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A Parity-Preserving Reversible QCA Gate with Self-Checking Cascadable Resiliency

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ABSTRACT A novel Parity-Preserving Reversible Gate (PPRG) is developed using Quantum-dot Cellular Automata (QCA) technology. PPRG enables rich fault-tolerance features, as well as reversibility attributes sought for energy-neutral computation. Performance of the PPRG design is validated through implementing thirteen standard combinational Boolean functions of three variables, which demonstrate from 10.7 to 41.9 percent improvement over the previous gate counts obtained with other reversible and/or preserving gate designs. Switching and leakage energy dissipation as low as 0.141 eV and 0.294 eV, for 1.5 E_k energy level are achieved using PPRG, respectively. The utility of PPRG is leveraged to design a one-bit full adder with 171 cells occupying only 0.19 μ m² area. Finally, fault detection and isolation properties are formalized into a concise procedure. PPRG-based circuits capable of self-configuring active recovery for selected three-variable standard functions are realized using a memoryless method irrespective of garbage outputs.

INDEX TERMS Quantum-dot cellular automata, reversible logic, parity-preserving, self-checking fault detection methodology, full adder

I. INTRODUCTION

Quantum-dot Cellular Automata (QCA) has been widely investigated for potential improvements over transistor-based technologies like Complementary Metal-Oxide-Semiconductor (CMOS). QCA offers high device density, low power consumption and high switching speed features [1], [2]. Due to these attractive attributes, quantum gates and circuits have been targeted for their enabling roles toward computational reversibility. Reversibility in a quantum computing structure is defined as a one-to-one mapping of inputs to outputs, which leads to low power consumption and error detection ability [3]. It is worth mentioning that the loss of one bit of information expends greater than or equal to kTln2 joules of energy, where k is Boltzman's constant and T the absolute temperature that the computation is operated [4]. As an example of the considerable previous research undertaken to construct reversible components based on nanotechnologies including QCA, use of the Bennett clock mechanism achieves less than kTln2 switching energy dissipation [5], [6]-[9].

In this paper, we first present a novel parity-preserving reversible gate (PPRG) which is then used to design a fault

tolerant reversible full adder (FA). In our proposed *Parity-Preserving Reversible Gate*, besides the one-to-one mapping feature of reversibility, the number of one's in the input is equal to that of the output. Therefore, any fault which causes mismatch in parity can be detected.

This paper is organized as follows. Section II presents review of the QCA and the reversible gates. Section III develops the functionality of PPRG and then realizes a fault tolerant full adder which is based on it. Section IV describes a fault detection and isolation methodology for PPRG-based designs. Finally, conclusions are provided in Section IV.

II. BACKGROUND

A. QCA REVIEW

QCA cells have been realized through several physical implementation methods such as semiconductor [1], [2], [10], metal island (metal-dot) [5], [10], [11], molecular [2], [5], [43], and nanomagnetic dot [5], [10], [12]. The first two are the most promising implementations, due to their high operation speed and integration density. Specifically, semiconductor QCA cells can be fabricated using existing industrial frameworks. The main difference between the metal dot

FIGURE 1. QCA cell with two possible polarizations.

and semiconductor QCA implementations is that metal dots are capacitively-coupled, while the quantum dots are coulombically-coupled in the semiconductor realization. The major challenge of these technologies is their low operating temperature, while molecular and nanomagnetic implementations can operate in room temperature. However, molecular integration is relatively complicated, and also it is not compatible with existing technologies for read and write operations. In contrast, nanomagnetic QCAs have been fabricated and shown proper functionality, although their performance are significantly lower than semiconductor and metal QCAs.

The basic element in QCA is a square archetype QCA cell, which is comprised of four quantum dots and two identical charges. Each cell has two certain polarization states which is obtained owing to the Coulomb interaction between the two free electrons in order to reach the maximum distance [1]. Unlike CMOS, QCA encodes binary data using intercell Coulomb repulsion between electrons that forms two stable diagonal positions, i.e., P=-1 and P=+1, which are assigned to denote a logic "0" and logic "1", respectively, as shown in Figure 1 [2].

Additionally, due to the Coulombic effects, binary data passes through a row of cascaded QCA cells which constitutes a QCA wire. In order for a QCA signal to propagate properly, synchronization and energy restoration are essential which are obtained by applying a specific four-phased clocking scheme. There are two types of QCA clocking schemes commonly utilized, the Landauer [4] (high speed) and the Bennett [3] (low power consumption). Although the Launder clocking suffers from abrupt switching, it can provide the system with two benefits, which are finegrained pipelining and high throughput. These have been emphasized in designing QCA circuits. The Landauer clocking scheme, which is generally used in QCA circuitry includes four distinct zones, Switch, Hold, Release, and Relax, where each zone is shifted by 90 degree compared to the previous zone, as shown in Figure 2a.

Considering clocking strategies in conjunction with circuit design strategies can lead to the concept of physical reversibility. The connection between logical reversibility and this concept is comprehensively discussed in [41]. If a logically-reversible QCA system can be implemented by employing physically reversible devices, associated power dissipation caused by information erasure can become zero. Although, the Launder clocking strategy used in this paper lends itself to circuits with high throughput and fine-grained pipelining, which are essential for the proposed highly cascadable gate, it still requires the circuit to

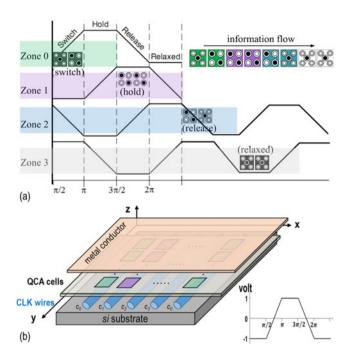


FIGURE 2. QCA clocking scheme (a) four-phased clock of the QCA zones, and (b) cross-sectional view.

be reversible at very fine levels. Adopting a more realistic and physical clocking strategy, as referred to uni-directional Bennett scheme [41], provides more flexibility in designing the reversible gates, since only the gate needs to be reversible as opposed to each segment of the gate. However, this strategy has lower throughput as compared to Launder clocking strategy and incurs a time overhead to the system. In order to combine the low power advantage of reversible computing with the high throughput advantage of pipelining, a combination of Bennett clocking and memory storage was proposed as an innovative approach which has been presented in [42].

The required adiabatic clocking mechanism is produced by CMOS circuits including a metal conductor, and wires such as nanowire [5] or CNTs [13]. The wires are placed under the QCA structure in the y-plane to generate the electric field whereas the conductor above the QCA cells spreads in the xy-plane to guide the produced electric field in z-direction, as shown in Figure 2b. The produced clock is then applied to the cells to control the height of the interdot barrier, either raising or reducing it, between dots within a QCA cell. A QCA cell is polarized due to the effects of adjacent cells during the Switch phase, and then in the Hold phase, interdot barriers are raised to the maximum height to maintain its polarization. In the Release phase, the cell moves to unpolarized state by losing its polarity, due to the reduction in the interdot barrier. Finally, in the Relax phase, the cell is unpolarized with negligible barrier. Our work is based on the aforementioned clocking mechanism [14]. Due to the QCA synchronization issues, specific implementation rules such as number of cells in a clock zone or synchronize flows

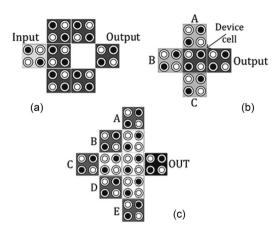


FIGURE 3. Layouts of (a) an inverter, (b) a 3-input majority gate, and (c) a 5-input majority gates.

arriving to a gate, must be considered during the design of a QCA-based circuit. Moreover, each QCA clock zone consist of at least two cells to preserve its influence on the subsequent clock zone.

Almost all QCA circuits are built based on the fundamental elements, the inverter gate and the Majority Gate (MG) [1], [2]. Figure 3 depicts widely used QCA designs for the inverter gate and the MGs. For MG designs, existence of electrostatic repulsion among the electrons of the input cells forces the central cell(s), i.e., device cell, to the stable polarization and propagate this state to the output cell as an output which is polarized to the majority polarization of inputs. The three-input MG, as shown in Figure 3b functions AB + BC + AC (A, B and C are the three inputs). MG could be also programmed such that it functions as an AND or an OR logic function, if one of the three inputs is set to -1 or +1, respectively.

Recently, several designs for five-input MG have been proposed [16]–[19] as shown in Figure 3c. The five-input MG outputs "1" if and only if at least three input cells are set to "1". It functions according to the following equation:

$$M(A, B, C, D, E) = ABC + ABD + ABE + ACD + ACE + ADE + BCD + BCE + BDE + CDE.$$
(1)

In similar manner to the three-input MG, by fixing the polarization of two of the five inputs in the five-input MG as logic "0" or logic "1", a 3-input AND gate or a three-input OR gate can be achieved, respectively.

B. REVERSIBLE GATES OVERVIEW

Due to the inability of conventional logic gates to restore the inputs from the produced outputs, referred to as *reversibility*, and leveraging reversible computing in nanotechnology, i.e., quantum computing, extensive researches have been studied. The main concept of reversible computing is that during the computation no information is lost and the total operation is reversible, i.e., the number of inputs is same as the number of outputs which have mathematically one-to-one mapping.

Commonly-cited reversible gates include Fredkin and Toffoli gates. The Toffoli gate [20] has two control inputs which

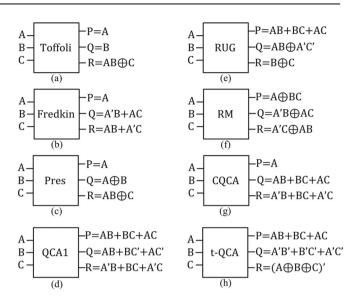


FIGURE 4. Block diagram of (a) Toffoli [20], (b) Fredkin [21], (c) Pres [23], (d) QCA1 [6], (e) RUG [24], (f) RM [25], (g) CQCA [26], and (h) t-QCA [27].

are copied the first two inputs to the first two outputs and the third output is controlled by the first two inputs. The Fredkin gate [21], also known as CSWAP gate, is a universal reversible gate that controlled by the first input. Here if A=1, the second and third input lines are swapped, otherwise if A=0, then the input lines propagates to the outputs.

Although reversible logic circuits target energy conservation, the leveraging of conventional methods for detecting errors using these circuits faces some challenges. Since one of the most widely used method for error detection is parity checking, parity-preserving reversible gates were sought and introduced [22]. Figure 4 shows the several schematic of three-input reversible and preserving gates. As shown in Figures 4a, 4b, 4c, 4d, 4e, and 4f are reversible gates and Figures 4g and 4h are preserving fault-tolerant gates. Only Figure 4b illustrates a preserving reversible gate as identified below.

A reversible gate with parity-preserving capability satisfies the following conditions:

- 1) Mapping of its inputs to outputs is bijective,
- 2) XOR of the inputs produces a result equal to the XOR of the outputs $(I_1 \oplus I_2 \oplus ... \oplus I_n = O_1 \oplus O_2 \oplus ... \oplus O_n)$.

III. PROPOSED PARITY-PRESERVING REVERSIBLE GATE

In this section, a QCA-based three-input, three-output Parity-Preserving Reversible Gate is proposed using one two-input XOR gate, two invertors, and two two-input multiplexers (MUXs). PPRG provides a one-to-one input-output mapping, i.e., each set of the input signals is exclusively mapped to a unique set of output signals. Thus, the input signal could be extracted by knowing only the output of the gate, which validates the PPRG reversible property. Figure 5a shows the schematic and its related truth table of the PPRG, in which $P = A \oplus B$, $Q = A.C + \overline{B}.\overline{C}$, and $R = \overline{A}.C + \overline{B}.\overline{C}$, where A, B, and C, are inputs and P, Q, and R are outputs of the gate.

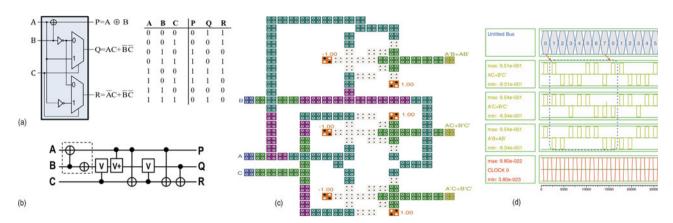


FIGURE 5. Proposed Parity-Preserving Reversible Gate (a) schematic and its truth table, (b) quantum representation, (c) layout, and (d) simulation results.

To overcome the difficulty of realizing a fault-tolerant reversible gate, our proposed gate is designed in a manner such that it provides equal parity for each input set and its corresponding output, if parity is the number of ones in each set. The truth table, shown in Figure 5a demonstrates the parity-preserving feature of the PPRG. Figure 5b depicts the quantum representation of the PPRG with a quantum cost of seven. The quantum cost of each reversible gate represents its computational complexity, which is calculated by counting the numbers of primitive gates, such as NOT, Controlled-V and Controlled-V+ gates [28].

Herein, a robust single-layered wire-crossing approach, proposed in [29], is leveraged to implement the QCA layout of the PPRG, as shown in Figure 5c. Both QCADesigner engines, the bistable approximation and the coherence vector [30] are utilized to validate functionality of the PPRG. The simulation waveform of proposed PPRG is shown in Figure 5d. It can be seen that the output is generated after a delay of one clock cycle (four clock phases). The inputs are applied to the PPRG gate at clock phase 0 and the outputs are available at clock phase 4. To consider realistic clock distribution, the two-Dimensional Wave (two-DW) clocking scheme proposed in [31] is utilized, as shown in Figure 6a. The two-DW approach comprises an array of identical square-shaped zones, which provides low computation time while maintaining acceptable implementation complexity. Figure 6b depicts the implementation of our PPRG using two-DW clocking mechanism (PPRG-2DW) along with the coplanar crossover for wire crossing, which provides outputs after a delay of 1.75 clock cycles (seven clock phases).

In order to evaluate the PPRG performance in comparison with previously proposed reversible gates, it is utilized to implement the thirteen standard three-variable Boolean functions, which can represent all the possible 256 combinational forms of three-input functions [32]. The number of gates required for different designs to implement the noted standard functions is listed in Table 1. The last row of the table shows the ability of PPRG to synthesis various logical functions with lower average gate count, which verifies the PPRG better performance in term of gate count. The same evaluation procedure

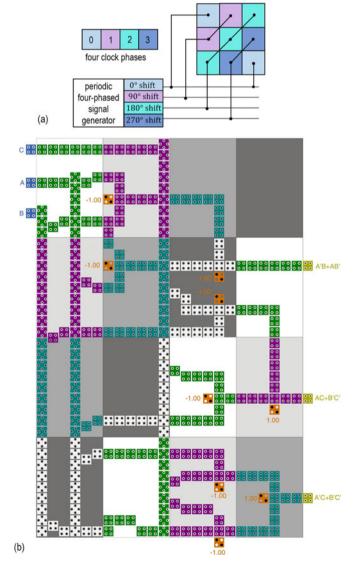


FIGURE 6. (a) Two-DW clocking scheme for the QCA designs [31], and (b) PPRG layout under the two-DW clocking scheme (PPRG-2DW).

TABLE 1. Gate Counts Comparison for Implementation of 13 Standard Functions.
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Standard functions	CQCA	t-QCA	Toffoli	Peres	QCA1	RUG	RM	Fredkin	PPRG
	[26]	[27]	[6]	[23]	[6]	[24]	[25]	[26]	(developed herein)
Reversible/Conservative	No/Yes	No/Yes	Yes/No	Yes/No	Yes/No	Yes/No	Yes/No	Yes/Yes	Yes/Yes
1. F = A.B.C	2	2	2	2	2	3	2	2	2
2. F = A.B	1	1	1	1	1	1	1	1	1
3. $F = A.B.C + \overline{A}.\overline{B}.\overline{C}$	3	8	3	3	2	2	2	3	2
4. $F = A.B.C + A.\overline{B}.\overline{C}$	6	2	5	4	3	3	3	4	3
5. F = A.B + B.C	2	2	2	2	2	3	2	2	2
6. $F = AB + \overline{A}.\overline{B}.C$	5	6	5	3	3	3	2	5	2
7. $F = \overline{A}.B.C + \overline{A}.\overline{B}.\overline{C} + A.B.\overline{C}$	6	6	6	4	3	3	3	6	3
8. F= A	1	1	1	1	1	1	1	1	1
9. F = A.B + B.C + A.C	1	1	5	4	1	1	5	5	2
10. $F=A.B+\overline{B}.C$	3	4	3	3	3	3	1	1	1
11. F= A.B+B.C+ \overline{A} . \overline{B} . \overline{C}	6	2	5	1	4	3	2	6	2
12. $F = A.B + \overline{A}.\overline{B}$	4	1	2	1	2	1	2	2	2
13. $F=A.B.C+\overline{A}.\overline{B}.C+A.\overline{B}.\overline{C}+\overline{A}.B.\overline{C}$	3	2	2	3	2	3	2	3	2
Total	43	38	42	32	29	30	28	41	25
Improvement (%)	41.9%	34.2%	40.5%	21.9%	13.8%	16.7%	10.7%	39%	-

can be readily achieved for two-variable Boolean functions, in which the obtained results show better performance for PPRG-based designs. Since, numbers two and three are prime, we can implement all n-variable Boolean functions using PPRG by partitioning it into m and p, two-variable and three-variable functions, respectively, where $n=2\times m+3\times p$. Accordingly, a reduced partitioning level is projected for the large scale QCA circuits after cascading.

It is worth noting that only the Fredkin gate and our proposed PPRG have both reversibility and parity-preserving features among all the gates listed in Table 1. Hence, a comparison between the Fredkin and PPRG is summarized in Table 2, which shows the superiority of our design in terms of cell count and area, in addition to the average number of required gates for implementing standard gates which is mentioned beforehand.

A. PPRG POWER ANALYSIS

A QCA power dissipation model has been proposed in [33] whereby total power dissipation of a QCA circuit is divided into two principle components, *leakage* and *switching*. Leakage power is the power losses throughout the clock alternations, from low-to-high or high-to-low, and power losses during the switching period is considered as switching power [34].

In order to expose the power efficiency of PPRG besides its beneficial structure, a comprehensive power analysis and comparison among the previously published Fredkin gate [21], RM [25], t-QCA-II [27] and PPRG is performed.

TABLE 2. Cost Comparison of Parity-Preserving Reversible Gates.

Reversible	# of gates for	Cell	Area $(\mu \text{m})^2$	Quantum
Gate	Standard Functions	count		cost
Fredkin [26]	41	191	0.37	5
PPRG	25	171	0.19	7
Improvement	+39%	+10.5%	+48.64%	-40%

QCAPro tool [33] is utilized as an adequate power estimator tool for estimating the power consumption of the structures at 2 K temperature under three different tunneling energy levels (0.5 E_k , 1.0 E_k , and 1.5 E_k). The power dissipation map for both PPRG implementations shown in Figures 5c and 6b, are illustrated in Figures 7 and 8, respectively. Cells with higher power dissipation are distinguished using thermal hotspots with darker colors.

Average leakage and switching energy dissipation of the two different PPRG implementations as well as the previously proposed gates are listed in Table 3. The power analysis results elaborates our PPRG design significant efficiency in both switching and leakage energy dissipation criteria. As expected, the average energy dissipation of the PPRG-2DW implementation is higher than PPRG, due to the realistic clocking considerations.

B. PPRG FAULT ANALYSIS

The parity-preserving feature of the PPRG could be utilized along with a fault mapping look-up table, demonstrated in Table 4, to detect the faults occurred in the gate input and

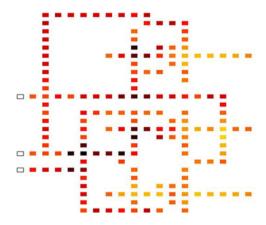


FIGURE 7. Power dissipation map for the PPRG in Figure 5c.

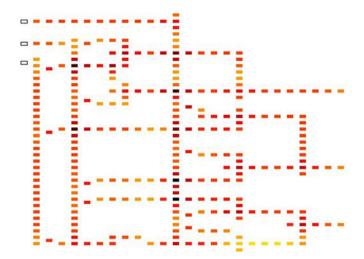


FIGURE 8. Power dissipation map for the PPRG-2DW in Figure 6b.

output pins. Table 4 lists different test inputs required for fault detection, which can be summarized in a unique test vector, called *defect isolation test vector* = {000, 001, 100, 111}.

Herein, the fault isolation process of the PPRG is described through an example. Consider that the input is equal to "111" and the propagated faulty output is "110" instead of being "010". In this case, error could be quickly observed by detecting the parity mismatch between the input parity (P_{in} ="1") and the output parity (P_{out} ="0"). Then, the fault mapping look-up table will be utilized to distinguish both faulty pin and fault type, based on the mapping between test inputs and faulty outputs. As in this example, the look-up table exhibits a stuck at zero fault in the input pin B.

C. FAULT-TOLERANT FULL ADDER BASED ON THE PROPOSED PPRG

The Full Adder is the basic building block of many arithmetic components. Additionally, complex quantum computing requires availability of a compatible conservative reversible adder. Thus, several fault-tolerant FAs based on the reversible gates have been proposed in the literature [35]–[37].

Figure 9 depicts the schematic and cell layout of our proposed fault tolerant PPRG-based FA. The design leverages three PPRGs, first gate produces $A \oplus B$, and second and third ones produce C_{out} and SUM outputs, respectively. Although conventionally in all reversible gates fan-out is not allowed, due to inherent quasi adiabatic clocking, in QCA logic gates fan-out is permitted [38]. The following equations express

TABLE 3. Leakage and Switching Energy Dissipation Results.

	leakage energy dissipation (eV)			switching energy dissipation (eV)			
Circuits	$0.5E_k$	$1.0E_k$	$1.5E_k$	$0.5E_k$	$1.0E_k$	$1.5E_k$	
RM [25] t-QCA-II [27] Fredkin [21] PPRG PPRG-2DW	0.117 0.067 0.101 0.058 0.079	0.318 0.186 0.283 0.168 0.251	0.534 0.316 0.482 0.294 0.463	0.309 0.227 0.213 0.193 0.577	0.251 0.191 0.175 0.166 0.512	0.205 0.161 0.143 0.141 0.443	

TABLE 4. Stuck-at Fault Mapping Look-Up Table for the PPRG Gate.

Fault	Test	Expected	Faulty	Stuck
suspicious	Input	Output	Output	At
PIN	"ABC"	"PQR"	"PQR"	Fault
A	100	111	011	Zero
	000	011	111	One
В	111	010	110	Zero
	001	001	101	One
С	111	010	000	Zero
	000	011	001	One
P	100	111	011	Zero
	111	010	110	One
Q	111	010	000	Zero
	001	001	011	One
R	100	111	110	Zero
	111	010	001	One

the functionality of proposed PPRG-based FA using the following gates depicted in Figure 9:

$PPRG_1$:

$$input_A = A$$
, $input_B = B$, $input_C = C$
 $output_P = P_1 = A \oplus B$

PPRG₂:

$$input_{A} = C, input_{B} = \overline{A}, input_{C} = P_{1}$$

$$output_{Q} = \mathbf{Q_{2}} = C.P_{1} + \overline{\overline{A}}.\overline{P_{1}} = C.(A \oplus B) + A.\overline{(A \oplus B)}$$

$$= A.\overline{B}.C + \overline{A}.B.C + A.B = A.B + B.C + A.C = \mathbf{C_{out}}$$
(2)

PPRG₃:

$$input_A = P_1, input_B = C, input_C = not used$$

$$\mathbf{P_3} = P_1 \oplus C = A \oplus B \oplus C = \mathbf{SUM}.$$

A comparative performance analysis between our proposed one-bit QCA FA and existing structures are given in Table 5. Herein, the cost function proposed in [39] is utilized to calculate the overall cost, which is a function of delay (t), number of QCA gates (G), and number of crossovers (C). Overall cost function is expressed as below

$$Cost = (N_{-gate} + C^{m}) \times t$$

$$N_{gate} = N_{MG}^{n} + N_{inv}, t = 4 \times N_{clk},$$

$$C = l \times coplanar \ crossing \ cost,$$
(3)

where N_{MG} , N_{inv} , and N_{clk} are number of MGs, inverters, and clocks, respectively. The parameter l denotes the number of layers, i.e., one for single layer and three for multilayer designs. Herein, since all the compared designs are single layer, l equals 1. It is worth noting that N_{MG} and C have greater effect on complexity, power consumption, and fabrication difficulty. Therefore, Cost has a quadratic relation with N_{MG} and C, i.e., n=m=2. Thus, the governing equation for cost calculation of one-bit FA is $FA_{cost} = (N_{MG}^2 + N_{inv} + C^2) \times t \times N_{RG}$, where N_{RG} is number of utilized reversible gates.

Results provided in Table 5 implies that the overall cost is significantly reduced for our proposed FA. It surpasses the other investigated designs with the exception of QCA1 [6],

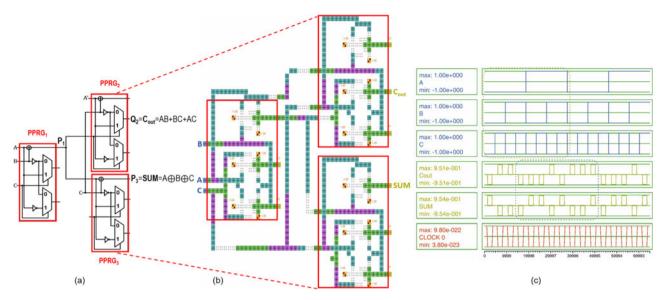


FIGURE 9. The proposed reversible full adder (a) schematic, (b) the related cell layout, and (c) simulation results.

which is not a parity-preserving design. Thus, proposed PPRG-based FA has the lowest overall cost comparing to the most cost-efficient designs using parity-preserving and reversible gates in their structure.

IV. FAULT ANALYSIS IN PPRG-BASED LOGIC DESIGNS

In this section, inherent characteristics of the proposed PPRG are utilized to introduce an effective fault detection and isolation approach for PPRG-based logic circuit designs. Herein, two different PPRG-based circuit topologies are investigated: 1) completely-cascaded arrangement, and 2) partially-cascaded arrangement.

A. COMPLETELY-CASCADED ARRANGEMENT

Figure 10 shows the structure of the completely-cascaded PPRG-based designs, in which all the three output terminals of each PPRG is directly connected to the inputs of the subsequent gate. Table 6 lists the output states in a completely-cascaded design according to the eight possible inputs. For instance, the first row of the table describes that applying a_0 as the primary input of the design, will result in obtaining a_0 as the level 4 output, i.e., the output of the fourth cascaded PPRG. Therefore, the period of the primary input propagation in the different output levels of a completely-cascaded PPRG-based design depends on the primary input, and can be obtained from the last column of the table. Herein, Table 6 is defined as a *select matrix* to be utilized in the following pseudocode which

TABLE 5. Comparison of Fault Tolerant Full Adder Deigns.

Reversible Gate	N_{MG}	N _{inv}	С	t	N_{RG}	Overall Cost	Cell count	Area $(\mu \text{m})^2$
Fredkin [21]	6	8	5	4	5	1,380	955	1.85
Toffoli [20]	4	5	3	4	4	480	672	1.48
QCA1 [6]	3	7	4	2	3	192	438	0.48
RUG [24]	7	11	10	8	2	2,560	594	0.92
PPRG	6	6	3	4	3	522	513	0.57

describes the algorithm proposed in this paper for fault detection and isolation of the PPRG-based circuits:

Procedure: Error Detection

```
Main_{input} \leftarrow Convert Primary_{input} \text{ to } a_0, \dots, a_7 \text{ type}
 1:
       ⊳ based on the Main<sub>input</sub> select proper row of selec-
     tion_matrix and copy into Test_Array
       Test\_Array \leftarrow selection\_matrix[Main_{input}]
 4:
      Design\_Length \leftarrow Length (PPRG-based design)
               ➤ Number of cascaded PPRGs in design
 5:
      F_1 \leftarrow Design\_Length/Length (Test_Array)
 6:
 7:
       F_2 \leftarrow Design\_Length \mod Length \text{ (Test\_Array)}
 8:
       if Main_{output} == Test\_Array[F_2] then
 9:
         Print "Fault free!"
         Break
10:
       else
11:
         Print "Fault detected!"
12:
13:
                              ▶ Run Error Isolation Procedure.
14:
       end if
15:
      end procedure
```

Figure 11 describes the above algorithm through an example. Consider the cascaded PPRG-based design in Figure 11a. If the design is fault free then applying "000" (a_0) as the primary input produces a_3 as a desired output. However, if the design is considered as fault suspicious, the Error Detection procedure will be performed. According to above mentioned procedure, the Design_Length, F_1 and F_2 are equal to five, one and one, respectively. First, output of the design is compared with the desired output which can be obtained using

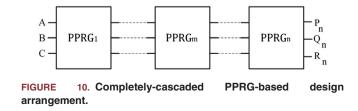


TABLE 6. Stuck-at Fault Mapping for the PPRG Gate.

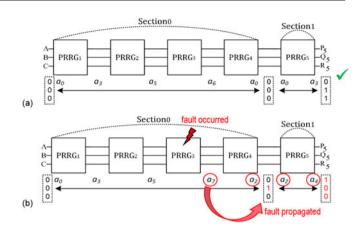
	nary put	Level 1 Output	Level 2 Output	Level 3 Output	Level 4 Output	Max Level
000	(a_0)	a_3	a_5	a_6	a_0	4
001	(a_1)	a_1				1
002	(a ₂)	a_4	a ₇	a_2		3
003	(a ₃)	a_5	a_6	a_0	a_3	4
004	(a ₄)	a ₇	a_2	a_4		3
005	(a ₅)	a ₆	a_0	<i>a</i> ₃	a_5	4
006	(a_6)	a_0	a_3	a_5	a_6	4
007	(a ₇)	a_2	a_4	a ₇		3

Test_Array which is a $1 \times Design_Length$ matrix that is equal to one of the rows of the select matrix. If they are equal then the design is fault free; otherwise, a fault is detected and Error Isolation procedure will be run. In this procedure, all sections are searched in order to find the faulty section by using the reversibility attribute of PPRGs. Then, the faulty PPRG can be detected in the isolated section via utilizing the parity-preserving feature of PPRG. Figures 11a and 11b show the fault free and faulty circuits, respectively. The required error detection and isolation steps are readily demonstrated in Figure 11c.

Procedure: Error Isolation for $i \leftarrow 0$; $i < F_1$; $i \leftarrow i + 1$ do 1: 2: \triangleright repeat this function F_1 times 3: **if** $Output(section[i]) \neq Main_{input}$ **then** 4: Print "Fault detected in section[i]!" 5: **goto** 28. end if 6: 7: end for \triangleright No error detected in F_1 sections. 8: Print "Fault detected in section[F_1]!" \triangleright Section F_1 is the last section in the design. 9: 10: **goto** 35. Check Section[i] for Fault Isolation operation: 11: 12: **for** $k \leftarrow 0$; $k < Length(Test_Array)$; $k \leftarrow k + 1$ **do** 13: **if** $Parity(PPRG[k]) \neq Parity(Primary_{input})$ **then** Print "Faulty PPRG detected!" 14: **Break** 15: end if 16: 17: end for Check Section[F_1] for Fault Isolation operation: 18: for $k \leftarrow 0$; $k < F_2$; $k \leftarrow k + 1$ do 19: **if** $Parity(PPRG[k]) \neq Parity(Primary_{input})$ **then** 20: Print "Faulty PPRG detected!" 21: **Break** 22: 23. end if end for 24: end procedure 25:

B. PARTIALLY-CASCADED ARRANGEMENT

In this PPRG-based circuit design, there are various connections between input and output terminals of the PPRGs, which might result in a design that is not completely-cascaded. Additionally, some of the outputs of the PPRGs might be unused in the structure of the design, which are called Garbage (G) outputs.



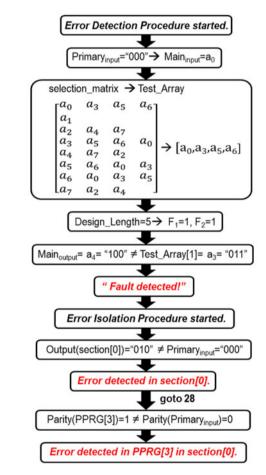


FIGURE 11. Cascaded PPRG-based design, (a) fault-free design, (b) faulty design, and (c) error detection and isolation steps.

In order to make the fault detection and isolation algorithm proposed for the completely-cascaded arrangement applicable for partially-cascaded PPRG-based designs, MUXs, and interconnections are added to the structure of the design. The primary design with n PPRGs is combined with $3 \times (n-1)$ MUXs which are placed at the input terminals of the PPRGs, as shown in Figure 12. Moreover, a fault flag is provided as the MUX selector control signal to determine the operating mode of the design. If a fault occurs, the fault flag will be set to "1" and MUXs will convert the partially-cascaded PPRG design to

(c)

FIGURE 12. Partially-cascaded PPRG-based design arrangement.

the completely-cascaded arrangement. Then the error detection and isolation procedure will be run. Otherwise, fault flag is equal to "0" and the design operates in regular mode. This topology is affected by overhead from MUXs which can be alleviated by using an ultra-dense MUX design which is proposed in [40].

Example: Consider Figure 13a realizing a partially-cascaded PPRG-based design which functions $F_7 = \overline{ABC}$ $+\overline{ABC} + AB\overline{C}$. Assigning *Primary*_{in} = "011" then the desirable out is "011". The fault-free state is shown in Figure 13b in which fault_flag="0". The blue-colored lines shows the interconnections which provides the desired output. Now assume that the circuit is faulty and the obtained output is

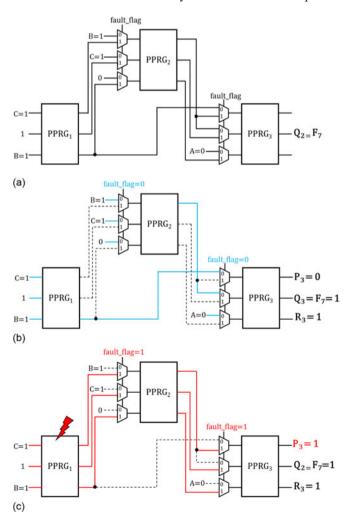


FIGURE 13. (a) Partially-cascaded PPRG-based design, (b) fault-free operating mode which set fault_flag to 0, and (c) faulty operating mode which means fault_flag equals 1, so the circuit converted to a completely-cascaded arrangement.

equal to "111". Therefore, fault_flag="1" will be equal to "1" as a result of which the design will be converted to a completely-cascaded arrangement. Interconnections in fault detection operating mode are shown by red lines in Figure 13c. Finally, the proposed fault detection and isolation algorithm will be executed to distinguish the faulty PPRG.

V. CONCLUSION

Energy-sparing gate designs using emerging technologies allow extensions in beneficial directions by embracing reversibility and the inclusion of inherent fault observability. In the case of QCA, the availability of appropriate clocking paradigms enables the utilization of parity-preserving gates. The feasibility of such features lies not only in the design of the gate itself, but also an efficient corresponding bit-level selfchecking methodology. Herein, PRRG focuses first on achieving high Boolean expressiveness for compact logic realizations. This results in significant improvements in the design of standard logic functions having three variables reducing average gate count by at least 10.7 percent compared to previous designs. The utility of PPRG is further enhanced by its resilient cascadability. This is evident in the realization of a fault-tolerant reversible one-bit full adder using 171 QCA cells occupying only 0.19 μ m² area. Beyond previous works, we also emphasize the beneficial role of utilizing PPRGs to yield larger QCA robust reversible circuits. While the fault detection and isolation methodology based on progressive suspect reduction as developed herein, provides a concise solution for configurable resiliency, other future extensions such as syndrome-based error correction could be investigated.

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