

Class 12

Chapter 10 - Vector Algebra

1. If θ is the angle between two vectors \mathbf{a} and \mathbf{b} , then $\|\mathbf{a}^\top \mathbf{b}\| = \|\mathbf{a} \times \mathbf{b}\|$ when θ is equal to

- a) 0 b) $\frac{\pi}{4}$ c) $\frac{\pi}{2}$ d) π

Solution:

Given,

$$\|\mathbf{a}^\top \mathbf{b}\| = \|\mathbf{a} \times \mathbf{b}\| \quad (1)$$

$$\text{Since, scalar product of two vectors is } \|\mathbf{a}^\top \mathbf{b}\| = \|\mathbf{a}\| \|\mathbf{b}\| \cos \theta \quad (2)$$

$$\text{and vector product of two vector is } \|\mathbf{a} \times \mathbf{b}\| = \|\mathbf{a}\| \|\mathbf{b}\| \sin \theta \quad (3)$$

Substituting (3) (2) in (1), we get

$$\implies \|\mathbf{a}\| \|\mathbf{b}\| \cos \theta = \|\mathbf{a}\| \|\mathbf{b}\| \sin \theta \quad (4)$$

$$\implies \cos \theta = \sin \theta \quad (5)$$

$$\implies \tan \theta = 1 \quad (6)$$

$$\implies \theta = \frac{\pi}{4} \quad (7)$$

!h

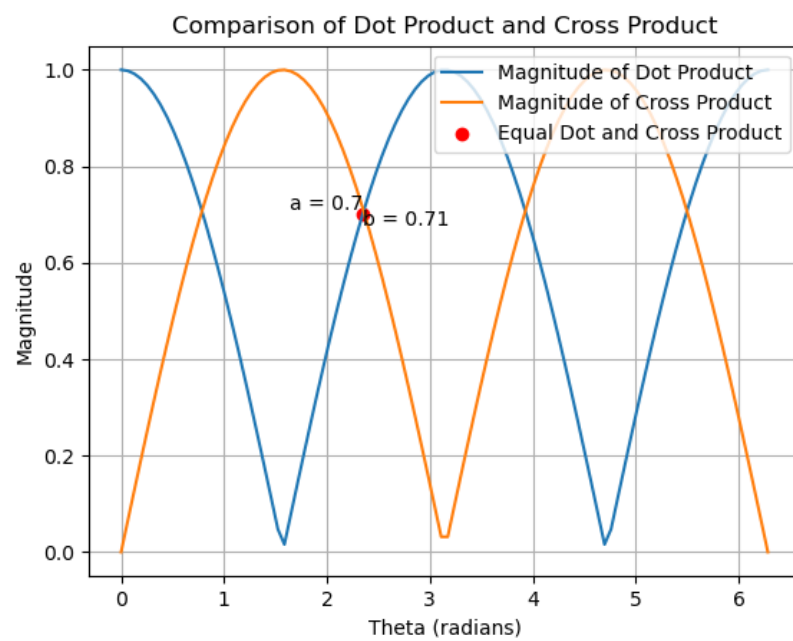


Figure 1: $\|\mathbf{a}^\top \mathbf{b}\| = \|\mathbf{a} \times \mathbf{b}\|$