

# Exercise\_Regression\_5.3

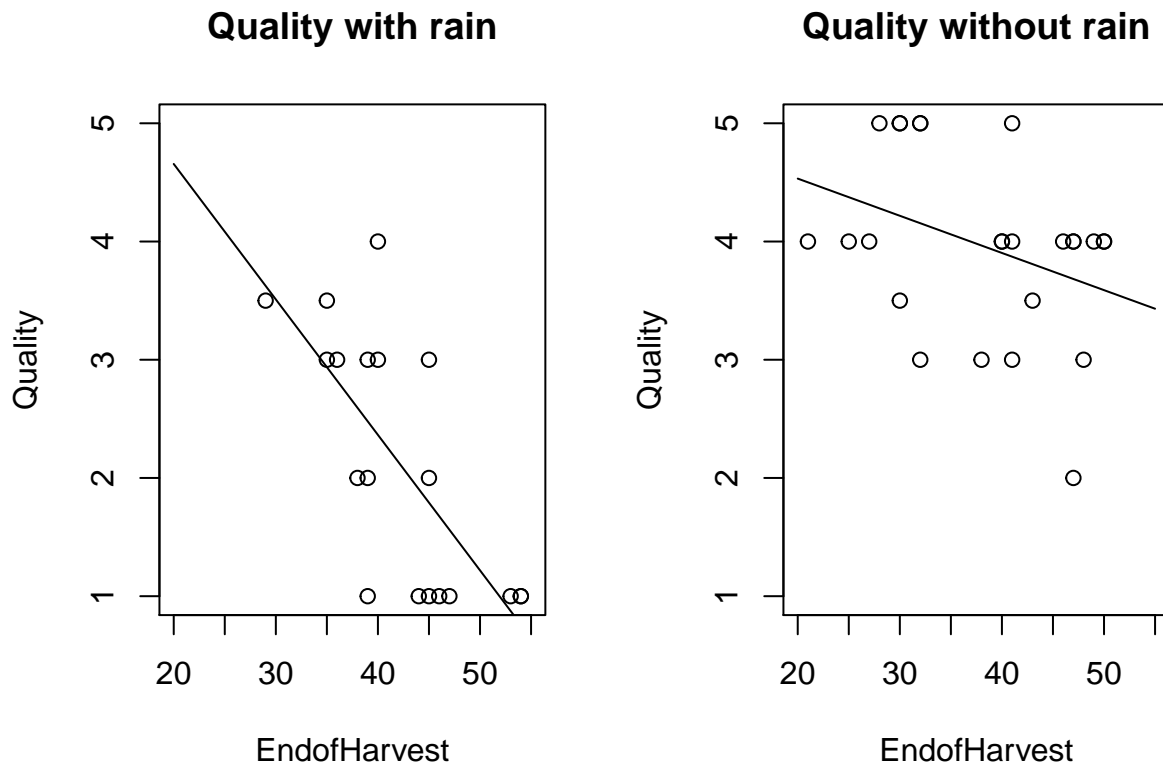
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*May 20, 2016*

The exercise uses information from the data set [Latour.txt](#)

## Task a)

```
dataT <- read.table("Latour.txt",header=TRUE)
par(mfrow=c(1,2))
x <- seq(20,55,0.1)
yrain <- 5.16122 - 0.03145*x + 1.78670 - 0.08314*x
yn0 <- 5.16122 - 0.03145*x
plot(dataT[dataT$Rain==1,]$EndofHarvest,dataT[dataT$Rain==1,]$Quality,
     main='Quality with rain', xlab='EndofHarvest', ylab='Quality', xlim=c(20,55), ylim=c(1,5))
lines(x,yrain)
plot(dataT[dataT$Rain==0,]$EndofHarvest,dataT[dataT$Rain==0,]$Quality,
     main='Quality without rain', xlab='EndofHarvest', ylab='Quality', xlim=c(20,55), ylim=c(1,5))
lines(x,yn0)
```



```
fit <- lm(dataT$Quality~dataT$EndofHarvest + dataT$Rain + dataT$EndofHarvest*dataT$Rain)
fit
```

```
##
## Call:
## lm(formula = dataT$Quality ~ dataT$EndofHarvest + dataT$Rain +
##     dataT$EndofHarvest * dataT$Rain)
##
## Coefficients:
##              (Intercept)              dataT$EndofHarvest
##                   5.16122                   -0.03145
##              dataT$Rain  dataT$EndofHarvest:dataT$Rain
##                   1.78670                   -0.08314
```

From this fit, we can see that  $\beta_0 = 5.16122$ ,  $\beta_1 = -0.03145$ ,  $\beta_2 = 1.78670$ , and  $\beta_3 = -0.08314$ , in the formula (5.10) given in the exercise. Based on the above 2 plots, as well as the information about the values for the  $\beta$ , the rate of change in quality clearly depends on whether there has been any unwanted rain during vintage.

## Task b)

We invert the functions for  $y_{no}$  and  $y_{rain}$ , and check the values for  $x$  in the area  $y = 4$  and  $y = 3$ , and see the difference. Since the functions  $y_{no}$  and  $y_{rain}$  are linear functions, this is going to give us an estimate relevant for question b).

$$y_{rain} = 6.94792 - 0.11459x \Leftrightarrow x_{rain} = \frac{-y+6.94792}{0.11459}$$

$$\text{We get } days_{rain} = \frac{-3+6.94792}{0.11459} - \frac{-4+6.94792}{0.11459} = 8.726765$$

$$y_{norain} = 5.16122 - 0.03145x \Leftrightarrow x_{norain} = \frac{-y+5.16122}{0.03145}$$

$$\text{We get } days_{norain} = \frac{-3+5.16122}{0.03145} - \frac{-4+5.16122}{0.03145} = 31.7965$$

So we have that you lose 1 entire quality point every 31.7965 days of harvest if there is no unwanted rain and every 8.726765 days of harvest if there IS unwanted rain.