

## 1. What is dt?

$dt = \text{time step}$   
 $dt$  is small amount of time the simulation moves forward in each update.

Examples:

- $dt = 1 \text{ ms} \rightarrow$  neuron updates every 0.001 seconds
- $dt = 0.5 \text{ ms} \rightarrow$  updates even more frequently
- $dt = 5 \text{ ms} \rightarrow$  slower update, less detail

Simple idea:

$dt = \text{"how fast the clock ticks" inside the simulation}$

## 2. Why do neurons update every millisecond?

→ Because real biological neuron fire & change voltage at millisecond precision.  
 To capture this, simulations also use very small dt values.

Brain works fast → simulation must also update fast.

## 3. Continuous vs Discrete Simulation

Real neuron:

- Voltage changes smoothly every moment (continuous time)

Computer simulation:

- Computer cannot update continuously
- So it updates in small jumps (discrete time)

Example:

Continuous = smooth flow

Discrete = step by step

Simulation mimics real behavior by using very small steps (dt).

## 4. Why smaller dt = smoother voltage curves?

Because the neuron updates more often

- More updates = small changes each time → smooth line
- Fewer updates = big jumps → rough / jagged line

Like drawing a curve with:

- 100 dots → smooth
- 10 dots → zig-zag

Smaller dt = more detail = more accurate simulation

## 5. What happens at each dt step? (simulation loop)

At each dt interval the neuron checks:

1. Input coming in?

2. Add input → voltage increases (integration)

3. Leak some voltage (decay)

4. If voltage > threshold → fire spike

5. Reset voltage

6. Move to next dt

This repeats like:

$$\begin{aligned} t &= 0 \\ t &= dt \\ t &= 2 \cdot dt \\ t &= 3 \cdot dt \end{aligned}$$

...  
 Simulation loop = time moves in small jumps.

\* short

- $dt = \text{"frame" of the brain movie}$
- Smaller dt = more frames → smoother
- Neurons change quickly → use ms-level dt
- Computer uses discrete steps
- Each dt = update the neuron once