

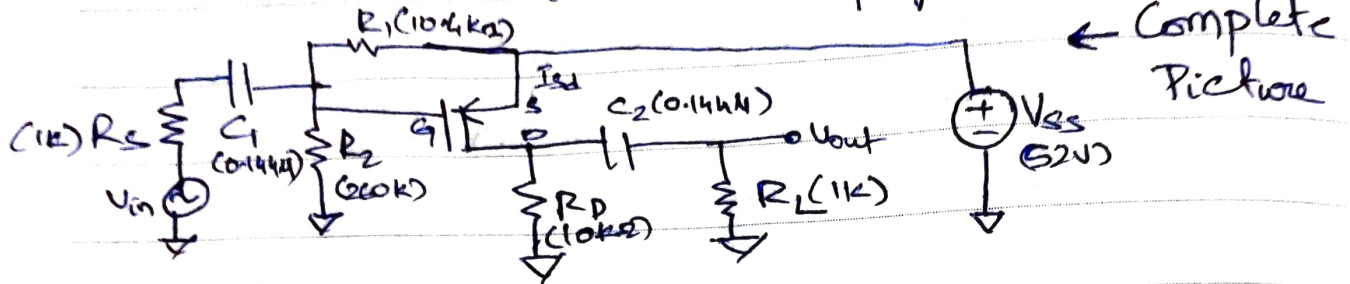


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## Assignment-3

### 1) PMOS Common Source Amplifier.



← Complete Picture

Given  $\mu_p C_{ox} \frac{W}{L} = 10^{-2}$   $g_m R_L = 10$  (Gain assuming  $R_D \gg R_L$ )

$R_L = R_S = 1k\Omega \Rightarrow g_m = 10m$

(Ignoring 'd' effects)

And  $I_{SD} = \frac{\mu_p C_{ox} W}{2L} (V_{SG} - V_T)^2 \Rightarrow g_m = \frac{\mu_p C_{ox} W}{L} (V_{SG} - V_T)$

$\Rightarrow 10^2 = 10^2 (V_{SG} - 1)$

$\Rightarrow V_{SG} = 2V$

And for saturation we need,  $V_{SD} \geq V_{SG} - V_T = 1V \Rightarrow V_{SD} = 2V$

As  $R_D \gg R_L$ , let's take  $R_D = 10R_L = 10k\Omega$ . Then

$V_{SD} = V_{SS} - I_{SD} R_D \Rightarrow V_{SS} = V_{SD} + I_{SD} R_D$

$\Rightarrow V_{SS} = 2V + \left( \frac{10^{-2} (1)^2}{2} \times 10 \times 10^3 \right) = 5.2V \Rightarrow V_{SS} = 5.2V$

And for  $V_{SG} = V_{SS} \frac{R_1}{R_1 + R_2} \Rightarrow \frac{R_1}{R_1 + R_2} = \frac{2}{5.2} = \frac{1}{2.6}$

$\Rightarrow R_1 = R$  then  $R_2 = 2.5R$ . But we know  $R_1 || R_2 \gg R_S$

So let  $R_1 || R_2 = 10 \times R_S \Rightarrow \frac{R \times 2.5R}{2.6R} = 10 \times 1k$

Hence we get,

$R_1 = \frac{260}{2.5} k = 10.4k\Omega$  and

$R_2 = 260k\Omega$

$\Rightarrow R = \frac{260 \times 2.5}{2.6} k$



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And for capacitances, at the input side, the effective time constant is given by

$$\tau = C(R_s + (R_1 \parallel R_2)) \text{ and we know minimum}$$

frequency  $10 \text{ kHz} \Rightarrow \omega = 2\pi \text{ K rad/s}$  and

$$\omega_{in} \gg \frac{1}{RC} \Rightarrow \omega_{in} = \frac{10}{RC} \Rightarrow C = \frac{10}{R \times \omega_{in}}$$

$$\Rightarrow C_1 = \frac{10}{(R_s + R_1 \parallel R_2) \times 2\pi \text{ K}} = \frac{10}{11\text{K} \times 2\pi \text{ K}} = \frac{10}{22\pi} \mu$$

$$\Rightarrow \boxed{C_1 = 0.144 \mu} \text{ Similarly for}$$

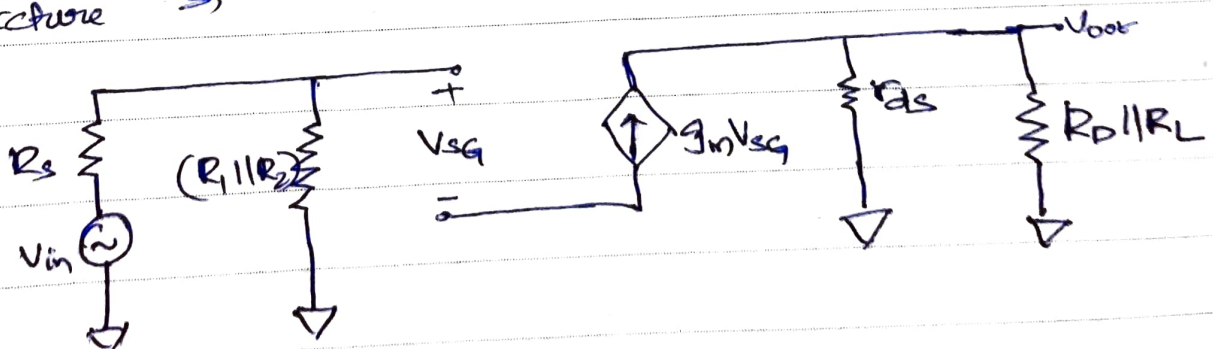
Output side  $R_{eff} = R_D + R_L$  and  $\omega_{in} \gg \frac{1}{RC}$ , then

$$\text{even } C_2 \text{ turns out to be } \frac{10}{11\text{K} \times 2\pi \text{ K}} \Rightarrow \boxed{C_2 = 0.144 \mu}$$

For the incremental picture, we have  $\lambda = 0.001 \text{ V}^{-1}$

$$\text{and } I_{DQ} = 5 \text{ mA} \Rightarrow g_m = \lambda I_{DQ} = 5 \text{ mS and } \boxed{r_{ds} = 0.2 \text{ M}\Omega}$$

Incremental gain  
Picture  $\rightarrow$





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2) Given NMOS device Characteristics param:  
 $\frac{W}{L} = 1$   $\mu_n C_{ox} = 100 \mu A/V^2$   $V_T = 1V$   $\lambda = 0.001 V^{-1}$

Assume that region of operation is always in saturation  $\Rightarrow I_{ds} = \frac{\mu_n C_{ox} W}{2L} (V_{gs} - V_T)^2$  (neglecting  $\lambda$ )

Intrinsic gain:  $\frac{V_o}{V_{in}} = -g_m r_{ds}$  ;  $r_{ds} = \frac{1}{g_{ds}} = \frac{1}{I_{ds} \lambda}$

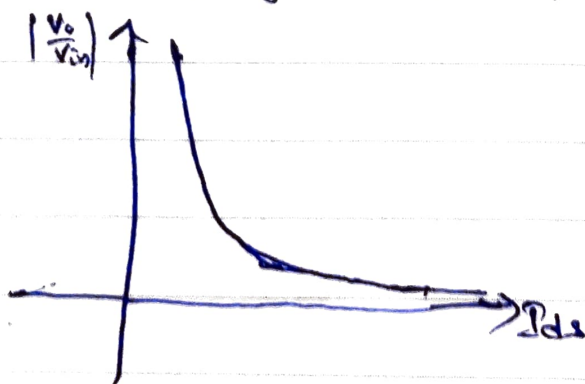
$$\Rightarrow \frac{V_o}{V_{in}} = - \left( \frac{\mu_n C_{ox} W}{L} (V_{gs} - V_T) \right) \cdot \frac{1}{\mu_n C_{ox} \frac{W}{2L} (V_{gs} - V_T)^2 \lambda}$$

$$= - \frac{2}{(V_{gs} - V_T) \lambda} = \frac{-2}{\sqrt{\frac{2L I_{ds}}{\mu_n C_{ox} W}} \lambda}$$

$$= - \frac{1}{\lambda} \sqrt{\frac{\mu_n C_{ox} W}{L}} \cdot \frac{1}{I_{ds}}$$

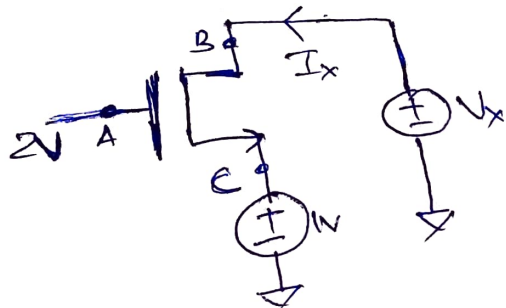
$$= - \sqrt{\frac{2 \times 100 \times 10^{-6} \times 1}{10^{-3} \times 10^{-3}}} \cdot \frac{1}{I_{ds}} = - \sqrt{\frac{200}{I_{ds}}}$$

Ignoring the sign for magnitude, we get





3)



$$\mu_n C_{ox} = 100 \mu A V^{-2}$$

$$V_T = 1V$$

$$\frac{W}{L} = 1$$

If we consider that NMOS, is symmetric w.r.t drain and source, i.e., the driving voltage is at the drain then

A will remain Gate but, for

$0V \leq V_x \leq 1V$  : C  $\rightarrow$  Drain B  $\rightarrow$  ~~Gate~~ Source

and when  $V_x > 1V$  : B  $\rightarrow$  Drain C  $\rightarrow$  Source

When  $0V \leq V_x \leq 1V$  :  $V_{DS} = 1 - V_x$

$$V_{GS} = 2 - V_x$$

$$V_{GS} - V_T = 1 - V_x$$

Just in saturation,

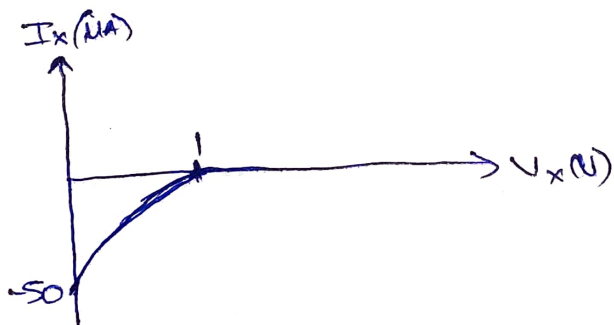
$$\begin{aligned} \text{Then } I_x &= -I_{DS} = -100 \mu \cdot \frac{1}{2} (1 - V_x)^2 \\ &= -50 (1 - V_x)^2 \mu A \end{aligned}$$

And when  $V_x > 1V$  : The  $V_{DS} = V_x - 1$

$$V_{GS} = 2 - 1 = 1V$$

$$V_{GS} - V_T = 0V \rightarrow \text{Cutoff}$$

$$I_x = 0$$

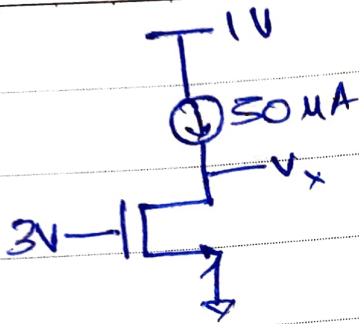




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4)



$$\mu_n C_{ox} = 100 \mu A V^{-2}$$

$$V_T = 1V \quad \frac{W}{L} = 1$$

Here  $I_{ds}$  is driven at  $50 \mu A$ .

Assume that NMOS is in saturation, then the corresponding

$$I_{ds} = \frac{\mu_n C_{ox} W}{2L} (V_{gs} - V_T)^2 = 100 \times 10^{-6} \times \frac{1}{2} (3 - 1)^2 = 200 \mu A$$

, but we only need  $50 \mu A$ .

$\therefore$  The NMOS is in linear region (triode region). Then we get

$$I_{ds} = 50 \mu A = \frac{\mu_n C_{ox} W}{L} (V_{gs} - V_T) V_{ds} - \frac{V_{ds}^2}{2}$$

$$\Rightarrow 50 \times 10^{-6} = 100 \times 10^{-6} \times 1 \left( 2(V_x) - \frac{V_x^2}{2} \right)$$

$$\Rightarrow 1 = 2V_x - \frac{V_x^2}{2} \Rightarrow V_x^2 - 4V_x + 1 = 0$$

$$\Rightarrow V_x = \frac{4 \pm \sqrt{16 - 4}}{2} = \frac{4 \pm 2\sqrt{3}}{2}$$

$$= 2 \pm \sqrt{3} V$$

As the NMOS is in linear region,  $V_{ds} > \frac{V_{gs} - V_T}{2}$   
 $\Rightarrow V_x > 2$

$$\therefore \boxed{V_x = 2 + \sqrt{3} V}$$