## Bits, Bytes, and Integers

Introduction to Computer Systems 2<sup>nd</sup> Lecture, Sep 12, 2024

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## **Today: Bits, Bytes, and Integers**

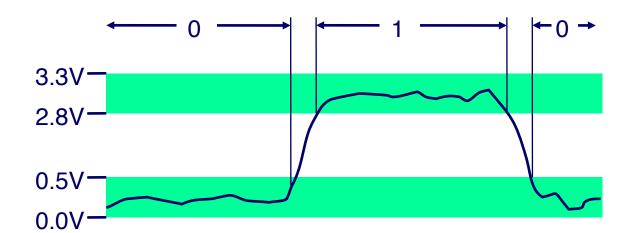
- Representing information as bits
- Bit-level manipulations
- Integers
  - Representation: unsigned and signed
  - Conversion, casting
  - Expanding, truncating
  - Addition, negation, multiplication, shifting
  - Summary
- Representations in memory, pointers, strings

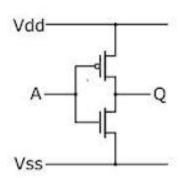
## **Binary Representations**

#### Base 2 Number Representation

- Represent 15213<sub>10</sub> as 11101101101101<sub>2</sub>
- Represent 1.20<sub>10</sub> as 1.0011001100110011[0011]...<sub>2</sub>
- Represent 1.5213 X 10<sup>4</sup> as 1.1101101101101<sub>2</sub> X 2<sup>13</sup>

#### Why Computers Use Binary?





Binary is the most practical system to use!

## **Encoding Byte Values**

- Byte = 8 bits
  - Binary 000000002 to 111111112
  - Decimal: 010 to 25510
  - Hexadecimal 00<sub>16</sub> to FF<sub>16</sub>
    - Base 16 number representation
    - Use characters '0' to '9' and 'A' to 'F'
    - Write FA1D37B<sub>16</sub> in C as
      - 0xFA1D37B
      - 0xfa1d37b

Why 8 bit?

## Hex Decimal

0	0	0000
1	1	0001
2	2	0010
3	3	0011
4	4	0100
5	5	0101
6	6	0110
7	7	0111
8	8	1000
9	9	1001
A	10	1010
В	11	1011
С	12	1100
D	13	1101
E	14	1110
F	15	1111
	•	

## **Data Representations**

C Data Type	Typical 32-bit	Intel IA32	x86-64
char	1	1	1
short	2	2	2
int	4	4	4
long	4	4	8
float	4	4	4
double	8	8	8
long double	-	-	10/16
pointer	4	4	8

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## **Boolean Algebra**

#### **Developed by George Boole in 19th Century**

- Algebraic representation of logic
  - Encode "True" as 1 and "False" as 0

And

Or

■ A&B = 1 when both A=1 and B=1

 $\blacksquare$  A | B = 1 when either A=1 or B=1

&	0	1
0	0	0
1	0	1

ı	0	1
0	0	1
1	1	1

Not

Exclusive-Or (Xor)

■ ~A = 1 when A=0

. = 1 when A=0	A^B = 1 when either A=1 or B=1, but not bot			
~	^ 0 1			
0 1				

## **General Boolean Algebras**

- Operate on Bit Vectors
  - Operations applied bitwise

All of the Properties of Boolean Algebra Apply

## **Example: Representing & Manipulating Sets**

#### Representation

- Width w bit vector represents subsets of {0, ..., w−1}
- $a_i = 1 \text{ if } j \in A$ 
  - 01101001 { 0, 3, 5, 6 }
  - **76543210**
  - 01010101 { 0, 2, 4, 6 }
  - **76543210**

#### Operations

<b>8</b>	Intersection	01000001	{ 0, 6 }
•	Union	01111101	{ 0, 2, 3, 4, 5, 6 }
^	Symmetric difference	00111100	{ 2, 3, 4, 5 }
<b>■</b> ~	Complement	10101010	{ 1. 3. 5. 7 }

## **Bit-Level Operations in C**

- Operations &, |, ~, ^ Available in C
  - Apply to any "integral" data type
    - long, int, short, char, unsigned
  - View arguments as bit vectors
  - Arguments applied bit-wise

#### Examples (Char data type)

- $\sim 0x41 \rightarrow 0xBE$ 
  - $\sim 01000001_2 \rightarrow 101111110_2$
- $\sim 0x00 \rightarrow 0xFF$ 
  - $\sim 000000002 \rightarrow 1111111112$
- $0x69 \& 0x55 \rightarrow 0x41$ 
  - $011010012 & 010101012 \rightarrow 010000012$
- $0x69 \mid 0x55 \rightarrow 0x7D$ 
  - 011010012 | 010101012 → 0111111012

## **Contrast: Logic Operations in C**

#### Contrast to Logical Operators

- **&**&, ||, !
  - View 0 as "False"
  - Anything nonzero as "True"
  - Always return 0 or 1
  - Early termination

#### Examples (char data type)

- $!0x41 \rightarrow 0x00$
- $!0x00 \rightarrow 0x01$
- $!!0x41 \rightarrow 0x01$
- $0x69 \&\& 0x55 \rightarrow 0x01$
- $0x69 || 0x55 \rightarrow 0x01$
- p && \*p (avoids null pointer access)

Watch out for && vs. &
(and || vs. |)...
one of the more common
oopsies in
C programming

## **Shift Operations**

- Left Shift: x << y
  - Shift bit-vector x left y positions
    - Throw away extra bits on left
    - Fill with 0's on right
- Right Shift: x >> y
  - Shift bit-vector x right y positions
    - Throw away extra bits on right
  - Logical shift
    - Fill with 0's on left
  - Arithmetic shift
    - Replicate most significant bit on left

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J	HU			ч	שט	ı ıa	VIU	, .

Shift amount < 0 or ≥ word size</p>

Argument x	01100010
<< 3	00010 <i>000</i>
<b>Log.</b> >> 2	00011000
<b>Arith.</b> >> 2	00011000

Argument x	<b>1</b> 0100010
<< 3	00010 <i>000</i>
Log. >> 2	00101000
<b>Arith.</b> >> 2	<i>11</i> 101000

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## **Encoding Integers**

#### Unsigned

$$B2U(X) = \sum_{i=0}^{w-1} x_i \cdot 2^i$$

#### **Two's Complement**

$$B2T(X) = -x_{w-1} \cdot 2^{w-1} + \sum_{i=0}^{w-2} x_i \cdot 2^i$$

Sign Bit

#### C short 2 bytes long

	Decimal	Hex	Binary
x	15213	3B 6D	00111011 01101101
У	-15213	C4 93	11000100 10010011

#### Sign Bit

- For 2's complement, most significant bit indicates sign
  - 0 for nonnegative
  - 1 for negative

## **Two-complement: Simple Example**

$$-16$$
 8 4 2 1
 $10 = 0$  1 0 1 0 8+2 = 10

$$-16$$
 8 4 2 1  
 $-10 = 1$  0 1 1 0  $-16+4+2 = -10$ 

## **Encoding Example (Cont.)**

x = 15213: 00111011 01101101y = -15213: 11000100 10010011

Weight	152	13	-152	213
1	1	1	1	1
2	0	0	1	2
4	1	4	0	0
8	1	8	0	0
16	0	0	1	16
32	1	32	0	0
64	1	64	0	0
128	0	0	1	128
256	1	256	0	0
512	1	512	0	0
1024	0	0	1	1024
2048	1	2048	0	0
4096	1	4096	0	0
8192	1	8192	0	0
16384	0	0	1	16384
-32768	0	0	1	-32768

$$B2T(X) = -x_{w-1} \cdot 2^{w-1} + \sum_{i=0}^{w-2} x_i \cdot 2^i$$

Sum 15213 -15213

## **Numeric Ranges**

#### Unsigned Values

• 
$$UMax = 2^w - 1$$
111...1

#### **■ Two's Complement Values**

■ 
$$TMin = -2^{w-1}$$
100...0

■ 
$$TMax = 2^{w-1} - 1$$
  
011...1

#### Other Values

Minus 1111...1

#### Values for W = 16

	Decimal	Hex	Binary
UMax	65535	FF FF	11111111 11111111
TMax	32767	7F FF	01111111 11111111
TMin	-32768	80 00	10000000 000000000
-1	-1	FF FF	11111111 11111111
0	0	00 00	00000000 00000000

#### **Values for Different Word Sizes**

	W				
	8 16 32		32	64	
UMax	255	65,535	4,294,967,295	18,446,744,073,709,551,615	
TMax	127	32,767	2,147,483,647	9,223,372,036,854,775,807	
TMin	-128	-32,768	-2,147,483,648	-9,223,372,036,854,775,808	

#### Observations

- $\blacksquare$  | TMin | = TMax + 1
  - Asymmetric range
- UMax = 2 \* TMax + 1

#### C Programming

- #include limits.h>
- Declares constants, e.g.,
  - ULONG\_MAX
  - LONG\_MAX
  - LONG\_MIN
- Values platform specific

## **Unsigned & Signed Numeric Values**

Χ	B2U( <i>X</i> )	B2T( <i>X</i> )
0000	0	0
0001	1	1
0010	2	2
0011	3	3
0100	4	4
0101	5	5
0110	6	6
0111	7	7
1000	8	-8
1001	9	<b>-</b> 7
1010	10	<b>–</b> 6
1011	11	<b>-</b> 5
1100	12	-4
1101	13	-3
1110	14	-2
1111	15	-1

#### Equivalence

Same encodings for nonnegative values

#### Uniqueness

- Every bit pattern represents unique integer value
- Each representable integer has unique bit encoding

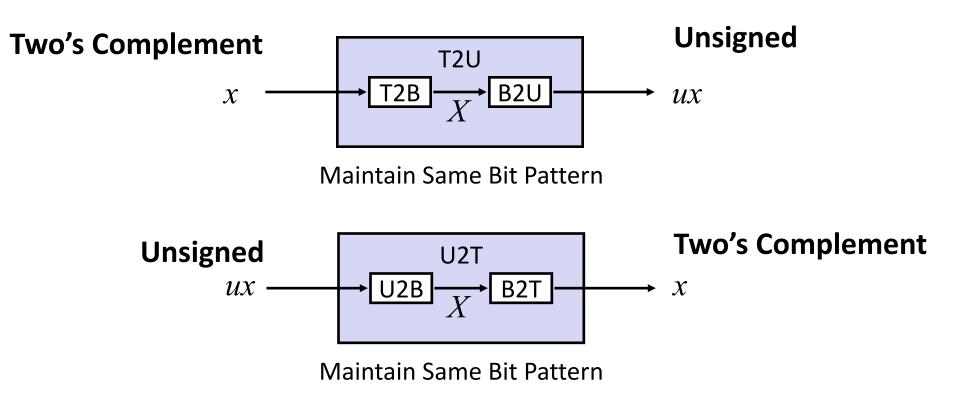
#### ■ ⇒ Can Invert Mappings

- $U2B(x) = B2U^{-1}(x)$ 
  - Bit pattern for unsigned integer
- $T2B(x) = B2T^{-1}(x)$ 
  - Bit pattern for two's comp integer

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## **Mapping Between Signed & Unsigned**

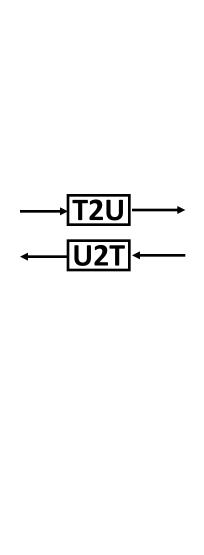


 Mappings between unsigned and two's complement numbers: keep bit representations and reinterpret

## Mapping Signed ↔ Unsigned

Bits
0000
0001
0010
0011
0100
0101
0110
0111
1000
1001
1010
1011
1100
1101
1110
1111

Signed
0
1
2
3
4
5
6
7
-8
-7
-6
-5
-4
-3
-2
-1

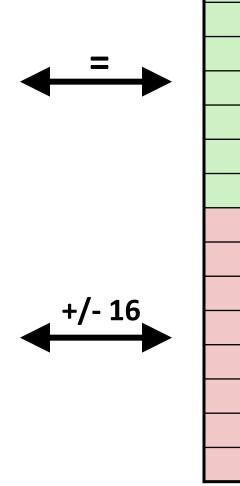


Unsigned
0
1
2
3
4
5
6
7
8
9
10
11
12
13
14
15

## Mapping Signed ↔ Unsigned

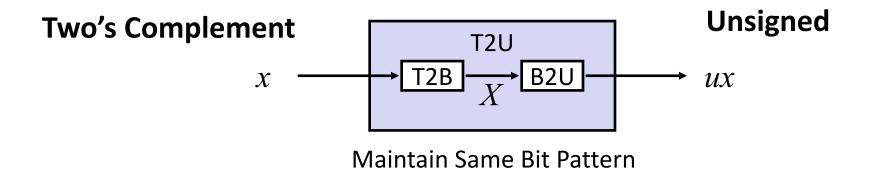
Bits
0000
0001
0010
0011
0100
0101
0110
0111
1000
1001
1010
1011
1100
1101
1110
1111

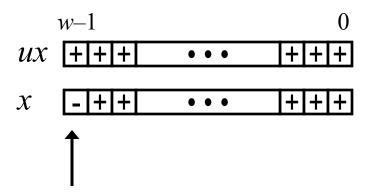
Signed
0
1
2
3
4
5
6
7
-8
-7
-6
-5
-4
-3
-2
-1



Unsigned
0
1
2
3
4
5
6
7
8
9
10
11
12
13
14
15

## **Relation between Signed & Unsigned**





Large negative weight becomes

Large positive weight

#### **Conversion Visualized**

2's Comp.  $\rightarrow$  Unsigned **UMax Ordering Inversion** UMax - 1Negative → Big Positive TMax + 1Unsigned TMax **TMax** Range 2's Complement Range

## Signed vs. Unsigned in C

#### Constants

- By default are considered to be signed integers
- Unsigned if have "U" as suffixOU, 4294967259U

#### Casting

Explicit casting between signed & unsigned same as U2T and T2U

```
int tx, ty;
unsigned ux, uy;
tx = (int) ux;
uy = (unsigned) ty;
```

Implicit casting also occurs via assignments and procedure calls

```
tx = ux;

uy = ty;
```

## **Casting Surprises**

#### Expression Evaluation

- If there is a mix of unsigned and signed in single expression, signed values implicitly cast to unsigned
- Including comparison operations <, >, ==, <=, >=
- **Examples for** W = 32: **TMIN = -2,147,483,648**, **TMAX = 2,147,483,647**

Constant <sub>1</sub>	Constant <sub>2</sub>	Relation	<b>Evaluation</b>
0	0U	==	unsigned
-1	0	<	signed
-1	0U	>	unsigned
2147483647	-2147483647-1	>	signed
2147483647U	-2147483647-1	<	unsigned
-1	-2	>	signed
(unsigned)-1	-2	>	unsigned
2147483647	2147483648U	<	unsigned
2147483647	(int) 2147483648U	>	signed

## Summary Casting Signed ↔ Unsigned: Basic Rules

- Bit pattern is maintained
- But reinterpreted
- Can have unexpected effects: adding or subtracting 2<sup>w</sup>
- Expression containing signed and unsigned int
  - int is cast to unsigned!!

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## **Sign Extension**

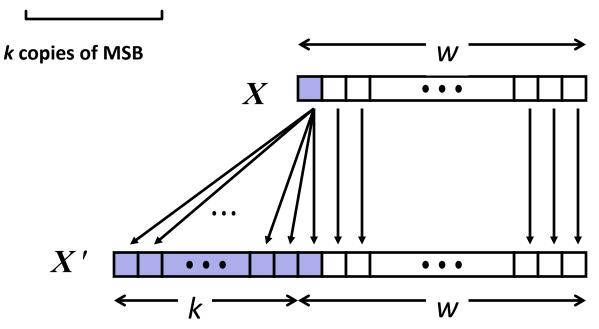
#### Task:

- Given w-bit signed integer x
- Convert it to w+k-bit integer with same value

#### Rule:

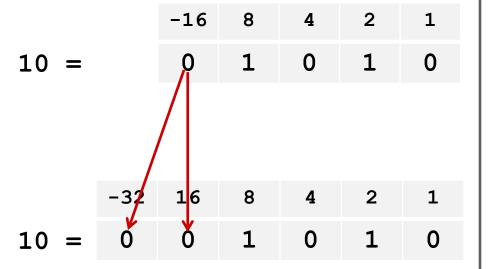
Make k copies of sign bit:

$$X' = X_{w-1}, ..., X_{w-1}, X_{w-1}, X_{w-2}, ..., X_0$$

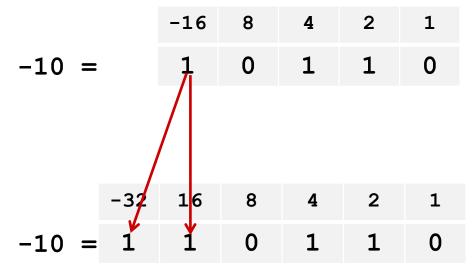


## Sign Extension: Simple Example

#### **Positive number**



#### **Negative number**



## **Sign Extension Example**

```
short int x = 15213;
int     ix = (int) x;
short int y = -15213;
int     iy = (int) y;
```

	Decimal	Hex	Binary		
x	15213	3B 6D	00111011 01101101		
ix	15213	00 00 3B 6D	00000000 00000000 00111011 01101101		
У	-15213	C4 93	11000100 10010011		
iy	-15213	FF FF C4 93	11111111 11111111 11000100 10010011		

- Converting from smaller to larger integer data type
- C automatically performs sign extension

## **Truncation: Simple Example**

#### No sign change

$$2 \mod 16 = 2$$

$$-16$$
 8 4 2 1  $-6$  = 1 1 0 1 0

$$-8$$
 4 2 1  $-6$  = 1 0 1 0

 $-6 \mod 16 = 26U \mod 16 = 10U = -6$ 

#### Sign change

$$-16$$
 8 4 2 1  $10 = 0$  1 0 1 0

$$-8$$
 4 2 1
 $-6$  = 1 0 1 0

 $10 \mod 16 = 10U \mod 16 = 10U = -6$ 

$$-16$$
 8 4 2 1  $-10$  = 1 0 1 1 0

$$-10 \mod 16 = 22U \mod 16 = 6U = 6$$

# **Summary: Expanding, Truncating: Basic Rules**

- Expanding (e.g., short int to int)
  - Unsigned: zeros added
  - Signed: sign extension
  - Both yield expected result
- Truncating (e.g., unsigned to unsigned short)
  - Unsigned/signed: bits are truncated
  - Result reinterpreted
  - Unsigned: mod operation
  - Signed: similar to mod

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## **Unsigned Addition**

Operands: w bits

u •••

True Sum: w+1 bits

+ v •••

u + v

Discard Carry: w bits

 $UAdd_w(u, v)$ 

#### Standard Addition Function

- Ignores carry output
- Implements Modular Arithmetic

$$s = UAdd_w(u, v) = u + v \mod 2^w$$

unsigned char		1110	1001	<b>E</b> 9	233
	+	1101	0101	+ D5	+ 213

## Hex Decimanary

	•	•	•
	)	0	0000
1		1	0001
2		2	0010
3	3	3	0011
4		4	0100
5	5	5	0101
(	5	6	0110
7	7	7	0111
8	3	8	1000
9	•	9	1001
Z	7	10	1010
E	3	11	1011
	7	12	1100
Ι	)	13	1101
E	I.	14	1110
F	'	15	1111

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unsigned char		1110	1001	<b>E</b> 9	233
	+	1101	0101	+ D5	+ 213
	1	1011	1110	1BE	446
		1011	1110	BE	190

# Hex Decimanary

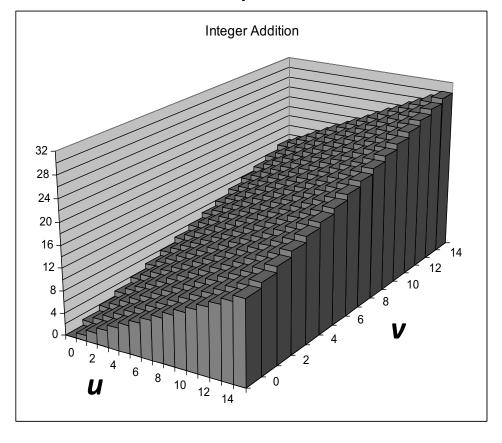
0	0	0000
1	1	0001
2	2	0010
3	3	0011
4	4	0100
5	5	0101
6	6	0110
7	7	0111
8	8	1000
9	9	1001
A	10	1010
В	11	1011
С	12	1100
D	13	1101
E	14	1110
F	15	1111

# Visualizing (Mathematical) Integer Addition

#### Integer Addition

- 4-bit integers u, v
- Compute true sum  $Add_4(u, v)$
- Values increase linearly with u and v
- Forms planar surface

### $Add_4(u, v)$

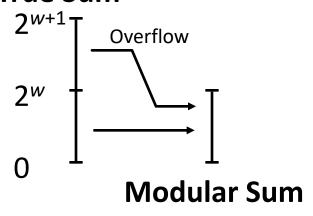


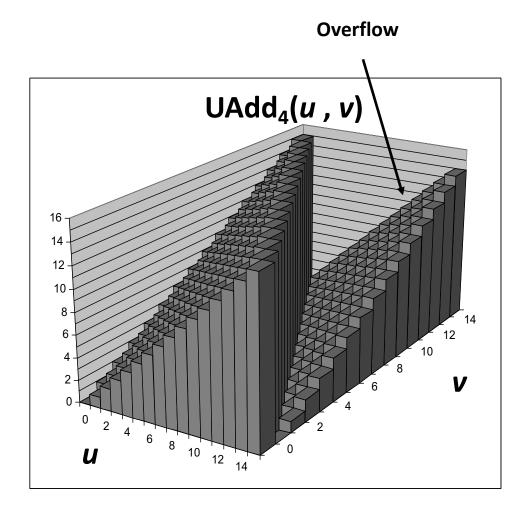
### **Visualizing Unsigned Addition**

#### Wraps Around

- If true sum  $\geq 2^w$
- At most once

#### **True Sum**





# **Two's Complement Addition**

Operands: w bits

True Sum: w+1 bits

Discard Carry: w bits

 $TAdd_{w}(u, v)$ 

#### TAdd and UAdd have Identical Bit-Level Behavior

Signed vs. unsigned addition in C:

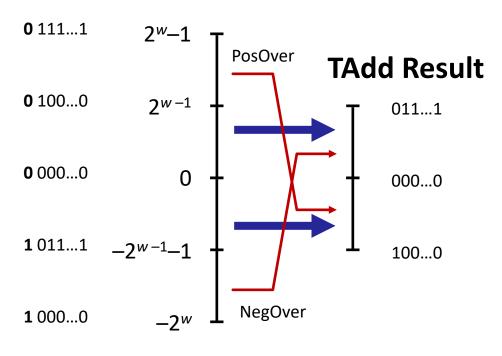
Will give s == t

### **TAdd Overflow**

### Functionality

- True sum requires w+1 bits
- Drop off MSB
- Treat remaining bits as 2's comp. integer

#### **True Sum**



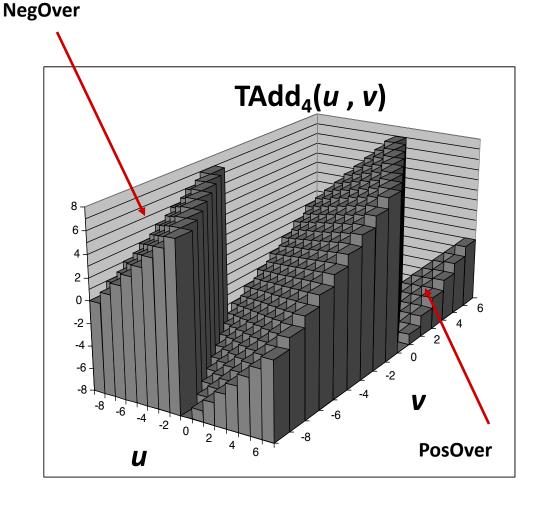
# Visualizing 2's Complement Addition

#### Values

- 4-bit two's comp.
- Range from -8 to +7

### Wraps Around

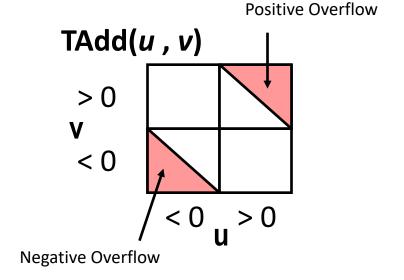
- If sum  $\geq 2^{w-1}$ 
  - Becomes negative
  - At most once
- If sum  $< -2^{w-1}$ 
  - Becomes positive
  - At most once



# **Characterizing TAdd**

#### Functionality

- True sum requires w+1 bits
- Drop off MSB
- Treat remaining bits as 2's comp. integer

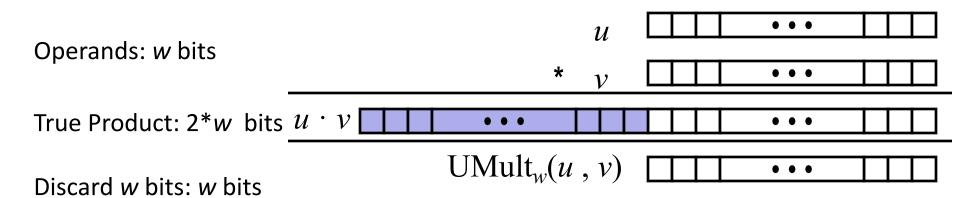


$$TAdd_{w}(u,v) = \begin{cases} u+v+2^{w} & u+v < TMin_{w} \text{ (NegOver)} \\ u+v & TMin_{w} \leq u+v \leq TMax_{w} \\ u+v-2^{w} & TMax_{w} < u+v \text{ (PosOver)} \end{cases}$$

## Multiplication

- Goal: Computing Product of w-bit numbers x, y
  - Either signed or unsigned
- But, exact results can be bigger than w bits
  - Unsigned: up to 2w bits
    - Result range:  $0 \le x * y \le (2^w 1)^2 = 2^{2w} 2^{w+1} + 1$
  - Two's complement min (negative): Up to 2w-1 bits
    - Result range:  $x * y \ge (-2^{w-1})*(2^{w-1}-1) = -2^{2w-2} + 2^{w-1}$
  - Two's complement max (positive): Up to 2w bits, but only for  $(TMin_w)^2$ 
    - Result range:  $x * y \le (-2^{w-1})^2 = 2^{2w-2}$
- So, maintaining exact results...
  - would need to keep expanding word size with each product computed
  - is done in software, if needed
    - e.g., by "arbitrary precision" arithmetic packages

# **Unsigned Multiplication in C**



### Standard Multiplication Function

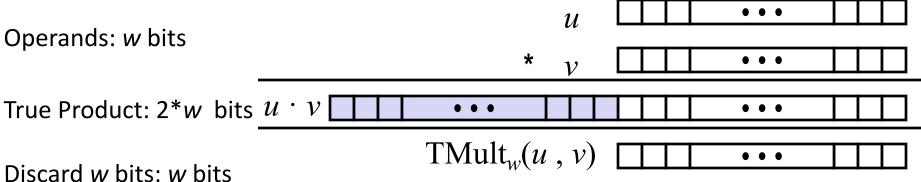
Ignores high order w bits

### Implements Modular Arithmetic

$$UMult_w(u, v) = u \cdot v \mod 2^w$$

		1110	1001		E9		233
*		1101	0101	*	D5	*	213
1100	0001	1101	1101	C	1DD		49629
		1101	1101		DD		221

# Signed Multiplication in C



### **Standard Multiplication Function**

- Ignores high order w bits
- Some of which are different for signed vs. unsigned multiplication
- Lower bits are the same

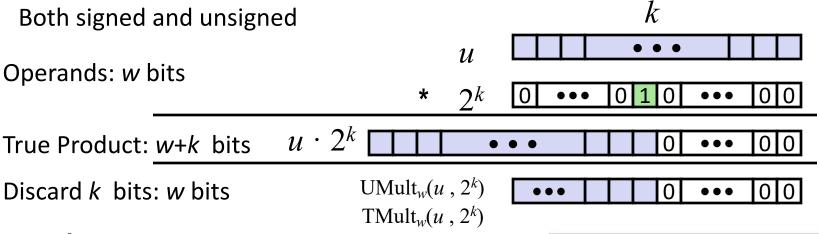
		1110	1001		<b>E9</b>		-23
*		1101	0101	*	D5	*	-43
0000	0011	1101	1101	C	3DD		989
		1101	1101		DD		-35

## Power-of-2 Multiply with Shift

#### **Operation**

- $\mathbf{u} << \mathbf{k}$  gives  $\mathbf{u} * \mathbf{2}^k$
- Both signed and unsigned

Operands: w bits



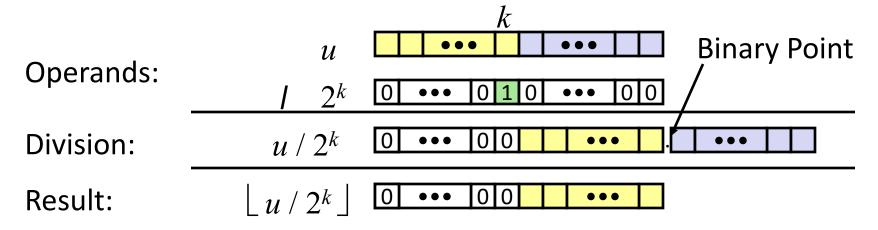
#### **Examples**

- u << 3
- (u << 5) (u << 3) ==
- Most machines shift and add faster than multiply
  - Compiler generates this code automatically

**Important Lesson: Trust Your Compiler!** 

## **Unsigned Power-of-2 Divide with Shift**

- Quotient of Unsigned by Power of 2
  - $\mathbf{u} \gg \mathbf{k}$  gives  $\lfloor \mathbf{u} / 2^k \rfloor$
  - Uses logical shift



	Division	Computed	Hex	Binary
x	15213	15213	3B 6D	00111011 01101101
x >> 1	7606.5	7606	1D B6	00011101 10110110
x >> 4	950.8125	950	03 B6	00000011 10110110
x >> 8	59.4257813	59	00 3B	00000000 00111011

## **Today: Bits, Bytes, and Integers**

- Representing information as bits
- Bit-level manipulations
- Integers
  - Representation: unsigned and signed
  - Conversion, casting
  - Expanding, truncating
  - Addition, negation, multiplication, shifting
  - Summary
- Representations in memory, pointers, strings

### **Arithmetic: Basic Rules**

#### Addition:

- Unsigned/signed: Normal addition followed by truncate, same operation on bit level
- Unsigned: addition mod 2<sup>w</sup>
  - Mathematical addition + possible subtraction of 2<sup>w</sup>
- Signed: modified addition mod 2<sup>w</sup> (result in proper range)
  - Mathematical addition + possible addition or subtraction of 2<sup>w</sup>

### Multiplication:

- Unsigned/signed: Normal multiplication followed by truncate,
   same operation on bit level
- Unsigned: multiplication mod 2<sup>w</sup>
- Signed: modified multiplication mod 2<sup>w</sup> (result in proper range)

# Why Should I Use Unsigned?

- Don't use without understanding implications
  - Easy to make mistakes

```
unsigned i;
for (i = cnt-2; i >= 0; i--)
  a[i] += a[i+1];
```

Can be very subtle

```
#define DELTA sizeof(int)
int i;
for (i = CNT; i-DELTA >= 0; i-= DELTA)
```

## **Counting Down with Unsigned**

Proper way to use unsigned as loop index

```
unsigned i;
for (i = cnt-2; i < cnt; i--)
  a[i] += a[i+1];</pre>
```

- See Robert Seacord, Secure Coding in C and C++
  - C Standard guarantees that unsigned addition will behave like modular arithmetic
    - $0-1 \rightarrow UMax$
- Even better

```
size_t i;
for (i = cnt-2; i < cnt; i--)
   a[i] += a[i+1];</pre>
```

- Data type size t defined as unsigned value with length = word size
- Code will work even if cnt = UMax
- What if cnt is signed and < 0?</p>

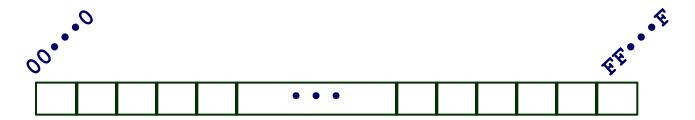
# Why Should I Use Unsigned? (cont.)

- *Do* Use When Performing Modular Arithmetic
  - Multiprecision arithmetic
- Do Use When Using Bits to Represent Sets
  - Logical right shift, no sign extension

## Today: Bits, Bytes, and Integers

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### **Byte-Oriented Memory Organization**



### Programs refer to data by address

- Conceptually, envision it as a very large array of bytes
  - In reality, it's not, but can think of it that way
- An address is like an index into that array
  - and, a pointer variable stores an address

### Note: system provides private address spaces to each "process"

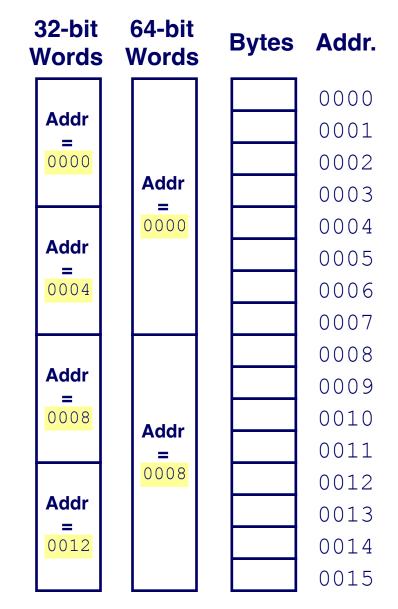
- Think of a process as a program being executed
- So, a program can clobber its own data, but not that of others

### **Machine Words**

- Any given computer has a "Word Size"
  - Nominal size of integer-valued data
    - and of addresses
  - Until recently, most machines used 32 bits (4 bytes) as word size
    - Limits addresses to 4GB (2<sup>32</sup> bytes)
  - Increasingly, machines have 64-bit word size
    - Potentially, could have 18 EB (exabytes) of addressable memory
    - That's 18.4 X 10<sup>18</sup>
    - Machines still support multiple data formats
      - Fractions or multiples of word size
      - Always integral number of bytes

## **Word-Oriented Memory Organization**

- Addresses Specify Byte Locations
  - Address of first byte in word
  - Addresses of successive words differ by 4 (32-bit) or 8 (64-bit)



# **Example Data Representations**

C Data Type	Typical 32-bit	Typical 64-bit	x86-64
char	1	1	1
short	2	2	2
int	4	4	4
long	4	8	8
float	4	4	4
double	8	8	8
long double	-	-	10/16
pointer	4	8	8

# **Byte Ordering**

- So, how are the bytes within a multi-byte word ordered in memory?
- Conventions
  - Big Endian: Sun, PPC Mac, Internet
    - Least significant byte has highest address
  - Little Endian: x86, ARM processors running Android, iOS, and Windows
    - Least significant byte has lowest address

## **Byte Ordering Example**

### Example

- Variable x has 4-byte value of 0x01234567
- Address given by &x is 0x100

Big Endian		0x100	0x101	0x102	0x103	
		01	23	45	67	
Little Endia	ın	0x100	0x101	0x102	0x103	
	_	67	45	23	01	

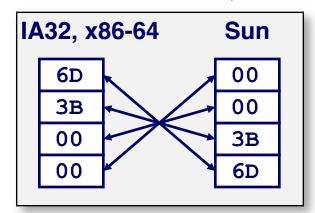
### **Representing Integers**

**Decimal: 15213** 

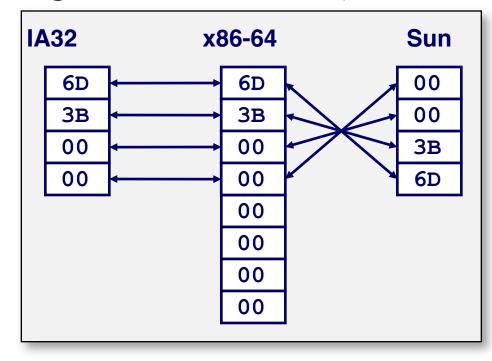
**Binary:** 0011 1011 0110 1101

**Hex:** 3 B 6 D

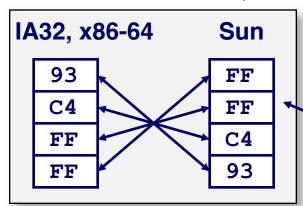
int A = 15213;



long int C = 15213;



int B = -15213;



Two's complement representation

### **Examining Data Representations**

- Code to Print Byte Representation of Data
  - Casting pointer to unsigned char \* allows treatment as a byte array

```
typedef unsigned char *pointer;

void show_bytes(pointer start, int len) {
  int i;
  for (i = 0; i < len; i++)
    printf("%p\t0x%.2x\n",start+i, start[i]);
  printf("\n");
}</pre>
```

#### **Printf directives:**

%p: Print pointer

%x: Print Hexadecimal

# show bytes Execution Example

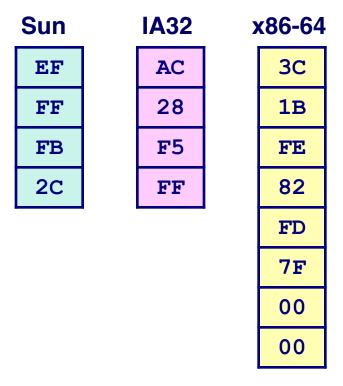
```
int a = 15213;
printf("int a = 15213;\n");
show_bytes((pointer) &a, sizeof(int));
```

### Result (Linux x86-64):

```
int a = 15213;
0x7fffb7f71dbc 6d
0x7fffb7f71dbd 3b
0x7fffb7f71dbe 00
0x7fffb7f71dbf 00
```

### **Representing Pointers**

int 
$$B = -15213;$$
  
int \*P = &B



Different compilers & machines assign different locations to objects

Even get different results each time run program

## Representing Strings

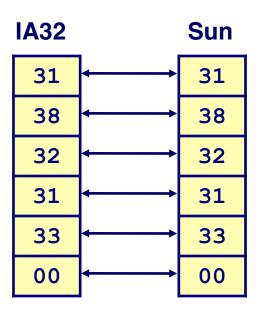
char S[6] = "18213";

#### Strings in C

- Represented by array of characters
- Each character encoded in ASCII format
  - Standard 7-bit encoding of character set
  - Character "0" has code 0x30
    - Digit i has code 0x30+l
  - man ascii for code table
- String should be null-terminated
  - Final character = 0

### Compatibility

Byte ordering not an issue



### **Reading Byte-Reversed Listings**

#### Disassembly

- Text representation of binary machine code
- Generated by program that reads the machine code

#### Example Fragment

Address	Instruction Code	<b>Assembly Rendition</b>		
8048365:	5b	pop %ebx		
8048366:	81 c3 ab 12 00 00	add \$0x12ab,%ebx		
804836c:	83 bb 28 00 00 00 00	cmpl \$0x0,0x28(%ebx)		

### Deciphering Numbers

- Value:
- Pad to 32 bits:
- Split into bytes:
- Reverse:

0x12ab

0x000012ab

00 00 12 ab

ab 12 00 00

### **Summary**

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## **Integer C Puzzles**

#### **Initialization**