Numpy: Lecture 4

- **Broadcasting**. The term **broadcasting** describes how **numpy** treats arrays with different shapes during arithmetic operations. Subject to certain constraints, the smaller array is "**broadcast**" across the larger array so that they have compatible shapes.
- Broadcasting is a powerful mechanism that allows numpy to work with arrays of different shapes when performing arithmetic operations. Frequently we have a smaller array and a larger array, and we want to use the smaller array multiple times to perform some operation on the larger array.

Alternative to Broadcasting

- For example, suppose that we want to add a constant vector to each row of a matrix. We could do it like this:
- import numpy as np

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- # We will add the vector v to each row of the matrix x,
- # storing the result in the matrix y
- x = np.array([[1,2,3], [4,5,6], [7,8,9], [10, 11, 12]])
- v = np.array([1, 0, 1])
- $y = np.empty_like(x) # 4,3$ Create an empty matrix with the same shape as x

Alternative to Broadcasting

- # Add the vector v to each row of the matrix x with an explicit loop
- **for** i **in** range(4):
- y[i, :] = x[i, :] + v

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- # Now y is the following
- # [[2 2 4]
- # [5 5 7]
- # [8 8 10]
- # [11 11 13]]
- print(y)

Alternative to Broadcasting

- This works; however when the matrix x is very large, computing an explicit loop in Python could be slow.
- Note that adding the vector v to each row of the matrix x is equivalent to forming a matrix vv by stacking multiple copies of v vertically.
- Then performing elementwise summation of x and vv. We could implement this approach like this:

Using Tile

```
• import numpy as np

    # We will add the vector v to each row of the matrix x,

    # storing the result in the matrix y

• x = np.array([[1,2,3], [4,5,6], [7,8,9], [10, 11, 12]])
• v = np.array([1, 0, 1])
• vv = np.tile(v, (4, 1)) # Stack 4 copies of v on top of each other
• print(vv) # Prints "[[1 0 1]
               # [101]
                # [101]
                    [1 0 1]]"
• y = x + vv # Add x and vv elementwise
print(y) # Prints "[[ 2 2 4
       #
             [5 5 7]
       # [8 8 10]
             [11 11 13]]"
```

- Numpy broadcasting allows us to perform this computation without actually creating multiple copies of v. Consider this version, using broadcasting:
- import numpy as np

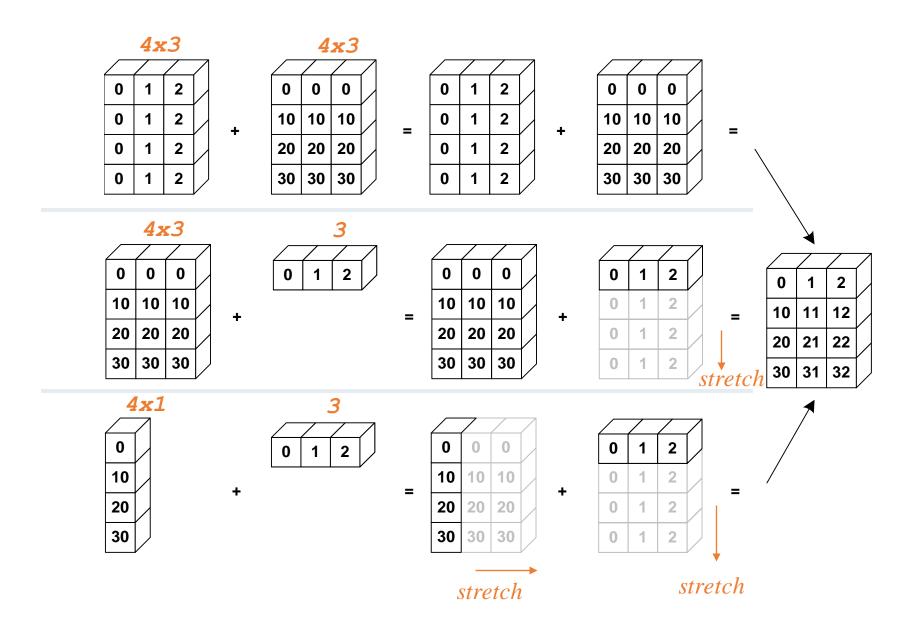
```
•
```

- # We will add the vector v to each row of the matrix x,
- # storing the result in the matrix y
- x = np.array([[1,2,3], [4,5,6], [7,8,9], [10, 11, 12]])
- v = np.array([1, 0, 1])
- y = x + v # Add vto each row of x using broadcasting
- print(y) # Prints "[[2 2 4]
- # [557]
- # [8 8 10]
- # [11 11 13]]"

• The line y = x + v works even though x has shape (4, 3) and v has shape (3,) due to broadcasting; this line works as if v actually had shape (4, 3), where each row was a copy of v, and the sum was performed elementwise.

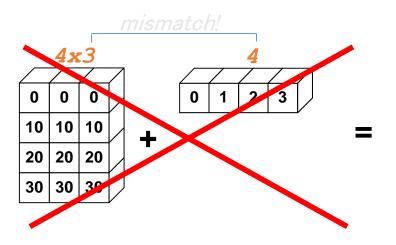
• Broadcasting typically makes your code more concise and faster, so you should strive to use it where possible.

Array Broadcasting



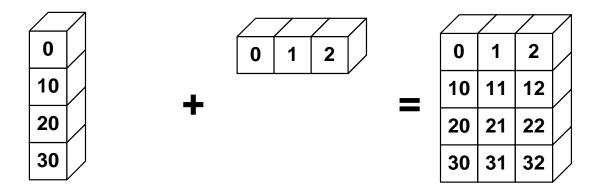
Broadcasting Rules

The *trailing* axes of both arrays must either be 1 or have the same size for broadcasting to occur. Otherwise, a "ValueError: frames are not aligned" exception is thrown.



Broadcasting in Action

```
>>> a = array((0,10,20,30))
>>> b = array((0,1,2))
>>> y = a[:, None] + b
```



- Broadcasting two arrays together follows these rules:
- If the arrays do not have the same rank, prepend the shape of the lower rank array with 1s until both shapes have the same length.
- The two arrays are said to be *compatible* in a dimension if they have the same size in the dimension, or if one of the arrays has size 1 in that dimension.
- The arrays can be broadcast together if they are compatible in all dimensions.
- After broadcasting, each array behaves as if it had shape equal to the elementwise maximum of shapes of the two input arrays.
- In any dimension where one array had size 1 and the other array had size greater than 1, the first array behaves as if it were copied along that dimension

- import numpy as np
- # Compute outer product of vectors
- v = np.array([1,2,3]) # v has shape (3,)
- w = np.array([4,5]) # w has shape (2,)
- # To compute an outer product, we first reshape v to be a column vector of shape (3, 1);
- we can then broadcast it against w to yield an output of shape (3, 2), which is the outer product of v and w:
- #[[45] [810] [1215]]
- print(np.reshape(v, (3, 1)) * w)
- # Add a vector to each row of a matrix
- x = np.array([[1,2,3], [4,5,6]])
- # x has shape (2, 3) and v has shape (3,) so they broadcast to (2, 3),
- # giving the following matrix:
- # [[2 4 6]
- # [5 7 9]]
- **print**(x + v)
- # Add a vector to each column of a matrix
- # x has shape (2, 3) and w has shape (2,).
- # If we transpose x then it has shape (3, 2) and can be broadcast

- # against w to yield a result of shape (3, 2); transposing this result
- # yields the final result of shape (2, 3) which is the matrix x with
- # the vector w added to each column. Gives the following matrix:
- #[[567]
- # [9 10 11]]
- print((x.T + w).T)
- # Another solution is to reshape w to be a column vector of shape (2, 1);
- # we can then broadcast it directly against x to produce the same
- # output.
- **print**(x + np.reshape(w, (2, 1)))
- •
- # Multiply a matrix by a constant:
- #x has shape (2, 3). Numpy treats scalars as arrays of shape ();
- # these can be broadcast together to shape (2, 3), producing the
- # following array:
- #[[246]
- # [81012]]
- print(x * 2)

When there are multiple inputs, then they all must be "broadcastable" to the same shape.

- All arrays are promoted to the same number of dimensions (by pre-prending 1's to the shape)
- All dimensions of length 1 are expanded as determined by other inputs with non-unit lengths in that dimension.

```
x = [1,2,3,4];
y=[[10],[20],[30]]
                                        x has shape (4,) the ufunc
print N.add(x,y)
                                        sees it as having shape (1,4)
[[11 12 13 14]
 [21 22 23 24]
                                        y has shape (3,1)
 [31 32 33 34]]
x = array(x)
                                        The ufunc result has shape
y = array(y)
                                        (3,4)
print x+y
[[11 12 13 14]
 [21 22 23 24]
 [31 32 33 34]]
```