

Reg.No.:

Name:



VIT

Vellore Institute of Technology

(Established in the University order number 1 of 1984)

## Continuous Assessment Test (CAT-I) – September 2023

|           |                            |                 |                           |
|-----------|----------------------------|-----------------|---------------------------|
| Programme | B.TECH                     | Semester        | Fall 2023-24              |
| Course    | Probability and Statistics | Code            | BMAT202L                  |
| Faculty   | Dr. G Y Mythili            | Slot & Class ID | F2+TF2<br>CH2023240101042 |
| Time      | 90 minutes                 | Max. Marks      | 50                        |

Q. No.

Answer All Questions (5 X 10 = 50 Marks)

1.

Calculate the first four moments about the mean and analyse the distribution.

|   |   |   |    |    |    |    |    |   |   |
|---|---|---|----|----|----|----|----|---|---|
| X | 0 | 1 | 2  | 3  | 4  | 5  | 6  | 7 | 8 |
| f | 1 | 8 | 28 | 56 | 70 | 56 | 28 | 8 | 1 |

2.

The prices of 2 commodities over 10 weeks are given below. Find out which price shows less variation.

|   |     |     |     |     |     |     |     |     |     |     |
|---|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| A | 54  | 55  | 53  | 56  | 52  | 52  | 58  | 49  | 50  | 51  |
| B | 108 | 107 | 105 | 106 | 105 | 103 | 102 | 104 | 104 | 101 |

3.

Given the following table.

|      |      |     |     |   |     |      |     |
|------|------|-----|-----|---|-----|------|-----|
| X    | -3   | -2  | -1  | 0 | 1   | 2    | 3   |
| p(x) | 0.05 | 0.1 | 0.3 | 0 | 0.3 | 0.15 | 0.1 |

Compute (i)  $E(X)$  (ii)  $E(2X \pm 3)$  (iii)  $P(X < 2)$  (iv)  $P(-2 < X < 2)$   
(v)  $V(X)$  (vi)  $V(2X \pm 3)$ 

4.

(i) Find the rank correlation coefficient from the following data.

|           |   |   |   |   |   |   |   |   |   |
|-----------|---|---|---|---|---|---|---|---|---|
| Rank in X | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| Rank in Y | 4 | 3 | 8 | 1 | 2 | 9 | 6 | 5 | 7 |

(ii) For a trivariate distribution, the following correlation coefficient were obtained  
 $r_{12} = 0.57, r_{13} = 0.65, r_{23} = 0.41$ . Find the partial correlation coefficient  $r_{23.1}$  and multiple correlation coefficient  $R_{2.13}$ .

5.

A research investigator collected data on savings and investment from 16 house-holds. Savings showed a mean of Rs. 6565.00 and a variance of Rs. 250.00. As against this, mean investment was found at Rs.4525.00 and variance as Rs.520.00. If the coefficient of correlation between savings and investment is 0.67, find the most approximate value of savings against an investment of Rs.9000 and that of investment against a savings of Rs.5600.

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CHENNAI

Reg. Number: 22BC1351

**Continuous Assessment Test (CAT) - I - February 2024**

|                            |   |   |              |   |                                    |
|----------------------------|---|---|--------------|---|------------------------------------|
| Programme                  | : | B. Tech.                                | Semester     | : | Winter                             |
| Course Code & Course Title | : | BMAT202L (Probability and Statistics)   | Slot         | : | C1+TC1                             |
| Faculty                    | : | Dr Prabhakar V.<br>Dr Harshavarthini S. | Class Number | : | CH2023240500894<br>CH2023240500895 |
| Duration                   | : | 90 Minutes                              | Max. Mark    | : | 50                                 |

**General Instructions:**

- Write only your registration number on the question paper in the box provided and do not write other information.
- Only non-programmable calculator without storage is permitted.

**Answer all questions.**

| Q. No           | Sub Sec. | Description  | Marks           |           |           |           |           |           |           |                |           |    |    |    |    |    |    |   |     |
|-----------------|----------|--|-----------------|-----------|-----------|-----------|-----------|-----------|-----------|----------------|-----------|----|----|----|----|----|----|---|-----|
| 1.              |          | <p>Calculate the <u>Median</u> and <u>Mode</u> of the data given in the following table.</p> <table><tr><td>Class interval</td><td>9.5-14.5</td><td>14.5-19.5</td><td>19.5-24.5</td><td>24.5-29.5</td><td>29.5-34.5</td><td>34.5-39.5</td><td>39.5-44.5</td></tr><tr><td>Frequency</td><td>10</td><td>15</td><td>17</td><td>25</td><td>18</td><td>12</td><td>8</td></tr></table>   | Class interval  | 9.5-14.5  | 14.5-19.5 | 19.5-24.5 | 24.5-29.5 | 29.5-34.5 | 34.5-39.5 | 39.5-44.5      | Frequency | 10 | 15 | 17 | 25 | 18 | 12 | 8 | 5+5 |
| Class interval  | 9.5-14.5 | 14.5-19.5  | 19.5-24.5       | 24.5-29.5 | 29.5-34.5 | 34.5-39.5 | 39.5-44.5 |           |           |                |           |    |    |    |    |    |    |   |     |
| Frequency       | 10       | 15   | 17              | 25        | 18        | 12        | 8         |           |           |                |           |    |    |    |    |    |    |   |     |
| 2.              |          | <p>The weekly salaries of a group of employees are given in the following table. Find the <u>mean</u> and <u>standard deviation</u> of the salaries.</p> <table><tr><td>Salary (In Rs.)</td><td>75</td><td>80</td><td>85</td><td>90</td><td>95</td><td>100</td></tr><tr><td>No. of persons</td><td>3</td><td>7</td><td>18</td><td>12</td><td>6</td><td>4</td></tr></table>   | Salary (In Rs.) | 75        | 80        | 85        | 90        | 95        | 100       | No. of persons | 3         | 7  | 18 | 12 | 6  | 4  | 10 |   |     |
| Salary (In Rs.) | 75       | 80   | 85              | 90        | 95        | 100       |           |           |           |                |           |    |    |    |    |    |    |   |     |
| No. of persons  | 3        | 7  | 18              | 12        | 6         | 4         |           |           |           |                |           |    |    |    |    |    |    |   |     |
| 3.              |          | <p>For the random variables <math>X</math> and <math>Y</math>, we define</p> $p(x, y) = P(X = x, Y = y) = \begin{cases} k(x + y), & \text{for } x = 1, 2, 3, 4 \text{ and } y = 1, 2, 3 \\ 0, & \text{Otherwise} \end{cases}$ <p>Find</p> <ul style="list-style-type: none"><li>(i) the value(s) of <math>k</math>, such that <math>p(x, y)</math> will be a joint PMF. [2]</li><li>(ii) both the marginal PMFs. [3]</li><li>(iii) both the conditional distributions. [3]</li><li>(iv) <math>P(X + Y &lt; 4)</math> [2]</li></ul>                         | 10              |           |           |           |           |           |           |                |           |    |    |    |    |    |    |   |     |
| 4.              |          | <p>The joint probability density function (PDF) of the random variables <math>X</math> and <math>Y</math> is defined as:</p> $f(x, y) = \begin{cases} k(6 - x - y), & \text{for } 0 < x < 2 \text{ and } 2 < y < 4 \\ 0, & \text{Otherwise} \end{cases}$ <p>Find</p> <ul style="list-style-type: none"><li>(i) the value(s) of <math>k</math>, such that <math>f(x, y)</math> will be a joint PDF. [2]</li><li>(ii) Justify whether <math>X</math> and <math>Y</math> are independent or not. [5]</li><li>(iii) <math>P(X + Y &lt; 3)</math> [3]</li></ul> | 10              |           |           |           |           |           |           |                |           |    |    |    |    |    |    |   |     |

|    |     |   |     |
|----|-----|---|-----|
| 5. | (a) | Suppose $X$ is a discrete random variable and has the moment generating function (MGF) $M_X(t) = \frac{1}{5}e^t + \frac{2}{5}e^{3t} + \frac{2}{5}e^{6t}$ . Hence find the corresponding probability mass function (PMF) of $X$ . And also find the $E(X)$ by using the given MGF. = (11, 1) | 5   |
|    | (b) | Suppose $Y$ is random variable with the probability density function $f_Y(y) = \begin{cases} \frac{1}{3}, & -1 < y < 2 \\ 0, & \text{otherwise} \end{cases}$ . Find the cumulative distribution function (CDF) and the MGF.   | 2+3 |

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CHENNAI

Reg. Number:

22BCE1335

**Continuous Assessment Test (CAT) - I - February 2024**

|                            |   |   |              |   |                                    |
|----------------------------|---|---|--------------|---|------------------------------------|
| Programme                  | : | B. Tech.                                | Semester     | : | Winter                             |
| Course Code & Course Title | : | BMAT202L (Probability and Statistics)   | Slot         | : | C2+TC2                             |
| Faculty                    | : | Prof. Vignesh R.<br>Dr Saroj Kumar Dash | Class Number | : | CH2023240500898<br>CH2023240503420 |
| Duration                   | : | 90 Minutes                              | Max. Mark    | : | 50                                 |

**General Instructions:**

- Write only your registration number on the question paper in the box provided and do not write other information.
- Only non-programmable calculator without storage is permitted.

**Answer all questions.**

| Answer all questions. |          |   |   |   |    |    |       |   |       |
|-----------------------|----------|---|---|---|----|----|-------|---|-------|
| Q. No                 | Sub Sec. | Description   |   |   |    |    | Marks |   |       |
| 1.                    | (a)      | A frequency table with missing data is given here. Find these missing data, so that the arithmetic mean will be 1.46. |   |   |    |    | 5     |   |       |
|                       |          | 0   | 1 | 2 | 3  | 4  |       | 5 | Total |
|                       |          | 46  | ? | ? | 25 | 10 |       | 5 | 200   |

|     |  |   |       |       |       |       |       |       |       |       |   |
|-----|--|---|-------|-------|-------|-------|-------|-------|-------|-------|---|
|     |  | Calculate the arithmetic mean for the following data: |       |       |       |       |       |       |       |       |   |
| (b) |  | Class   | 10-19 | 20-29 | 30-39 | 40-49 | 50-59 | 60-69 | 70-79 | 80-89 |   |
|     |  | Freque<br>ncy   | 2     | 4     | 9     | 11    | 12    | 6     | 4     | 2     | 5 |

2.

Find the standard deviation for the following data giving wages of 220 persons.

|                |       |       |        |         |         |         |         |         |
|----------------|-------|-------|--------|---------|---------|---------|---------|---------|
| $x$            | 70-80 | 80-90 | 90-100 | 100-110 | 110-120 | 120-130 | 130-140 | 140-150 |
| No. of persons | 12    | 18    | 35     | 42      | 50      | 45      | 20      | 8       |

10

|    |  |  |    |
|----|--|--|----|
| 3. |  | A random variable $X$ has the following probability distribution:<br>$f_X(x) = \begin{cases} k^2 x(x-1), & x \in (1, 2) \\ 0, & \text{otherwise} \end{cases}$ <p>Find</p> <p>(i) the value(s) of <math>k</math>, such that the probability distribution will be the property density function (PDF). [3]</p> <p>(ii) <math>P(X \leq 6)</math>. [3]</p> <p>(iii) The minimum value of <math>b</math> such that <math>P(X \leq b) &gt; \frac{1}{2}</math>. [4]</p> | 10 |
|----|--|--|----|

|    |  |    |
|----|--|----|
| 4. | <p>Let <math>X</math> and <math>Y</math> be two random variables with the joint probability distribution:</p> $f(x, y) = \begin{cases} k(x + y - 3xy^2), & \text{for } 0 < x < 1 \text{ and } 0 < y < 1 \\ 0, & \text{Otherwise} \end{cases}$ <p>Hence find:</p> <ul style="list-style-type: none"> <li>(i) the value(s) of <math>k</math> such that the <math>f(x, y)</math> will be a joint PDF. [2]</li> <li>(ii) both the marginal PDFs. [3]</li> <li>(iii) both the conditional density functions. [3]</li> <li>(iv) justify whether <math>X</math> and <math>Y</math> are independent or not. [2]</li> </ul> | 10 |
| 5. | (a) Let $X$ be a random variable with moment generating function (MGF) $M_X(t) = (1/2)(1 + e^t)$ . Derive the variance of $X$ .  | 5  |
|    | (b) Let $Y$ be a random variable with the probabilities defined as: $P(Y = 2) = \frac{1}{7}$ , $P(Y = 3) = \frac{3}{7}$ , $P(Y = 5) = \frac{2}{7}$ , $P(Y = 8) = \frac{1}{7}$ , and $P(Y = y) = 0$ for $y \in (-\infty, \infty) - \{2, 3, 5, 8\}$ . Find the MGF of $Y$ . And hence find the $E(Y)$ by using this MGF.   | 5  |

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**VIT**Vellore Institute of Technology  
CHENNAI

22BPS110

**Continuous Assessment Test I - August 2024**

|   |   |
|---|---|
| Programme : B Tech  | Semester : Fall 2024-25   |
| Course : Probability and Statistics   | Code : BMAT202L   |
| Faculty : Dr. Amit Kumar Rahul<br>Dr. B. Jaganathan<br>Dr. S. Devi Yamini<br>Dr. Sethukumarasamy K<br>Dr. Manimaran J<br>Dr. Dhivya M | Slot : E1+TE1   |
| Time : 90 Minutes   | Class ID : CH2024250102209<br>CH2024250102210<br>CH2024250102211<br>CH2024250102212<br>CH2024250102213<br>CH2024250102214 |
|   | Max. Marks : 50 Marks   |

1. Find the mean, median, third quartile of the following distribution:

[10]

| Class     | 11-15 | 16-20 | 21-25 | 26-30 | 31-35 | 36-40 | 41-45 | 46-50 | 51-55 |
|-----------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| Frequency | 8     | 15    | 39    | 47    | 52    | 41    | 28    | 16    | 4     |

2. An incomplete distribution is given below:

[10]

| Class Interval | 0 - 10 | 10 - 20 | 20 - 30 | 30 - 40 | 40 - 50 | 50 - 60 | 60 - 70 |
|----------------|--------|---------|---------|---------|---------|---------|---------|
| Frequency      | 10     | 20      | ?       | 40      | ?       | 25      | 15      |

the median is 35, and the total frequency is 170. Find the missing frequencies.

3. (a) The mileage (in thousands of miles) obtained by car owners using a certain type of tire is represented by a random variable with the following probability density function (PDF): (5 Marks)

[10]

$$f(x) = \frac{1}{20} e^{-x/20}, \text{ for } x > 0$$

$$= 0, \text{ for } x \leq 0$$

Find the probabilities that one of these tyres will-last

- (i) at most 10,000 miles. (1 Mark)
- (ii) anywhere from 16,000 to 24,000 miles. (2 Marks)
- (iii) at least 30,000 miles. (1 Mark)

(b) The joint density function of random variables  $X$  and  $Y$  is given by:

$$f(x, y) = \begin{cases} e^{-x-y} & ; x \geq 0, y \geq 0 \\ 0 & ; \text{elsewhere} \end{cases}$$

find  $P(X > 1)$ ,  $E(X)$ ,  $E(Y)$ ,  $E(XY)$ ,  $E(X + Y)$  Check whether  $X$  and  $Y$  are independent or not? (5 Marks)



5. The applications for a post were interviewed by the personnel manager and the training manager.  $H$  was placed first by the personnel manager followed by  $F, D, B, I, C, J, G, A$  and  $E$  in that order. The training manager placed  $F$  first followed by  $D, H, I, C, B, A, J, E$  and  $G$  in that order. Calculate the value of Spearman's rank correlation coefficient. Interpret the value obtained. [10]
6. A security check at an airport has two express lines. Let  $X$  and  $Y$  denote the number of customers in the first and second line at any given time. The joint probability function of  $X$  and  $Y$  is summarized by the following table. [10]

| $X \backslash Y$ | 0   | 1    | 2     | 3     |
|------------------|-----|------|-------|-------|
| 0                | 0.1 | 0.2  | 0     | 0     |
| 1                | 0.2 | 0.25 | 0.05  | 0     |
| 2                | 0   | 0.05 | 0.05  | 0.025 |
| 3                | 0   | 0    | 0.025 | 0.05  |

- (i) Find the marginal function of  $X$  and  $Y$ . (2 Marks)  
 (ii) Find the probability that more than two customers are in line. (2 Marks)  
 (iii) Find  $P(|x - y| = 1)$ . (5 Marks)  
 (iv) Check whether  $X$  and  $Y$  independent? (1 Mark)