

$$2.4b) \quad t^* = \frac{b_1}{556.3}$$

$$556.3 = \frac{MSE}{\sum (x_i - \bar{x})^2} = \frac{0.388}{2379.925} = 1.63 \times 10^{-4}$$

$$MSE = 0.388$$

$$t^* = \frac{0.039}{\sqrt{1.63 \times 10^{-4}}} = 3.05$$

$$3.05 > t(1 - 0.01/2, 118) = 2.62, H_1 = \text{True}$$

alternatives

$$H_0: B_1 = 0$$

$$H_1: B_1 \neq 0$$

decision rule

$$|t^*| \leq 2.86, H_0 = \text{True}$$

$$|t^*| > 2.86, H_1 = \text{True}$$

2.4c)

$$P\text{-value} = 0.0028$$

Since $0.0028 < 0.01$, we can conclude H_1

2.6 b)

alternatives

$$H_0: \beta_1 = 0$$

$$H_1: \beta_1 \neq 0$$

decision rule

$$|t^*| \leq t(1-0.05/2; 10-2) = 2.306, H_0 = T$$

$$|t^*| > 2.306, H_1 = \text{True}$$

$$t^* = \frac{b_1}{s\{b_1\}} = \frac{4}{\sqrt{0.22}} = 8.53 > 2.306, H_1 = \text{True}$$

$$s^2\{b_1\} = 0.22$$

$$p\text{-value} = 2.75 \times 10^{-5}$$

Since $2.75 \times 10^{-5} < 0.05$, we can conclude H_1

2.14 a)

$$\hat{Y} = 89.6$$

confidence interval = (87.29, 91.98)

$$87.29 \leq E\{Y_h\} \leq 91.98$$

2.27a)

$$\hat{Y} = 156.35 - 1.19x$$

alternatives

decision rule

$$H_0: \beta_1 \geq 0$$

$$H_0 = \text{True if } t^* \geq -1.67$$

$$H_1: \beta_1 < 0$$

$$H_1 = \text{True if } t^* < -1.67$$

$$t^* = -13.19 < -1.67. \text{ Thus } H_1 = \text{True}$$

$$p\text{-score} = 2.06 \times 10^{-19} = 0+$$

b)

No, it cannot because the dataset/scope of the model does not include newborns (or $x=0$).

2.27c)

$$t(0.975, 58) = 2.0017$$

$$b_1 = -1.19$$

$$-1.19 - (2.0017 \cdot 0.0902) \leq \beta_1 \leq -1.19 + (2.0017 \cdot 0.0902)$$

$$-1.37 \leq \beta_1 \leq -1.01$$

It's not important to know the specific ages for this estimate because we use the slope, t value, & the se. of the slope to get our estimate. And since the slope is the average of our data as a whole, we know then with 95% confidence that women whose age differs by one year has decreased muscle mass between -1.37 & -1.01

2.65)

Infection Risk = X_1

$$0.534 \leq \beta_1 \leq 0.987$$

Available facilities & services = X_2

$$0.023 \leq \beta_1 \leq 0.067$$

Routine Chest X-ray = X_3

$$0.021 \leq \beta_1 \leq 0.055$$

The X_2 & X_3 variables seem to have a similar slope & confidence interval at 95%. But Infection risk's slope is larger than the others