



Fundamentals of Deep Learning

Part 2: How a Neural Network Trains



Agenda

- Part 1: An Introduction to Deep Learning
- Part 2: How a Neural Network Trains
- Part 3: Convolutional Neural Networks
- Part 4: Data Augmentation and Deployment
- Part 5: Pre-Trained Models
- Part 6: Advanced Architectures

Recap of the Exercise

What just happened?

Loaded and visualized our data

Edited our data (reshaped, normalized, to categorical)

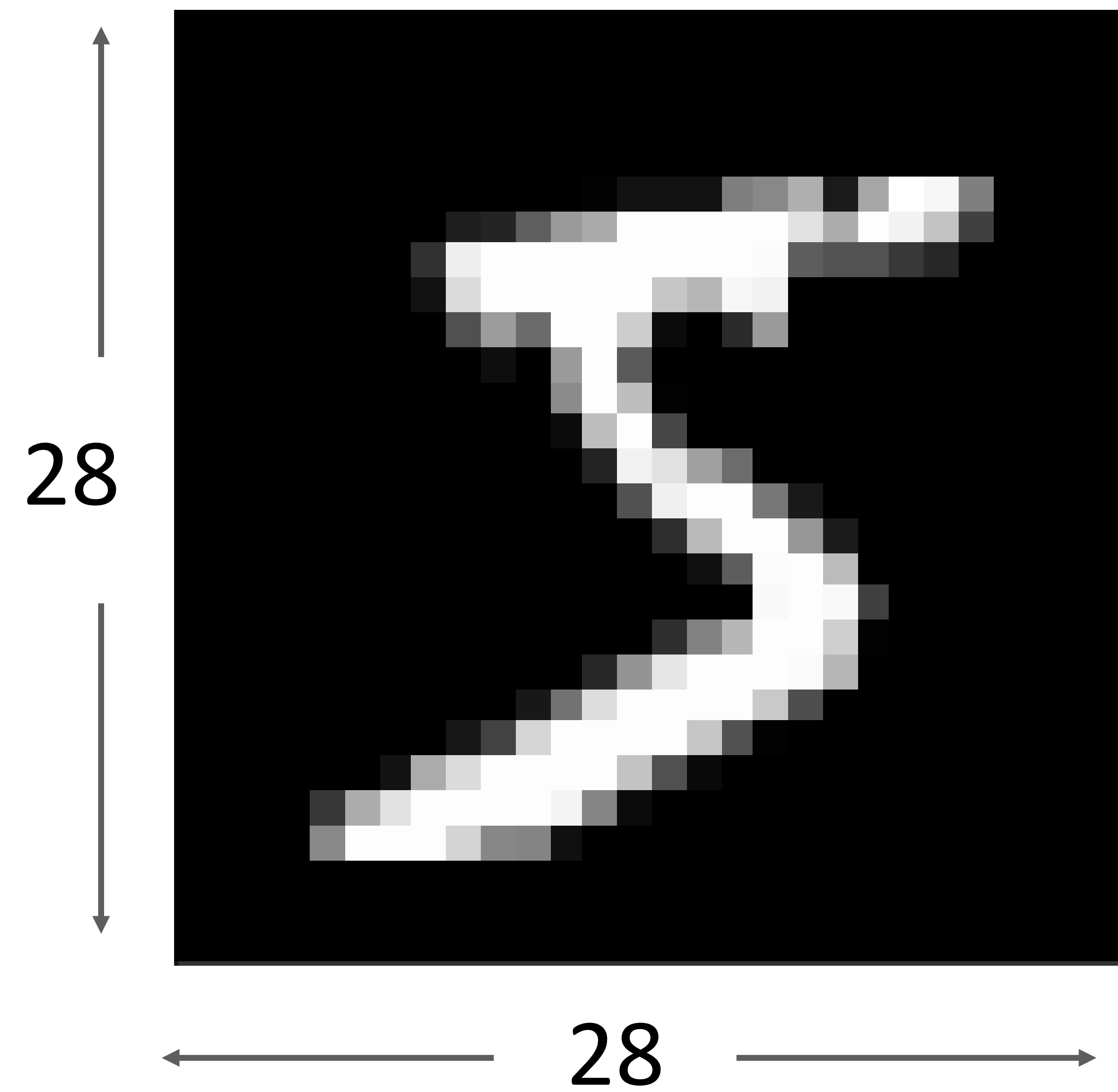
Created our model

Compiled our model

Trained the model on our data

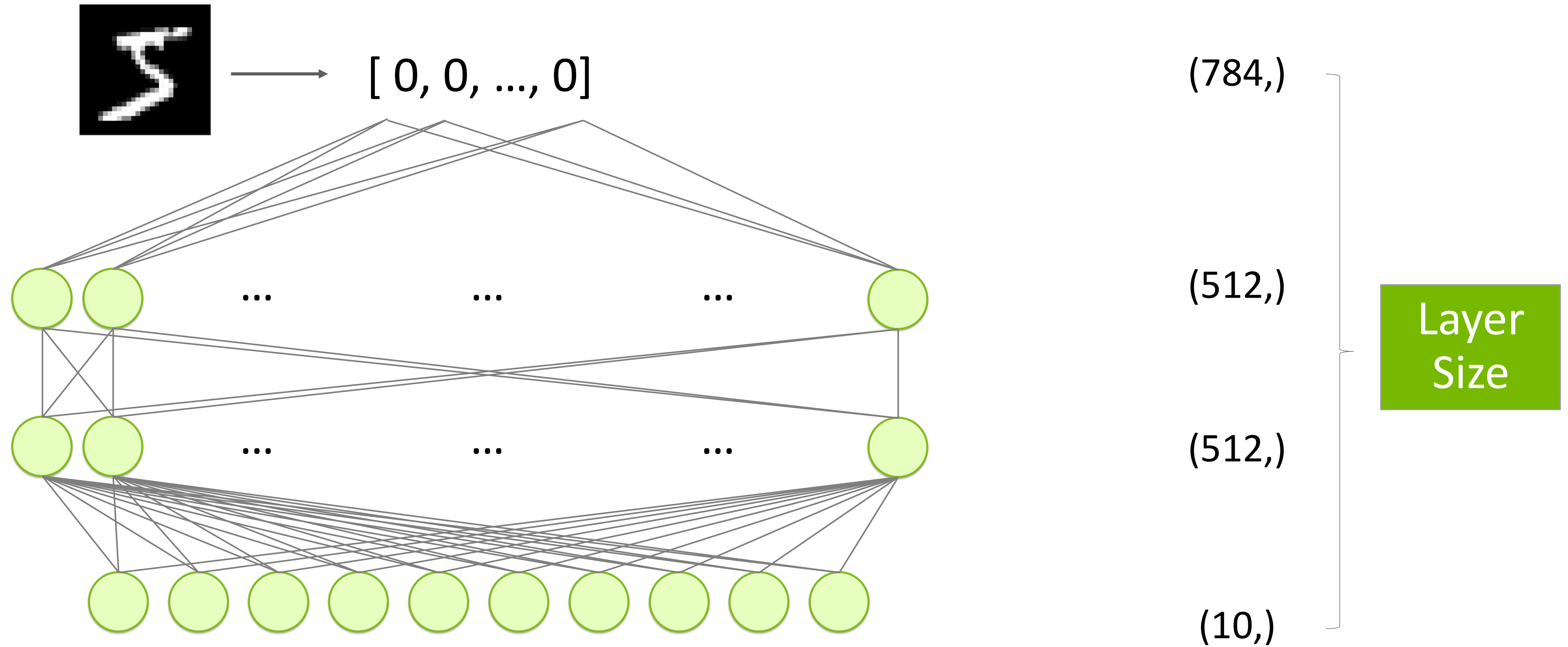
Data Preparation

Input as an Array



[0,0,0,24,75,184,185,78,32,55,0,0,0...]

An Untrained Model



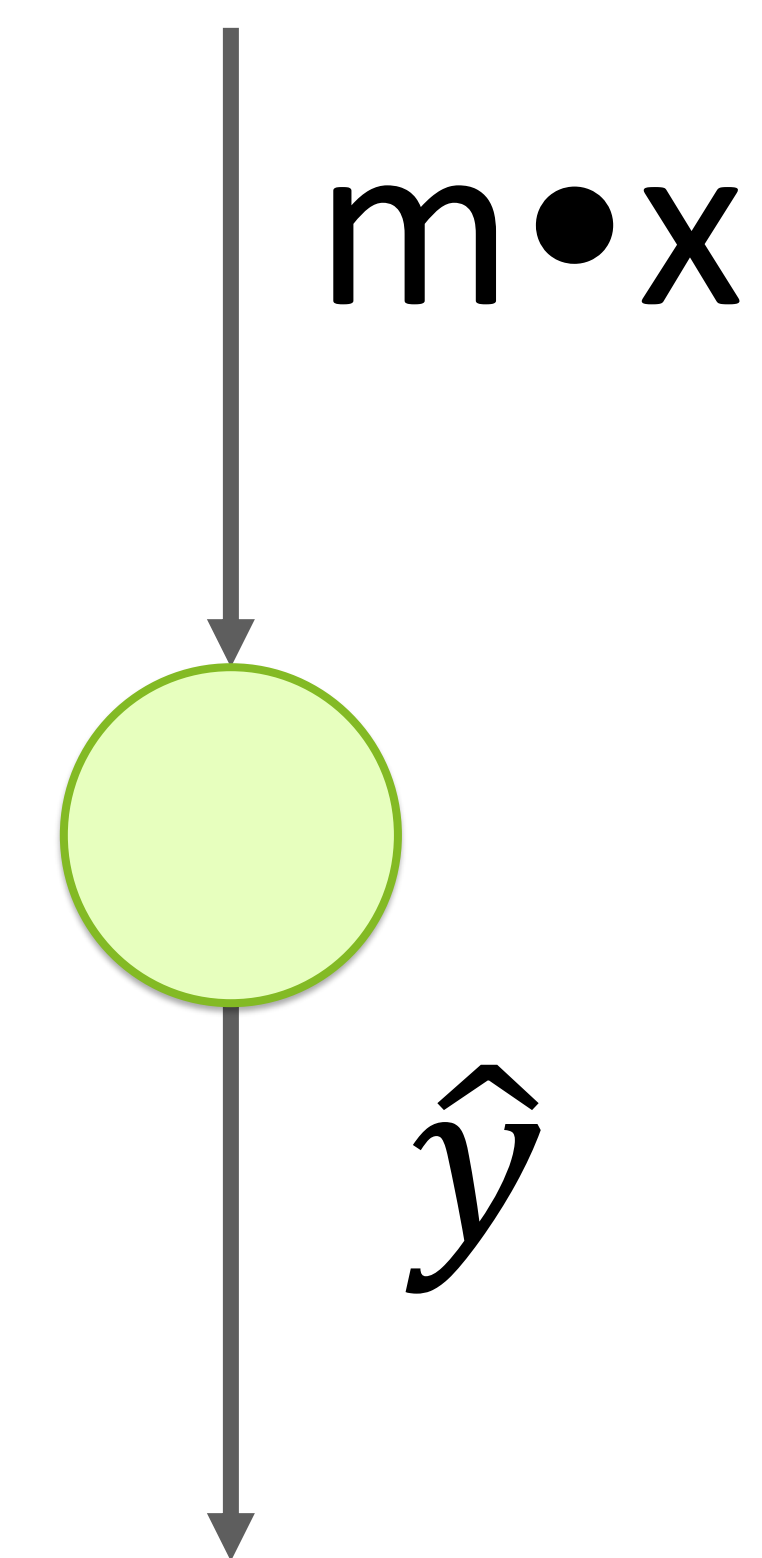
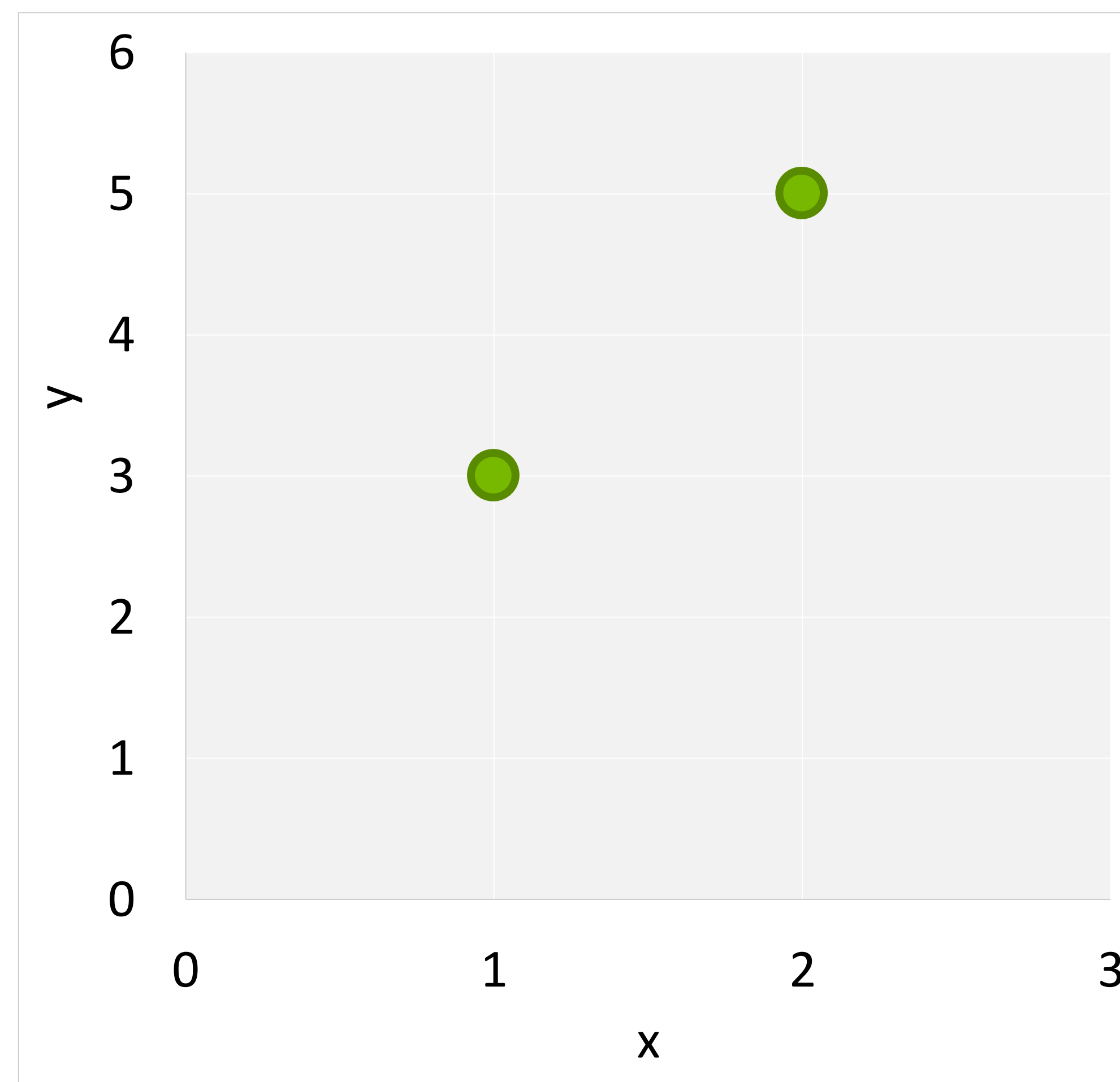


A Simpler Model

A Simpler Model

$$y = mx + b$$

x	y
1	3
2	5



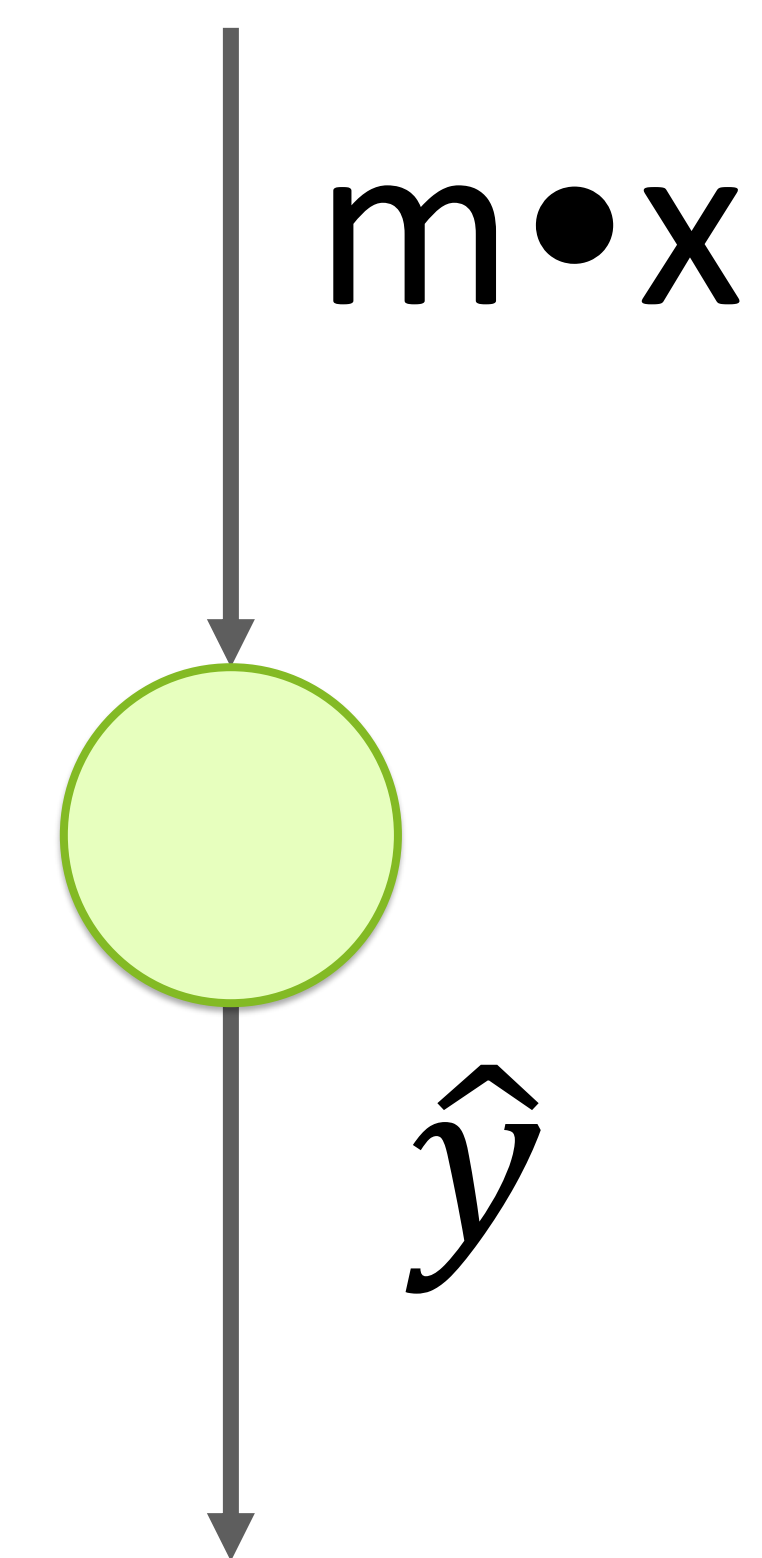
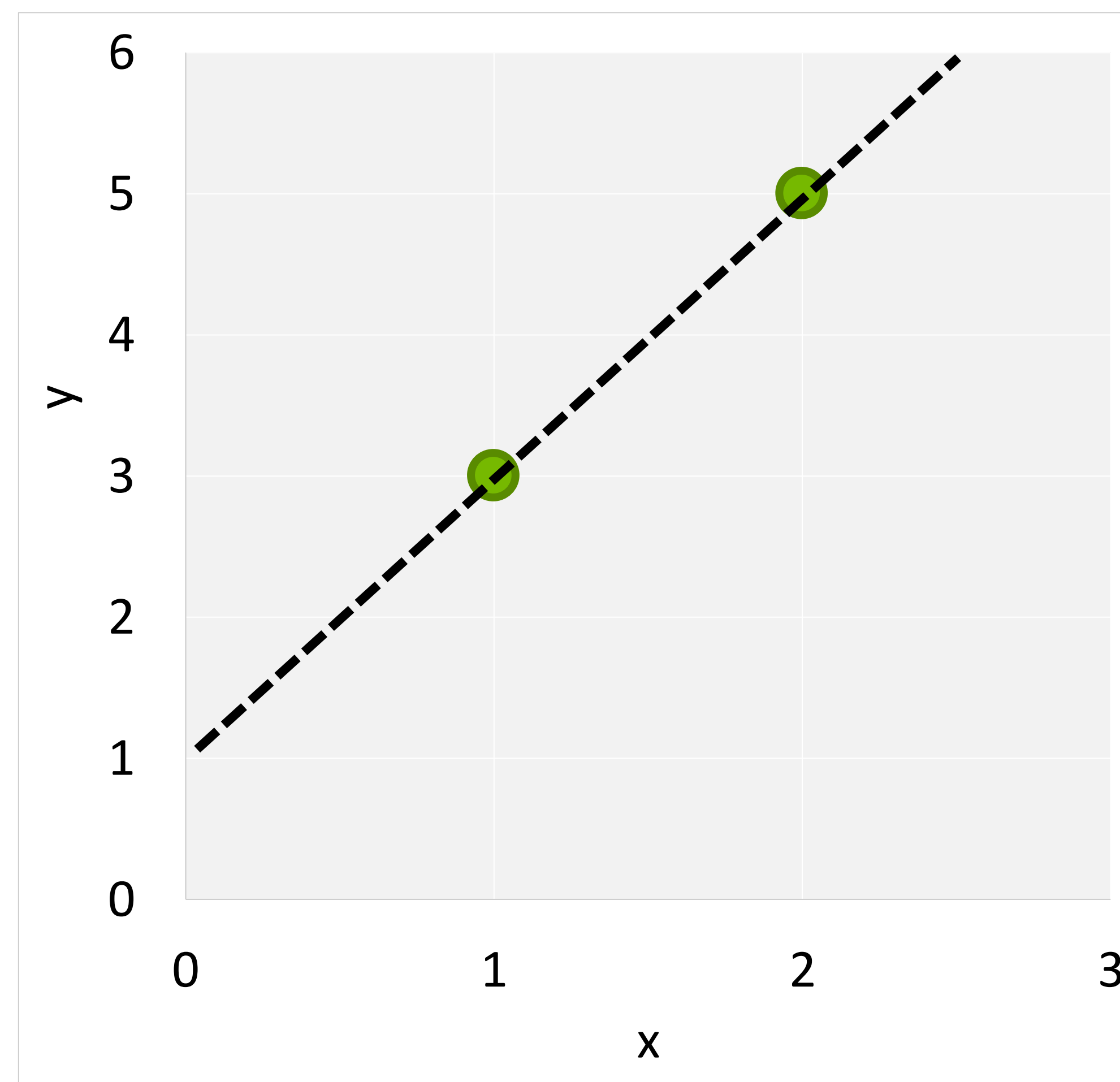
$$m = ?$$

$$b = ?$$

A Simpler Model

$$y = mx + b$$

x	y
1	3
2	5



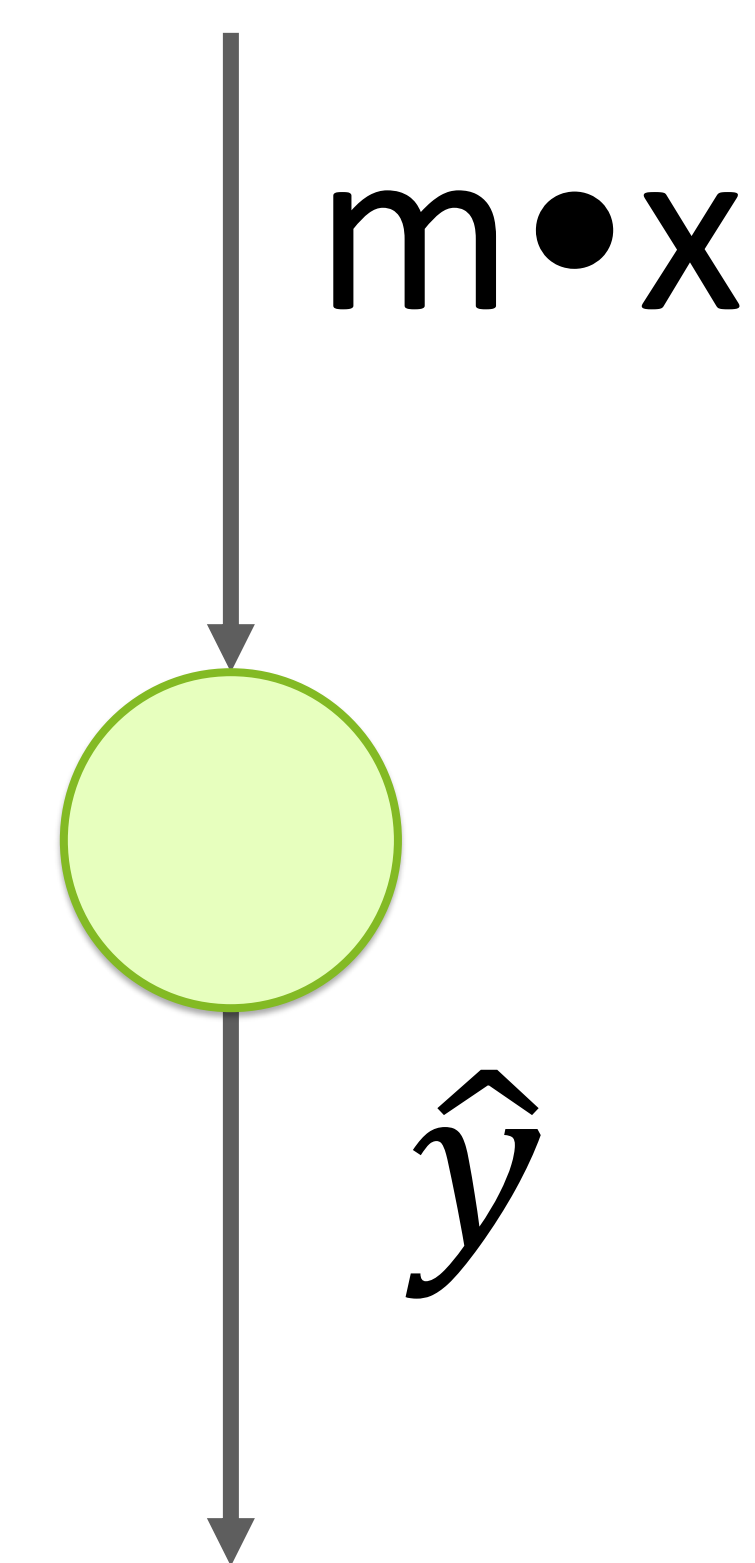
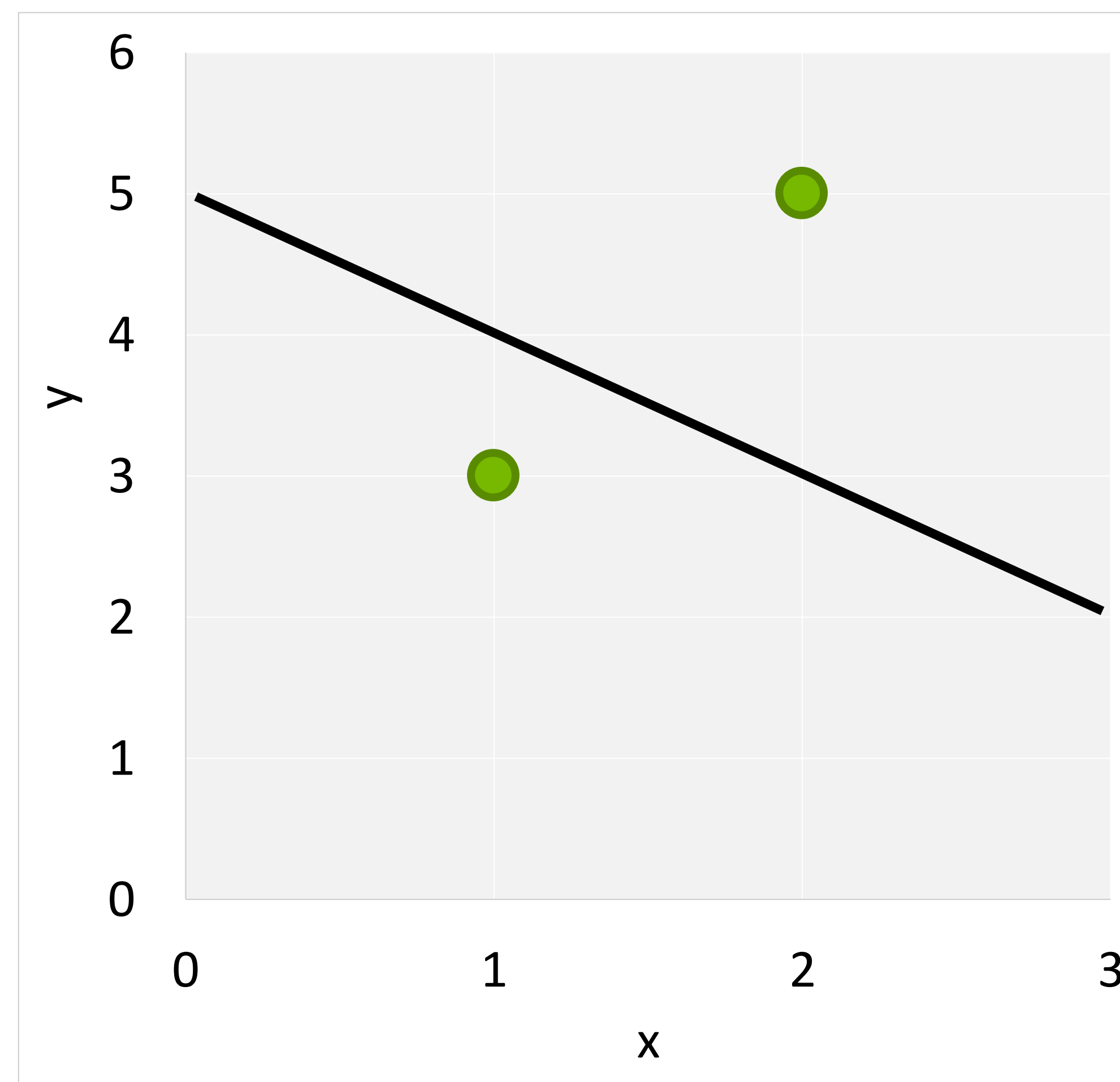
$$m = ?$$

$$b = ?$$

A Simpler Model

$$y = mx + b$$

x	y	\hat{y}
1	3	4
2	5	3



Start Random

$$m = -1$$

$$b = 5$$

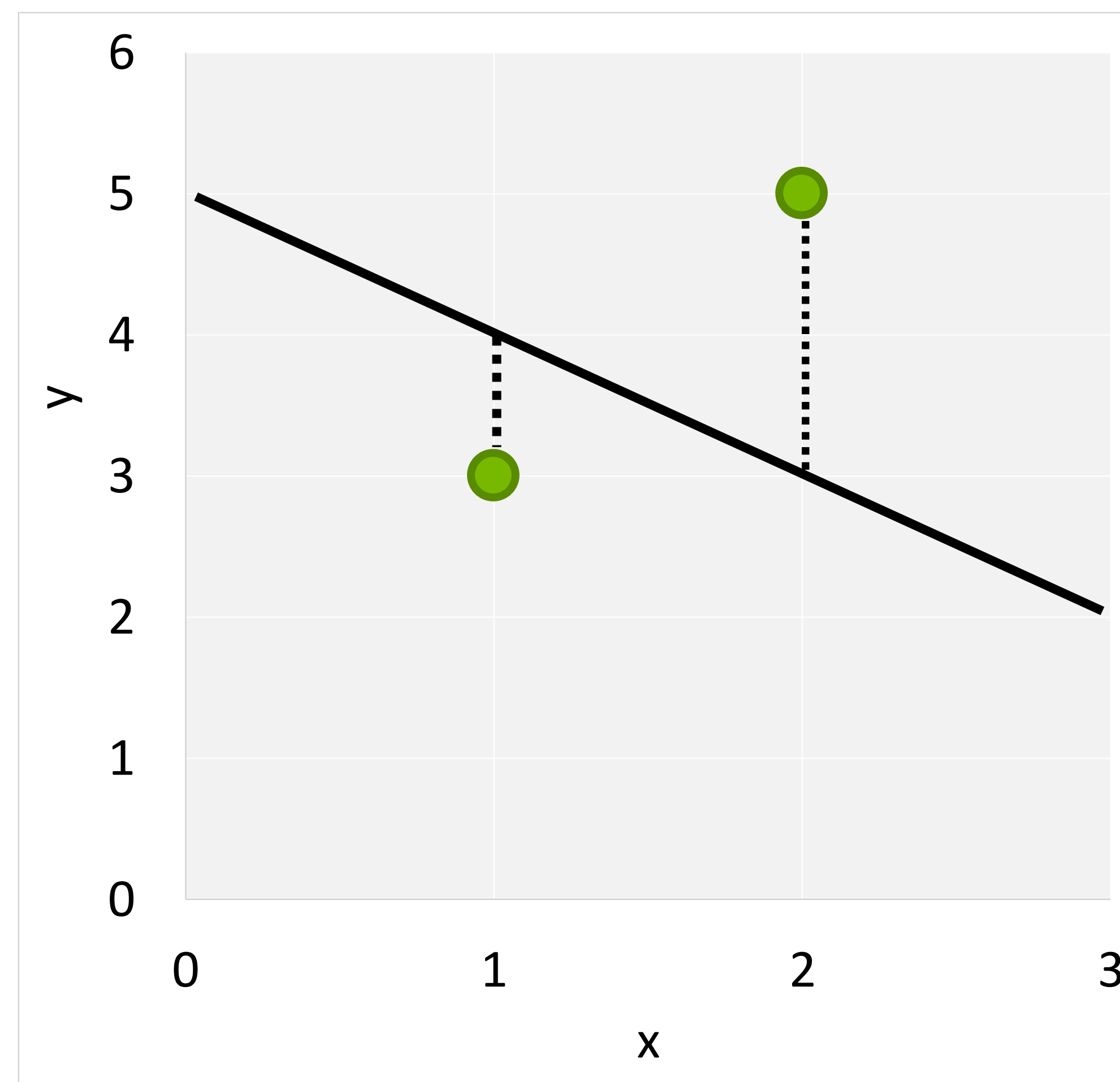
A Simpler Model

$$y = mx + b$$

x	y	\hat{y}	err^2
1	3	4	1
2	5	3	4

MSE = 2.5

RMSE = 1.6



$$MSE = \frac{1}{n} \sum_{i=1}^n (y_i - \hat{y}_i)^2$$

$$RMSE = \sqrt{\frac{1}{n} \sum_{i=1}^n (y_i - \hat{y}_i)^2}$$

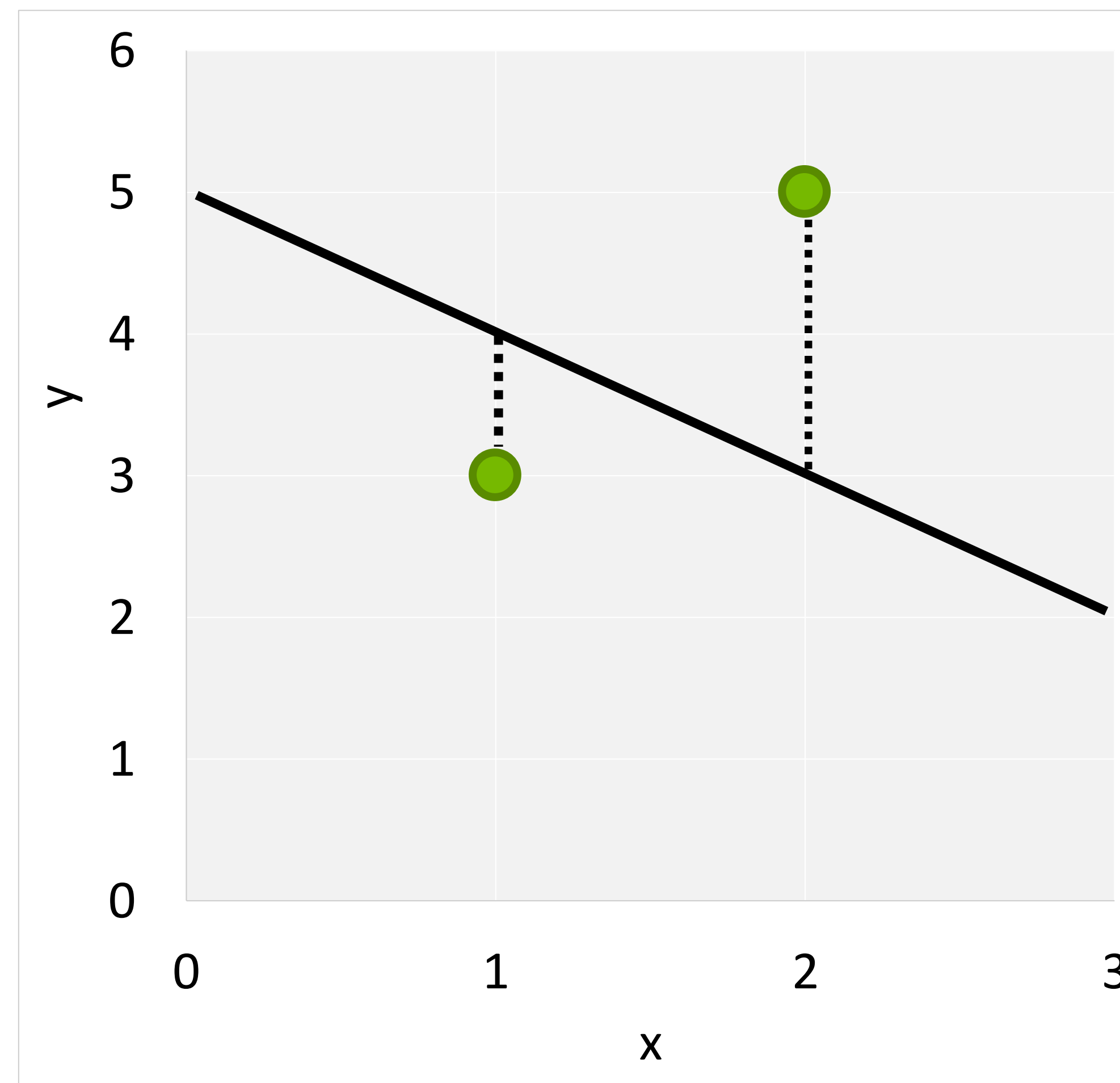
A Simpler Model

$$y = mx + b$$

x	y	\hat{y}	err^2
1	3	4	1
2	5	3	4

MSE = 2.5

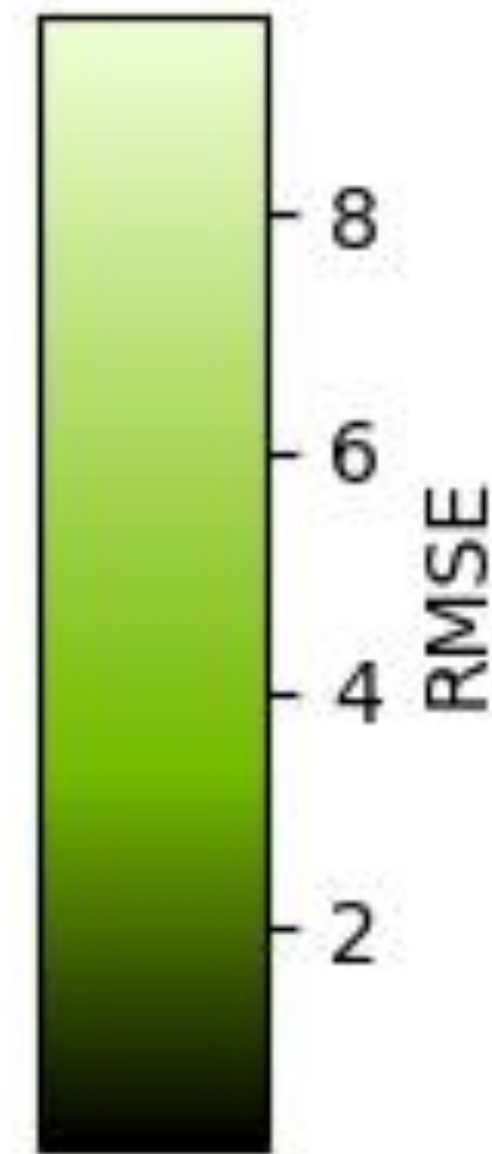
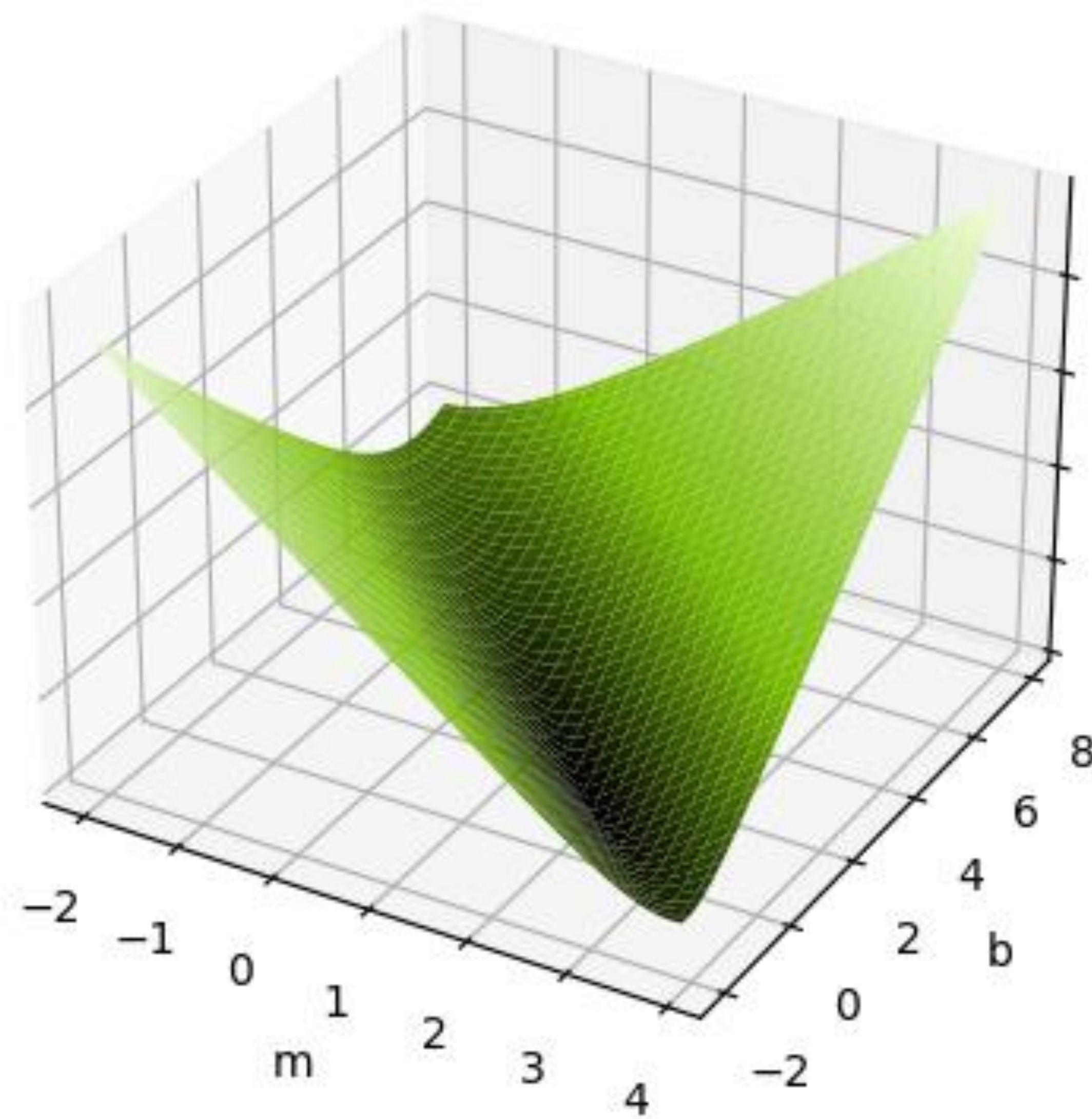
RMSE = 1.6



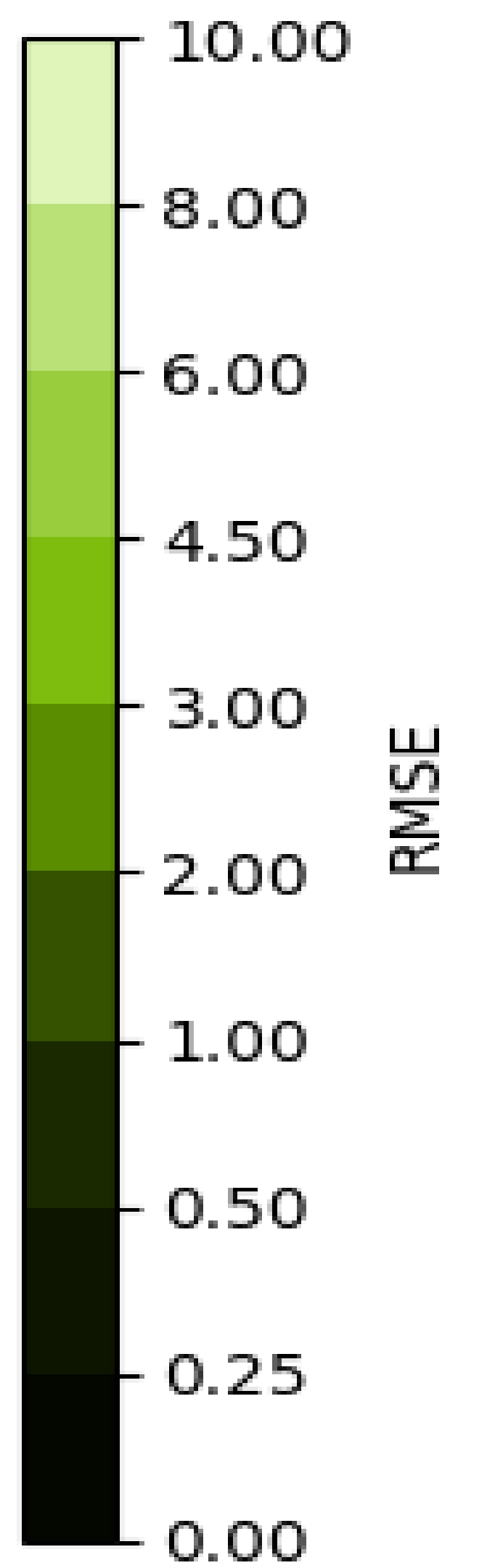
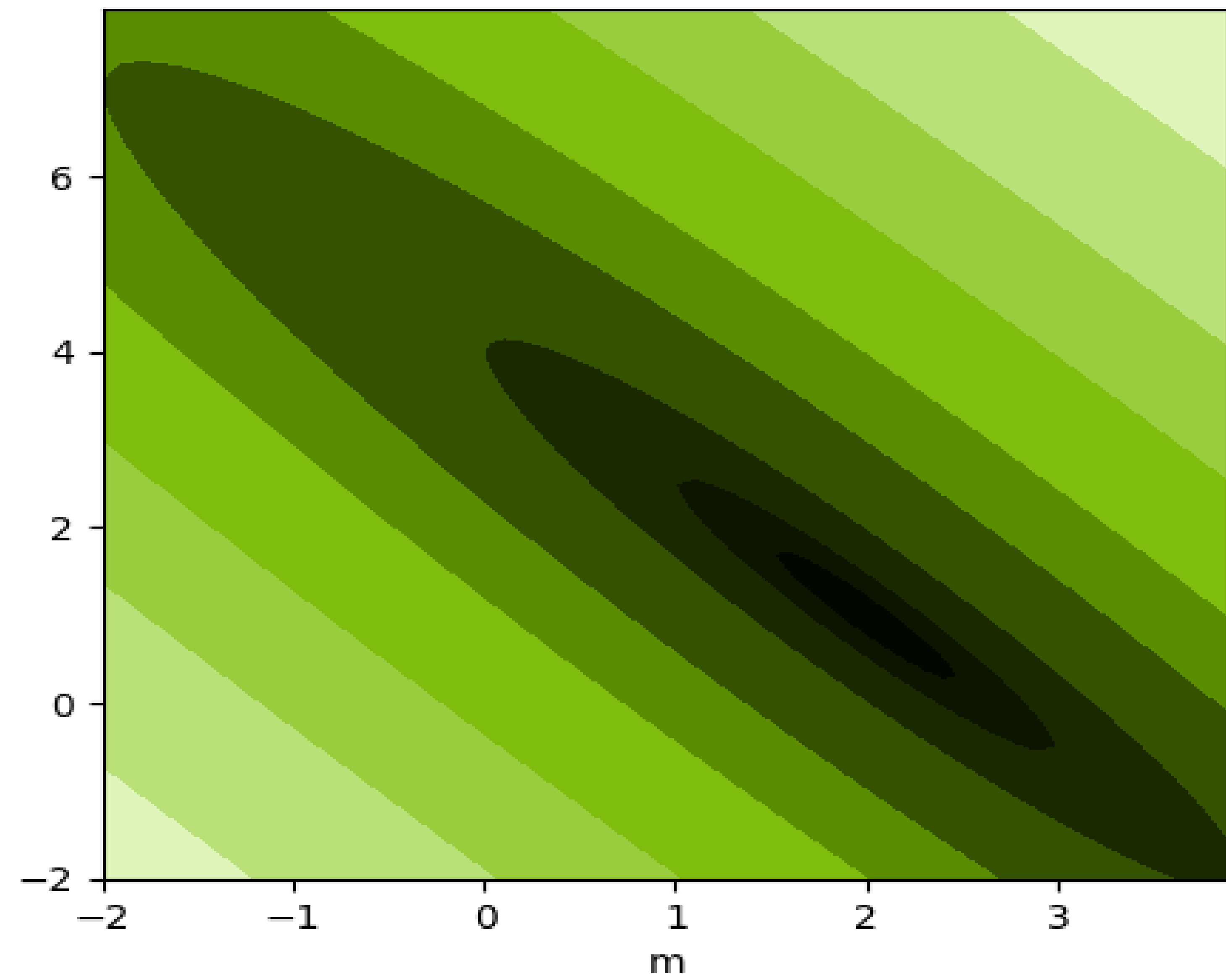
```
1 data = [(1, 3), (2, 5)]
2 m = -1
3 b = 5
4
5
6 def get_rmse(data, m, b):
7     """Calculates Mean Square Error"""
8     n = len(data)
9     squared_error = 0
10    for x, y in data:
11        # Find predicted y
12        y_hat = m*x+b
13        # Square difference between
14        # prediction and true value
15        squared_error += (
16            y - y_hat)**2
17        # Get average squared difference
18        mse = squared_error / n
19        # Square root for original units
20        return mse **.5
21
```

The Loss Curve

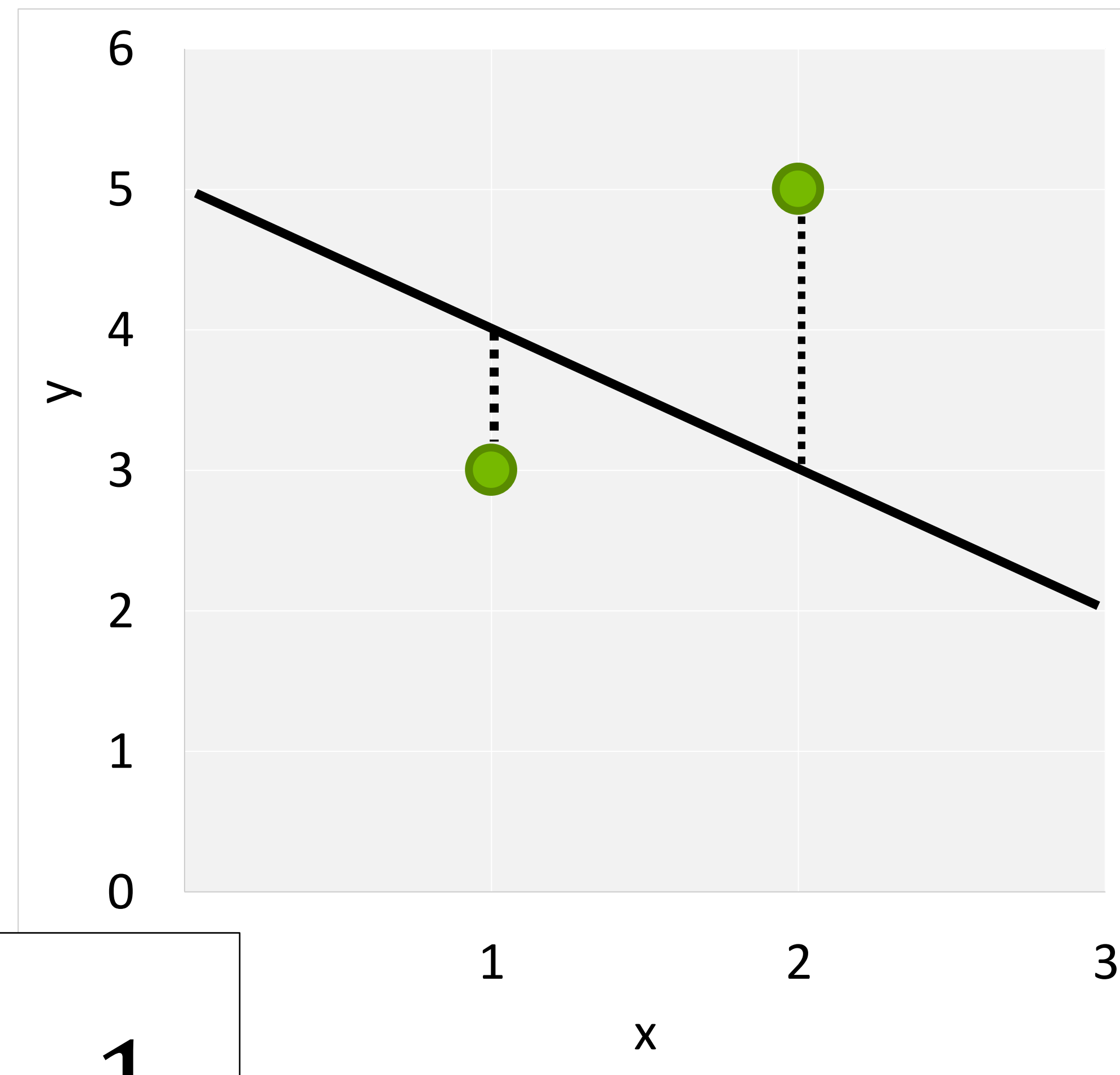
Loss Surface



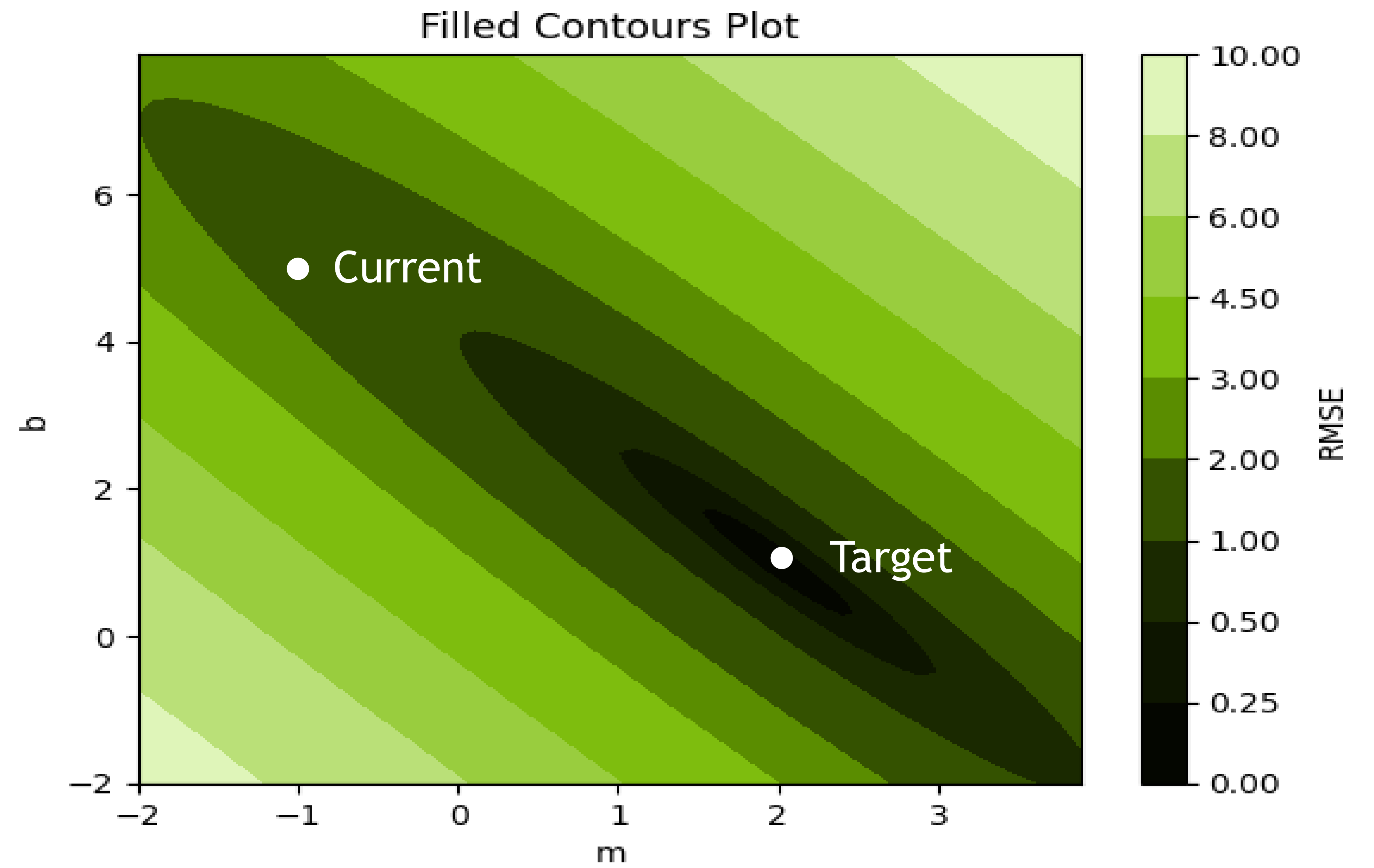
Filled Contours Plot



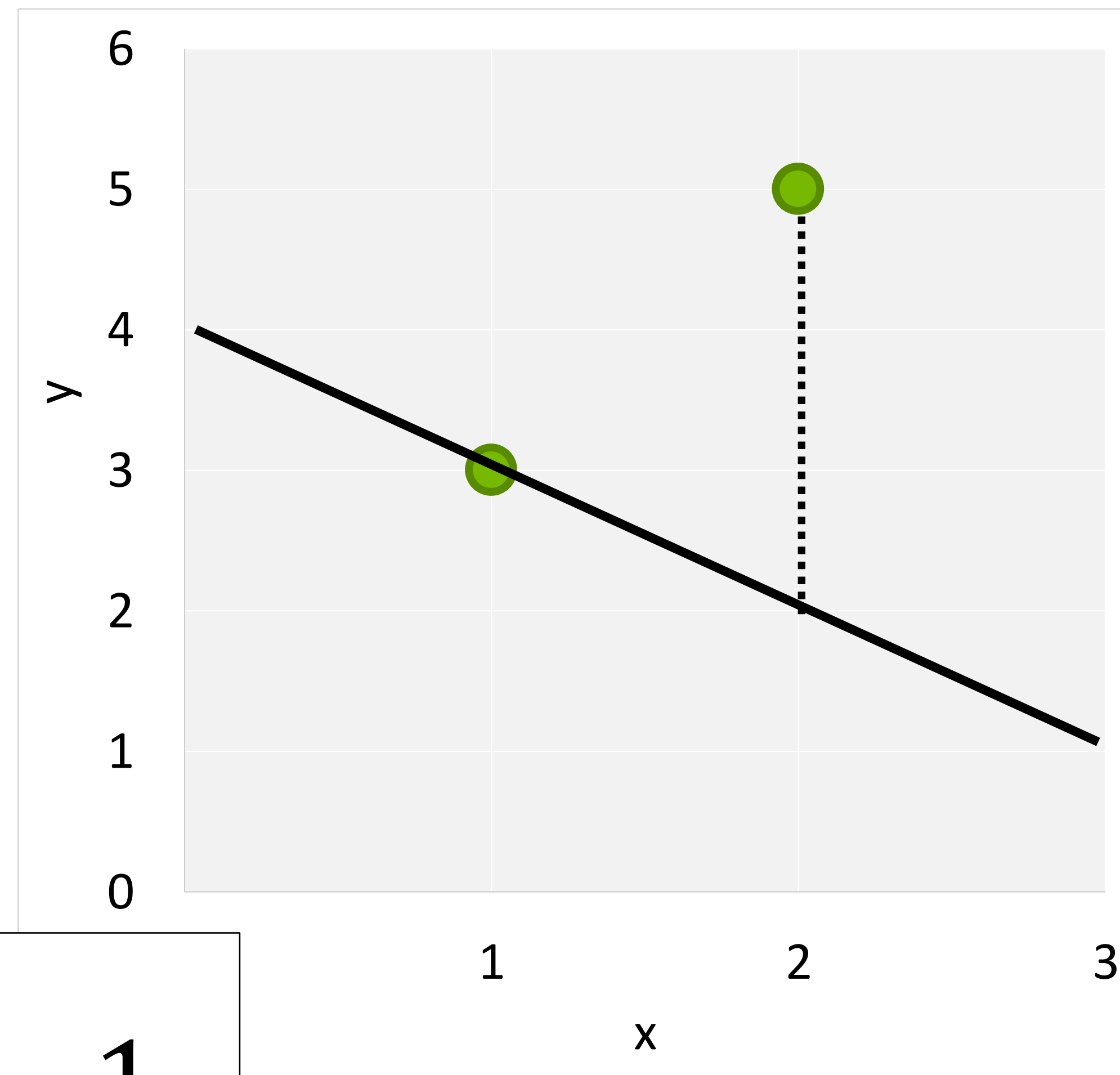
The Loss Curve



$$m = -1$$
$$b = 5$$

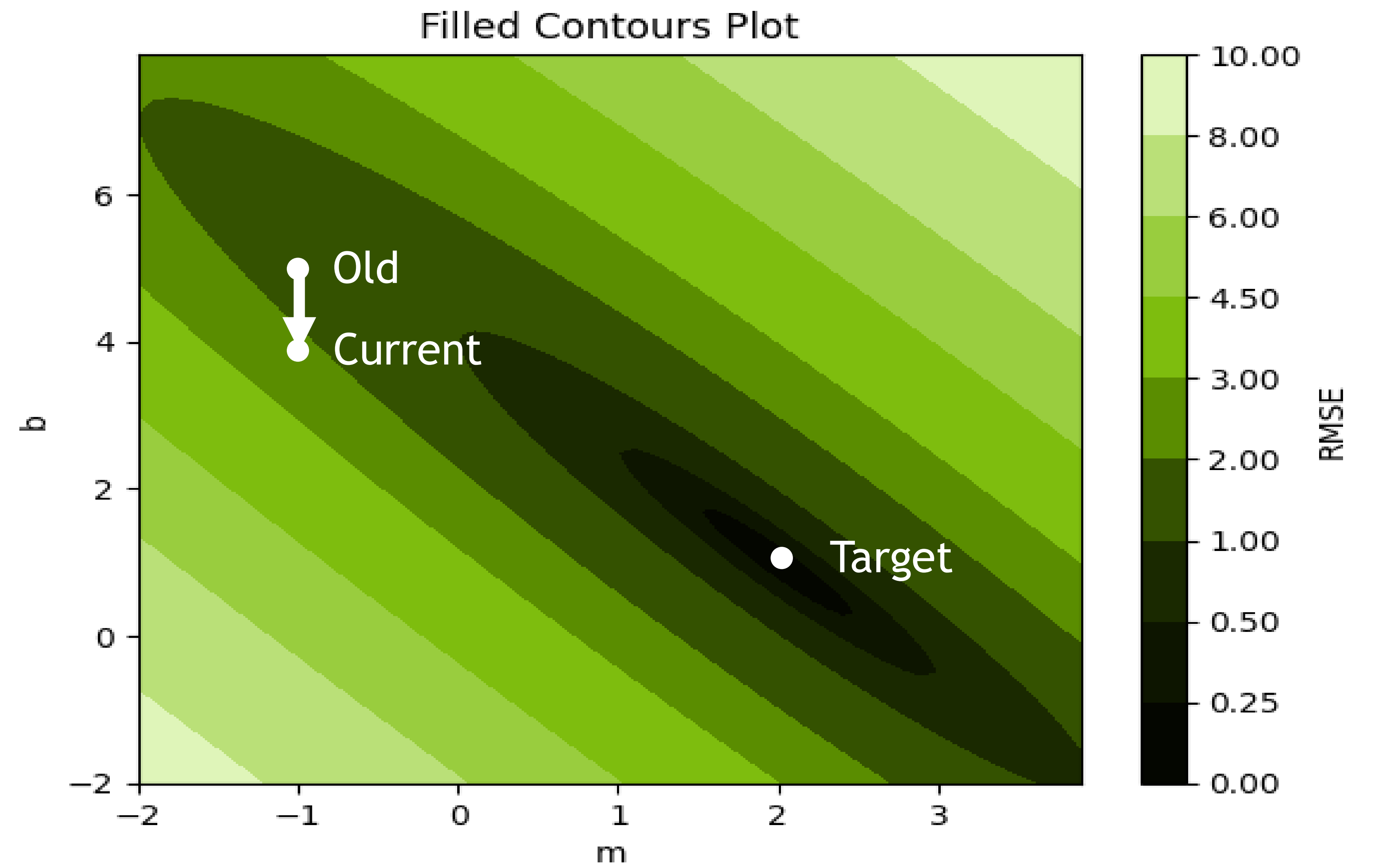


The Loss Curve

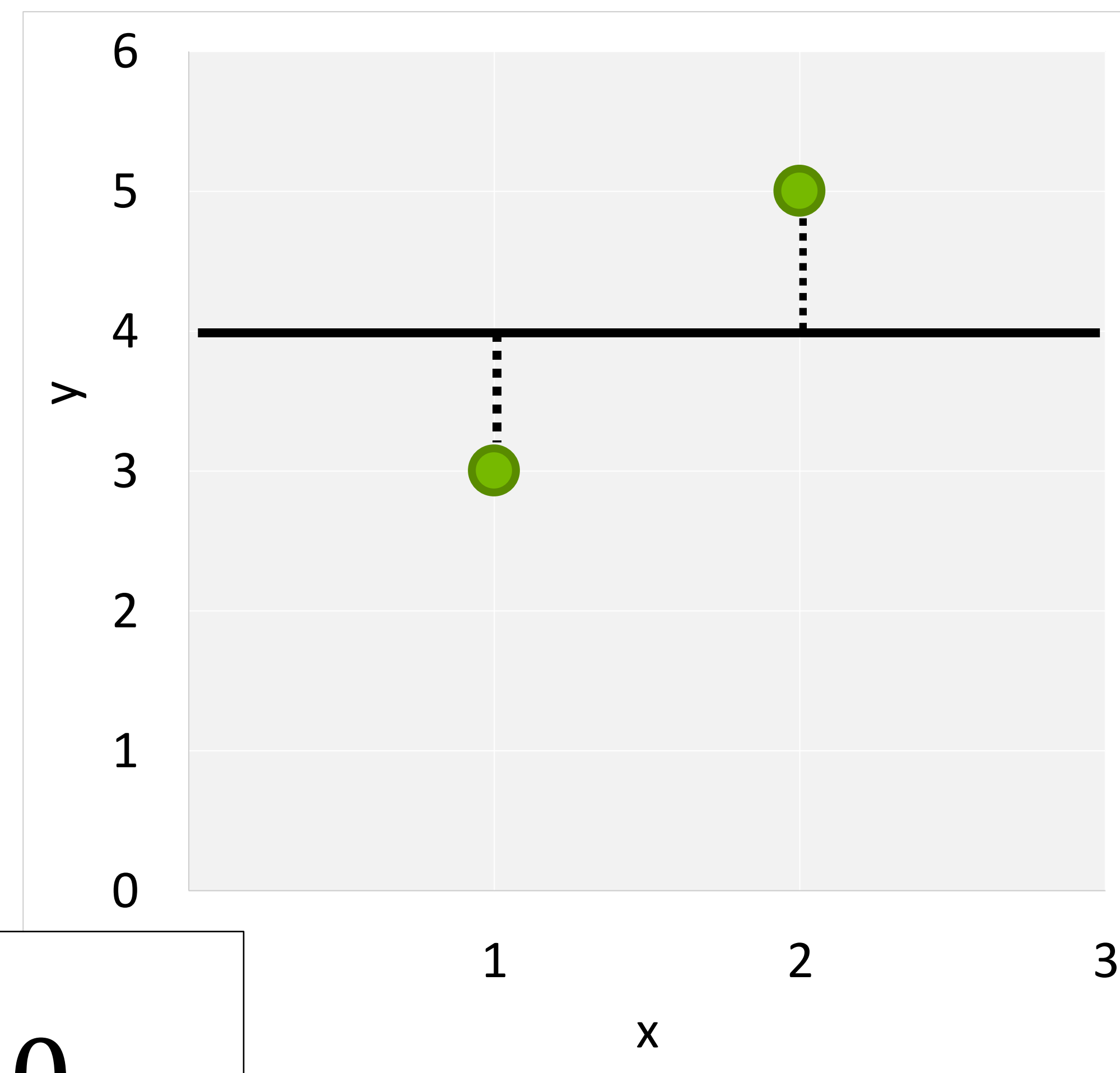


$$m = -1$$

$$b = 4$$

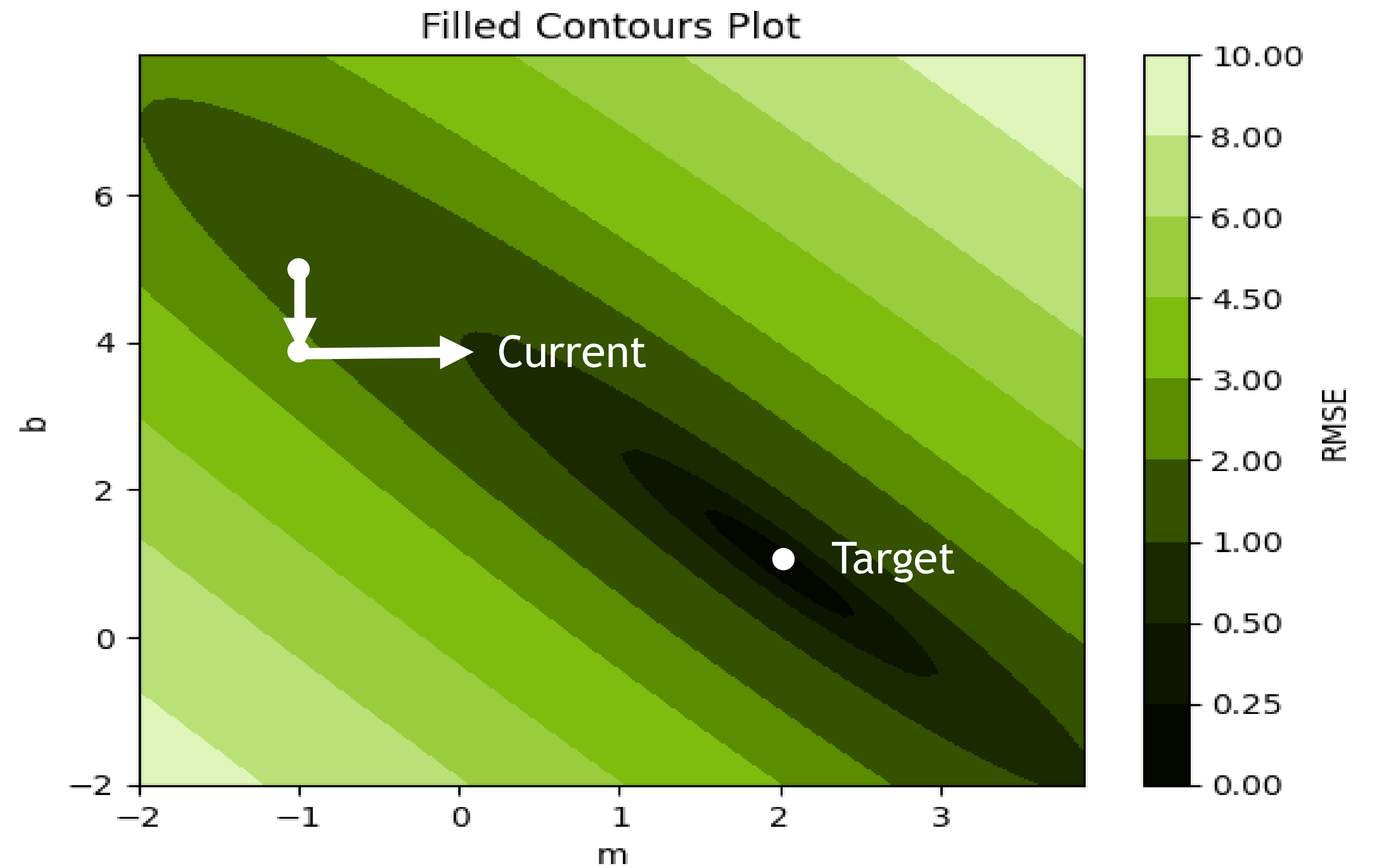


The Loss Curve



$$m = 0$$

$$b = 4$$



The Loss Curve

The Gradient

Which direction loss decreases the most

λ : The learning rate

How far to travel

Epoch

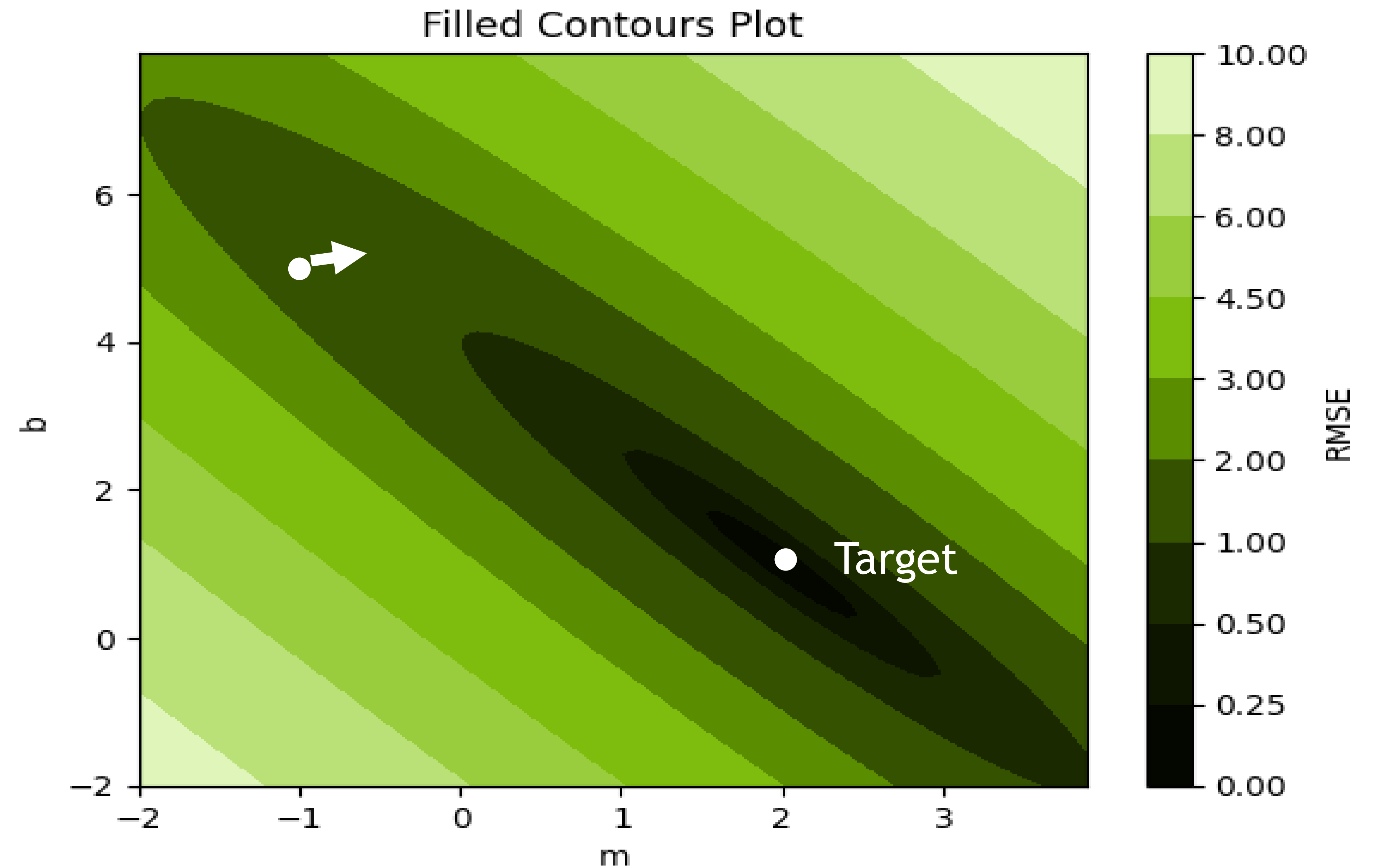
A model update with the full dataset

Batch

A sample of the full dataset

Step

An update to the weight parameters



The Loss Curve

The Gradient

Which direction loss decreases the most

λ : The learning rate

How far to travel

Epoch

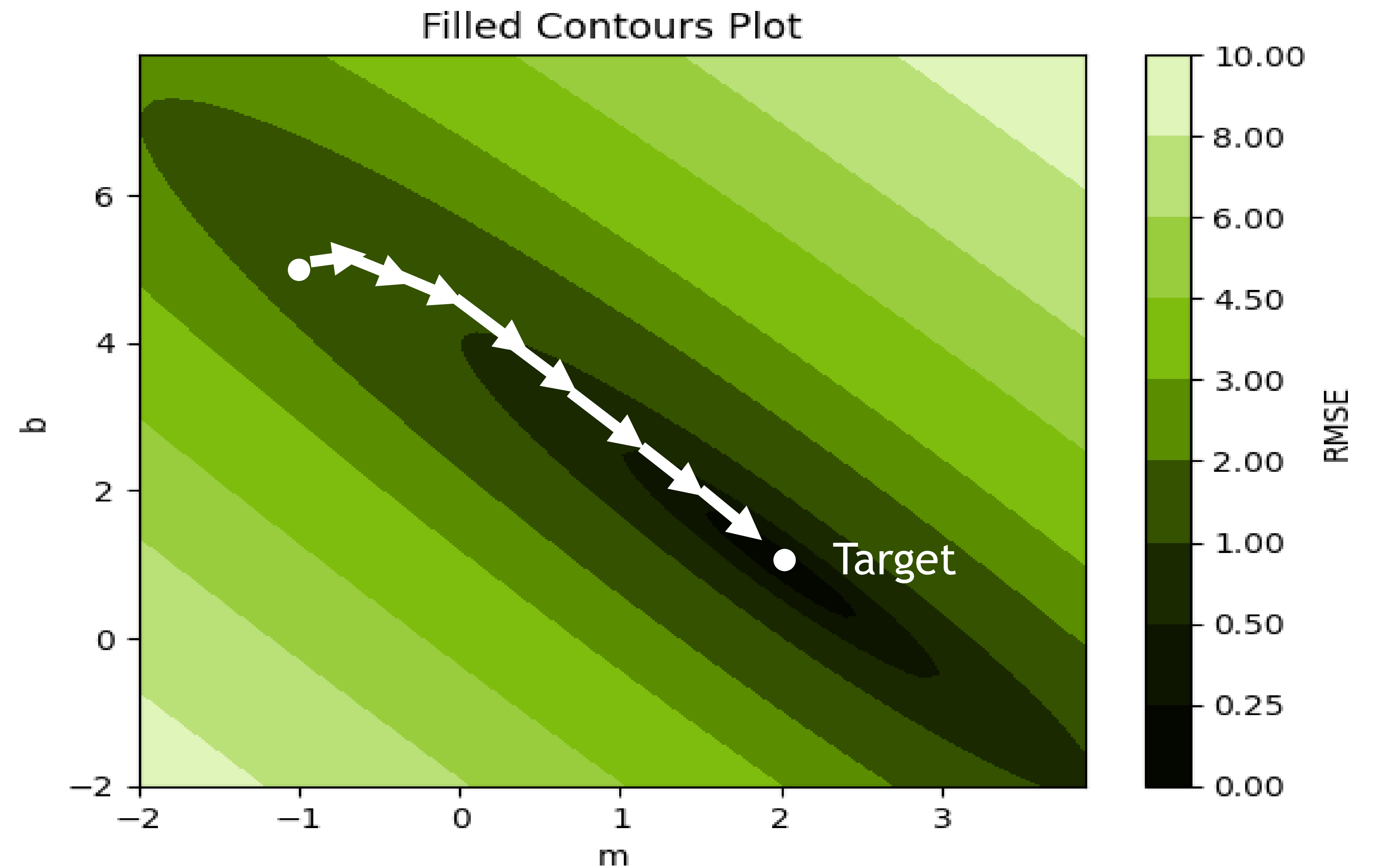
A model update with the full dataset

Batch

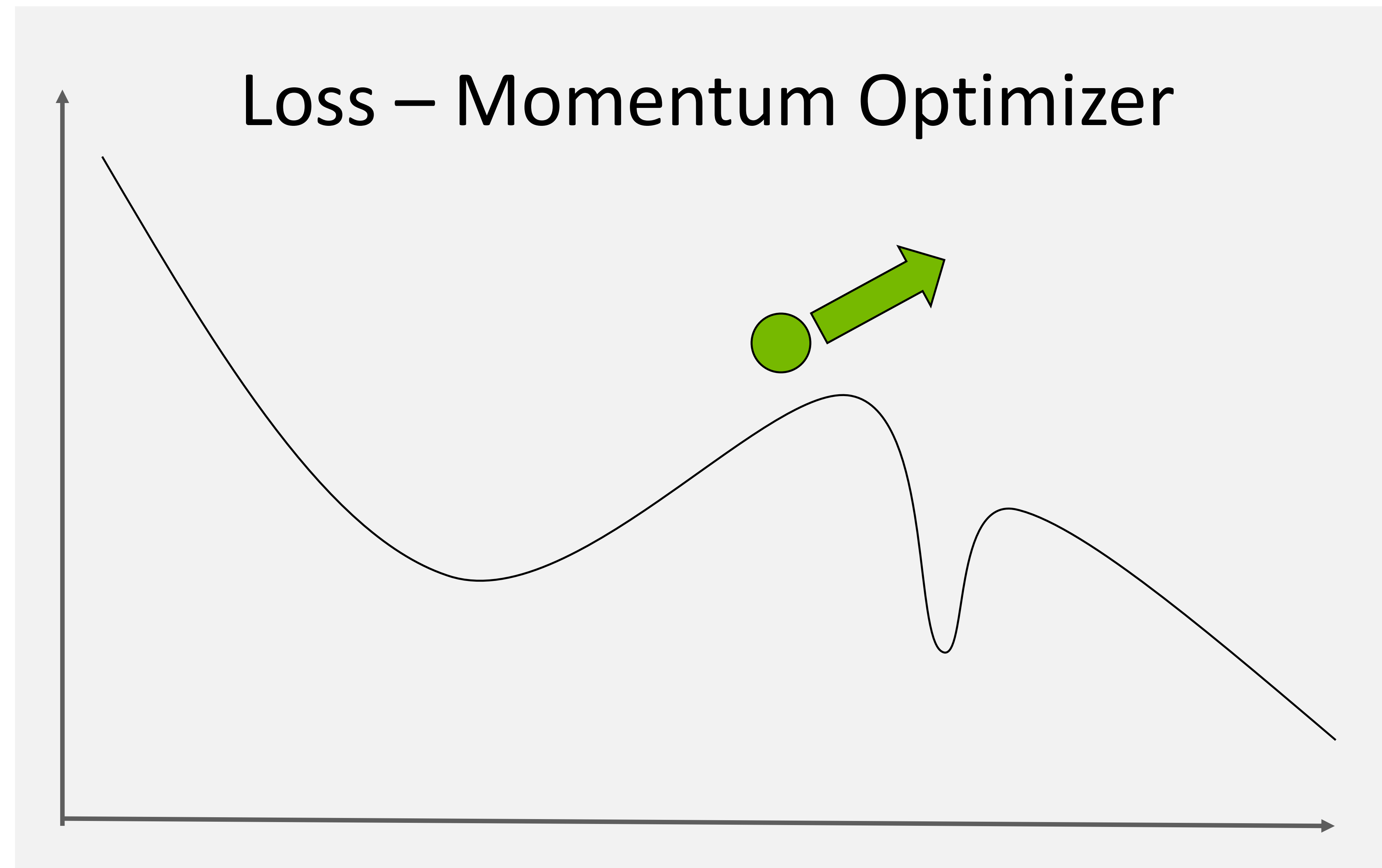
A sample of the full dataset

Step

An update to the weight parameters



Optimizers

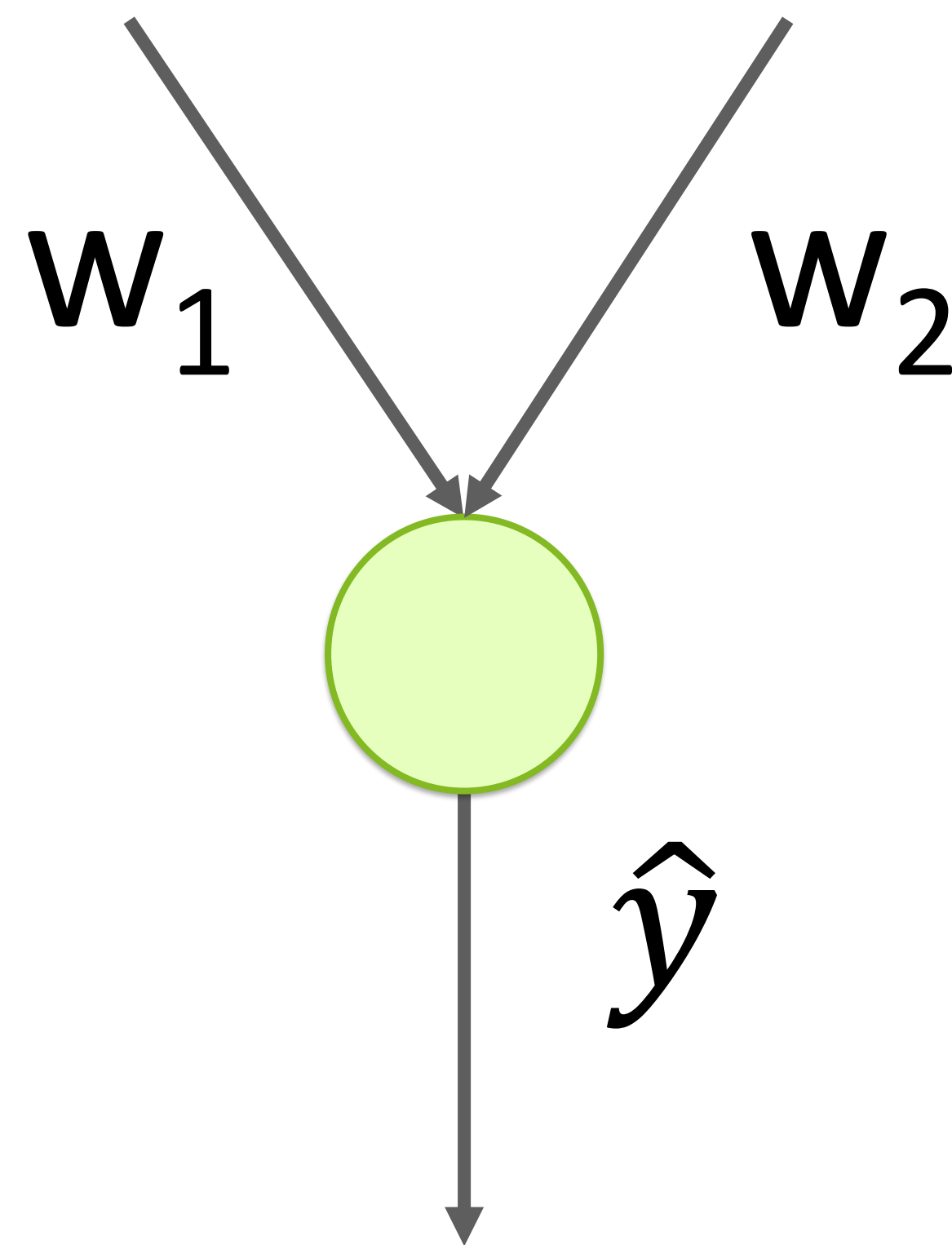


- Adam
- Adagrad
- RMSprop
- SGD



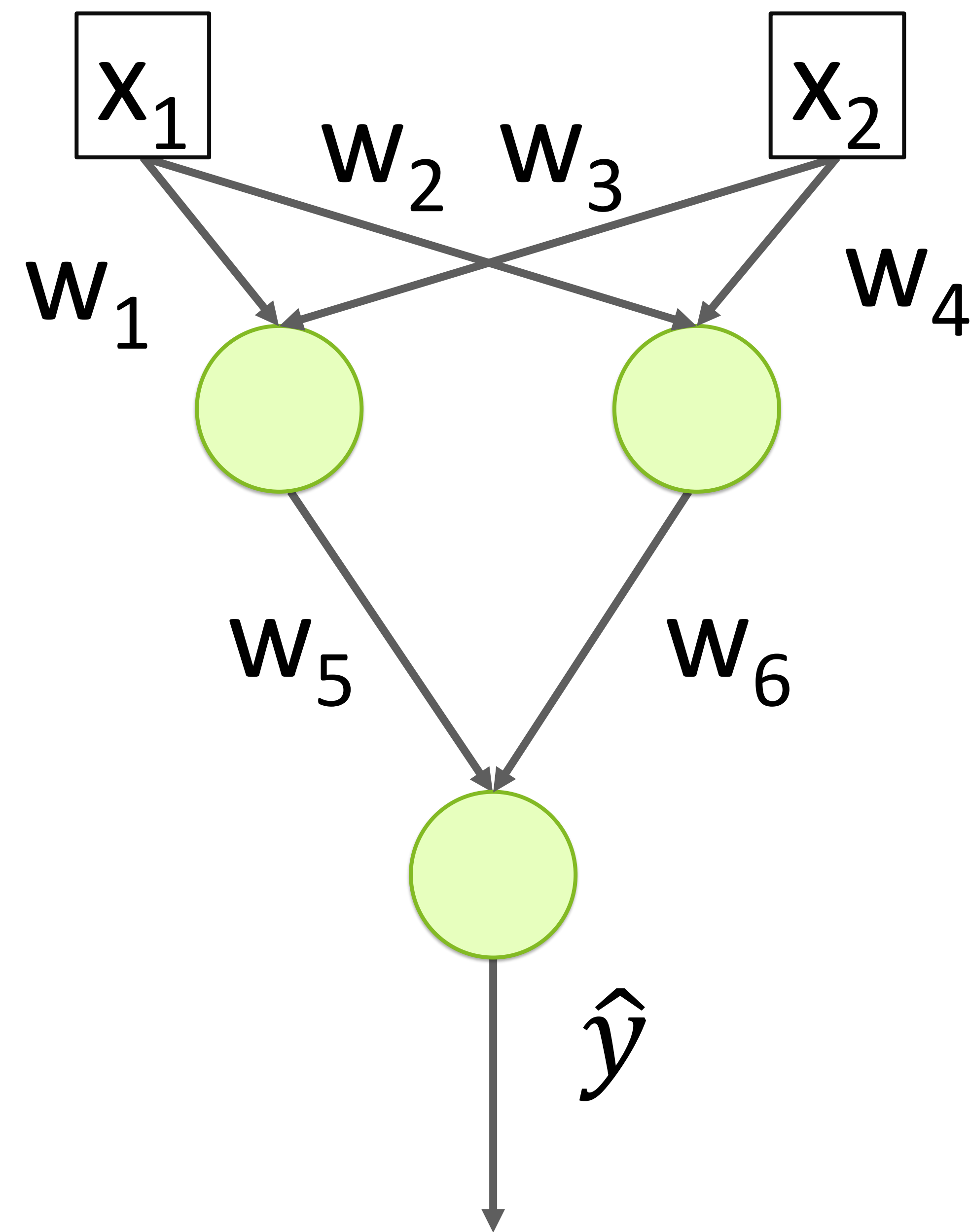
From Neuron to Network

Building a Network



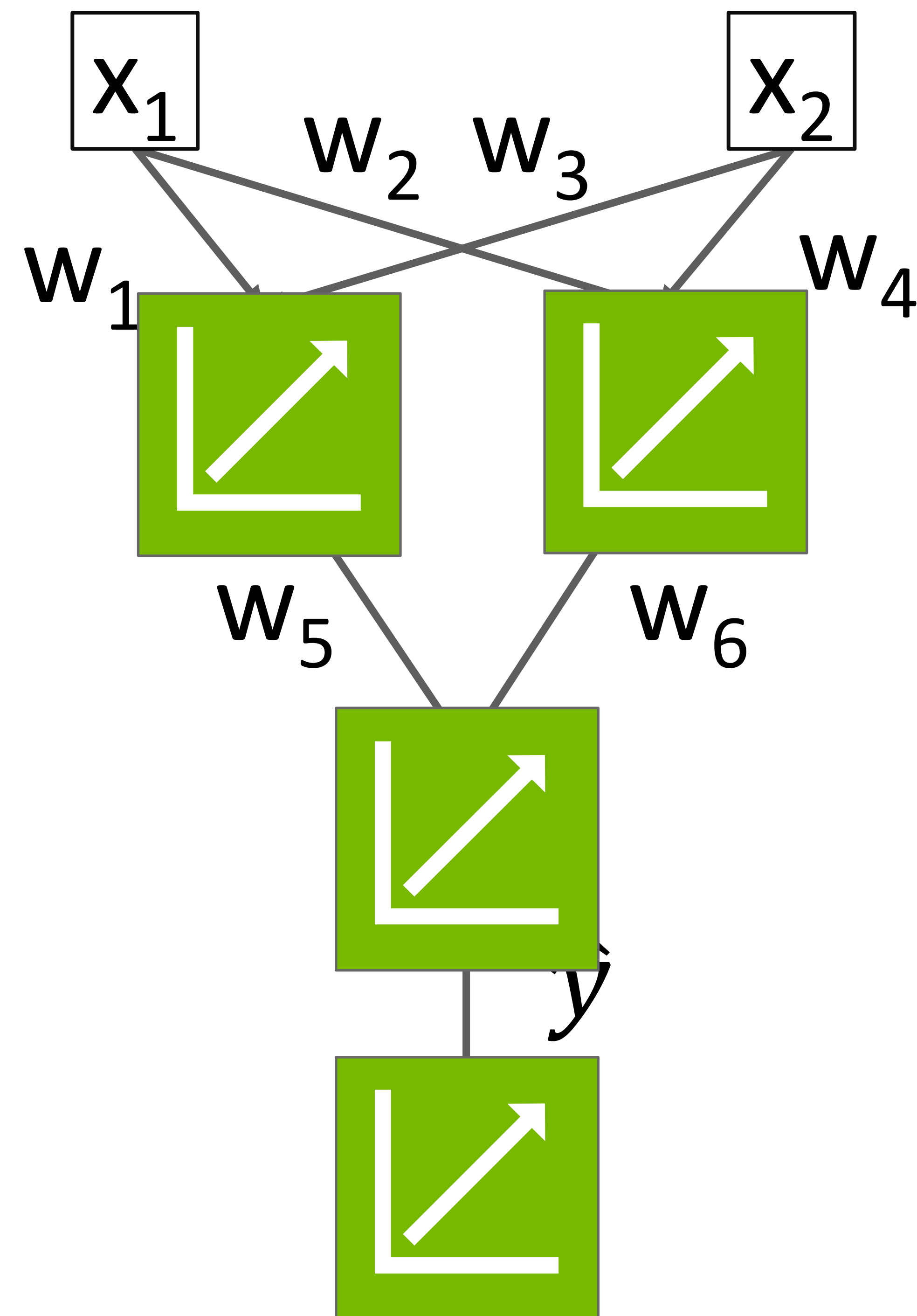
- Scales to more inputs

Building a Network



- Scales to more inputs
- Can chain neurons

Building a Network



- Scales to more inputs
- Can chain neurons
- If all regressions are linear, then output will also be a linear regression

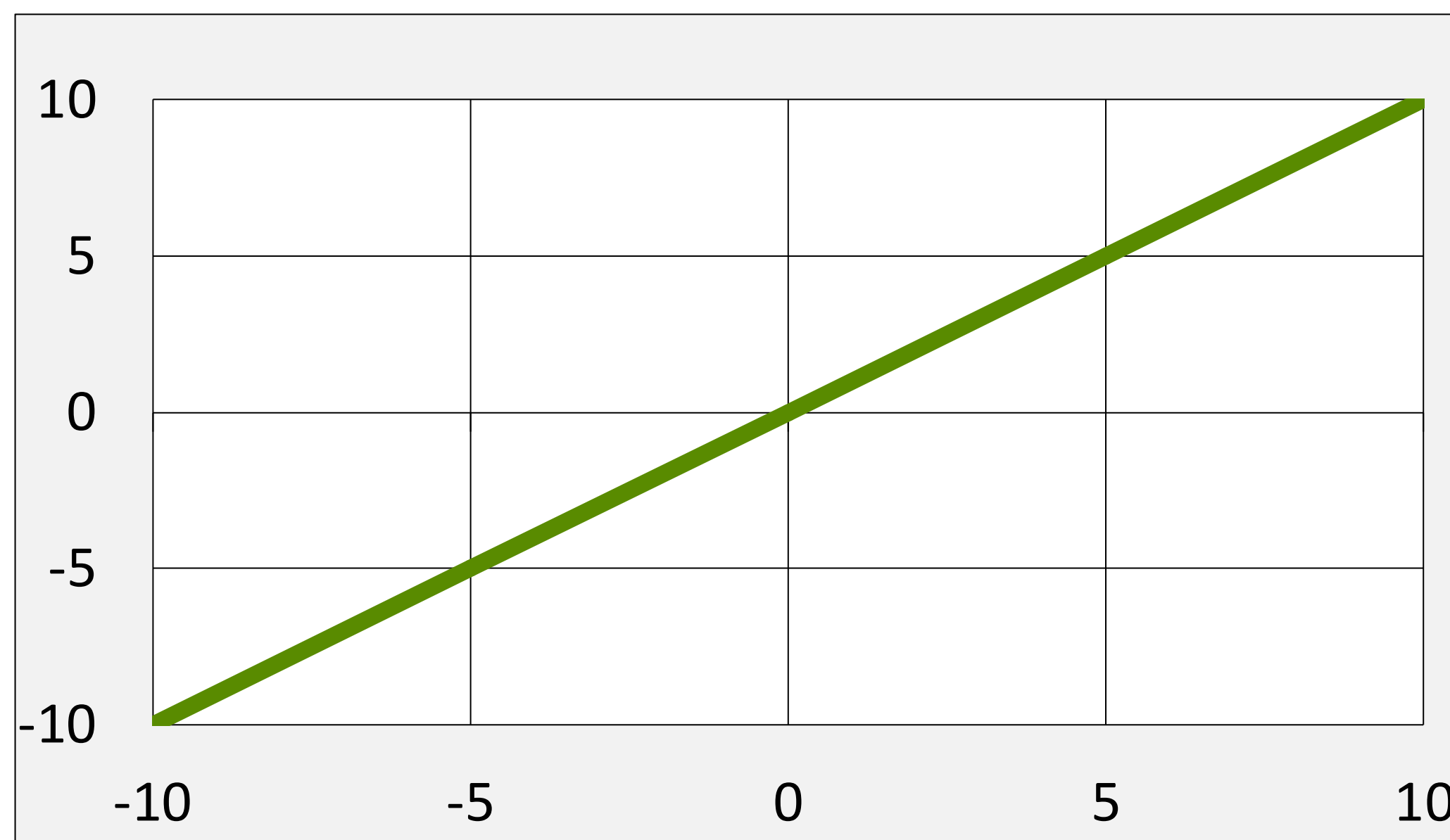
Activation Functions

Activation Functions

Linear

$$\hat{y} = wx + b$$

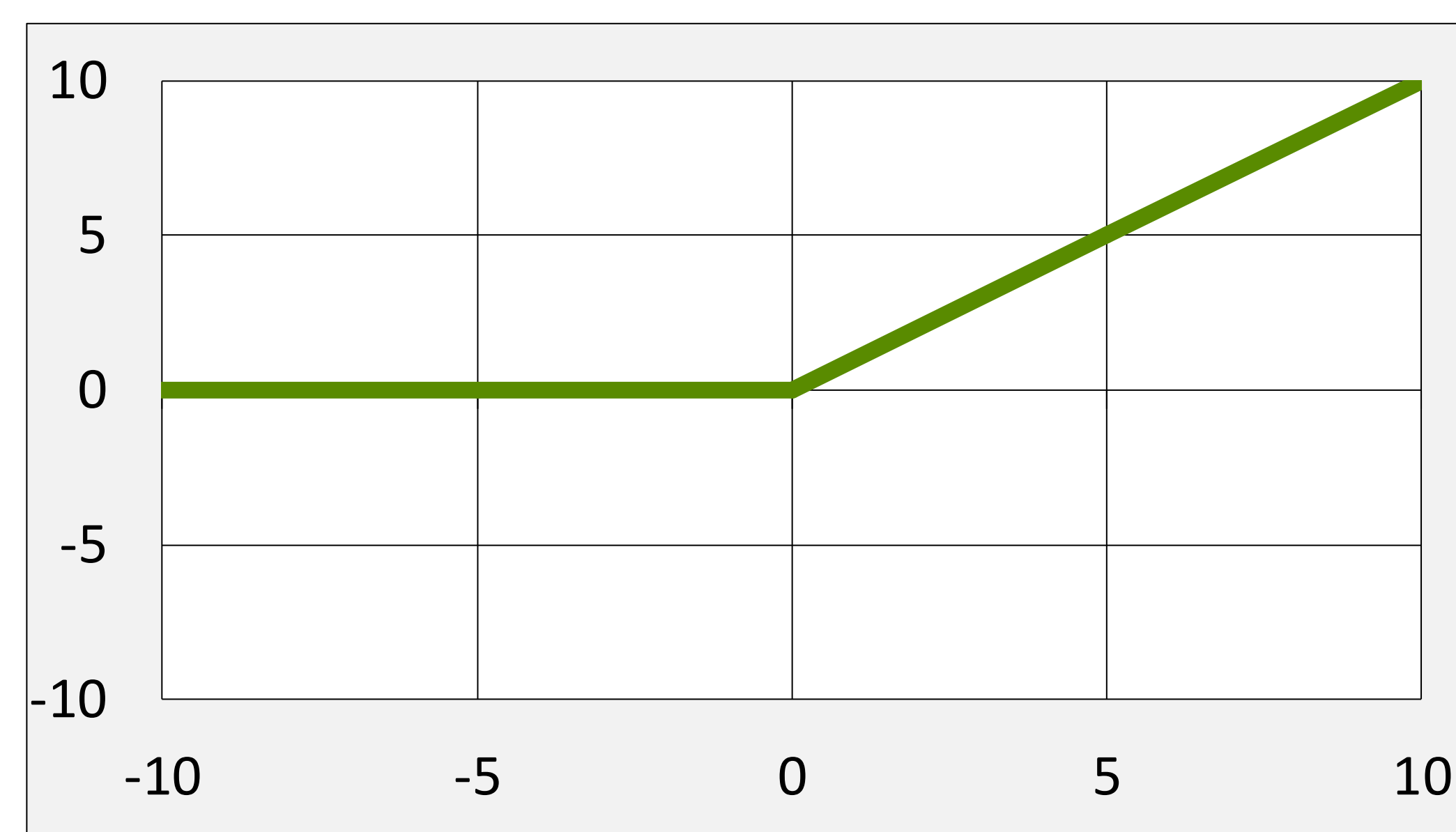
```
1 # Multiply each input
2 # with a weight (w) and
3 # add intercept (b)
4 y_hat = wx+b
```



ReLU

$$\hat{y} = \begin{cases} wx + b & \text{if } wx + b > 0 \\ 0 & \text{otherwise} \end{cases}$$

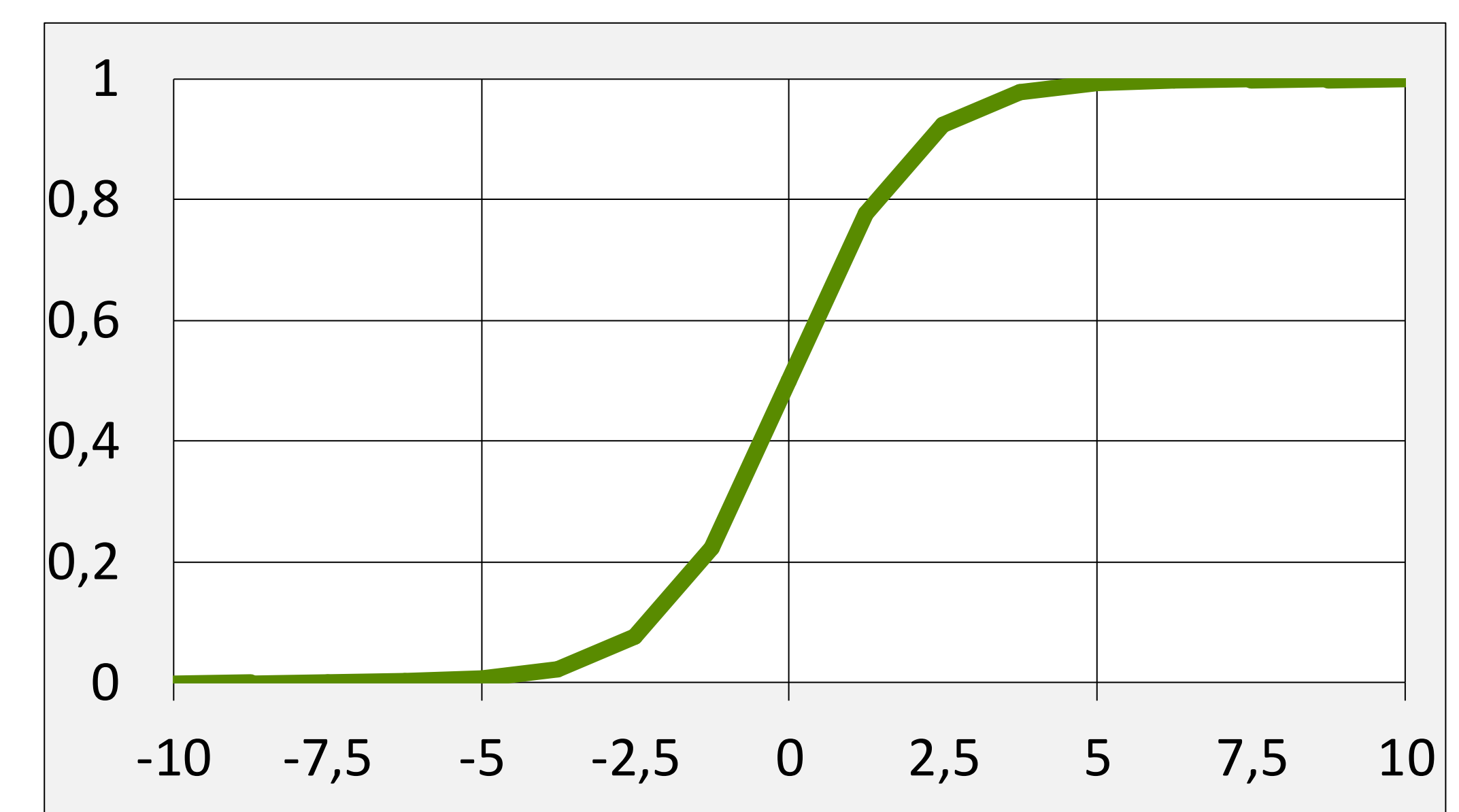
```
1 # Only return result
2 # if total is positive
3 linear = wx+b
4 y_hat = linear * (linear > 0)
```



Sigmoid

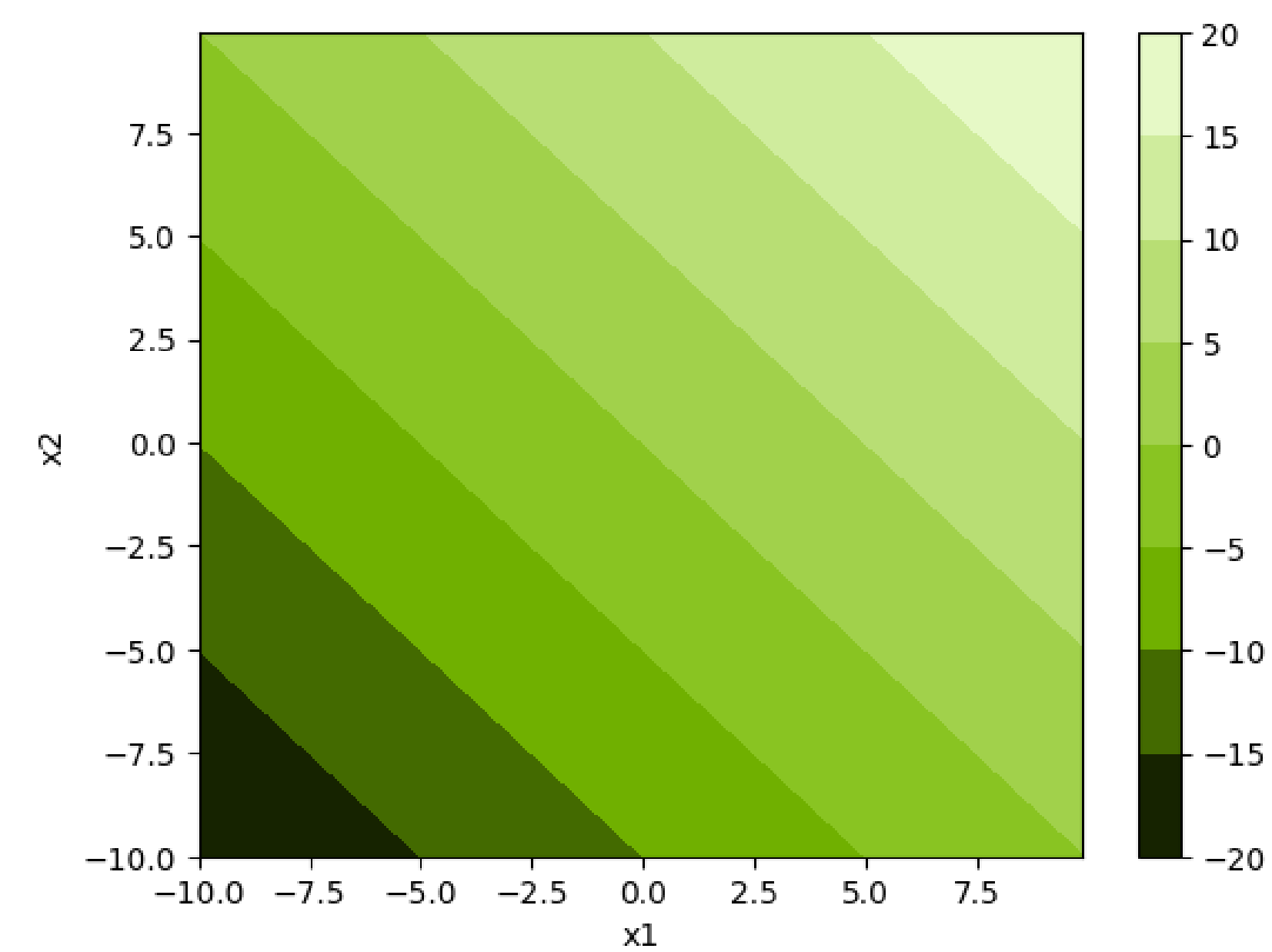
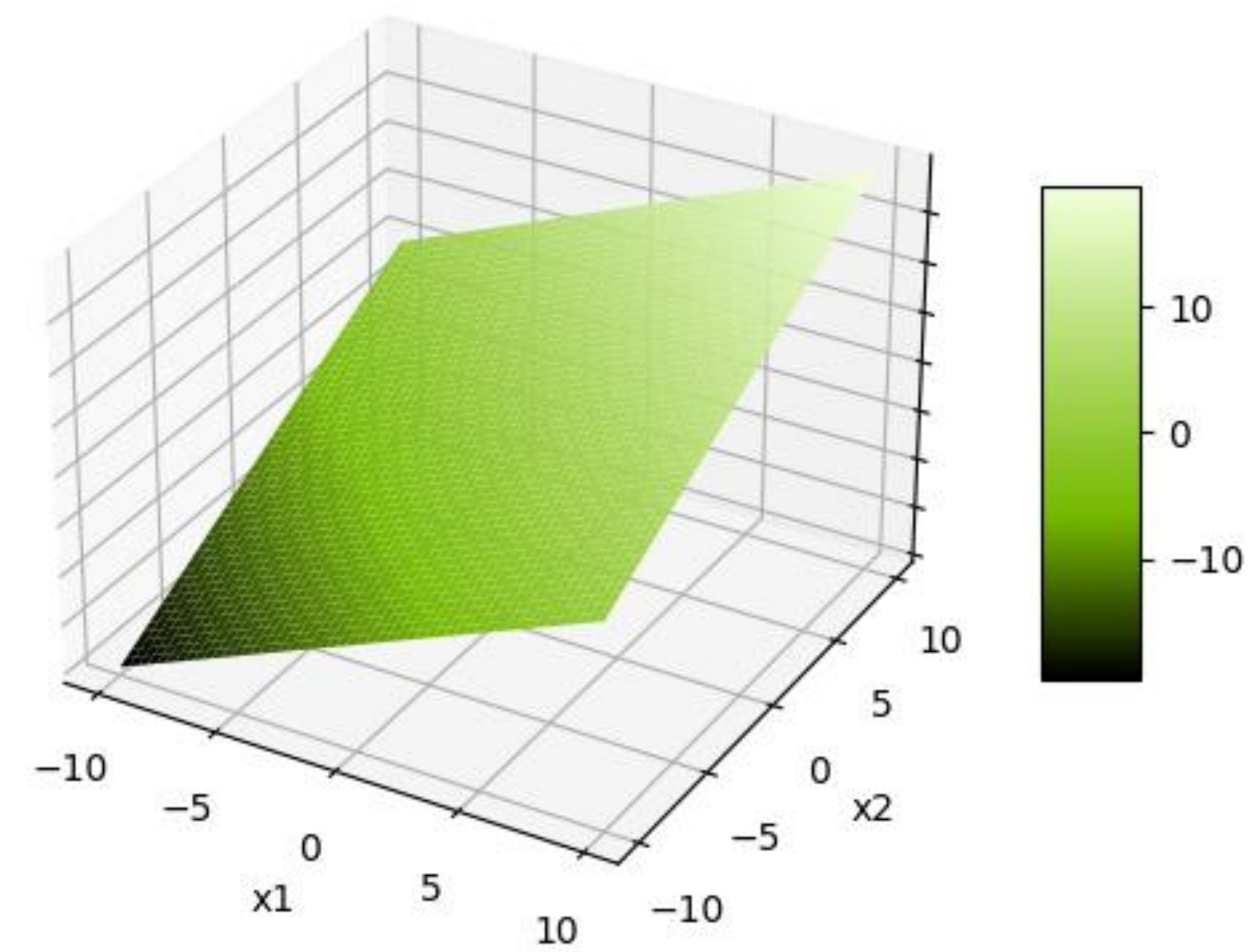
$$\hat{y} = \frac{1}{1 + e^{-(wx+b)}}$$

```
1 # Start with line
2 linear = wx + b
3 # Warp to - inf to 0
4 inf_to_zero = np.exp(-1 * linear)
5 # Squish to -1 to 1
6 y_hat = 1 / (1 + inf_to_zero)
```

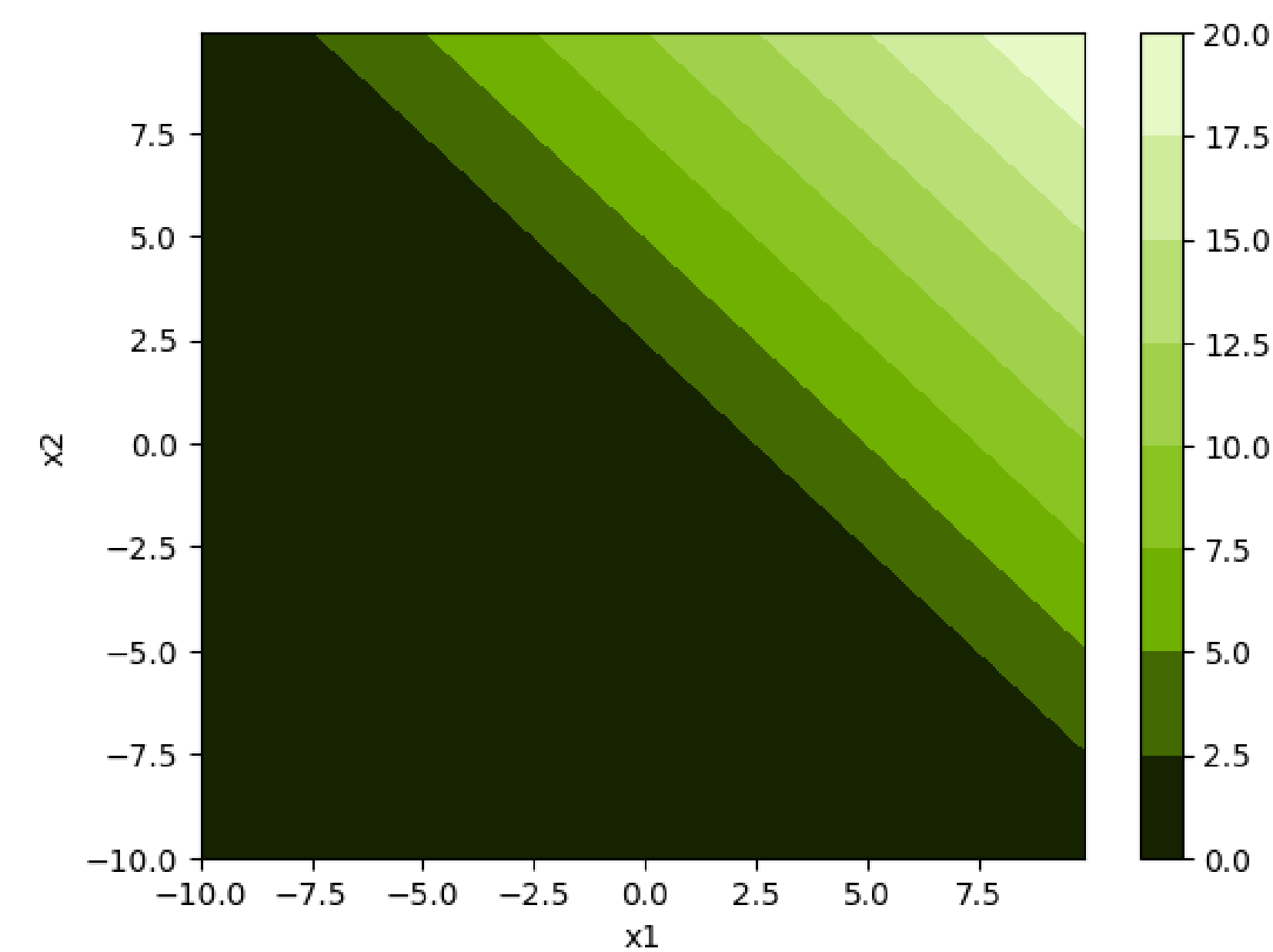
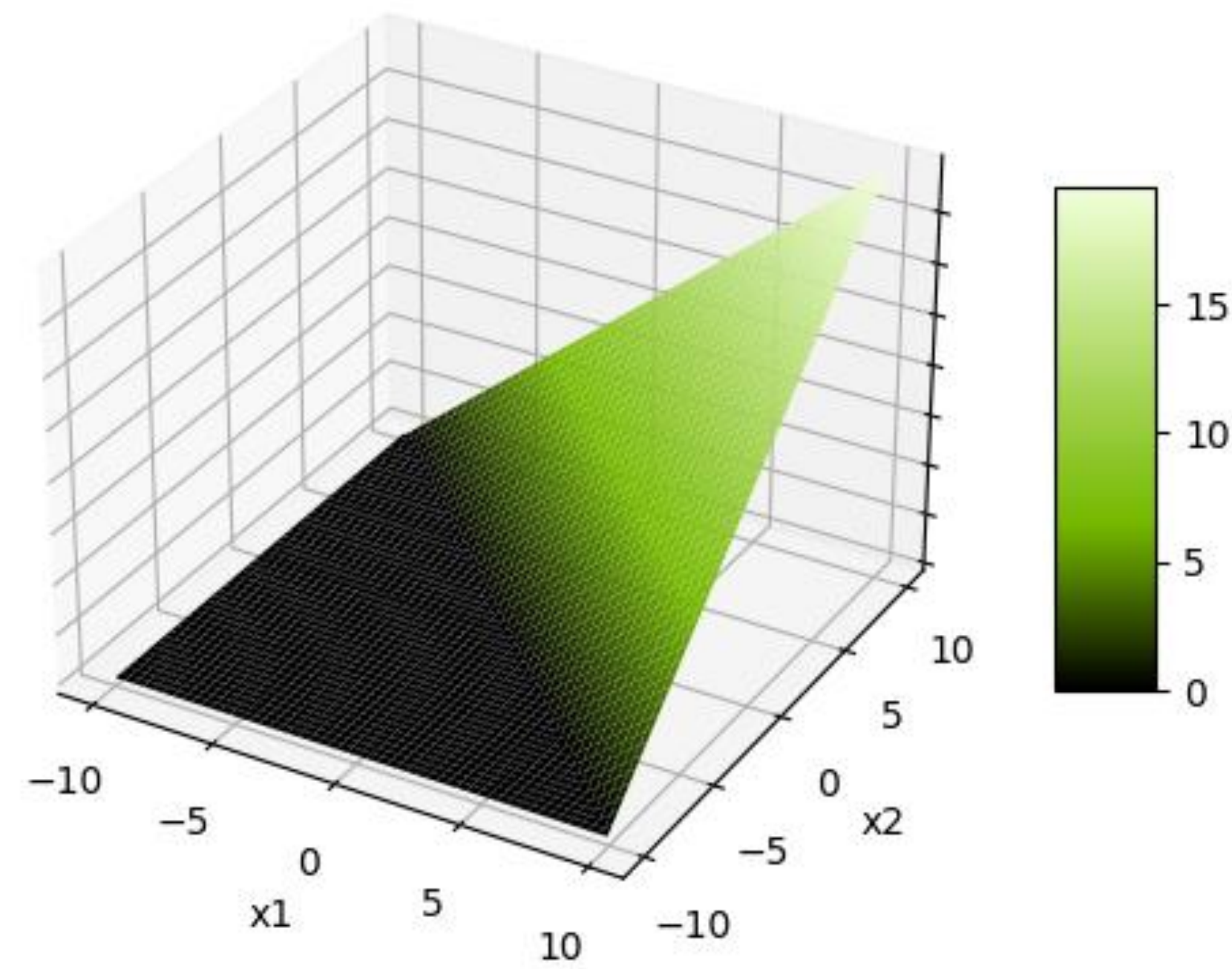


Activation Functions

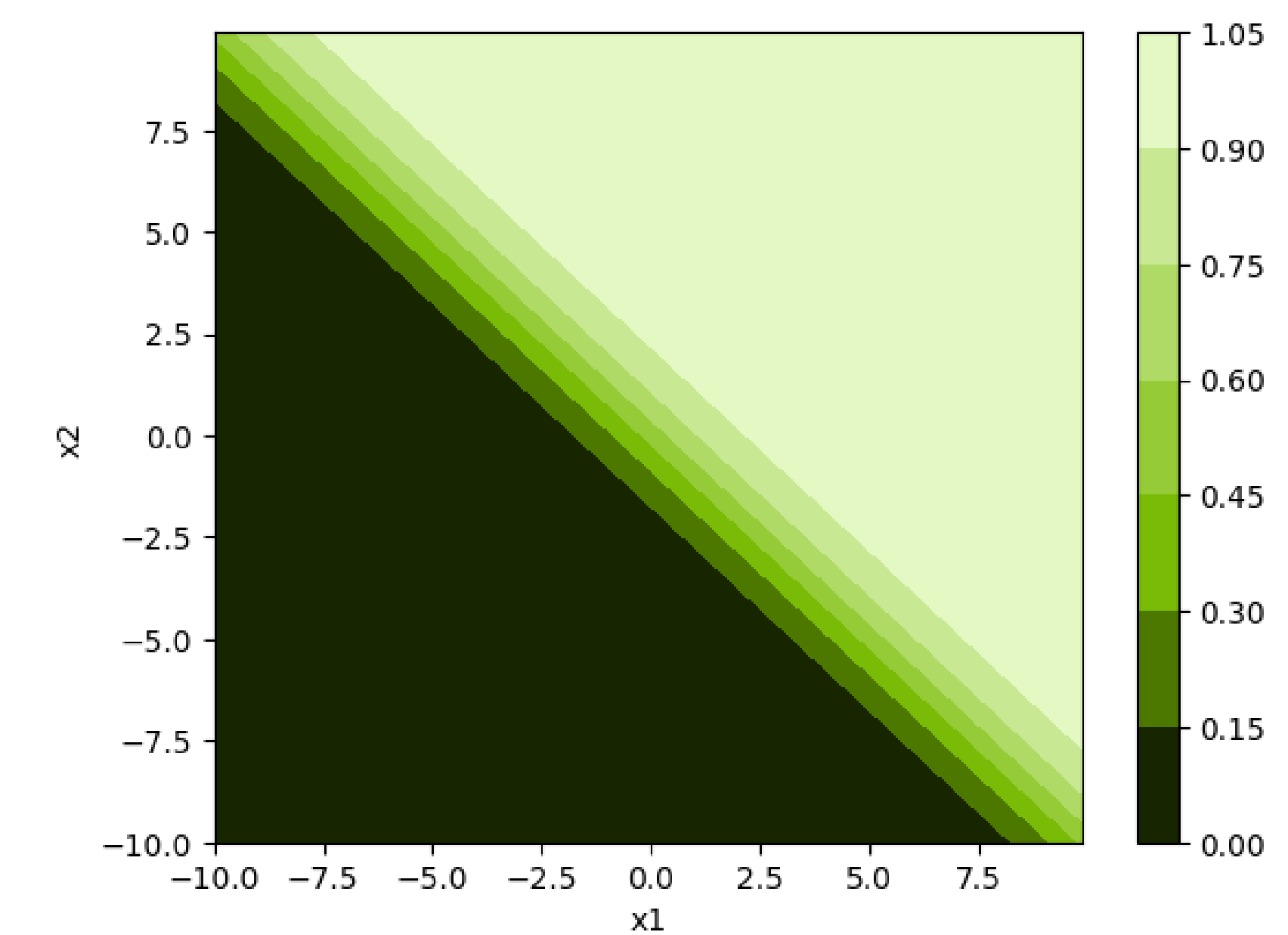
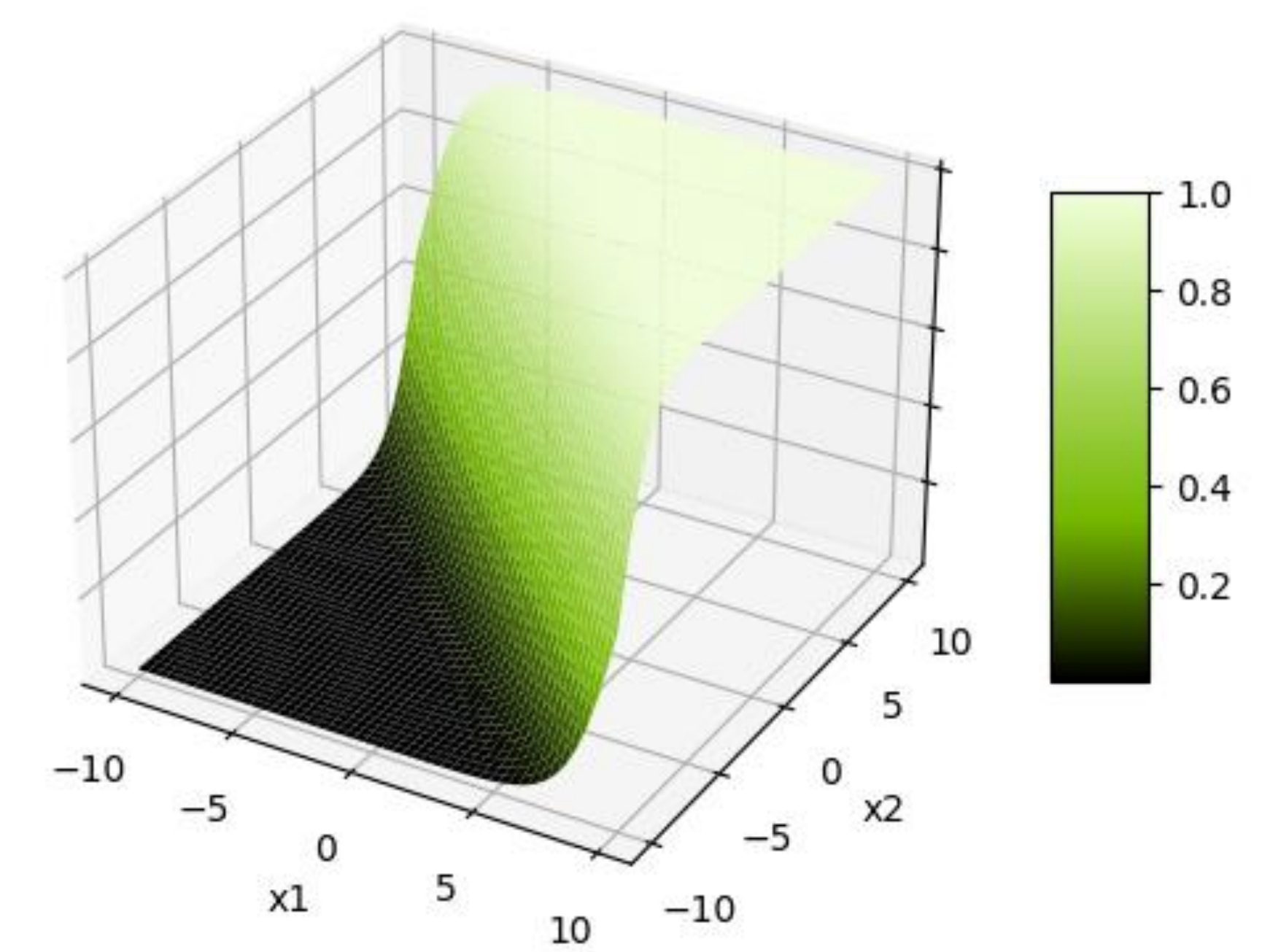
Linear



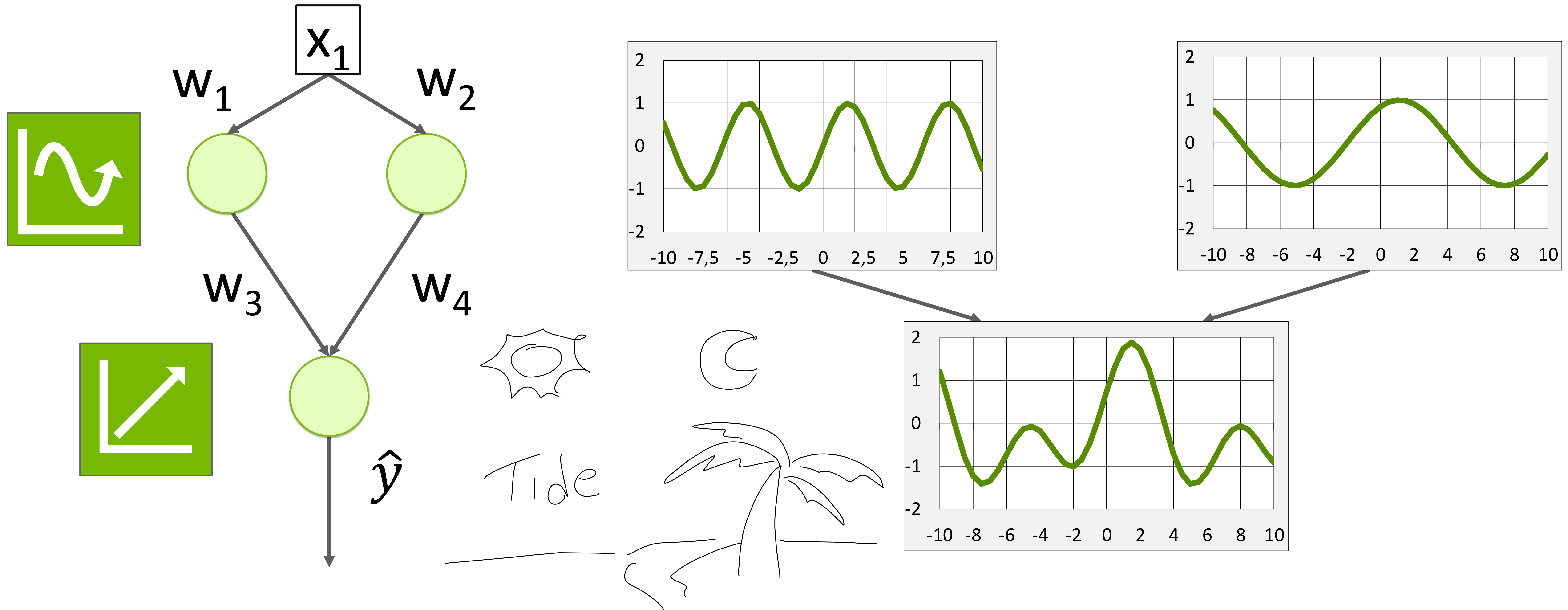
ReLU



Sigmoid



Activation Functions





Overfitting

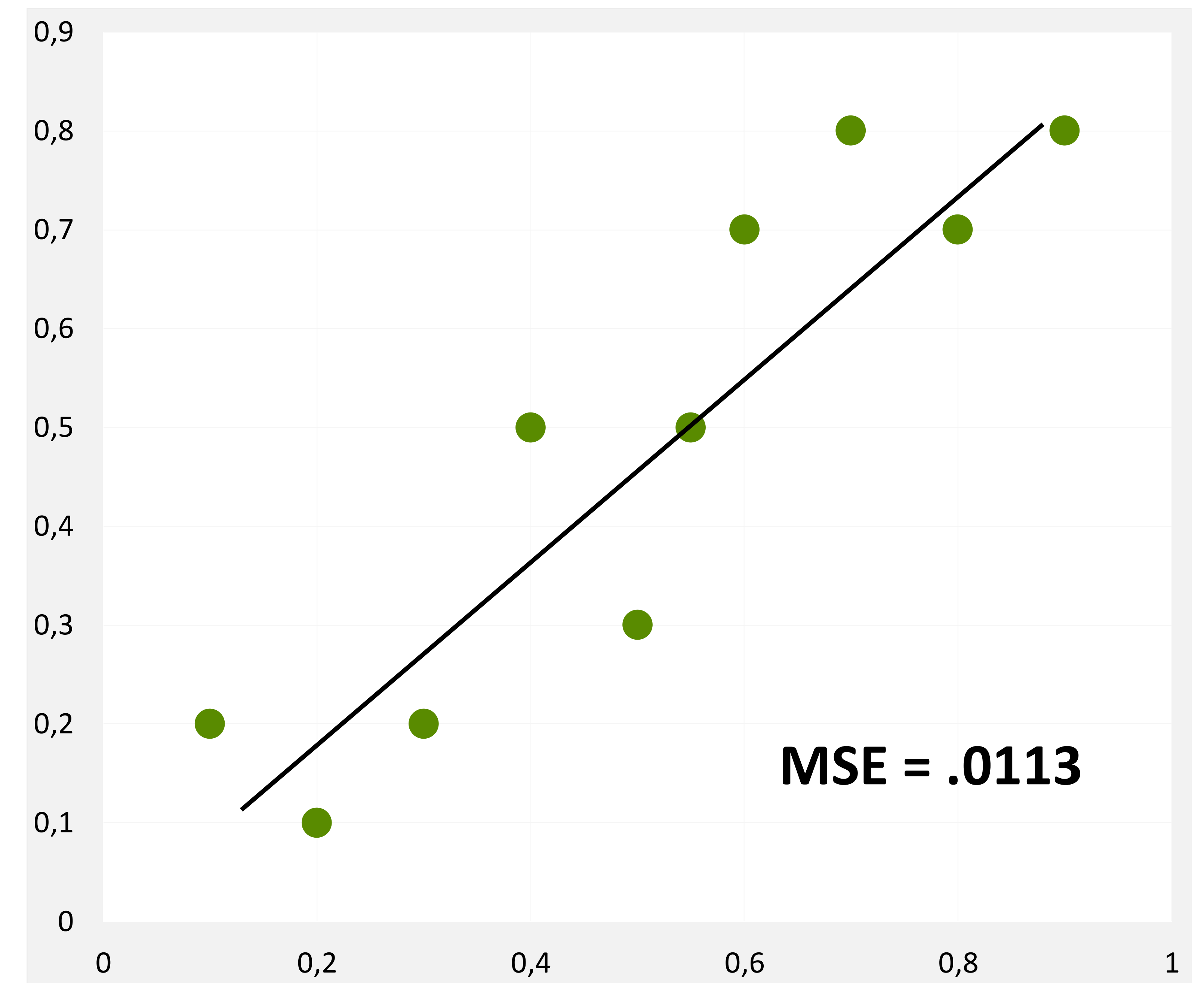
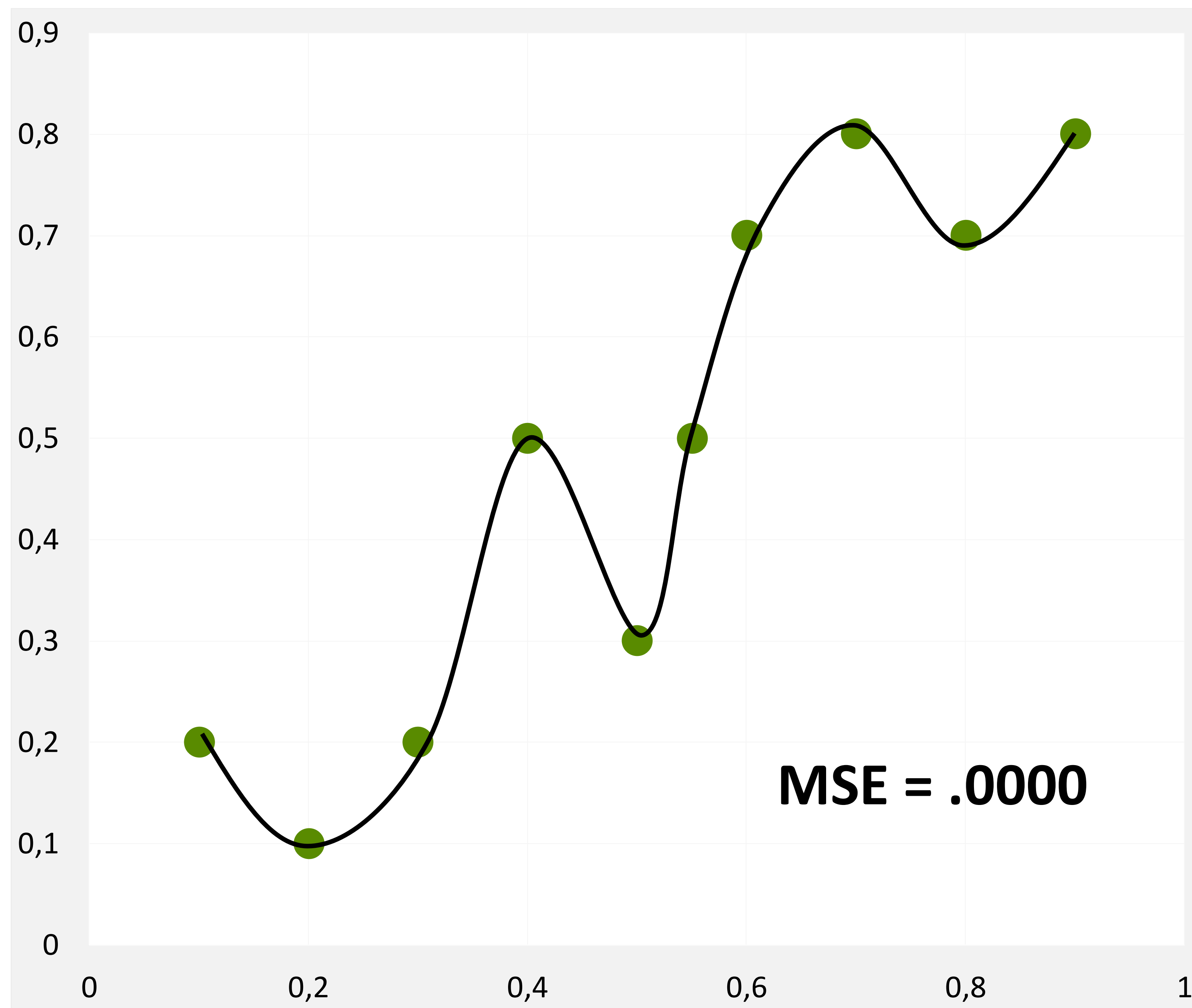
Overfitting

Why not have a super large neural network?



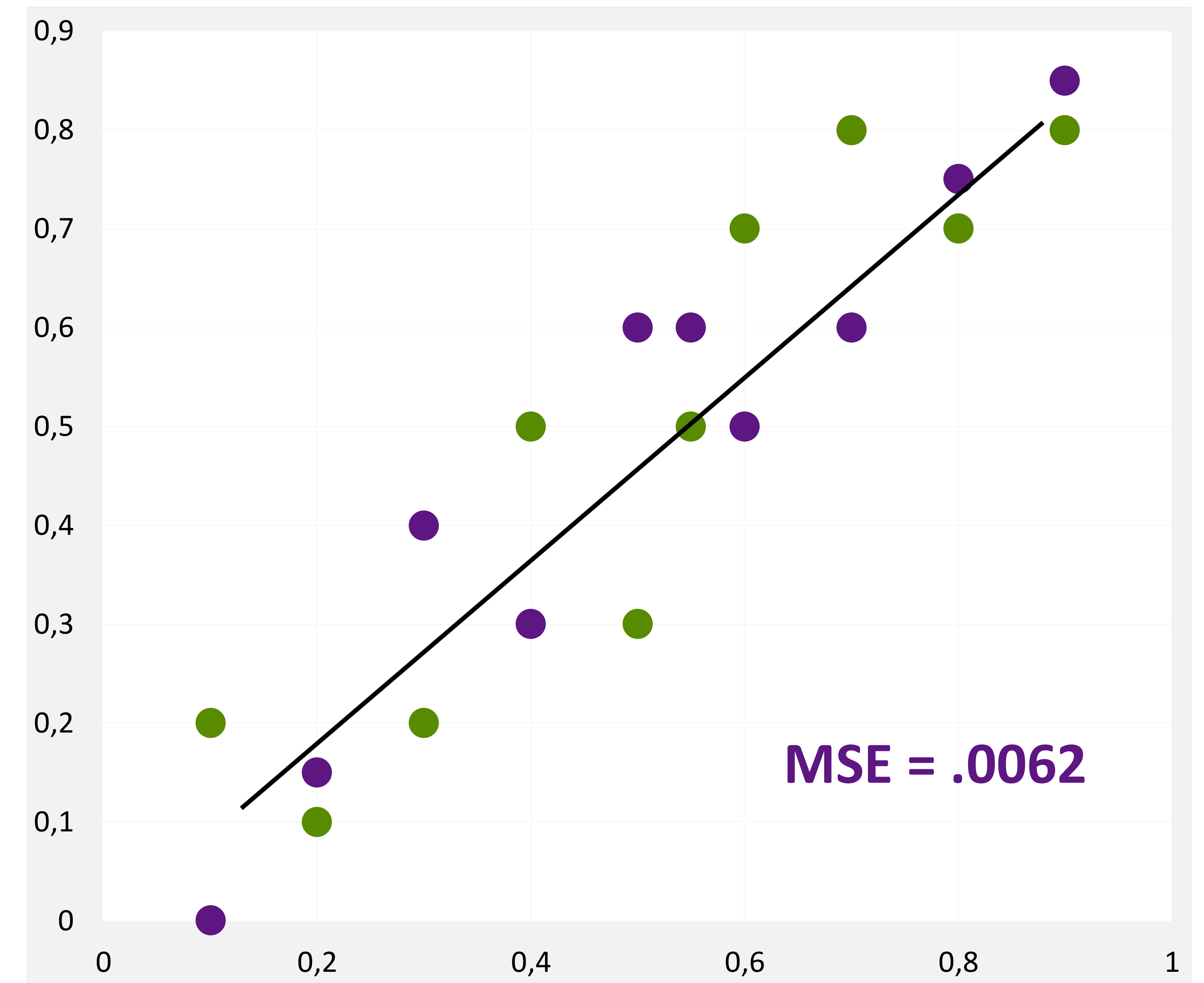
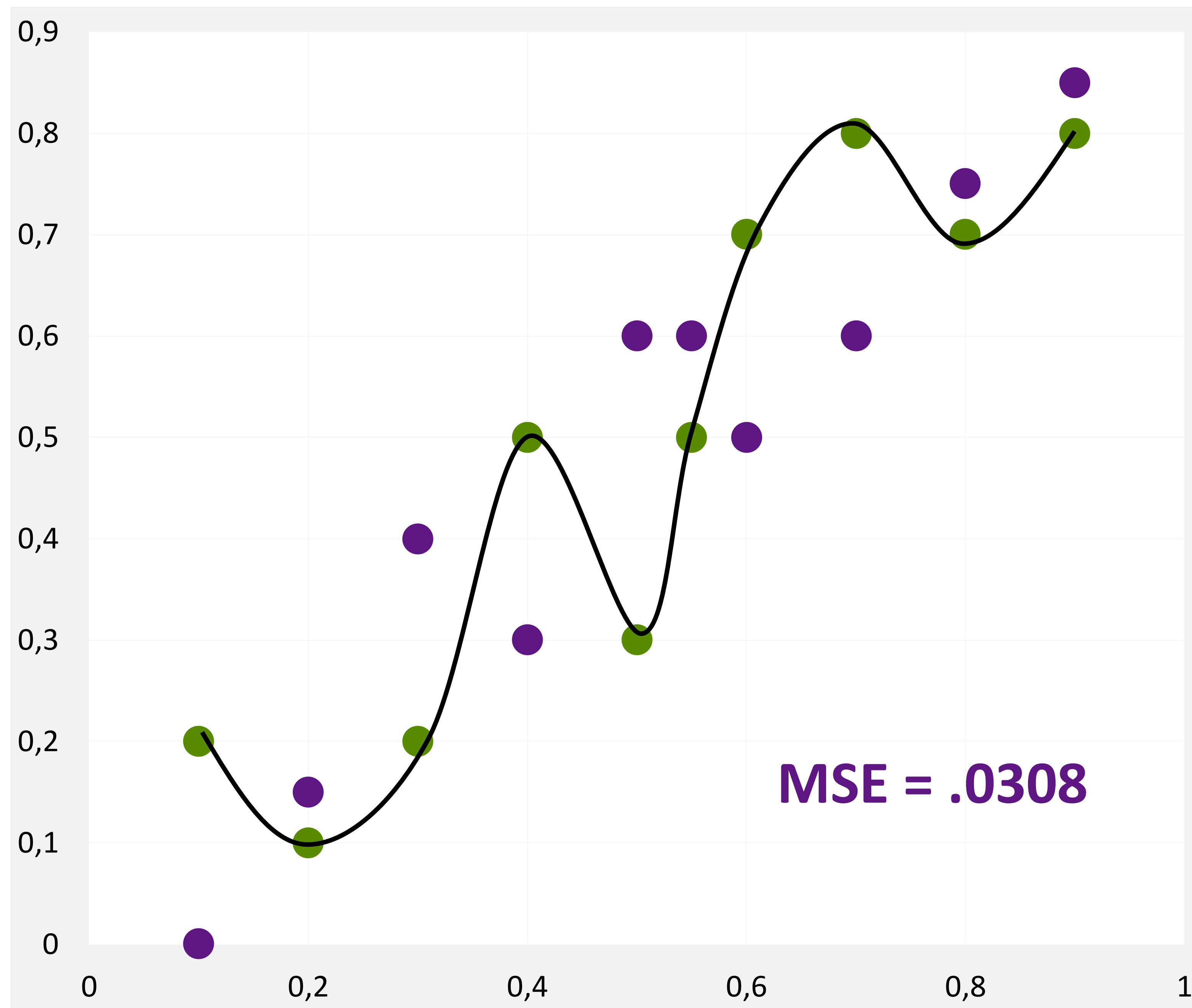
Overfitting

Which Trendline is Better?



Overfitting

Which Trendline is Better?



Training vs Validation Data

Avoid memorization

Training data

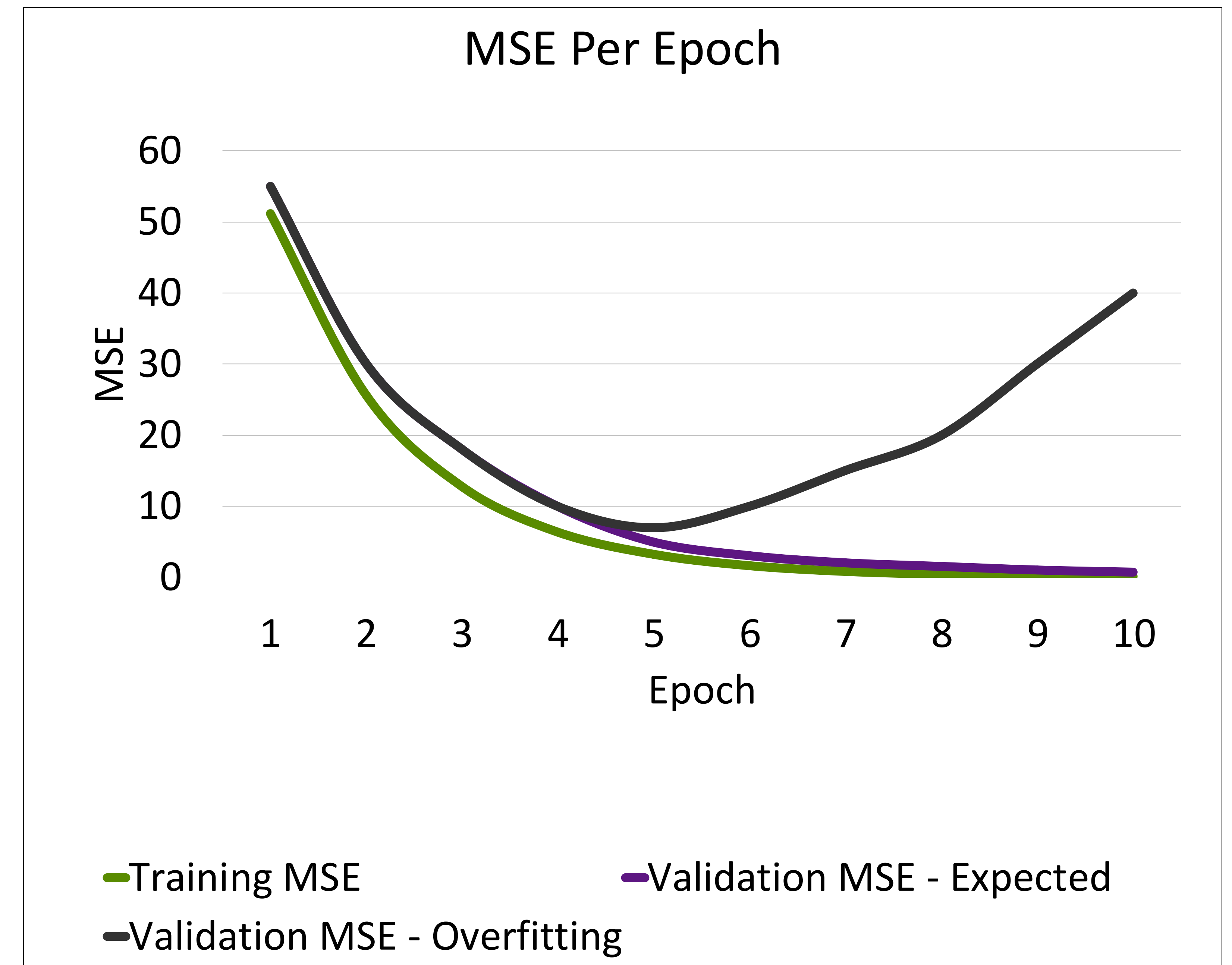
- Core dataset for the model to learn on


Validation data

- New data for model to see if it truly understands (can generalize)

Overfitting

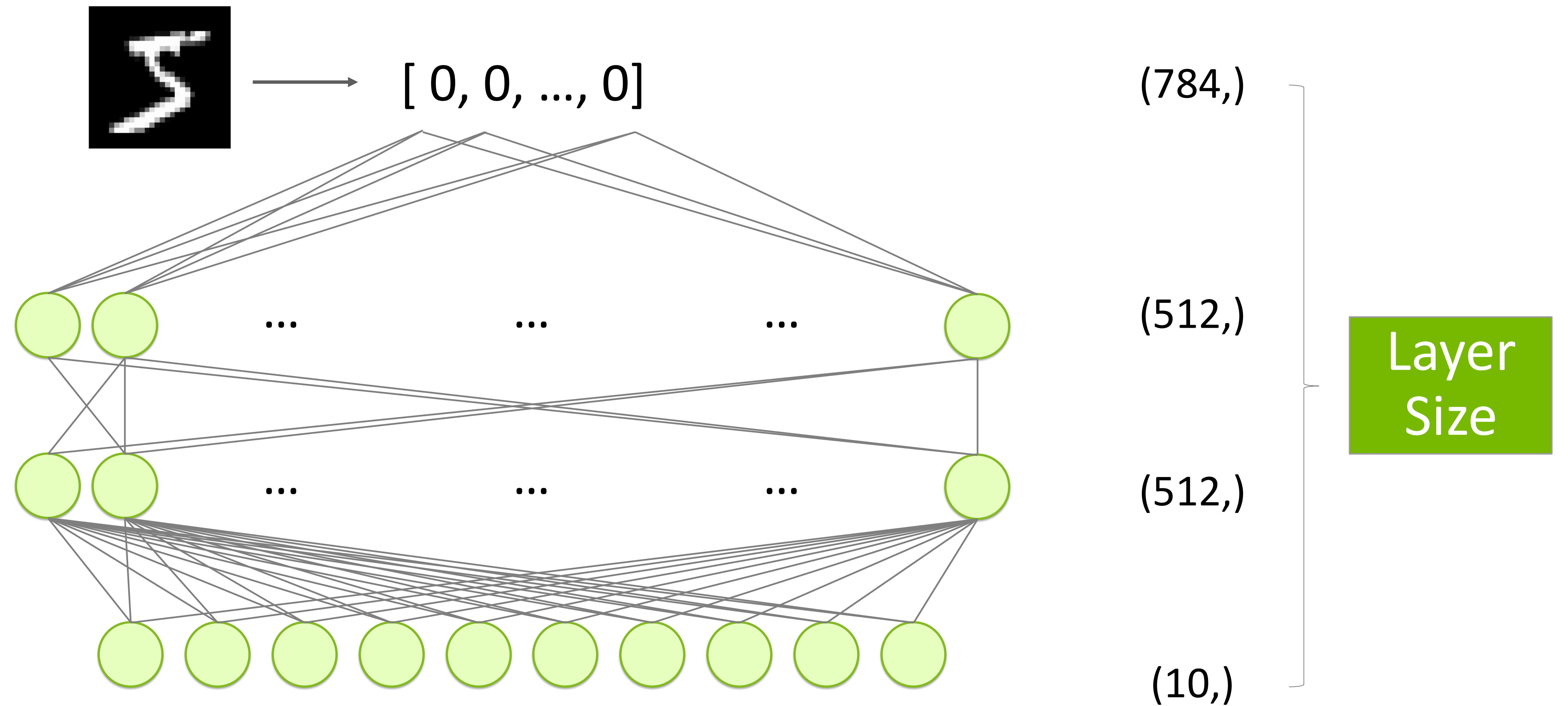
- When model performs well on the training data, but not the validation data (evidence of memorization)
- Ideally the accuracy and loss should be similar between both datasets





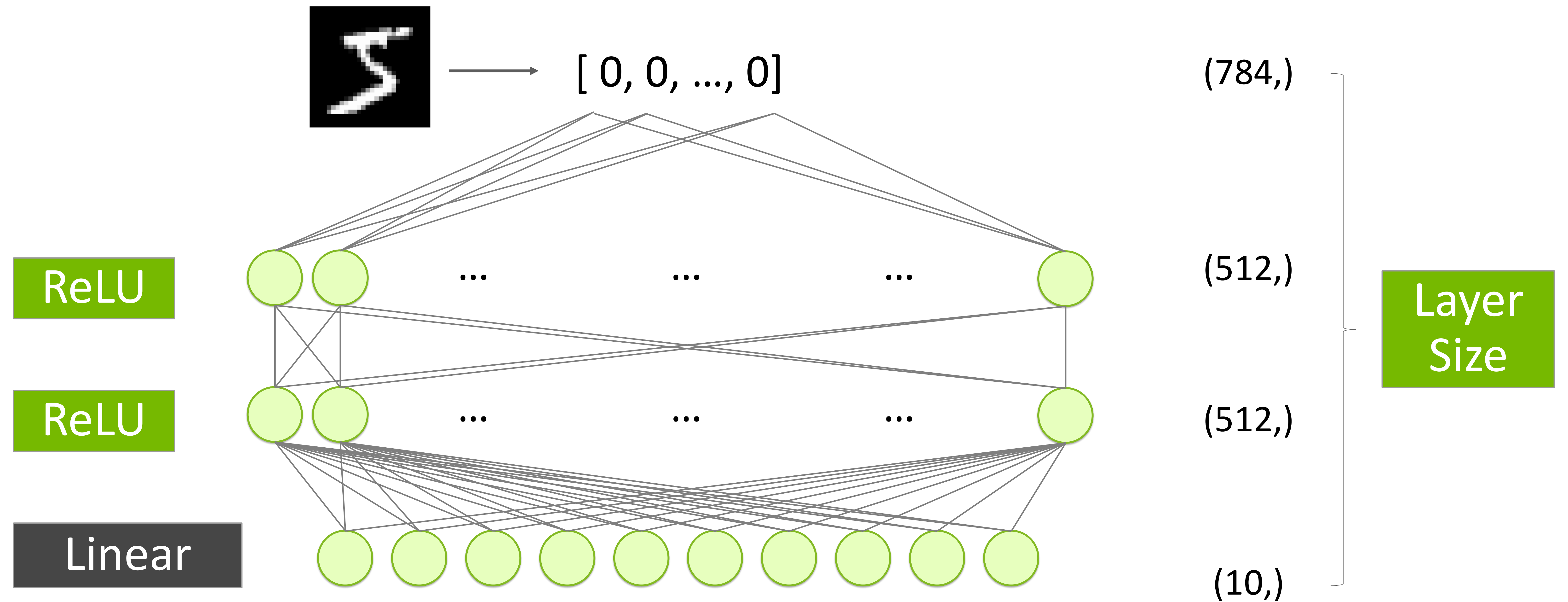
From Regression to Classification

An MNIST Model



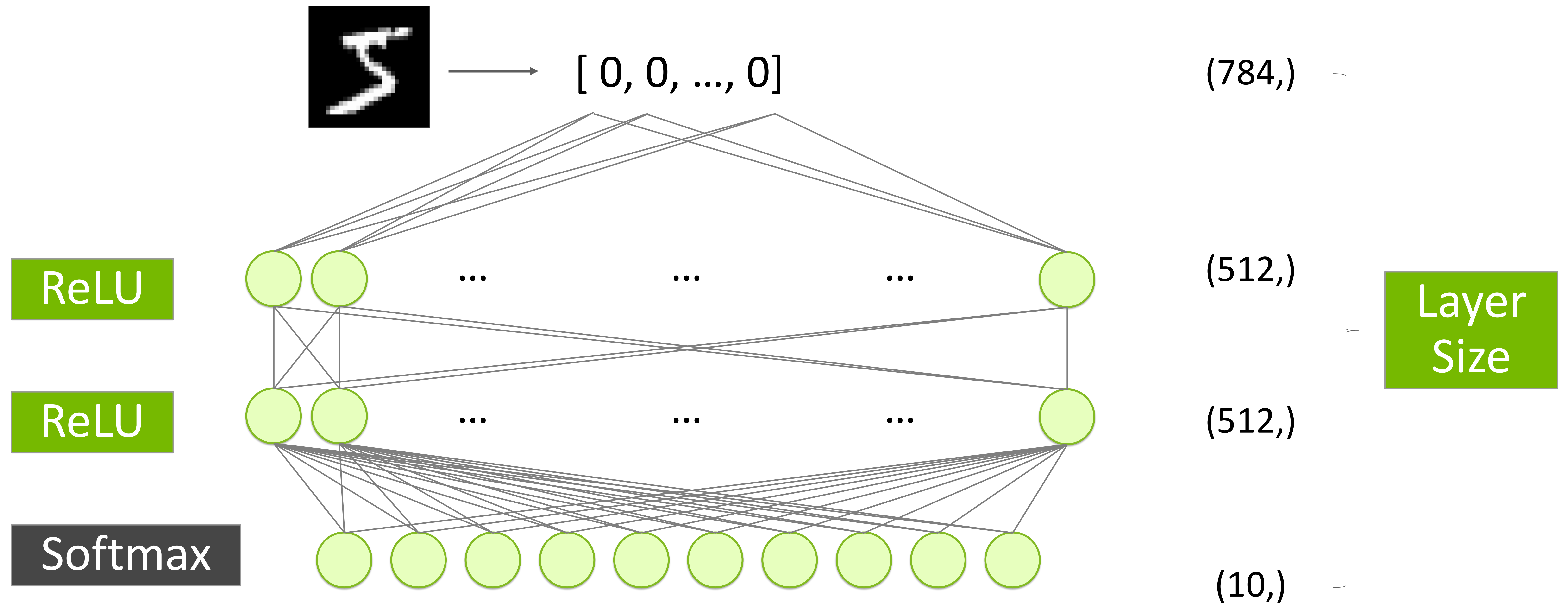
An MNIST Model

During Prediction

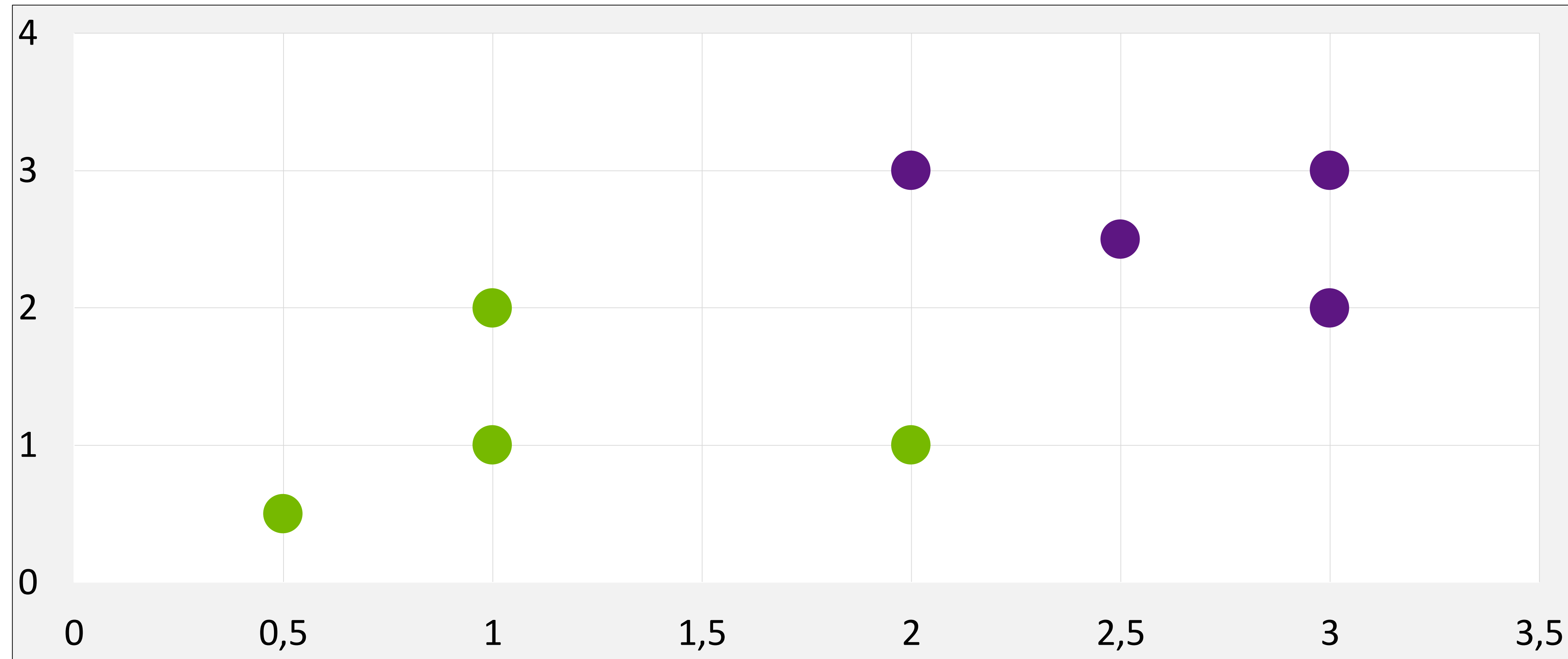


An MNIST Model

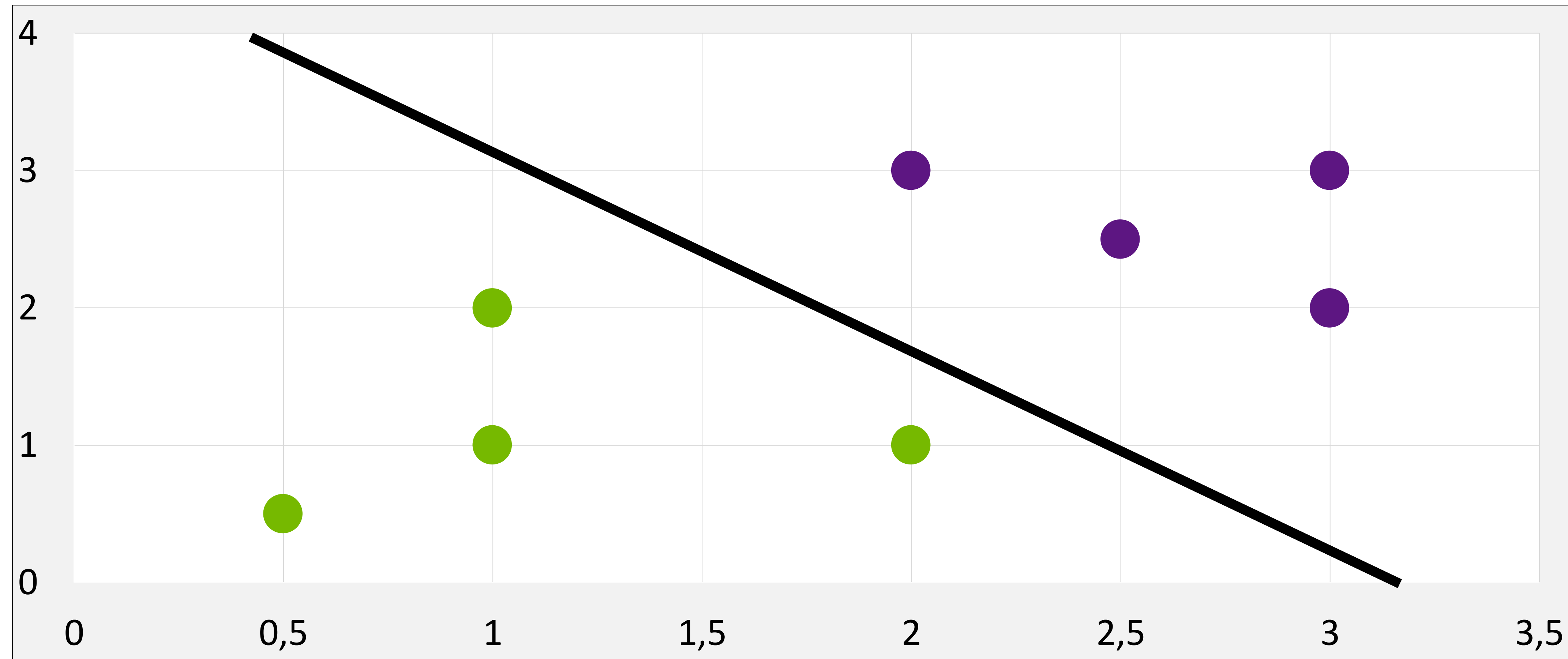
During Training



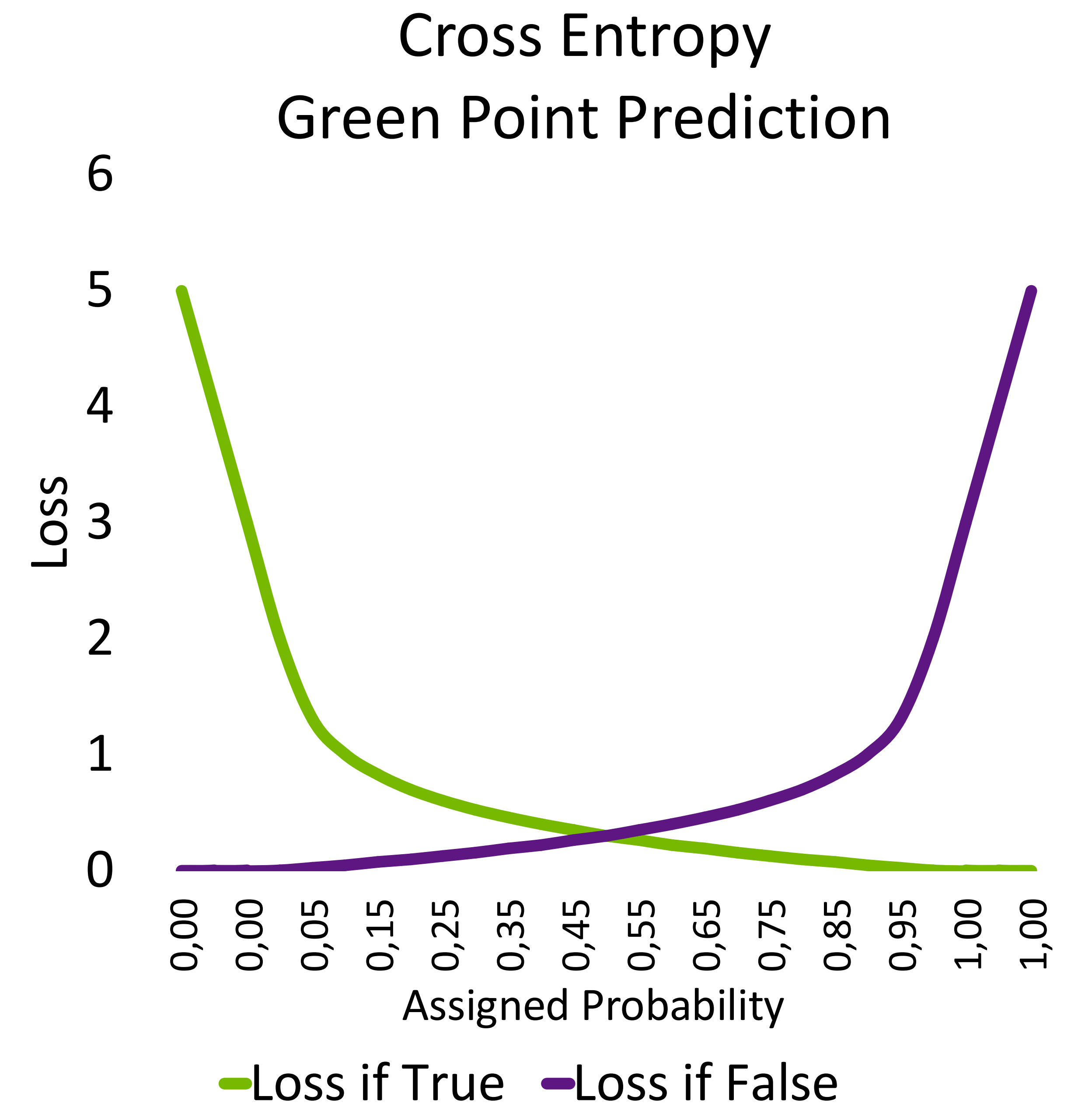
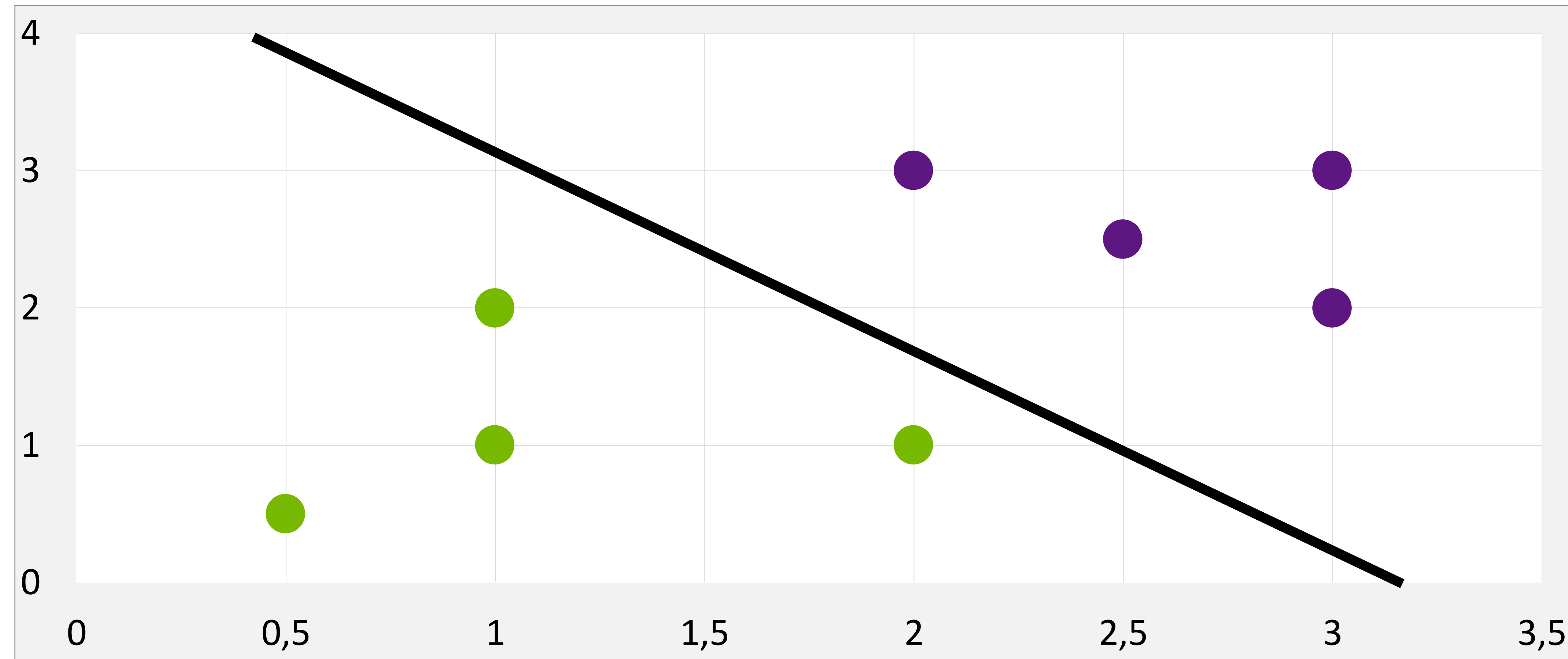
RMSE For Probabilities?



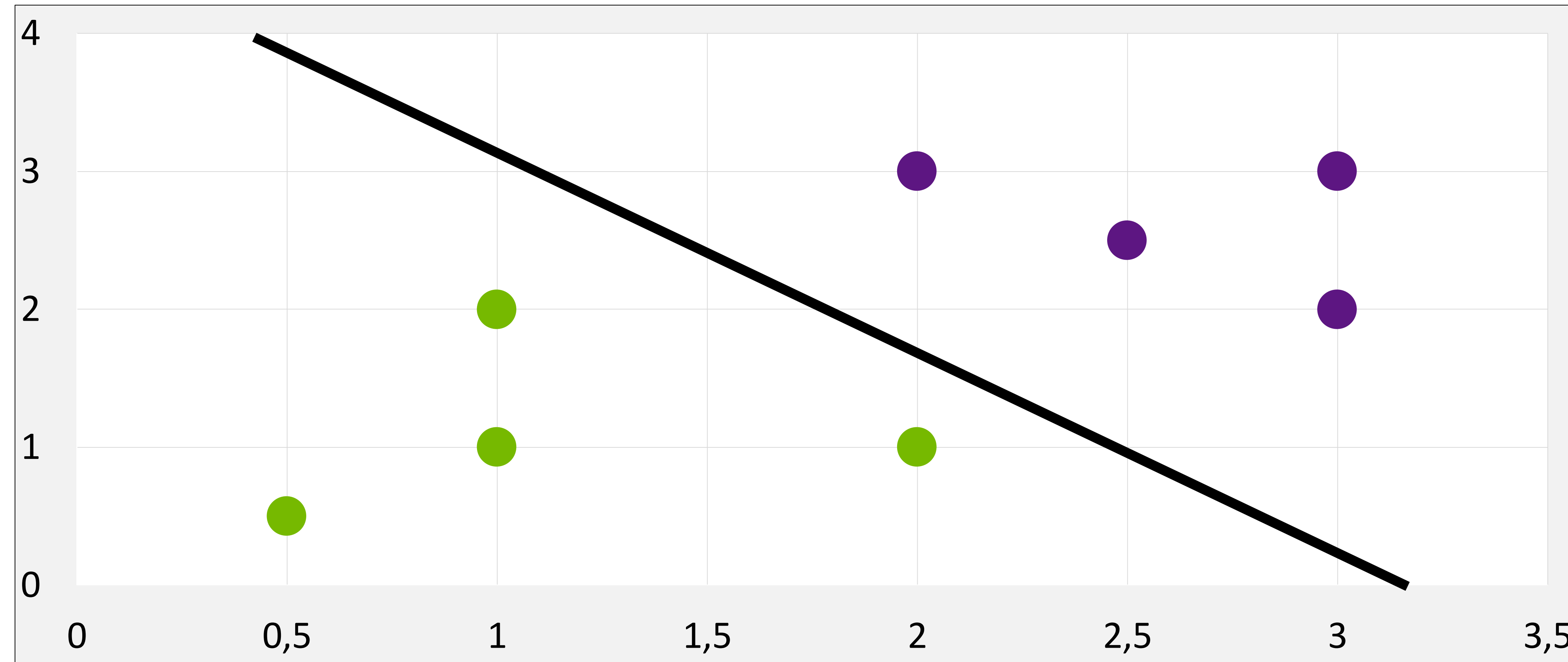
RMSE For Probabilities?



Cross Entropy



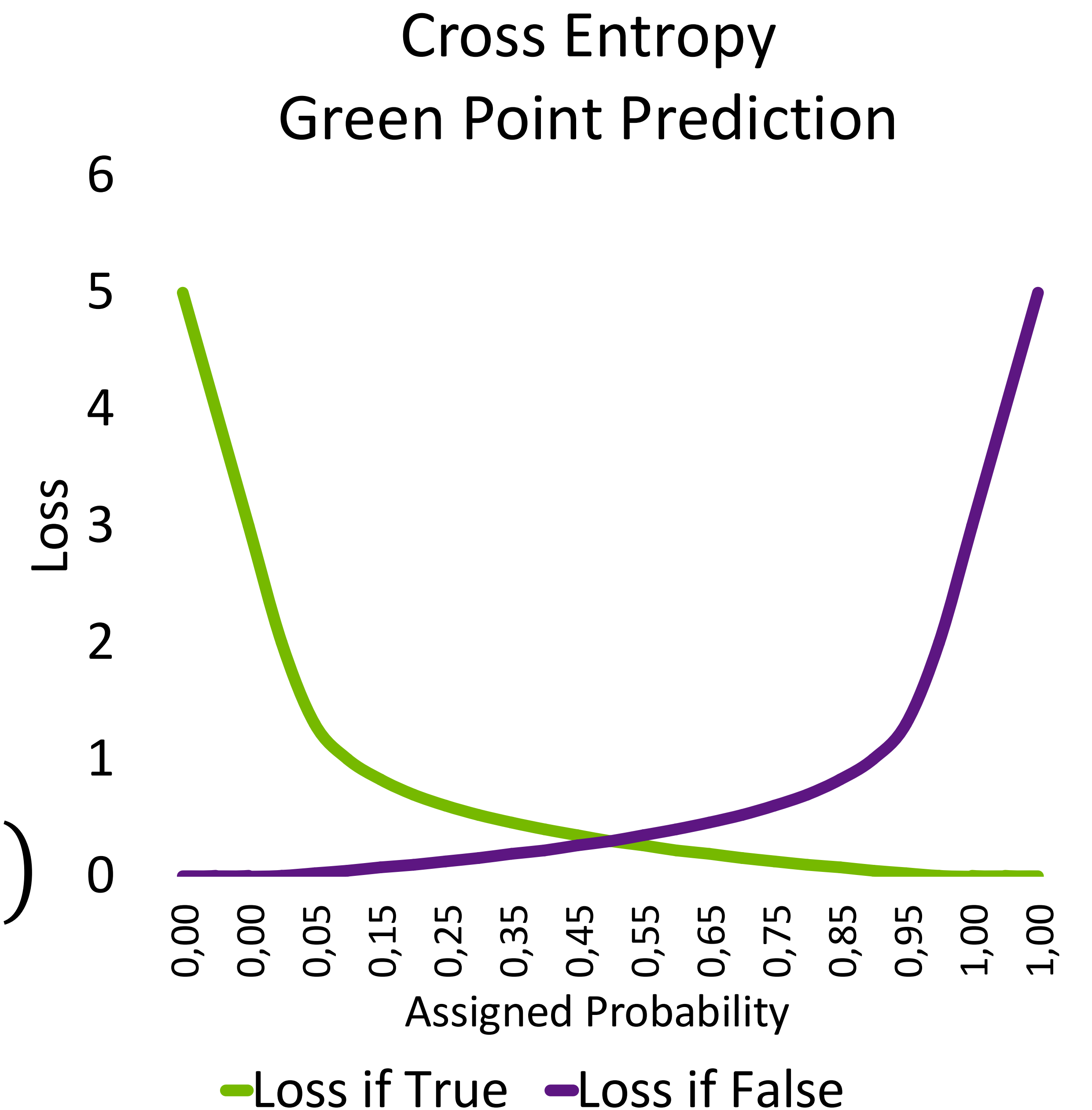
Cross Entropy



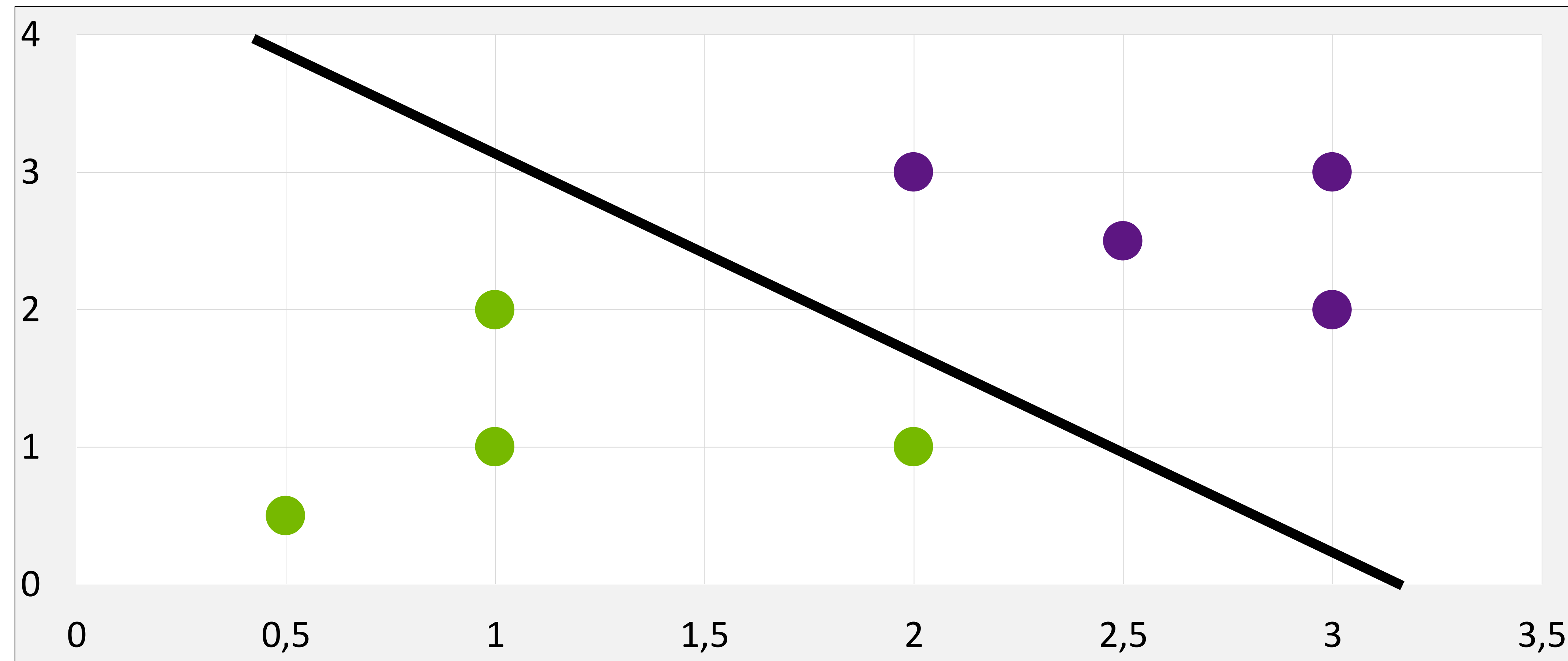
$$Loss = -((t(x) \cdot \log(p(x)) + (1 - t(x)) \cdot \log(1 - p(x)))$$

$t(x)$ = target (0 if False, 1 if True)

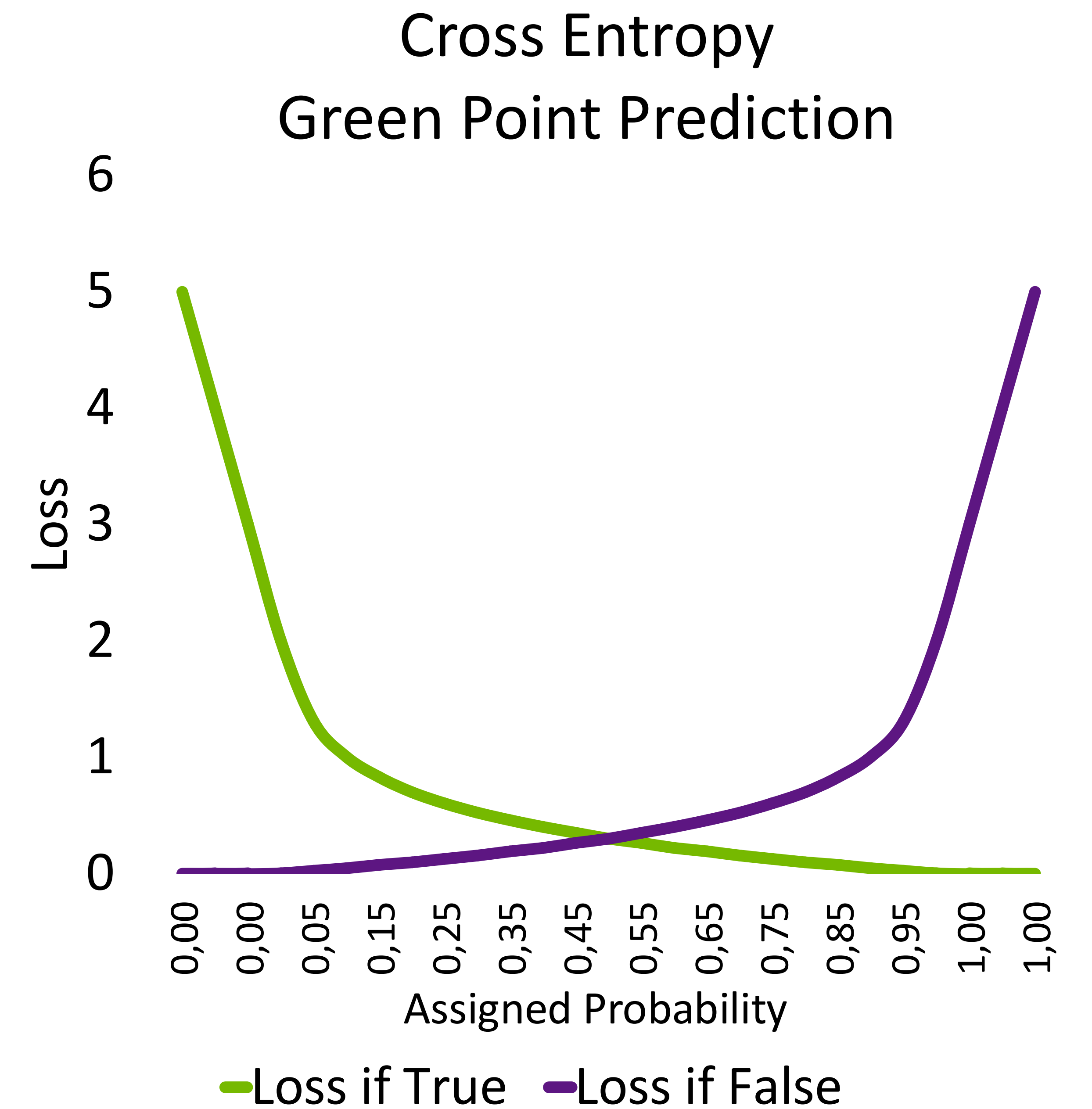
$p(x)$ = probability prediction of point x



Cross Entropy



```
1 def cross_entropy(y_hat, y_actual):  
2     """Infinite error for misplaced confidence."""  
3     loss = log(y_hat) if y_actual else log(1-y_hat)  
4     return -1*loss
```

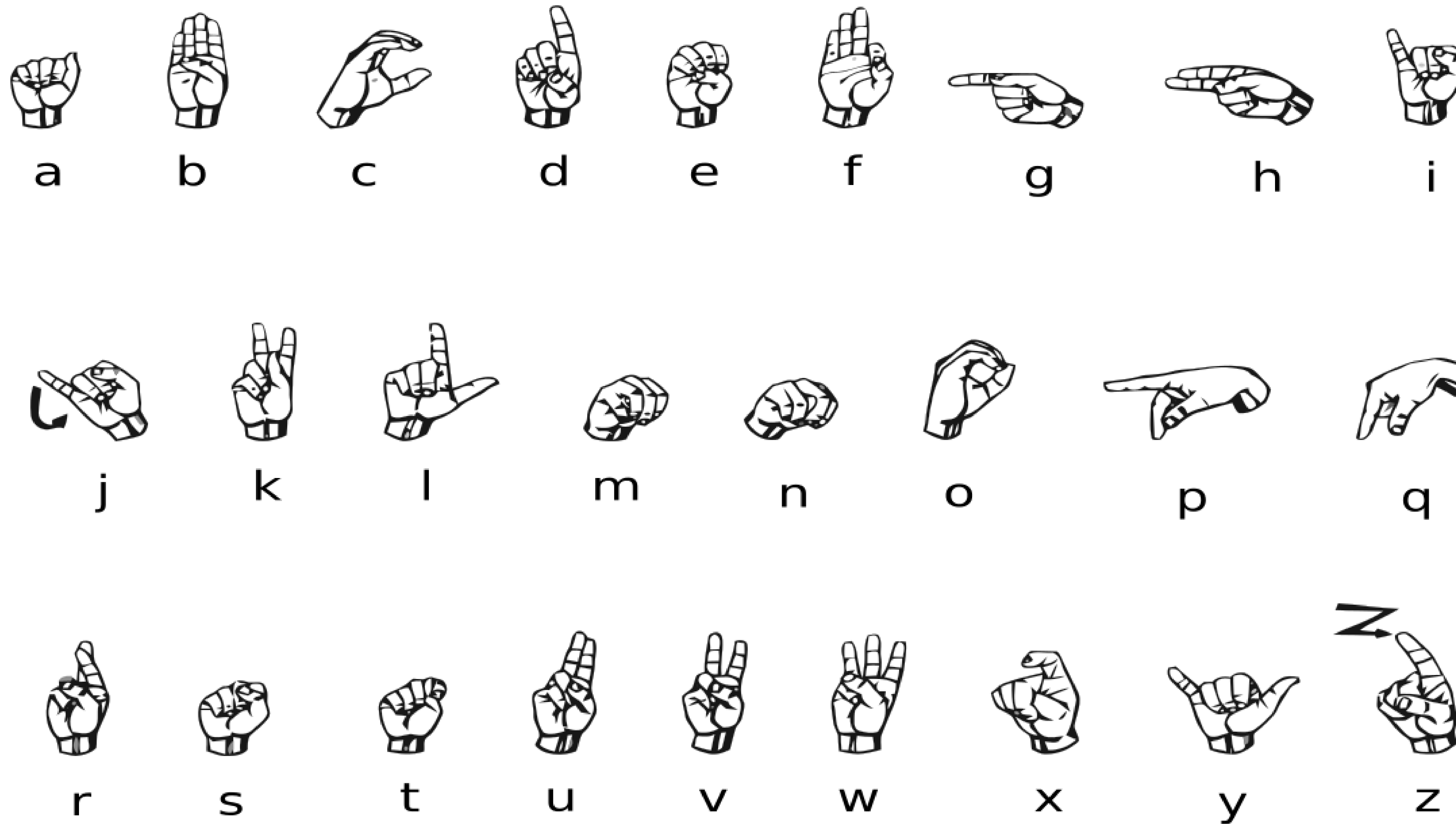




Bringing it Together

The Next Exercise

The American Sign Language Alphabet





Let's go!



Appendix: Gradient Descent

Helping the Computer Cheat Calculus

Learning from Error

$$MSE = \frac{1}{n} \sum_{i=1}^n (y - \hat{y})^2 = \frac{1}{n} \sum_{i=1}^n (y - (mx + b))^2$$

$$MSE = \frac{1}{2} ((3 - (m(1) + b))^2 + (5 - (m(2) + b))^2)$$

$$\frac{\partial MSE}{\partial m} = 5m + 3b - 13$$

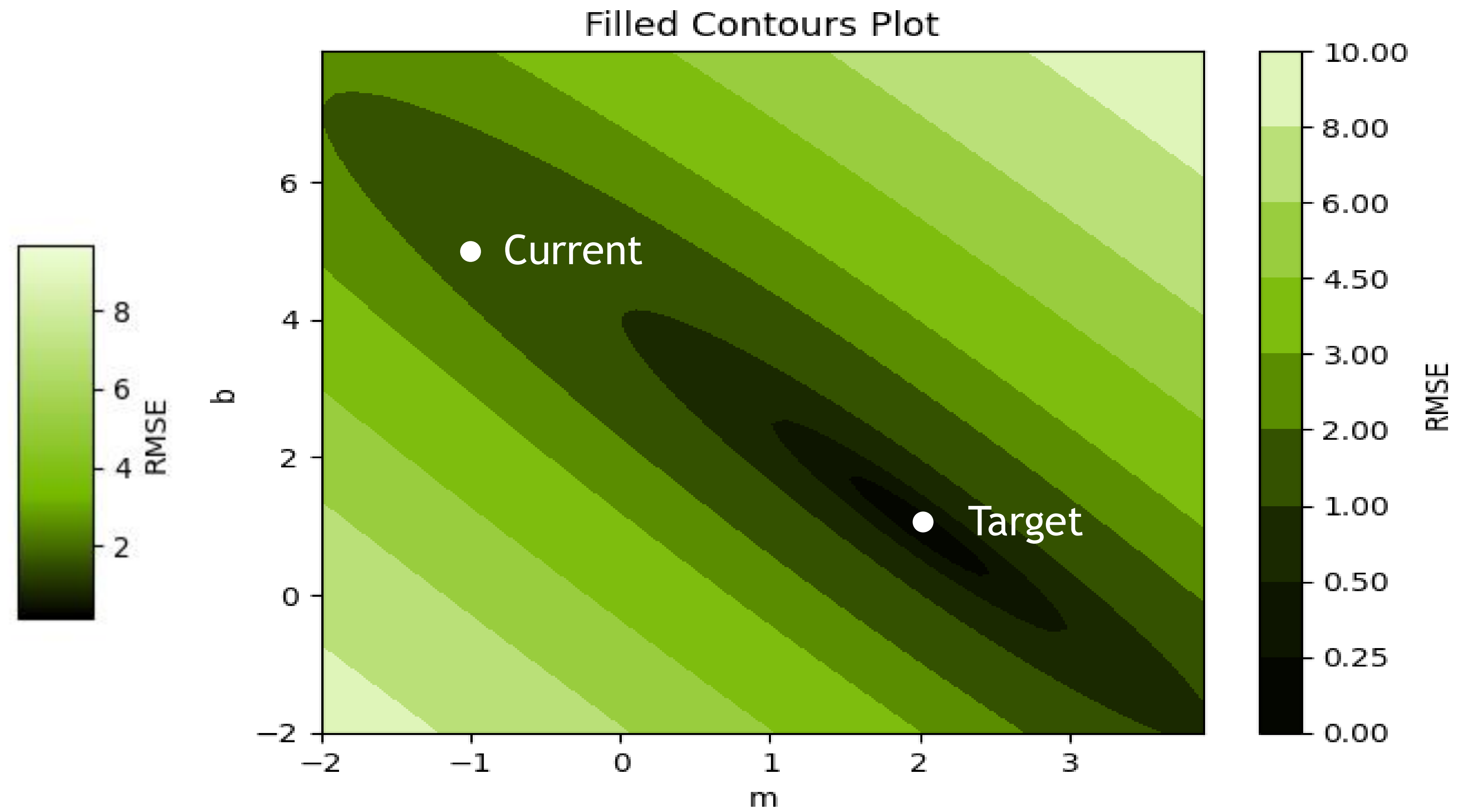
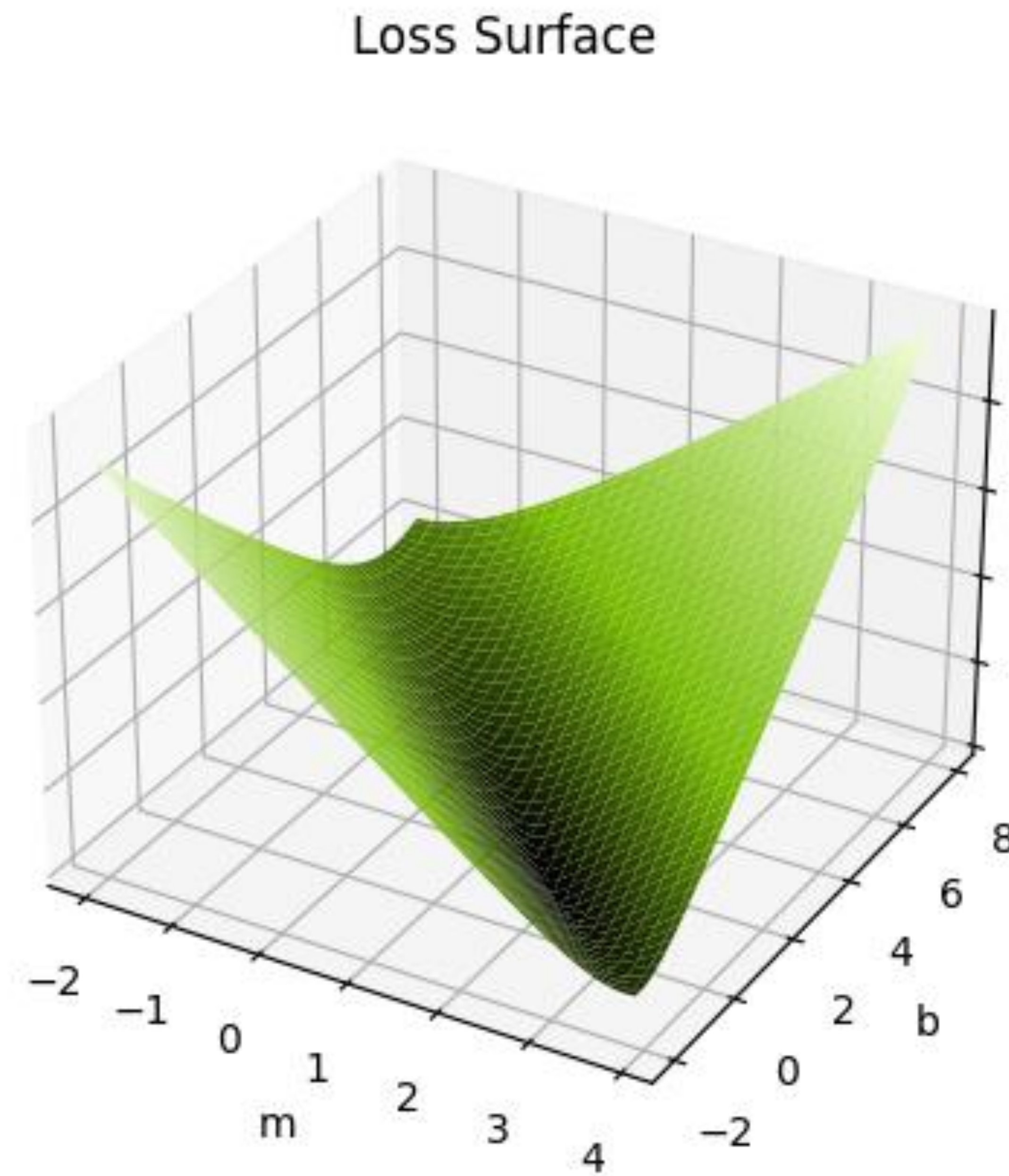
$$\frac{\partial MSE}{\partial b} = 3m + 2b - 8$$

$$\frac{\partial MSE}{\partial m} = -3$$

$$\frac{\partial MSE}{\partial b} = -1$$

$$m = -1$$
$$b = 5$$

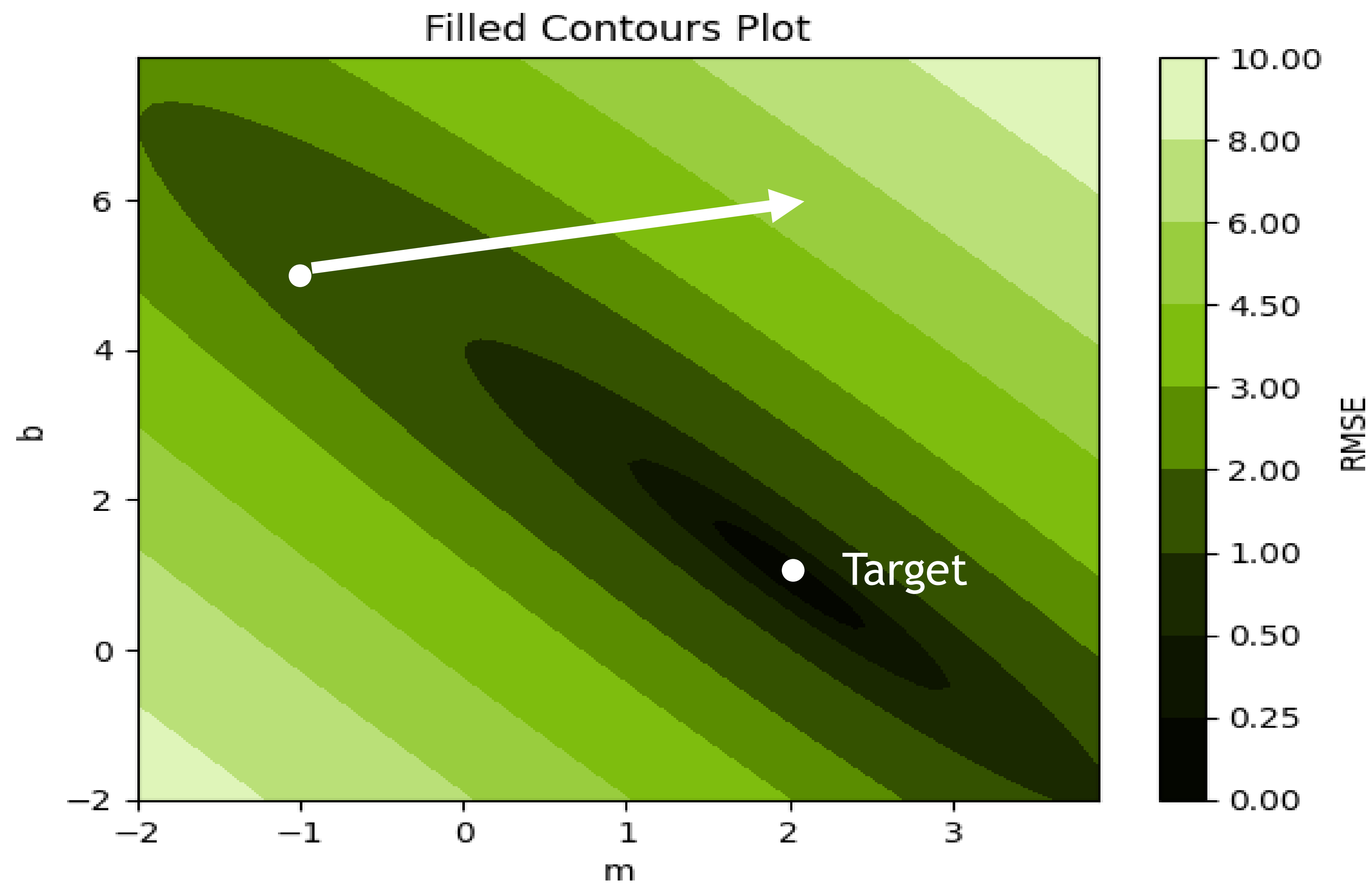
The Loss Curve



The Loss Curve

$$\frac{\partial MSE}{\partial m} = -3$$

$$\frac{\partial MSE}{\partial b} = -1$$

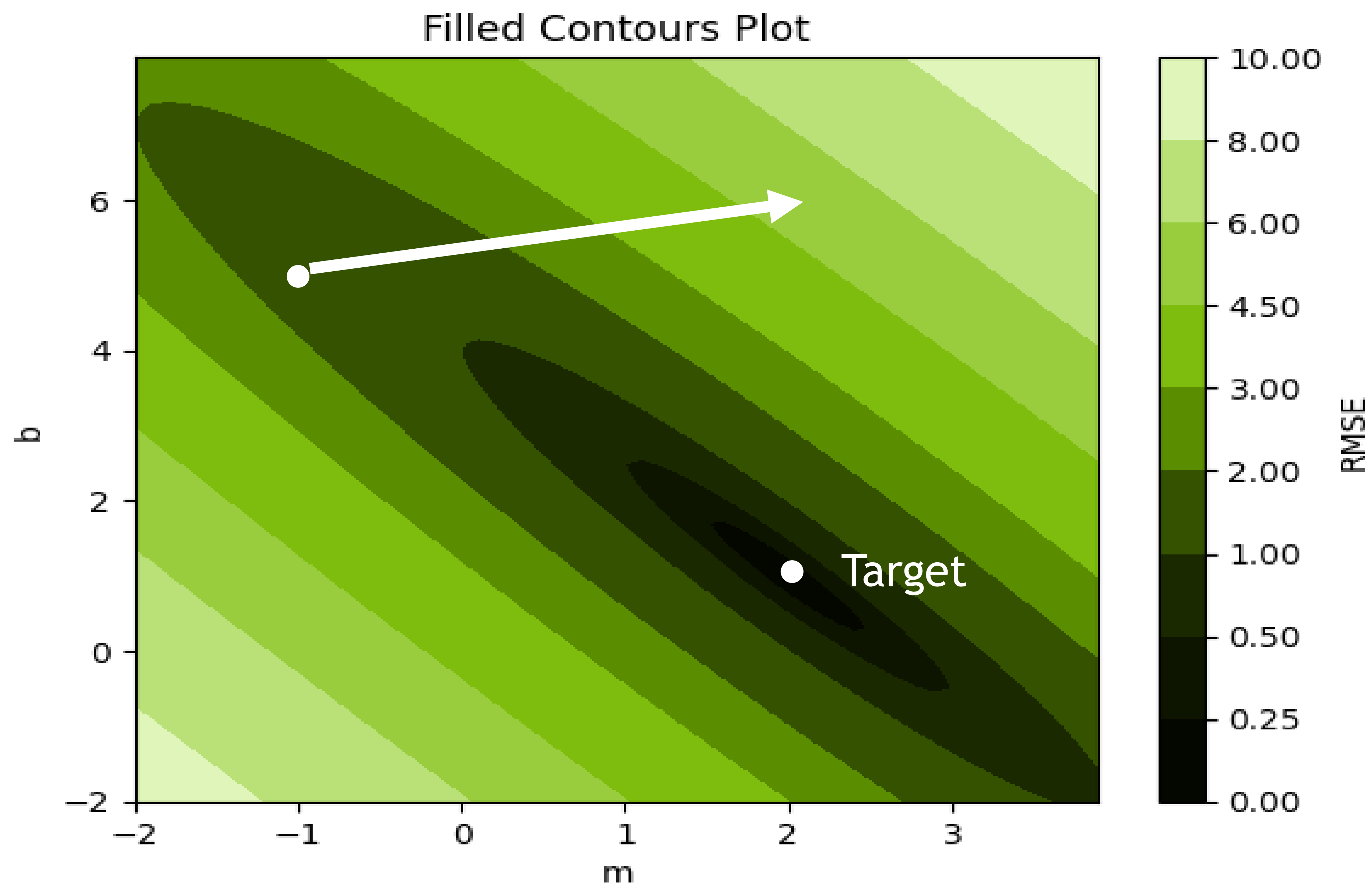


The Loss Curve

$$\frac{\partial MSE}{\partial m} = -3 \quad \frac{\partial MSE}{\partial b} = -1$$

$$m := m - \lambda \frac{\partial MSE}{\partial m}$$

$$b := b - \lambda \frac{\partial MSE}{\partial b}$$



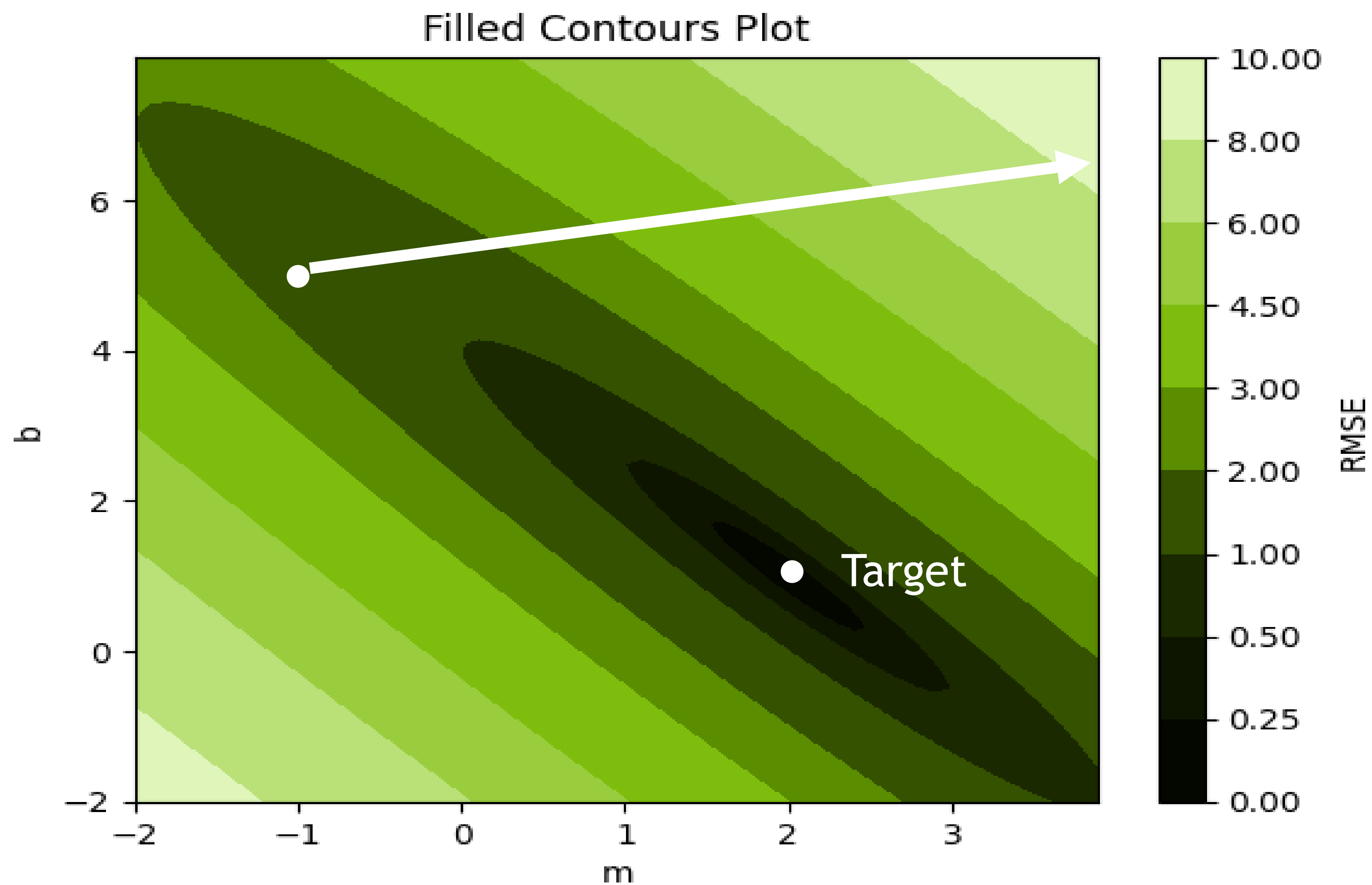
The Loss Curve

$$\frac{\partial MSE}{\partial m} = -3 \quad \frac{\partial MSE}{\partial b} = -1$$

$$m := m - \lambda \frac{\partial MSE}{\partial m}$$

$$\lambda = 2$$

$$b := b - \lambda \frac{\partial MSE}{\partial b}$$



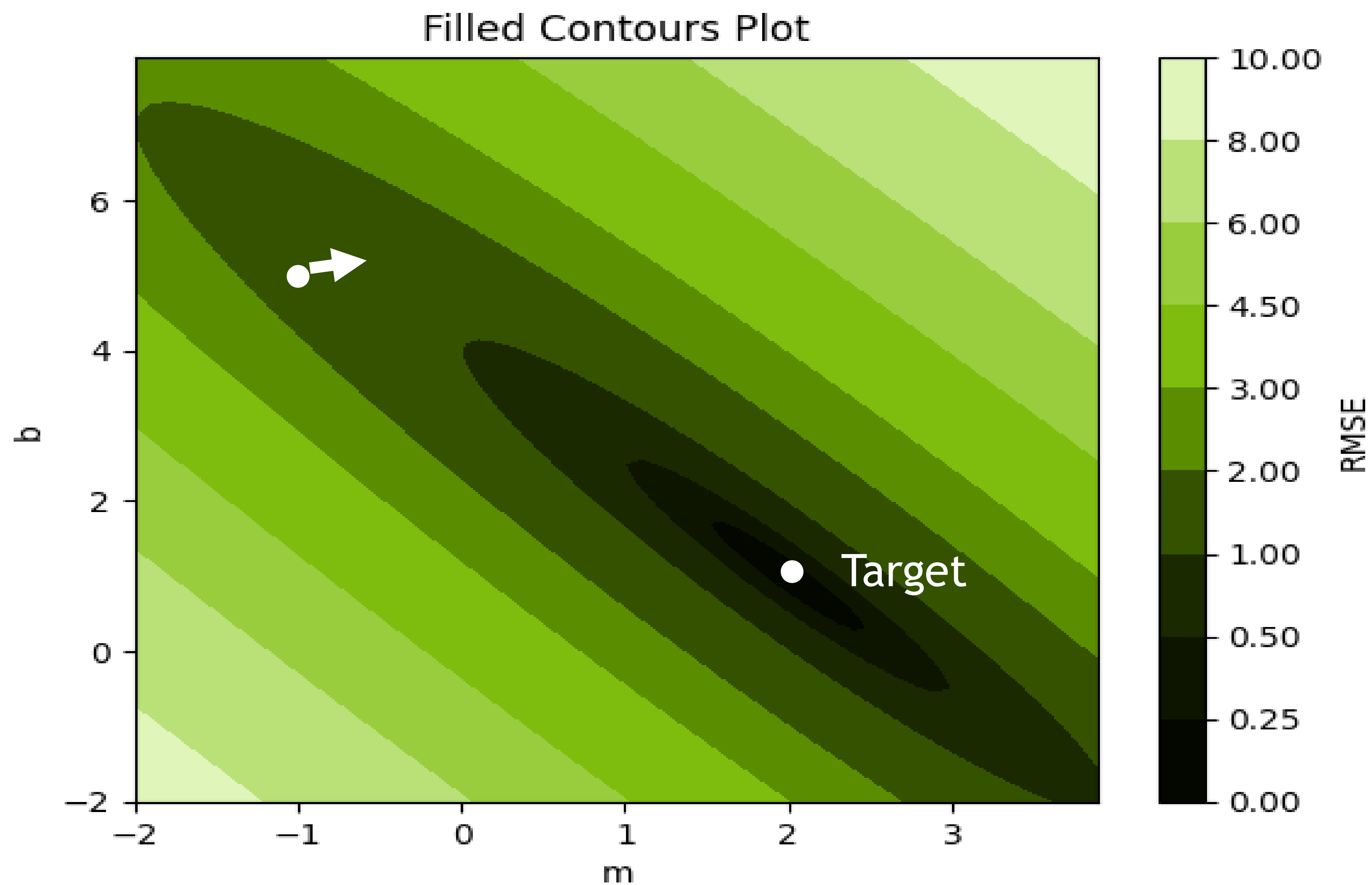
The Loss Curve

$$\frac{\partial MSE}{\partial m} = -3 \quad \frac{\partial MSE}{\partial b} = -1$$

$$m := m - \lambda \frac{\partial MSE}{\partial m}$$

$$\lambda = .1$$

$$b := b - \lambda \frac{\partial MSE}{\partial b}$$



The Loss Curve

$$\lambda = .1$$

$$m := -1 + 3 \lambda = -0.7$$

$$b := 5 + \lambda = 5.1$$

