times 4$	$\begin{bmatrix} 1 \times 1, 128 \\ 3 \times 3, 128 \\ 1 \times 1, 512 \end{bmatrix} \times 4$	$\begin{bmatrix} 1 \times 1, 128 \\ 3 \times 3, 128 \\ 1 \times 1, 512 \end{bmatrix} \times 4$	$\begin{bmatrix} 1 \times 1, 128 \\ 3 \times 3, 128 \\ 1 \times 1, 512 \end{bmatrix} \times 8$
conv4_x	14×14	$\begin{bmatrix} 3 \times 3, 256 \\ 3 \times 3, 256 \end{bmatrix} \times 2$	$\begin{bmatrix} 3 \times 3, 256 \\ 3 \times 3, 256 \end{bmatrix} \times 6$	$\begin{bmatrix} 1 \times 1, 256 \\ 3 \times 3, 256 \\ 1 \times 1, 1024 \end{bmatrix} \times 6$	$\begin{bmatrix} 1 \times 1, 256 \\ 3 \times 3, 256 \\ 1 \times 1, 1024 \end{bmatrix} \times 23$	$\begin{bmatrix} 1 \times 1, 256 \\ 3 \times 3, 256 \\ 1 \times 1, 1024 \end{bmatrix} \times 36$
conv5_x	7×7	$\begin{bmatrix} 3 \times 3, 512 \\ 3 \times 3, 512 \end{bmatrix} \times 2$	$\begin{bmatrix} 3 \times 3, 512 \\ 3 \times 3, 512 \end{bmatrix} \times 3$	$\begin{bmatrix} 1 \times 1, 512 \\ 3 \times 3, 512 \\ 1 \times 1, 2048 \end{bmatrix} \times 3$	$\begin{bmatrix} 1 \times 1, 512 \\ 3 \times 3, 512 \\ 1 \times 1, 2048 \end{bmatrix} \times 3$	$\begin{bmatrix} 1 \times 1, 512 \\ 3 \times 3, 512 \\ 1 \times 1, 2048 \end{bmatrix} \times 3$
	1×1	average pool, 1000-d fc, softmax				
FLOPs		$1.8 \times 10^9$	$3.6 \times 10^9$	$3.8 \times 10^9$	$7.6 \times 10^9$	$11.3 \times 10^9$

ures for ImageNet. Building blocks are shown in brackets (see also Fig. 5), with the numbers of block

Figure 5: Model architecture comparison between the different ResNets

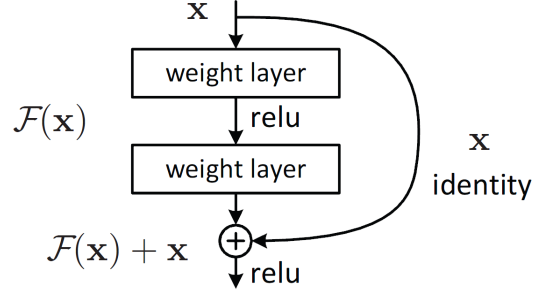


Figure 6: Illustration of a residual block structure

ConvNet Configuration					
A	A-LRN	B	C	D	E
11 weight layers	11 weight layers	13 weight layers	16 weight layers	16 weight layers	19 weight layers
input (224 × 224 RGB image)					
conv3-64	conv3-64 LRN	conv3-64 <b>conv3-64</b>	conv3-64 conv3-64	conv3-64 conv3-64	conv3-64 conv3-64
maxpool					
conv3-128	conv3-128	conv3-128 <b>conv3-128</b>	conv3-128 conv3-128	conv3-128 conv3-128	conv3-128 conv3-128
maxpool					
conv3-256 conv3-256	conv3-256 conv3-256	conv3-256 conv3-256	conv3-256 conv3-256 <b>conv1-256</b>	conv3-256 conv3-256 <b>conv3-256</b>	conv3-256 conv3-256 conv3-256 <b>conv3-256</b>
maxpool					
conv3-512 conv3-512	conv3-512 conv3-512	conv3-512 conv3-512	conv3-512 conv3-512 <b>conv1-512</b>	conv3-512 conv3-512 <b>conv3-512</b>	conv3-512 conv3-512 conv3-512 <b>conv3-512</b>
maxpool					
conv3-512 conv3-512	conv3-512 conv3-512	conv3-512 conv3-512	conv3-512 conv3-512 <b>conv1-512</b>	conv3-512 conv3-512 <b>conv3-512</b>	conv3-512 conv3-512 conv3-512 <b>conv3-512</b>
maxpool					
FC-4096					
FC-4096					
FC-1000					
soft-max					

Figure 7: Model architecture comparison between the different VGGs

stage	output	ResNet-50	ResNeXt-50 (32×4d)
conv1	112×112	7×7, 64, stride 2	7×7, 64, stride 2
conv2	56×56	3×3 max pool, stride 2	3×3 max pool, stride 2
		$\begin{bmatrix} 1 \times 1, 64 \\ 3 \times 3, 64 \\ 1 \times 1, 256 \end{bmatrix} \times 3$	$\begin{bmatrix} 1 \times 1, 128 \\ 3 \times 3, 128, C=32 \\ 1 \times 1, 256 \end{bmatrix} \times 3$
conv3	28×28	$\begin{bmatrix} 1 \times 1, 128 \\ 3 \times 3, 128 \\ 1 \times 1, 512 \end{bmatrix} \times 4$	$\begin{bmatrix} 1 \times 1, 256 \\ 3 \times 3, 256, C=32 \\ 1 \times 1, 512 \end{bmatrix} \times 4$
conv4	14×14	$\begin{bmatrix} 1 \times 1, 256 \\ 3 \times 3, 256 \\ 1 \times 1, 1024 \end{bmatrix} \times 6$	$\begin{bmatrix} 1 \times 1, 512 \\ 3 \times 3, 512, C=32 \\ 1 \times 1, 1024 \end{bmatrix} \times 6$
conv5	7×7	$\begin{bmatrix} 1 \times 1, 512 \\ 3 \times 3, 512 \\ 1 \times 1, 2048 \end{bmatrix} \times 3$	$\begin{bmatrix} 1 \times 1, 1024 \\ 3 \times 3, 1024, C=32 \\ 1 \times 1, 2048 \end{bmatrix} \times 3$
	1×1	global average pool 1000-d fc, softmax	global average pool 1000-d fc, softmax
# params.		$25.5 \times 10^6$	$25.0 \times 10^6$
FLOPs		$4.1 \times 10^9$	$4.2 \times 10^9$

Table 1. (Left) ResNet-50. (Right) ResNeXt-50 with a 32×4d template (using the reformulation in Fig. 3(c)). Inside the brackets are the shape of a residual block, and outside the brackets is the number of stacked blocks on a stage. “C=32” suggests grouped convolutions [24] with 32 groups. The numbers of parameters and FLOPs are similar between these two models.

Figure 8: Model architecture comparison between ResNet50 and ResNeXt50

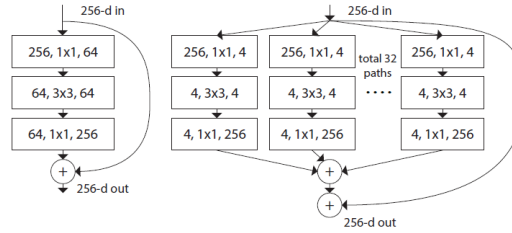


Figure 9: Illustration of a ResNeXt residual block structure compared to the a ResNet residual block structure

Model	Lowest Training Loss	Highest Training Accuracy
Resnet18	0.10	0.97
Resnet34	0.11	0.96
Resnet50	0.10	0.96
Resnet101	0.14	0.95
Resnet152	0.09	0.97
VGG11	0.05	0.98
VGG13	<b>0.05</b>	<b>0.99</b>
VGG16	0.06	0.98
VGG19	0.06	0.98
ResNeXt50	0.11	0.97
ResNeXt101	0.31	0.92

Table 2: The lowest training loss and highest training accuracy observed for each model



Model	Lowest Validation Loss	Highest Validation Accuracy
Resnet18	0.31	0.92
Resnet34	0.27	0.93
Resnet50	0.35	0.92
Resnet101	0.29	0.93
Resnet152	0.36	0.93
VGG11	0.23	0.92
VGG13	0.27	0.92
VGG16	<b>&lt;0.15</b>	<b>0.94</b>
VGG19	0.20	0.91
ResNeXt50	0.26	0.92
ResNeXt101	0.21	0.92

Table 3: The lowest validation loss and highest validation accuracy observed for each model

Original image



Figure 10: Original test image

Shuffled grid of puzzle pieces



Figure 11: Sample input to solver

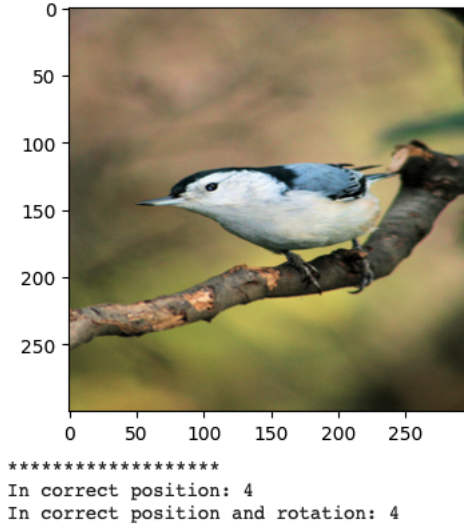


Figure 12: Final solver output

Model Name	# of correct pos.	# of correct pos. and rot.
ResNet18	3	3
ResNet34	1	1
ResNet50	1	1
ResNet101	3	3
ResNet152	1	1
<b>VGG11</b>	<b>9</b>	<b>9</b>
VGG13	4	4
VGG16	1	1
VGG19	2	1
ResNeXt50	6	6
ResNeXt101	3	3

Table 4: Solver result for a 3x3 board. The correct board should feature 9 correct positions and 9 correct rotations

Model Name	# of correct pos.	# of correct pos. and rot.
<b>ResNet18</b>	<b>4</b>	<b>4</b>
ResNet34	2	1
ResNet50	2	2
<b>ResNet101</b>	<b>4</b>	<b>4</b>
ResNet152	4	2
<b>VGG11</b>	<b>4</b>	<b>4</b>
<b>VGG13</b>	<b>4</b>	<b>4</b>
VGG16	2	2
<b>VGG19</b>	<b>4</b>	<b>4</b>
<b>ResNeXt50</b>	<b>4</b>	<b>4</b>
<b>ResNeXt101</b>	<b>4</b>	<b>4</b>

Table 5: Solver result for a 2x2 board. The correct board should feature 4 correct positions and 4 correct rotations