

Advanced Inventory Management System

Design an **Inventory Management System** for a warehouse using advanced Java Collections. The warehouse has the following requirements:

1. **Inventory Tracking:**

- Each item in the inventory has a unique ID, a name, a category (e.g., electronics, furniture, groceries), and a quantity.
- You need to store these items efficiently to support operations such as searching, adding, updating, and deleting items based on their unique ID.

2. **Category-wise Sorting and Retrieval:**

- Items within a category should always be sorted in descending order of their quantity.
- Efficient retrieval of all items belonging to a particular category is required.

3. **Restocking Notifications:**

- If the quantity of any item drops below a specified threshold, it should trigger a notification (console output).

4. **Bulk Operations:**

- Allow merging of two inventories while ensuring no duplicate item IDs exist. In case of duplicate IDs, retain the item with the higher quantity.

5. **Complex Query Support:**

- Provide a function to retrieve the top **k** items with the highest quantity, regardless of category.

Constraints:

- The system should handle at least **100,000 items** efficiently.
- Your solution should make optimal use of Java's collection framework classes like **Map**, **Set**, **Queue**, or any others as needed.

Deliverables:

1. A well-documented Java class implementing the inventory system.
2. A test suite to demonstrate the functionality and edge cases of the implemented system.