Part 3: RA (12 points)

Write relational algebra expressions equivalent to Booktown queries 2, 3, 4 and 5 listed above. (2+3+3+4 points) (Notice that you do not need to represent the sorted order of the results of the queries in your relational algebra expressions. There may be a possibility for partial credit.)

Query2:

$$\pi_{\text{Subject}}(\sigma_{\text{Book_ID} = \text{NULL}}(\text{Subjects} \bowtie \text{Subject_ID} = \text{Books}, \text{Subject_ID})))$$

Query3:

$$\rho(E, Editions) \wedge \rho(B, Books) \wedge \rho(A, Authors)$$

$$\pi_{ISBN}(\sigma_{B.Book_ID} = E.Book_ID \text{ AND } B.Author_ID = A.Author_ID \text{ AND } A.First_Name = 'Agatha' \text{ AND } A.Last_Name = 'Christie'}$$
 (E X B X A))

Query4:

$$\rho(A, Authors) \land \rho(B1, Books) \land \rho(B2, Books) \land \rho(S1, Subjects) \land \rho(S2, Subjects)$$

$$\boldsymbol{\pi}_{A.First_Name, A.Last_Name}(\boldsymbol{\sigma}_{A.Author_ID} \text{ in } (\boldsymbol{\pi}_{B1.Author_ID}(\boldsymbol{\sigma}_{S1.Subject = 'Children/YA'}(B1 \bowtie B1.Subject_ID = S1.Subject_ID))) x A.Author_ID in } (\boldsymbol{\pi}_{A.Author_ID}(\boldsymbol{\sigma}_{S2.Subject = 'Fiction'}(B2 \bowtie B2.Subject_ID = S2.Subject_ID))) A)$$

Query5:

```
\begin{split} &\rho(A,\,Authors)\,\,{}^{\wedge}\,\rho(A1,\,Authors)\,\,{}^{\wedge}\,\rho(B,\,Books)\\ &\boldsymbol{\pi}_{A.Author\_ID,\,A.First\_Name,\,A.Last\_Name}(\boldsymbol{\sigma}_{NOT}(\boldsymbol{\pi}_{B.Subject\_ID}(\boldsymbol{\sigma}_{A1.First\_Name\,=\,'J.\,K.'\,\,AND\,\,A1.Last\_Name\,=\,'Rowling'}(B)\\ &\bowtie\,A1.Author\_ID\,=\,B.Author\_ID)) \end{split}
```

 $\pi_{\text{B.Subject ID}}(\sigma_{\text{B.Author ID} = \text{A.Author ID}}(B))) A)$

Part 4: Normalization (20 points)

For this part, consider the following table and functional dependencies

```
F = {id → name, GPA, major, school;

GPA → major;

school → major;

name, major → id }
```

- 1. List the candidate keys for this relation using ONLY the functional dependencies (4 points)
 - id
 - name, major

Superkeys →

- id
- name, major
- name, GPA
- name, school
- 2. Is the relation 3NF? Justify your answer (6 points)
 - Yes. For the first relation id is a super key. Similarly for the fourth relation, name,major is a super key. For the second and third relations, 'major' is part of the name, major candidate key. Thus the relation is 3NF.
- 3. Is the relation BCNF? Justify your answer (6 points)
 - No. The second and third relations (GPA → major and school → major) violate BCNF as GPA and School are not super keys.
- 4. Which of the functional dependencies are violated in the snapshot of the table provided? (4 points)
 - GPA to major (english and astronomy)
 - School to major (engineering and cs)