

## Part 1

- In standard matrix multiplication, multiplying two  $n \times n$  matrices by each other has the following costs:

- Multiplication:  $n^3$  steps
- Addition:  $(n - 1)n^2$  steps

Together, the total cost of the standard algorithm is  $n^3 + (n - 1)n^2 = (2n - 1)n^2$

- In Strassen's method, we can calculate the total cost by first calculating the costs of  $P_1$  to  $P_7$  as described in the lecture notes and the costs of the additions/subtractions of these products.

From the notes, we have the submatrices A, B, C, D, E, F, G, H which are of size  $n/2$  and the following 7 products:

- $P_1 = A(F - H)$
- $P_2 = (A + B)H$
- $P_3 = (C + D)E$
- $P_4 = D(G - E)$
- $P_5 = (A + D)(E + H)$
- $P_6 = (B - D)(G + H)$
- $P_7 = (A - C)(E + F)$

of which we can use to make:

- $AE + BG = P_5 + P_4 - P_2 + P_6$
- $AF + BH = P_1 + P_2$
- $CE + DG = P_3 + P_4$
- $CF + DH = P_5 + P_1 - P_3 - P_7$

For a  $n * n$  matrix, the cost  $C(n)$  can be

Note that the cost of  $P_1$ ,  $P_2$ ,  $P_3$  and  $P_4$  are the same ad