

Documentation Up To 8 April

Carles Roca Reverter

April 2024

1 Introduction

1.

After reading the corresponding papers to understand the problem formulation and current state-of-art() and the proposed algorithm to solve the optimization (MVSRM, surrogate model) we tested some single-objective and multi-objective functions on the algorithm to how to format our future function and to check that it works correctly.

For instance, trying with the multi-objective (2 objectives) Binh and Korn function we get this correct convex Pareto Set.

2. After that, we studied the grid to be analysed and defined the admittance matrix in terms of their parameters and the cost function function to evaluate when using HVAC.

Note that in the power flow all buses are considered PQ buses except bus 6, which is the slack bus and represents the grid we are supplying power to. Also, we are allowing the reactive power compensation to be placed in the 5 different possible positions through the line (pre and post offshore trafo, midcable and pre and post onshore trafo), rather than just 3

2 Vector of unknowns

$$\mathbf{v} = [vol_{tr}, \quad n_{cables}, \quad react_{bi1}, \quad \dots, \quad react_{bi5}, \quad react_{cont1}, \quad \dots, \quad react_{cont5}, \quad react_{bi5}, \quad S_{trafo}]$$

- Binary variables of the shunt reactors: Binary. Whether we put or not a shunt reactor at position i.
- Transmission voltage: Choice (a integer number is assigned which corresponds to a set of parameters for that voltage level)
- Number of cables: Integer
- Transformer rated power: Continuous
- Shunt reactors value: Continuous. Sizing of the compensation at position i in p.u.

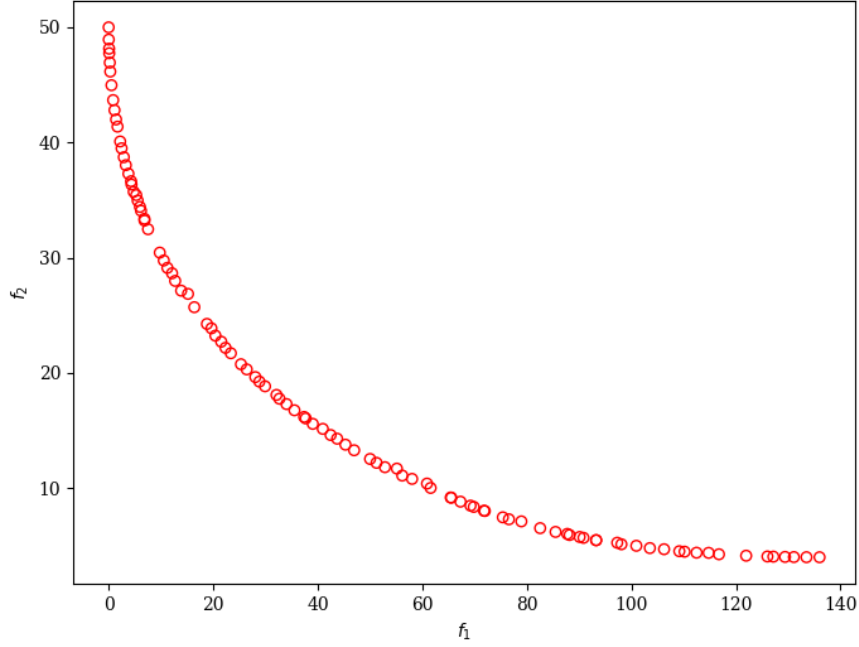


Figure 1: Convex Pareto Set obtained for Binh and Korn function with MVRSM multi-objective

3 Constraints AC

Equality constraints: POWER FLOW

$$\mathbf{h}_m(\mathbf{x}) = \mathbf{0}$$

$$\mathbf{S}_i = \mathbf{V}_i \left(\sum_{j=1}^{\mathbf{N}_{\text{nodes}}} \mathbf{Y}_{ij} \mathbf{V}_j \right)^*$$

$$\underline{s}_1 - (p_{owf} + jq_{owf}) = 0$$

$$\underline{s}_1 - \underline{u}_1 [(2\underline{y}_{tr} + \underline{y}_l)\underline{u}_1 - (\underline{y}_{tr})\underline{u}_2]^* = 0$$

$$\underline{s}_2 - \underline{u}_2 [-(\underline{y}_{tr})\underline{u}_1 + (2\underline{y}_{\pi 1} + \underline{y}_l + \underline{y}_{tr})\underline{u}_2 - (\underline{y}_{\pi 1})\underline{u}_3]^* = 0$$

$$\underline{s}_3 - \underline{u}_3 [-(\underline{y}_{\pi 1})\underline{u}_2 + (2\underline{y}_{\pi 1} + 2\underline{y}_{\pi 2} + \underline{y}_l)\underline{u}_3 - (\underline{y}_{\pi 2})\underline{u}_4]^* = 0$$

$$\underline{s}_4 - \underline{u}_4 [-(\underline{y}_{\pi 2})\underline{u}_3 + (2\underline{y}_{\pi 2} + \underline{y}_l + \underline{y}_{tr})\underline{u}_4 - (\underline{y}_{tr})\underline{u}_5]^* = 0$$

$$\underline{s}_5 - \underline{u}_5 [-(\underline{y}_{tr})\underline{u}_4 + (2\underline{y}_{tr} + \underline{y}_l + \underline{y}_g)\underline{u}_5]^* = 0$$

$$\mathbf{Y} = \begin{bmatrix} (2\underline{y}_{tr} + \underline{y}_l) & -\underline{y}_{tr} & 0 & 0 & 0 & 0 \\ -\underline{y}_{tr} & (2\underline{y}_{\pi 1} + \underline{y}_l + \underline{y}_{tr}) & -\underline{y}_{\pi 1} & 0 & 0 & 0 \\ 0 & -\underline{y}_{\pi 1} & (2\underline{y}_{\pi 1} + 2\underline{y}_{\pi 2} + \underline{y}_l) & -\underline{y}_{\pi 2} & 0 & 0 \\ 0 & 0 & -\underline{y}_{\pi 2} & (2\underline{y}_{\pi 2} + \underline{y}_l + \underline{y}_{tr}) & -\underline{y}_{tr} & 0 \\ 0 & 0 & 0 & -\underline{y}_{tr} & (2\underline{y}_{tr} + \underline{y}_l + \underline{y}_g) & -\underline{y}_g \\ 0 & 0 & 0 & 0 & -\underline{y}_g & \underline{y}_g \end{bmatrix}$$

Inequality constraints: LIMITATIONS

$$\mathbf{g_n}(\mathbf{x}) \leq \mathbf{0}$$

$$U_{kj} - U_{max} \leq 0$$

$$U_{min} - U_{kj} \leq 0$$

$$I_{kj} - I_{max} \leq 0$$

$$Q_{min} - Q_{gj} \leq 0$$

$$Q_{gj} - Q_{max} \leq 0$$

$$Y_{l-ij} - Y_{l-i}^{max} \leq 0$$

$$N_{react} - N_{react}^{max} \leq 0$$

4 Newton-Rapshon Solver code

For solving the PF, we code a simple solver using the Newton-Rapshon method. Note we are computing the Jacobian with the explicit form (derivatives) rather than numerically, which yields faster results.

After solving the PF, we compute technical costs with their corresponding penalization and the investment resulting from the decided combination of parameters.

A fist trial was intended using single-objective, which means you sum up all the costs as objective and try to minimize that using MRVSM. We obtained the following results:

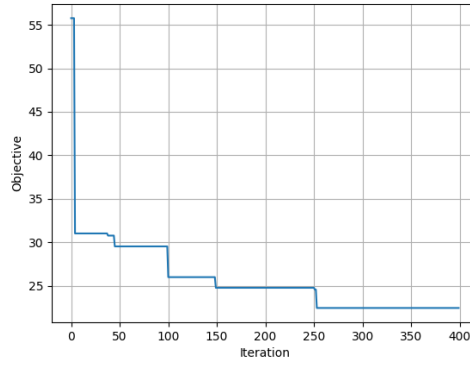


Figure 2: Evolution of cost function objective as iterations go on

As we can see, it seems the algorithm is able to minimize the objective function and follows a reasonable path. Nevertheless it would be interesting to start evaluating the problem as a multi-objective. Why? This way we can evaluate the trade off between investments and technical costs and therefore try to find the Pareto set of our optimization problem.

4.1 Multi-objective

Then, we adaptades the cost function for a multi-objective output and uses the correspondent form of the MVRSM. As a first step we consider a fixed value for transmission voltage and number of cables, without adding any reactor and let free the trafo powers variable to see if the problem definitions is well formulated. As we can see in the image we have 2 good news: We are getting the set of points we were expecting and the algorithm is converging to the optimal ones (see how the color of the points indicates the evolution). Yellow points from the last iterations are falling in the optimal zones.

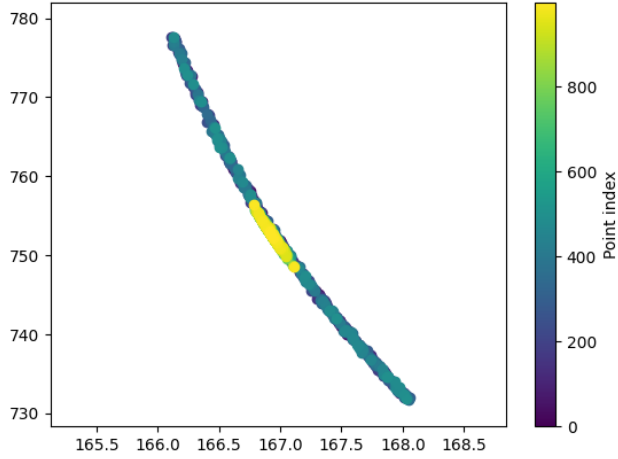


Figure 3: Convex Pareto Set letting only trafo rated power as free variable (x-axis is investment, y-axis is tech cost)

Now it is interesting to add the compensations as potential investment and also let transmission voltage and number of cables as free parameters. If we let the function to introduce just one compensator (for instance an offshore one between the plant and the trafo) we obtain the following: Clearly the top

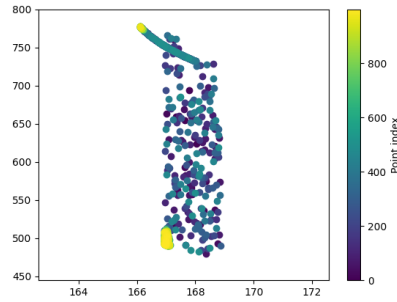


Figure 4: Plot fix vol and just 1 reactor

curved part corresponds to the combinations where it is NOT adding the shunt reactance and the only free parameter is the trafo (same result as before). Is difficult for me to interpret this results, since it seems like the cost of adding is so small compared to other ones. If we virtually (multiplying by a factor x10) increase the reactors costs and allow for all possible combinations:

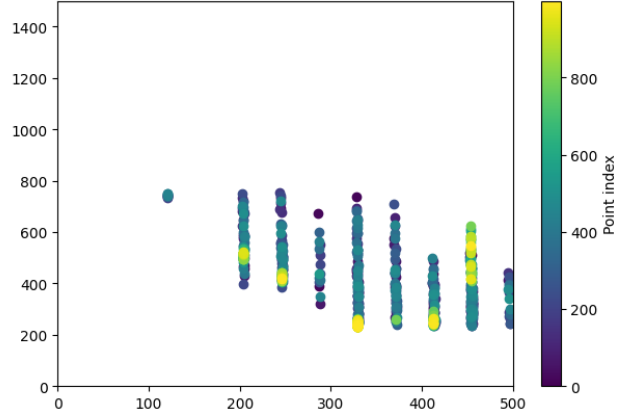


Figure 5: Discrete combinations of reactors

Here we kind of see a "discretized" Pareto of the reactor combinations. Note here we can see the first signs of Lauren's comments about the difficulty of convergence of the algorithm for non-convex and smooth Pareto's, as it seems that the final iterations are not always leading to optimal points.

Now we want to put all variables into play, including different voltages levels and number of cables.

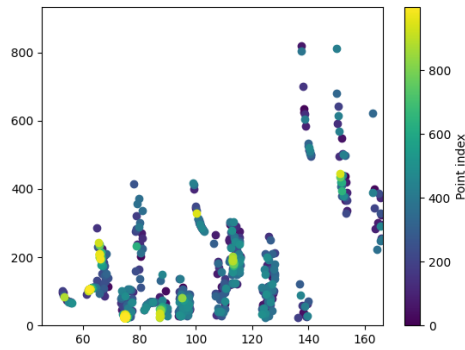


Figure 6: Reactors 1 and 2 and all combinations of voltages and number of cables

We can also plot the Pareto dominant points: To see how useful is the al-

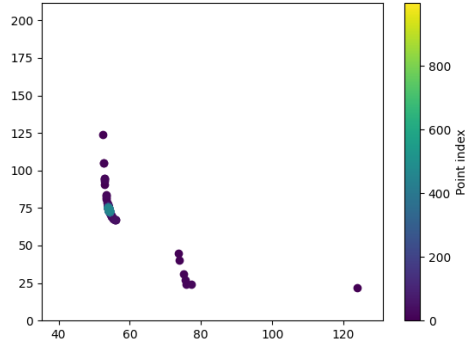


Figure 7: Pareto set: note it is a zoom to the lower left part of previous plot

gorithm, we can compare the results obtained with a random search of 1000 evaluations (now all 5 reactors are considered). From this random evaluation we

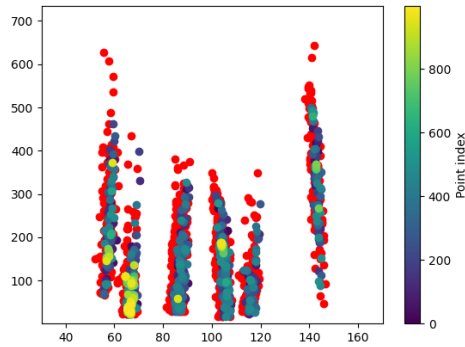


Figure 8: Red dots are purely random evaluations

can infer the following. For the current definition of the problem the algorithm is not being that useful because a relatively small set of random evaluations is able to "reach" the optimal solutions too. This could be due by the fact that only a small number of possible investments is considered and computationally talking it is easy to reach optimal operating points by just "brute force" using random evaluations.

Also we can try to somehow simulate what would happen if we used the voltage variable as a continuous range, which is not feasible in reality, to check if somehow we can obtain a smoother plot and indicate that we are in the right

direction. Note that to do that we have to "invent" a cost function (which is in reality of discrete nature and does not follow a clear continuous function). That's why the order of magnitude of the following results must not be taken as representative, but just as an experiment trying to simulate this extra continuous variable.

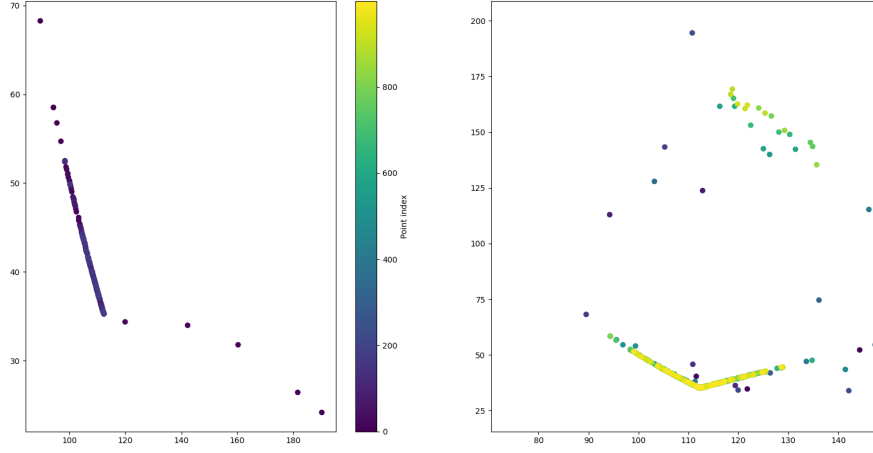


Figure 9: Dominant points (left) and obtained points (right) with continuous transmission voltage level.

5 Next steps

Next steps are the following one:

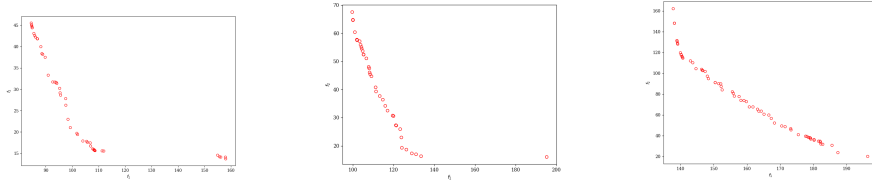
- Try to modify MVRSM for non-convex Pareto sets using the tricks commented by Laurens. Fixating at the worst objective at each iteration.
- Study if there are more useful algorithms for this kind of problem such as genetic ones (i.e. NSGA-II or NSGA-III) .
- Ponder different wind conditions in the cost calculation using probability to take into account different power generations and needs of reactive compensation.
- Go for a further complex analysis which considers the meshing between the turbines inside the wind power plant (electrical collection system). This includes a much bigger number of decision variables in the problem (discrete) , which potentially would allow to really take advantage of MVRSM strength and derive into a smoother Pareto set.

6 NSGA-II

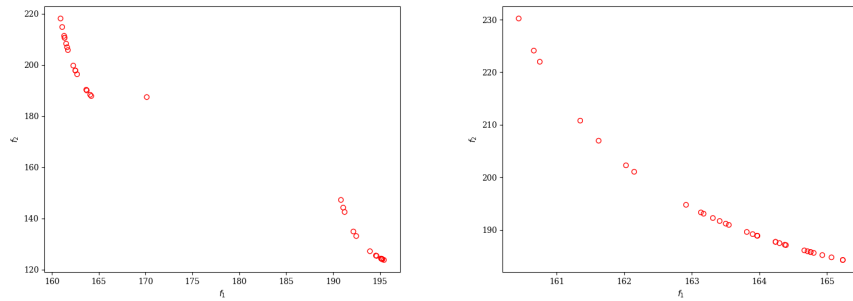
Now we will expose the first results obtained when implementing a new type of algorithm: NSGA-II with uses a meta-heuristic genetic approach.
general first impressions:

- Results are better than MVRSM
- Each voltage level and/or number of cables has to be evaluated separately (to avoid power flow not converging in any of them) to get good results. If not, algorithm "breaks" when the PF dos not converge.
- For now, technical constraints are treated with a penalty function. To determine optimal point in the pareto set, since weights and importance are not fully clear, I would go for an utopia point analysis with the Pareto front.
- We should investigate how the different crowding functions work and which suits better (seems we get similar results with all the 2-objective oriented ones)

We attach some results obtained:



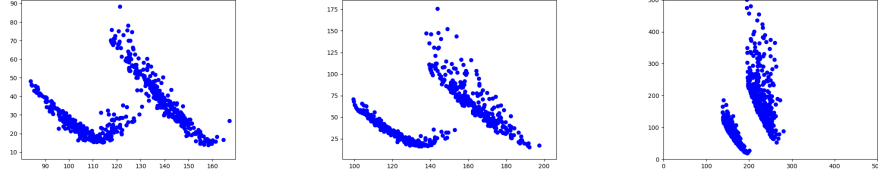
(a) 200 MW for distances, 80, 100 and 150 km respectively



(b) 1000 MW for distance 80 km. It is clear the 2 sets represented by 2 or 3 cables in parallel. On the right, zoom to 2 cable zone

We also can see how it compares to a set of random evaluations:
As we can see in this 200 MW case, the algorithm is able to find the pareto

front positioned on the lower part of the plot, which is the optimal one. Note that for this case, the upper set corresponds to 3 cables, that for small power plants lead to overvoltages, increasing technical costs.



(a) 200 MW for distances, 80, 100 and 150 km respectively with random evaluations

Another interesting insight from the random evaluations is that our exploration space seems to be formed by n (where n is the number of cable we are testing) convex sets.

Now we have to see how we select the optimal point in the pareto front. We can use the utopia point method, which is a way to select the point that is closest to the anchor point in the pareto front. This is done by normalizing the objectives and then selecting the point that minimizes the euclidean distance to the anchor point in the normalized space.

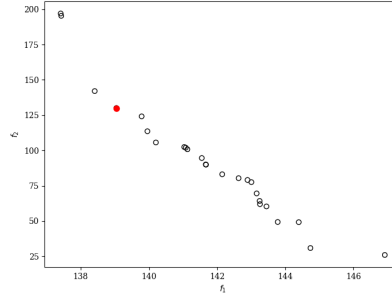


Figure 12: Utopia point approach result (red dot) with equal weights for both objectives for 200 MW and 150 km

Ara cal mirar quis es el nostres set unknowns solucio i comprar amb resultats paper. Aclarir que passa amb la compensacio que en alguns casos mai la posa, fare ultima revisio funcions de costos i pw.