

Solutions

Exercises 1: Computer architecture

- 1) Write the disjunctive normal form for the following value table. Simplify it by using the mathematical and the Karnaugh-Veitch-Methode.

| A | B | C | Q |
|---|---|---|---|
| 0 | 0 | 0 | 0 |
| 0 | 0 | 1 | 1 |
| 0 | 1 | 0 | 1 |
| 0 | 1 | 1 | 1 |
| 1 | 0 | 0 | 0 |
| 1 | 0 | 1 | 0 |
| 1 | 1 | 0 | 1 |
| 1 | 1 | 1 | 1 |

$$(\bar{A} \wedge \bar{B} \wedge C) \vee (\bar{A} \wedge B \wedge \bar{C}) \vee (\bar{A} \wedge B \wedge C) \vee (A \wedge B \wedge \bar{C}) \vee (A \wedge B \wedge C)$$

with the + for \vee and \cdot for \wedge its easier to deal

$$\bar{A} \bar{B} C + \bar{A} B \bar{C} + \bar{A} B C + A B \bar{C} + A B C$$

$$\bar{A} \bar{B} C + \bar{A} B (\bar{C} + C) + A B (\bar{C} + C)$$

$$\bar{A} \bar{B} C + \bar{A} B (1) + A B (1)$$

$$\bar{A} \bar{B} C + \bar{A} B + A B$$

$$\bar{A} \bar{B} C + (\bar{A} + A) B$$

$$\bar{A} \bar{B} C + (1) B$$

$$\bar{A} \bar{B} C + B$$

$$(\bar{A} C + B)(\bar{B} + B)$$

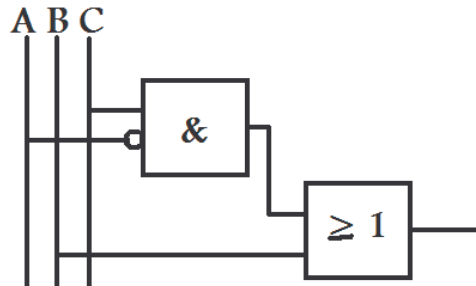
$$(\bar{A} C + B) 1$$

$$\bar{A} C + B$$

| | \bar{B} | B |
|-----------|-----------|---|
| \bar{A} | 0 | 1 |
| A | 0 | 1 |
| | \bar{C} | C |

$$B \vee (\bar{A} \wedge C)$$

- 2) Draw the logic gate for above table.



- 3) Simplify the following term

$$\begin{aligned}
 & x_1 x_2 \bar{x}_3 \bar{x}_4 + \bar{x}_1 x_2 \bar{x}_3 \bar{x}_4 + \bar{x}_1 \bar{x}_2 \bar{x}_3 x_4 + \bar{x}_1 \bar{x}_2 x_3 x_4 + \bar{x}_1 x_2 x_3 \bar{x}_4 + x_1 x_2 x_3 \bar{x}_4 \\
 & \quad \swarrow \quad \searrow \quad \quad \quad \swarrow \quad \searrow \quad \quad \quad \swarrow \quad \searrow \\
 & \quad x_2 \bar{x}_3 \bar{x}_4 \quad + \quad \bar{x}_1 \bar{x}_2 x_4 \quad + \quad x_2 x_3 \bar{x}_4 \\
 & \quad \quad \quad \swarrow \quad \searrow \\
 & \quad \quad x_2 \bar{x}_4 \quad + \quad \bar{x}_1 \bar{x}_2 x_4
 \end{aligned}$$

Quine-McCluskey-Algorithm

- 4) The standard Boolean algebra uses the element set of 0 and 1 and the operations AND, OR and NOT on it. Show that at least the operations AND and NOT or OR and NOT are enough to construct the algebra.

$$A \wedge B = \overline{\overline{A} \vee \overline{B}} \quad \text{Involution} \quad \text{DeMorgan}$$

- 5) Calculate the binary representation of 2303?

$$\begin{aligned}
 2303 / 2 &= 1151 \quad R = 1 \\
 1151 / 2 &= 575 \quad R = 1 \\
 575 / 2 &= 287 \quad R = 1 \\
 287 / 2 &= 143 \quad R = 1 \\
 143 / 2 &= 71 \quad R = 1 \\
 71 / 2 &= 35 \quad R = 1 \\
 35 / 2 &= 17 \quad R = 1 \\
 17 / 2 &= 8 \quad R = 1 \\
 8 / 2 &= 4 \quad R = 0 \\
 4 / 2 &= 2 \quad R = 0 \\
 2 / 2 &= 1 \quad R = 0 \\
 1 / 2 &= 0 \quad R = 1 \\
 &\Rightarrow 100011111111
 \end{aligned}$$

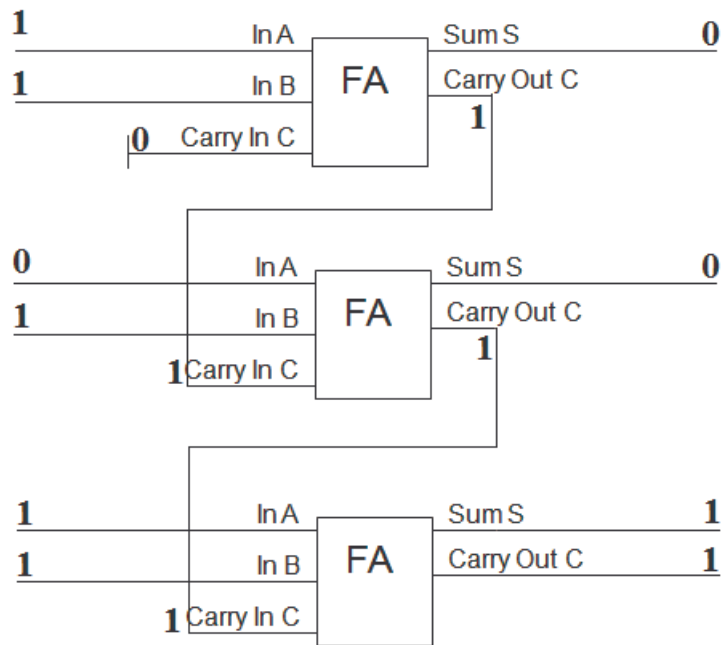
- 6) How many Bytes do you need to represent 1023?

10 Bits are needed \Rightarrow 2 Bytes

- 7) Which decimal number is coded with 10101010

$$1 * 2 + 1 * 8 + 1 * 32 + 1 * 128 = 170$$

- 8) Draw the gate-combination to add 101 and 111 with full-adder and give the states at each input/output?



=> 1100

- 9) Give the value table for XOR with two inputs?

| A | B | OUT |
|---|---|-----|
| 0 | 0 | 0 |
| 0 | 1 | 1 |
| 1 | 0 | 1 |
| 1 | 1 | 0 |