Plotting with R

Sebastian Walter Seminar talk 03.07.2009



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I. Graphics in R

- i. Basic plotting
- ii. High level plots
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i. Basic plotting

Elementary functions





Setting up the plot window

par(mfrow) Defines the number of plots and their layout per window

plot.new() Creates a new window

plot.window() Defines the window's limits

axis() Draws an axis, location specified by a number

grid() Draws a grid into the window

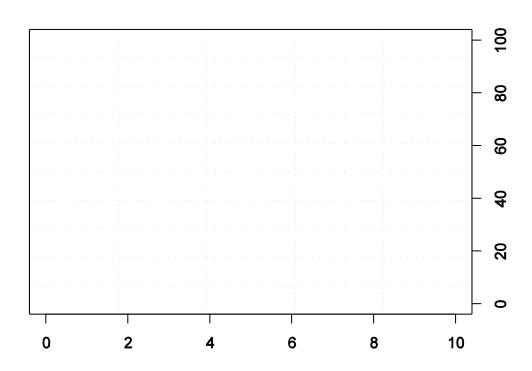
box() Draws a box around the window



Setting up the plot window

- > plot.new()
- > plot.window(c(0, 10), c(0, 100))
- > axis(1)
- > axis(4)
- > grid(5, 10)
- > box("plot")

Setting up the plot window







Labelling the plot

title() Inserts a heading, axis' labels or a subheading at the bottom

mtext() Inserts a text or expression at the specified marginal line

(=> dealing with expressions, try ,demo(plotmath)')

text() Inserts a text or expression at the specified coordinates

legend() Inserts a legend at the speciefied coordinates

(=> try ,locator(1)' instead of x-, y-coordinates to make live easier)





Labelling the plot

- > plot.new()
- > plot.window(c(0, 10), c(0, 100))
- > title(main = "Heading", sub = "Sub-heading", xlab = "x-axis", ylab = "y-axis")
- > mtext("User's text", side = "2", line = "2")
- > mtext(expression(sqrt(sigma) + pi), side = "1", line = "1")
- > text(c(5, 5), c(55, 50), c("Hello...", "...there"))
- > legend(4, 20, "Legend", fill = "blue2")

Labelling the plot

Heading

y-axis User's text

Hello...

Legend

 $\sqrt{\sigma} + \pi$

x-axis Sub-heading



rug()



Elementary low-level plots

points() Draws a point or any other ASCII-symbol

segements() Draws the connection between two points

arrows() Like ,segements()' but with an arrowhead

lines() Draws the connection between several points

rect() Draws a rectangle, specified by two corners

polygon() Draws a polygon which may be filled or shaded

abline() Draws a line specified by ist slope and y-intercept

symbols() Draws symbols suchs as circles or thermometers

Inserts a density-projection on an axis, given a data set



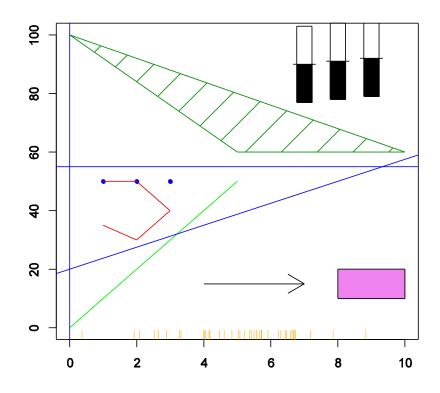


Elementary low-level plots

```
> plot.new()
> plot.window(c(0, 10), c(0, 100))
> axis(1)
> axis(2)
> box("plot")
> points(c(1, 2, 3), c(50, 50, 50), pch = 20, col = "blue2")
> segments(0, 0, 5, 50, col = "green2")
> arrows(4, 15, 7, 15, code = 2)
> lines(c(1, 2, 3, 2, 1), c(35, 30, 40, 50, 50), col = "red2")
> rect(8, 10, 10, 20, col = "violet")
> polygon(c(0, 10, 5), c(100, 60, 60), density = 3, angle = 45, col = "green4")
> rug(rnorm(40, 5, 2), col = "orange")
> abline(20, 3.75, col = "blue", h = 55, v = 0)
> symbols(7:9, 90:92, thermometers = t(matrix(c(0.1, 0.5, 0.5), 3, 3)), add = T)
```



Elementary low-level plots



I. Graphics in R

- i. Basic plotting
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ii. High level plots

Core graphical functions in R





plot() Basic 2-dimensional scatterplot, symbols can be customised

curve() Plots a curve from a given expression or function

pie() Plots a pie-diagram. Radius and appearance are to be set.

barplot() Plots a 2-dimensional barplot. Several data sets can be plotted

hist() Plots a 2-dimensional histogram, plots frequency or density

dotchart() Plots a Cleveland dotchart, substitute for a barplot,

supports various grouping options of data

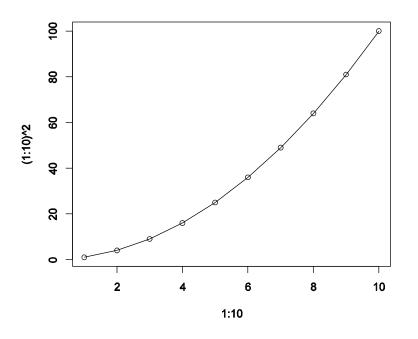


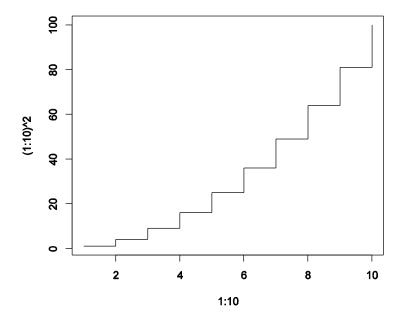
```
> par(mfrow = c(2, 1))
```

```
> plot(1:10, (1:10)^2, type = "o")
```

$$>$$
 plot(1:10, (1:10)^2, type = "s")



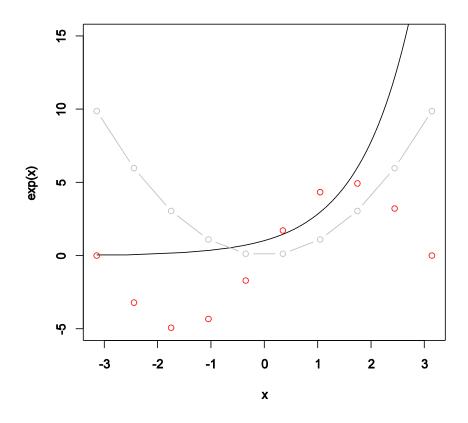






- > curve(exp(x), xlim = c(-pi, pi), ylim = c(-5, 15))
- > curve(x^2, add = T, col = "grey", type = "b", n = 10)
- > curve(5 * sin(x), add = T, col = "red", type = "p", n = 10)









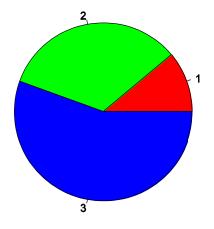
Code

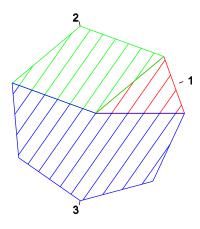
```
> par(mfrow = c(2, 1))
```

```
> pie(c(1, 3, 5), col = c("red", "green", "blue"), )
```

> pie(c(1, 3, 5), col = c("red", "green", "blue"), edges=10, density=5, angle=55)

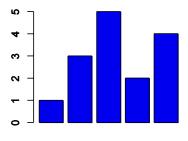


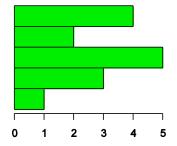


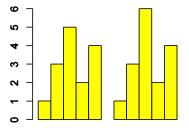


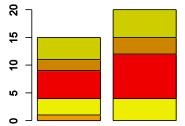


- > barplot(c(1, 3, 5, 2, 4), col = "blue2")
- > barplot(c(1, 3, 5, 2, 4), col = "green2", horiz = T, space = 0)
- > barplot(cbind(c(1, 3, 5, 2, 4), c(1, 3, 6, 2, 4)), col = "yellow", beside = T)
- > barplot(cbind(c(1, 3, 5, 2, 4), c(0, 4, 8, 3, 5)), col = c("orange2", "yellow2",
- + "red2", "orange3", "yellow3"), beside = F)





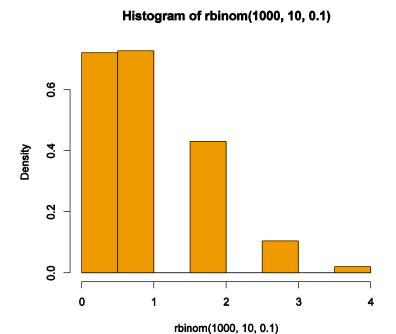


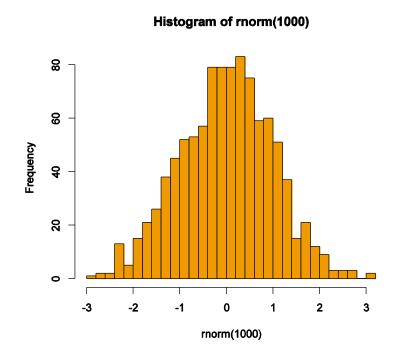




- > par(mfrow = c(2, 1))
- > hist(rbinom(1000, 10, 0.1), freq = F, col = "orange2")
- > hist(rnorm(1000), breaks = 40, freq = T, col = "orange2")

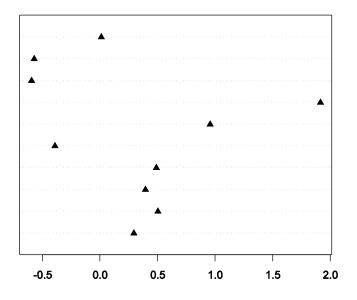


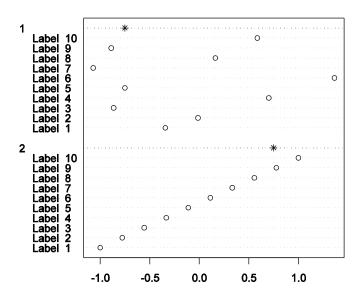






- > par(mfrow = c(2, 1))
- > dotchart(rnorm(10), pch = 17)
- > dotchart(cbind(rnorm(10), seq(-1, 1, length = 10)), labels = c(paste("Label ",
- + 1:10), gdata = c(-0.75, 0.75), gpch = 8)









boxplot() Plots a boxplot. Can compare multiple datasets in one window

pairs() Extended scatterplot, good for more complex data

coplopt() Plots a conditioning plot (scatterplot depending on a variable)

stripchart() Plots a stripchart, substitute for a boxplot for discrete data

mosaicplot() Plots a mosaicplot, multidimensional contigency tables.

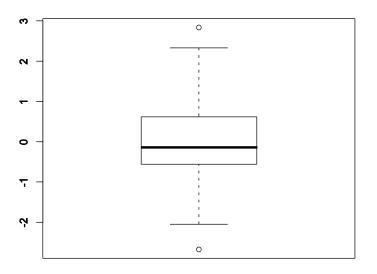
Usefull to spot dependencies, several graphical options

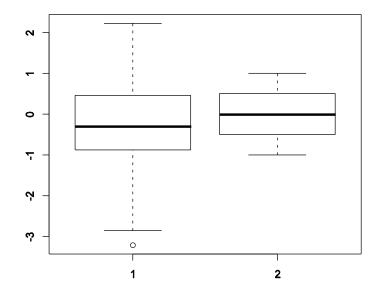
stars() Plots stars or so called ,radar diagrams', substitutes pie plot.

- > par(mfrow = c(2, 1))
- > boxplot(rnorm(100))
- > boxplot(cbind(rnorm(100), seq(-1, 1, length = 100)))









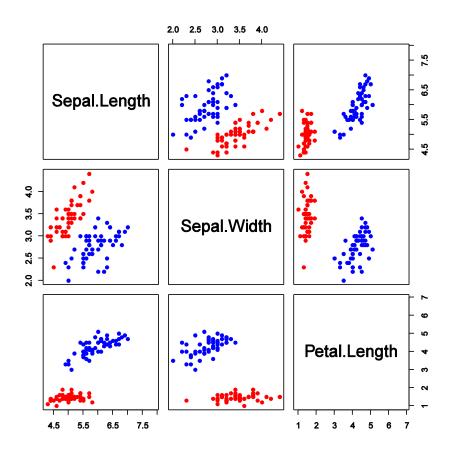




Code

> pairs(iris[1:3], col = c("red", "blue")[unclass(iris\$Species)], pch = 16)



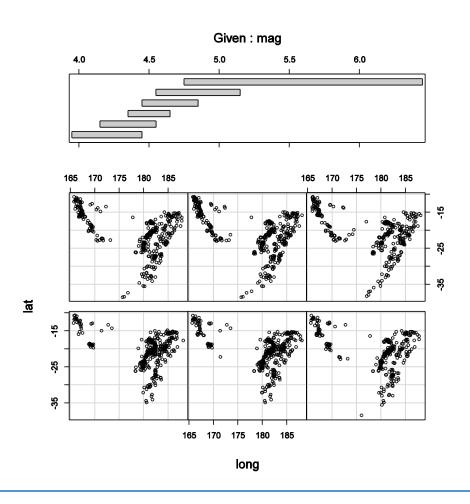




Code: [Source: R documentation]

> coplot(lat ~ long | mag, data = quakes, cex = 0.75)

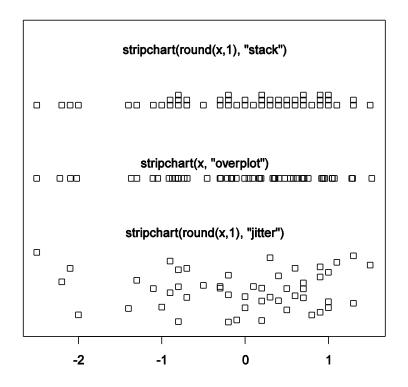






Code: [Source: R documentation]

```
> x <- stats::rnorm(50)
> xr <- round(x, 1)
> stripchart(x)
> m <- mean(par("usr")[1:2])
> text(m, 1.04, "stripchart(x, \"overplot\")")
> stripchart(xr, method = "stack", add = TRUE, at = 1.2)
> text(m, 1.35, "stripchart(round(x,1), \"stack\")")
> stripchart(xr, method = "jitter", add = TRUE, at = 0.7)
> text(m, 0.85, "stripchart(round(x,1), \"jitter\")")
```



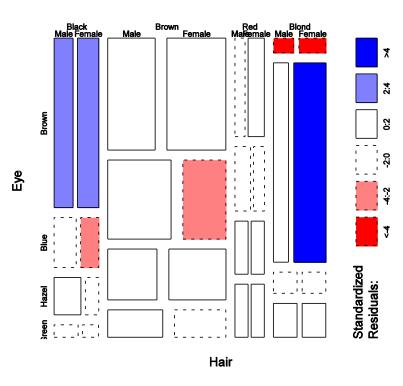




Code: [Source: R documentation]

- > data(HairEyeColor)
- > mosaicplot(HairEyeColor, shade = TRUE)

HairEyeColor



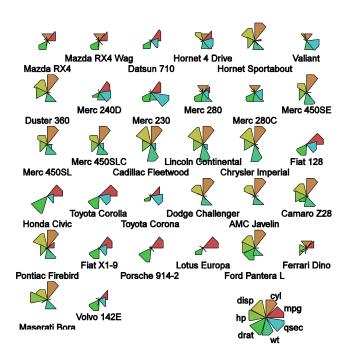


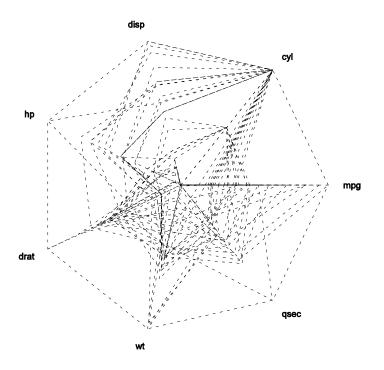
Code: [Source: R documentation]

- > par(mfrow = c(2, 1))
- > palette(rainbow(12, s = 0.6, v = 0.75))
- > stars(mtcars[, 1:7], len = 0.8, key.loc = c(12, 1.5), draw.segments = TRUE)
- > stars(mtcars[, 1:7], locations = c(0, 0), radius = FALSE, key.loc = c(0, 0),
- +lty = 2)



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qqnorm() Plots a qq-plot that compares quantiles to the normal-distrib.

(the ,qq.plot' function from ,car' package can compare to any other distrib.)

qqline() Inserts a line though 1st and 3rd quantile (low level)

qqplot() Analog to qqnorm, compares to any other data set

contour() Plots a contour plot, visualises the level curves of a data set.

image() Plots a contour plot in a ,heat map' style

persp() Plots a surface on the x-y plane, only built in 3D-function,

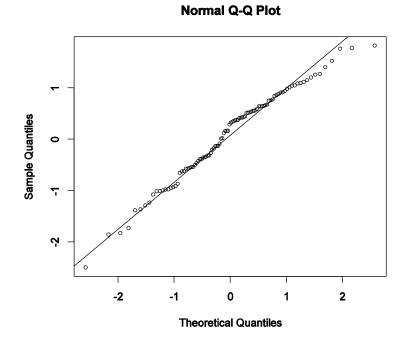
can be rotated via ,theta' and ,phi' parameters

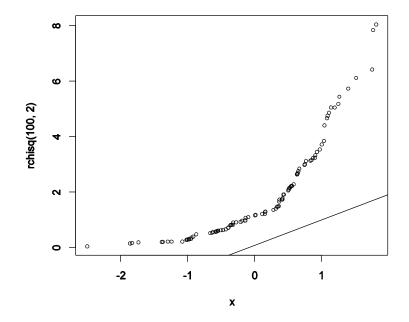


Code

- > par(mfrow = c(2, 1))
- > qqnorm(x <- rnorm(100), cex = 0.7)
- > qqline(x)
- > qqplot(x, rchisq(100, 2), cex = 0.7)
- > qqline(x)









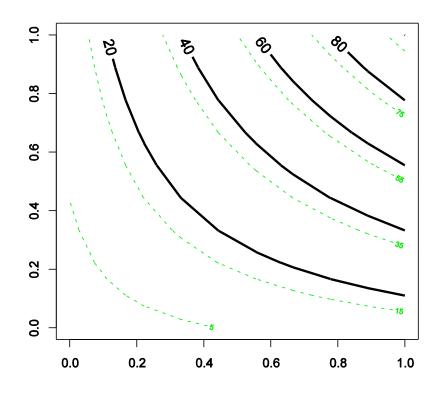
Code

```
> z <- (matrix(c(1:10, 2 * 1:10, 3 * 1:10, 4 * 1:10, 5 * 1:10, 6 * 1:10, 7 * 1:10,
```

> contour(z, nlevels = 4, levels = c(5, 15, 35, 55, 75, 95), col = "green2", add =

T,
$$Ity = 2$$





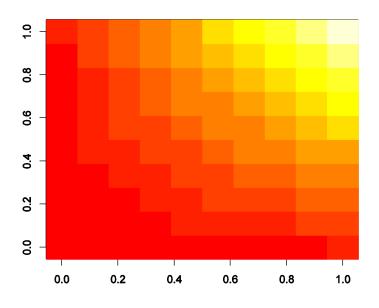


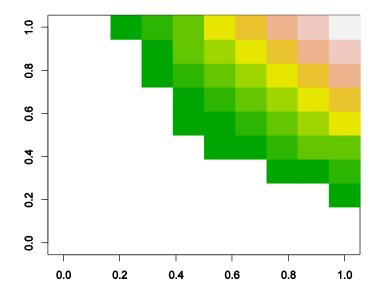


Code

```
> par(mfrow = c(2, 1))
> z <- (matrix(c(1:10, 2 * 1:10, 3 * 1:10, 4 * 1:10, 5 * 1:10, 6 * 1:10, 7 * 1:10,
+ 8 * 1:10, 9 * 1:10, 10 * 1:10), 10, 10))
> image(z)
> image(z, col = terrain.colors(10), zlim = c(30, 100))
```









Code

```
> par(mfrow = c(2, 1))
```

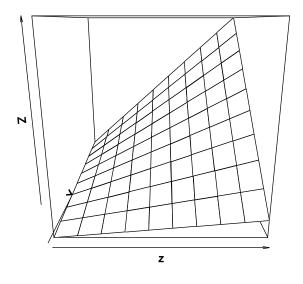
```
> z <- (matrix(c(1:10, 2 * 1:10, 3 * 1:10, 4 * 1:10, 5 * 1:10, 6 * 1:10, 7 * 1:10,
```

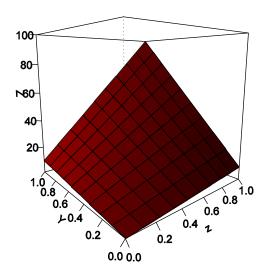
```
+ 8 * 1:10, 9 * 1:10, 10 * 1:10), 10, 10))
```

> persp(z)

> persp(z, theta = -40, phi = 10, col = "red", shade = 1.5, ticktype = "detailed")







I. Graphics in R

- i. Basic plotting
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- iii. Common parameters
- iv. Additional packages

iii. Common parameters

,Mother's little helper'





Functional parameters (1/2)

axes Determines whether axes are drawn or not

las Determines alignment of axes' labels

main / sub Inserts a sub-/ heading

xlab / ylab Inserts the x- and y-axis' labels

xlim / ylim Sets the x- and y-axis' domain of definition (2-dim. vectors)

bg Sets the background colour





Functional parameters (2/2)

font Sets fonttype such as bold or italic.

(There are sub.paramters such as font.lab, font.axis, font.main...)

Sets the number of tickmarks on the axes.

(Note that it needs a 3-dim. Vector input but the 3rd component is ignored.)

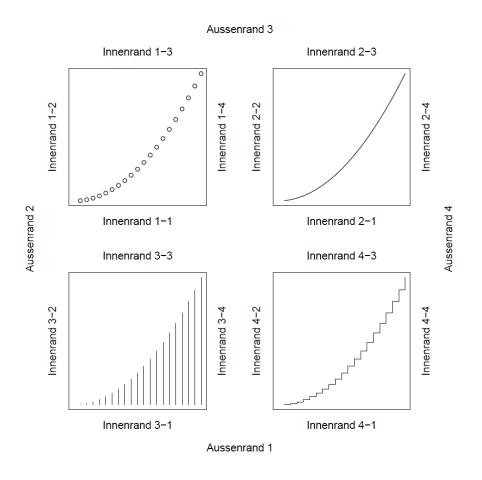
add Surpresses the plot.new() call of a high level function.

Causes the plot to be drawn in the same window.

oma, omi, omd Controls the size of outer margins.

xlog / ylog Sets the x- or y-axis to logarithmic scale

Margins of a plot window [Source: Alexander Bauer]







Sets colour of curves, symbols, ... Vector input possible. col

Sets the style of the boundary box (U-shaped, L-shaped,...) bty

Sets the line width. lwd

Sets the line type, such as points, lines, both,... lty

Sets the symbol. Numeric value, Vector input possible. pch

> 1-25: Standard R symbols

ASCII characters 32-127:

NA: blank

Sets the symbols' size. Vector input possible. cex

Code

```
> par(mfrow = c(2, 2))
```

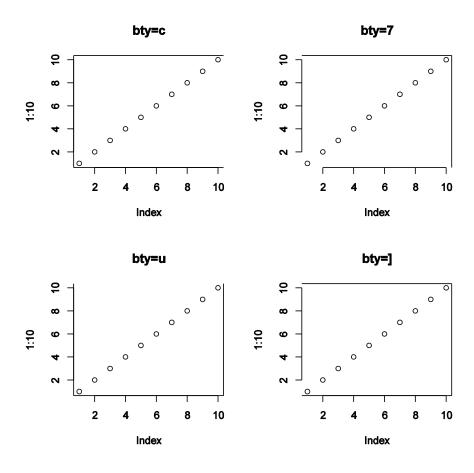
```
> plot(1:10, bty = "c", main = "bty=c")
```

$$>$$
 plot(1:10, bty = "7", main = "bty=7")

$$>$$
 plot(1:10, bty = "u", main = "bty=u")

$$>$$
 plot(1:10, bty = "]", main = "bty=]")



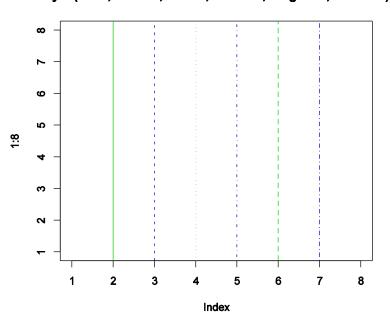


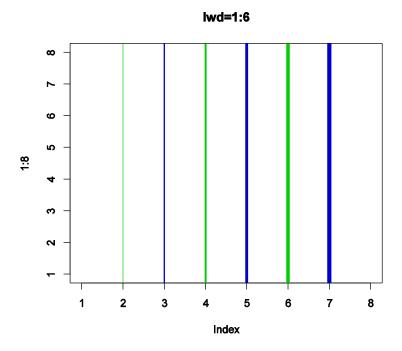


Code

- > par(mfrow = c(2, 1))
- > plot(1:8, cex = 0, main = "Ity=c(solid, dashed, dotted, dotdash, longdash,
- twodash)")
- > abline(v = 2:7, lty = 1:6, col = c("green3", "blue3"))
- > plot(1:8, cex = 0, main = "lwd=1:6")
- > abline(v = 2:7, lwd = 1:6, col = c("green3", "blue3"))

Ity=c(solid, dashed, dotted, dotdash, longdash, twodash)





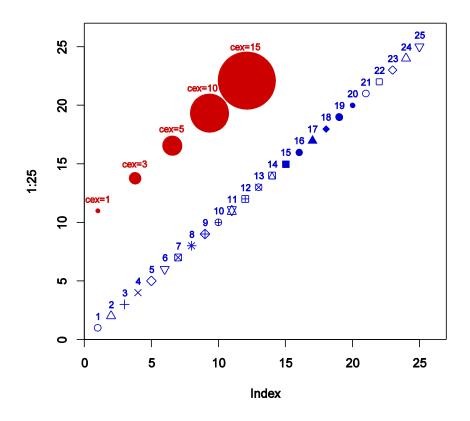




Code

```
> plot(1:25, xlim = c(1, 26), ylim = c(1, 26), pch = 1:25, cex = 1.2, col = "blue3")
> text(1:25, 2:26, cex = 0.75, col = "blue3")
> curve(x + 10, add = T, type = "p", n = 10, col = "red3", cex = c(1, 3, 5, 10, + 15, 0, 0), pch = 20)
> text(c(1, 3.75, 6.5, 8.8, 12), c(12, 15, 18, 21.5, 25), cex = 0.75, col = "red3", + label = c("cex=1", "cex=3", "cex=5", "cex=10", "cex=15"))
```









Colours (1/2)

colors() Returns a list of prebuilt colours in R. Note: Many standard

colours come in shaded variations, e.g. "red2", "red3",...

Creates a colour from the RGB scheme. rgb()

(red, green, blue, intesity, alpha-value (transparency))

Creates a colour from the HSV scheme. hsv()

(hue, saturation, value, alpha-value (transparency))

Creates a colour from the HCL scheme. hcl()

(hue, chroma, luminance, alpha-value (transparency))

gray() Creates a shade of gray from a level





Colours (2/2)

rainbow()

Creates a gradient of colour in a rainbow-style.

diverge_hcl()

Creates a gradient of colour from two hcl-colours.

heat.colors()

Creates a gradient of colour in a 'heatmap'-style

terrain.colors()

Creates a gradient of colour in green-brown style

topo.colors()

Creates a gradient of colour in green-brown-blue style.

cm.colors()

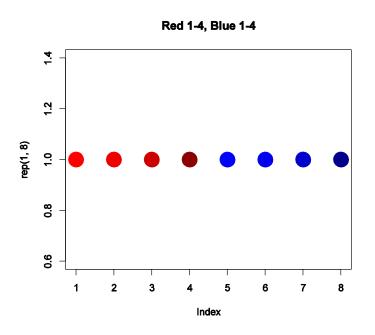
Creates a gradient of colour from light blue to pink.

Code

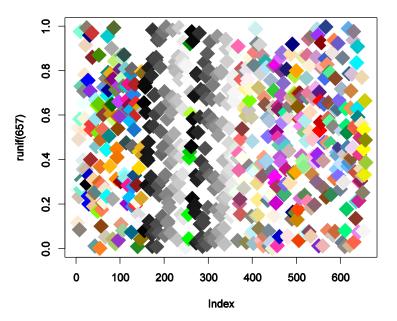
- > par(mfrow = c(2, 1))
- > plot(rep(1, 8), col = c(paste("red", 1:4), paste("blue", 1:4)), pch = 20, cex = 5,
- + main = "Red 1-4, Blue 1-4")
- > plot(runif(657), col = colors(), pch = 18, cex = 3)











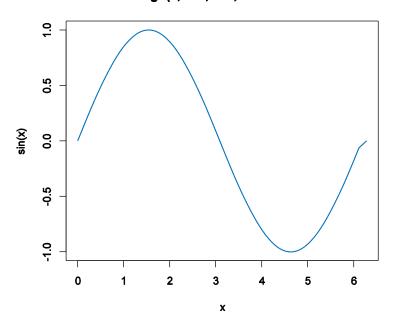


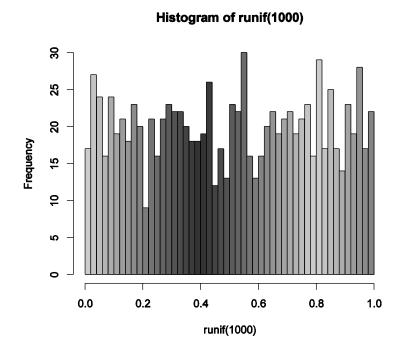


Code

- > par(mfrow = c(2, 1))
- > blau <- rgb(0, 114, 186, maxColorValue = 255)
- > curve(sin(x), xlim = c(0, 2 * pi), lwd = 1.5, col = blau, main = "TUM-Blau:
- rgb(0, 114, 186, maxCol=255)"
- > hist(runif(1000), breaks = 40, col = gray(c(seq(0.8, + 0.2, length = 20),
- seq(0.2, 0.8, length = 20))))

TUM-Blau: rgb(0, 114, 186, maxColorValue=255





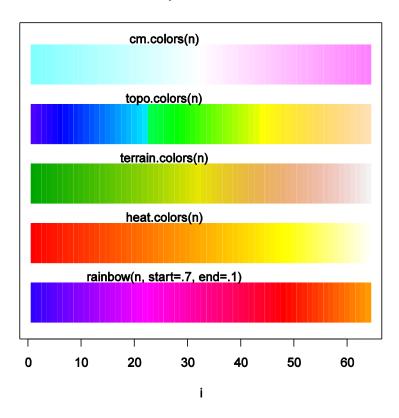


Code: [Source: R documentation]

```
> demo.pal <- function(n, border = if (n < 32) "light gray" else NA, main = paste("color palettes; n+ n),
ch.col = c("rainbow(n, start=.7, end=.1)", "heat.colors(n)", "terrain.colors(n)",
+ "topo.colors(n)", "cm.colors(n)")) {
+ nt <- length(ch.col)
+ i < -1:n
+ i <- n/nt
+ d <- j/6
+ dv <- 2 * d
+ plot(i, i + d, type = "n", yaxt = "n", ylab = "", main = main)
+ for (k in 1:nt) {
+ \text{ rect}(i - 0.5, (k - 1) * i + dy, i + 0.4, k * j, col = eval(parse(text = ch.col[k])),
+ border = border)
+ text(2 * j, k * j + dy/4, ch.col[k])
+ }
+ }
> n <- if (.Device == "postscript") 64 else 16
> demo.pal(n)
```



color palettes; n= 64



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iv. Additional packages

This is where the fun begins...



Additional packages

- Installation via ,utils:::menuInstallPkgs()' or windows setup
- CRAN, R-project homepage: http://cran.r-project.org
- Overview of graphical packages http://addictedtor.free.fr/graphiques
- Another site dedicated to graphics in R http://bm2.genes.nig.ac.jp/RGM2/
- Good overview of some packages with examples.
 http://www.stat.ucl.ac.be/ISpersonnel/lecoutre/stats/chiers/_gallery.pdf



Additional packages

- Some important packages
 - Lattice
 - Vcd
 - Rgraphivz



Lattice package

- Quite popular
- Comes with an own plot device, started with 'trellis.device(),
- Powerful tool for multiple plots in one window and complex data
- Most function are called with a formular like, x y | z'
- Re-does some built in function...
- ...but provides new functions too
- Lattice / Trellis homepage:

ttp://cm.bell-labs.com/cm/ms/departments/sia/project/trellis/index.html





Lattice package functions (1/2)

barchart() barplot() Barplot

bwplot()
boxplot()

densityplot() - / rug() + hist() Estimates density.

dotplot() dotchart() Dotplot

histogram() hist() Histogram

qqmath() qqnorm() QQ-plot: Data vs. distribution

qq() qqplot() QQ-plot: Data vs. data

stripplot() stripchart() 1-dim. Scatterplot





Lattice package functions (2/2)

xyplot() plot() 2-dim. Scatterplot

contourplot() contour() Countourplot

levelplot() image() Sort of discrete countourplot

cloud() - 3-dim. Scatterplot

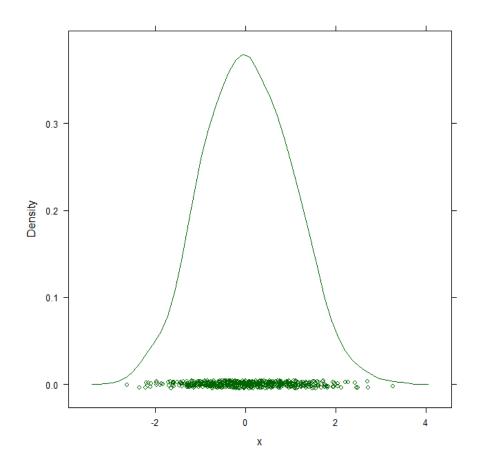
wireframe() persp() 3-dim. surface

splom() pairs() Several Scatterplots

parallel() - Several conditioning plots



Lattice package: densityplot() [Source: demo(lattice)]

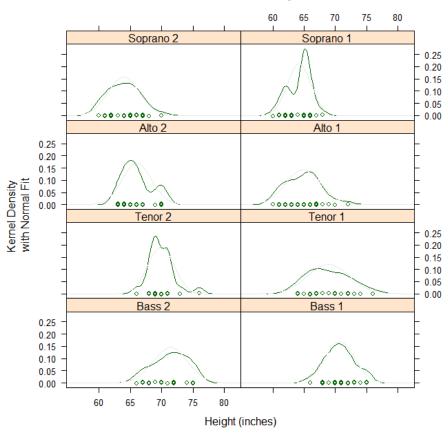






Lattice package: densityplot() [Source: demo(lattice)]

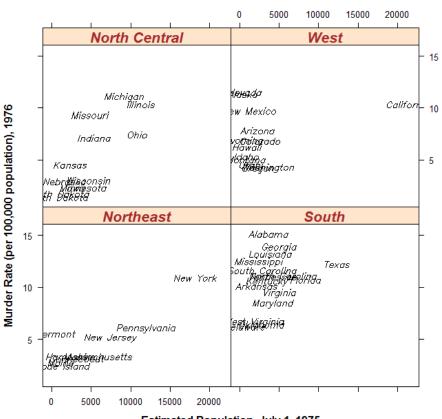
Estimated Density





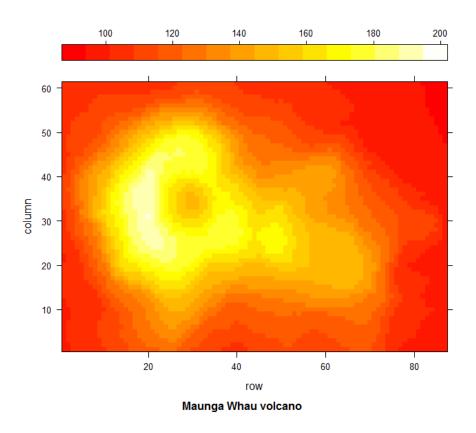
Lattice package: xyplot() [Source: demo(lattice)]

Murder Rates in US states



Estimated Population, July 1, 1975

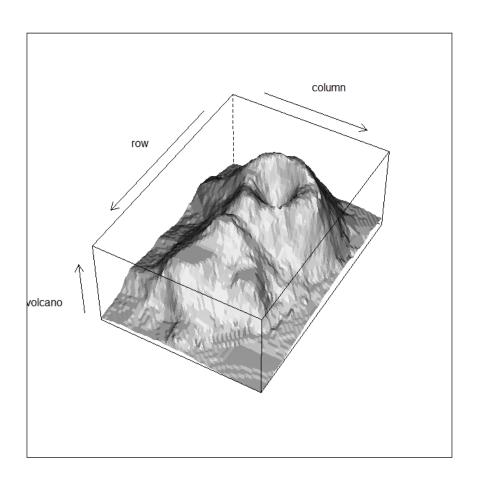
Lattice package: levelplot() [Source: demo(lattice)]







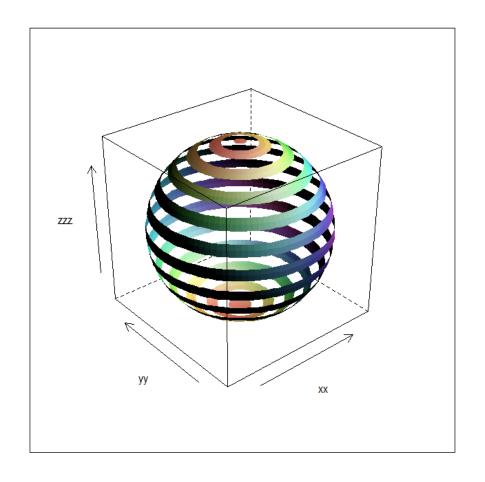
Lattice package: wireframe() [Source: demo(lattice)]







Lattice package: wireframe() [Source: demo(lattice)]





vcd-package

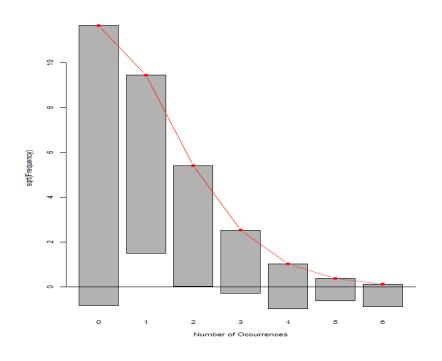
- Several new plots
- Documentation of the vcd package at CRAN R-Project http://cran.r-project.org/web/packages/vcd/index.html

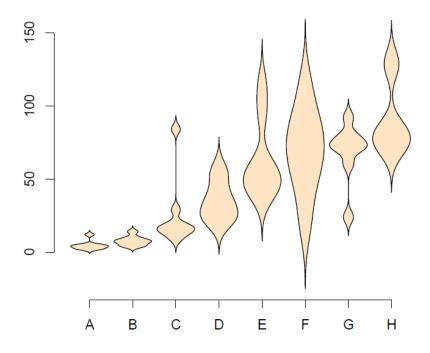
Images source:

http://www.stat.ucl.ac.be/ISpersonnel/lecoutre/stats/chiers/_gallery.pdf



vcd package: rootogram() & simple.violinplot()

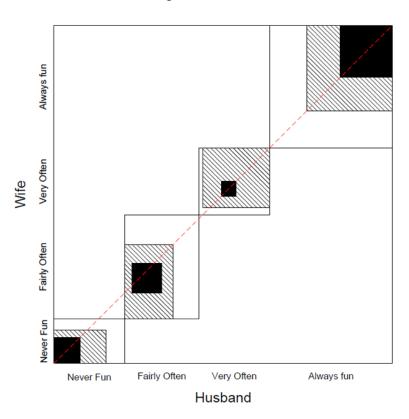


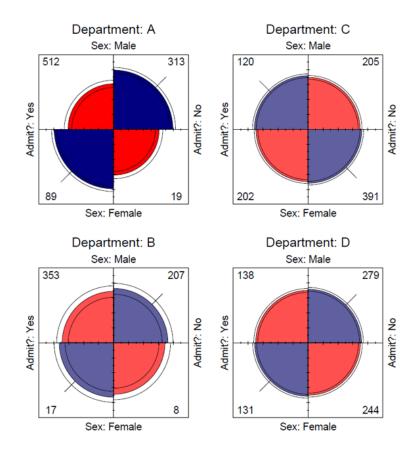




vcd package: agreementplot() & fourfoldplot()

Agreement Chart

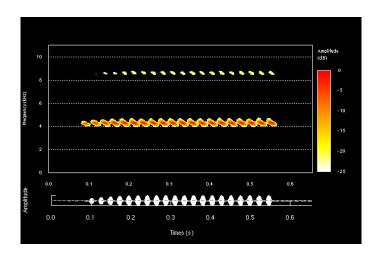


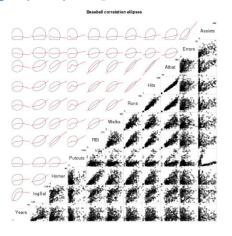


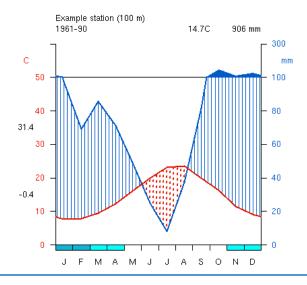


Other packages: [Source: http://addictedtor.free.fr/graphiques]



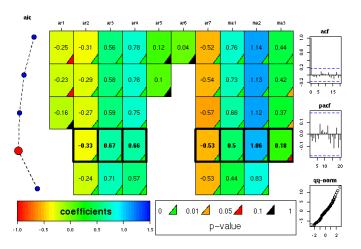


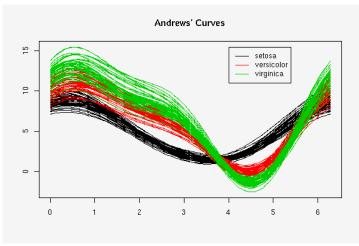


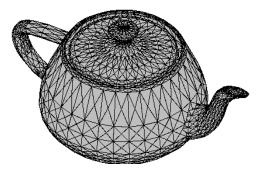




Other packages: [Source: http://addictedtor.free.fr/graphiques]











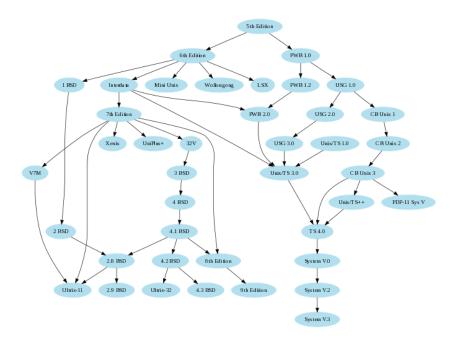


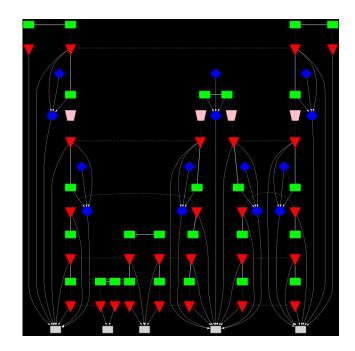
Drawing graphs with R

- There actually is a way to draw graphs in R!
- ...with 3rd party Software though.
- Requires BioConductor and Graphviz software
- ...and the Rgraphivz package
- Tutorial to drawing graphs with R by Peter Cock

http://www2.warwick.ac.uk/fac/sci/moac/currentstudents/peter_cock/r/rgraphviz/

Drawing graphs with R





II. 3-dimensional barplots: hist3d

- i. Motivation
- ii. Implementation
- iii. The Code step by step
 - iv. Results
 - v. hist3drot
 - vi. Alternatives

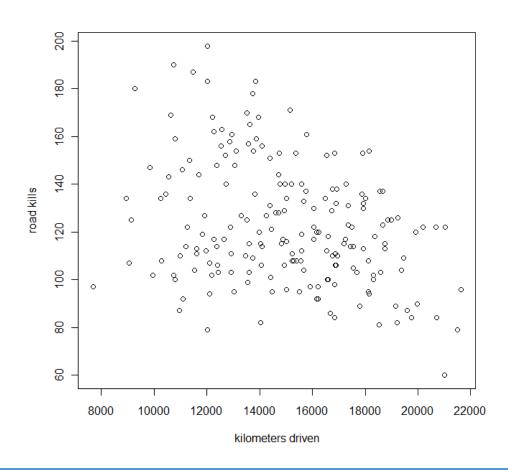
i. Motivation

What about 3-dimensional barplots?

Motivation

- "barplot()" function is 2-dimensional
- There is no built-in 3-dimensional barplot function
- There seems to be no package to do the job
- There may however be the need
 - Example: ,Seatbelts' data
 - Want to visualise: # road kills vs. # kilometeres driven
 - Frequency / Sort of 3-dimensional histogram

Motivation

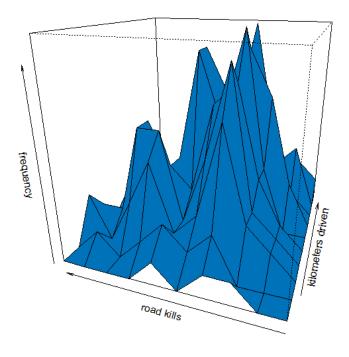




Motivation

Plotting the "pure" data with persp:

persp-plot of Haufigkeit



II. 3-dimensional barplots: hist3d

- i. Motivation
- ii. Implementation
- iii. The Code step by step
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 - vi. Alternatives

ii. Implementation

Basic ideas





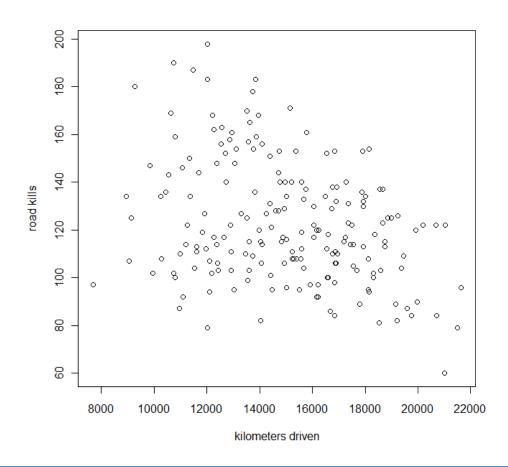
Prepare data:

- 1. Divide the domain of definition into squares
- Count the datapoints in the squares (=frequency)

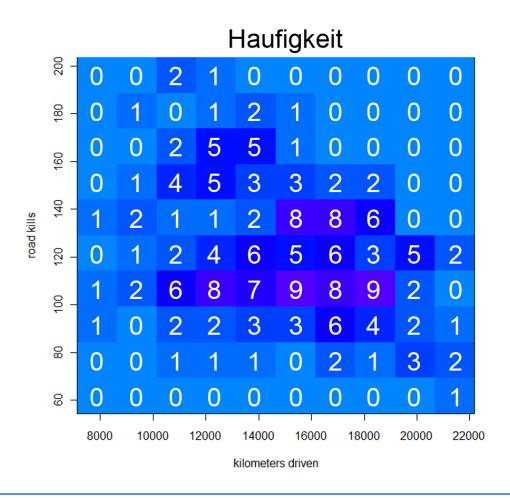
Plot:

- 3. Divide the existing squares into smaller squares (=finer grid)
- 4. Fill this fine grid with "old" values from the rough grid
- 5. Plot a persp() function

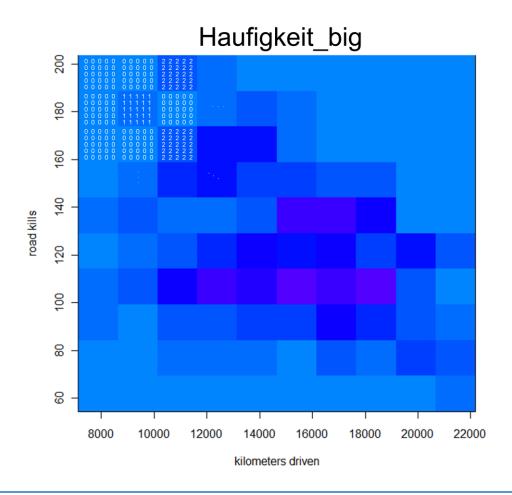
=> The fine grid will force persp() to plot something like a 3-dim. bar

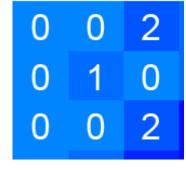


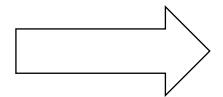








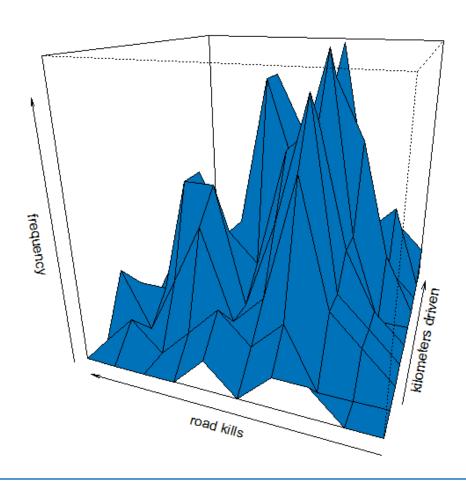




0 0 0 0 0 0	0 0 0 0 0	2 2 2 2 2
0 0 0 0 0	0 0 0 0 0	2 2 2 2 2
0 0 0 0 0	0 0 0 0 0	2 2 2 2 2
0 0 0 0 0	0 0 0 0 0	2 2 2 2 2
0 0		0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
0 0 0 0 0 0	0 0 0 0 0 0	2 2 2 2 2
0 0 0 0 0 0	0 0 0 0 0 0	2 2 2 2 2
0 0 0 0 0 0	0 0 0 0 0 0	2 2 2 2 2
0 0 0 0 0 0	0 0 0 0 0 0	2 2 2 2 2

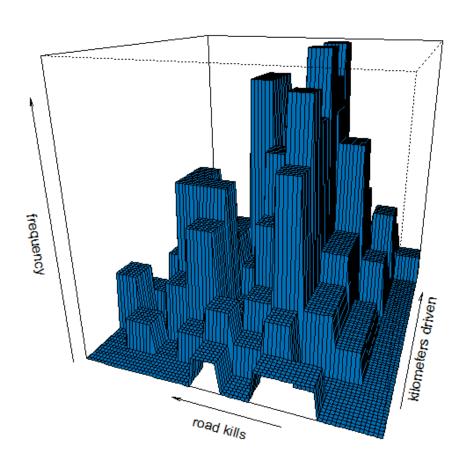


persp-plot of Haufigkeit





persp-plot of Haufigkeit_big



II. 3-dimensional barplots: hist3d

- i. Motivation
- ii. Implementation
- iii. The Code step by step
 - iv. Results
 - v. hist3drot
 - vi. Alternatives

iii. The Code – step by step

Take a deep breath...

The Code – step by step

```
hist3d <- function(x,y, nx=10, ny=10, approx=75
   # x = Wert x-Achse
   # y = Wert y-Achse
   # nx = Anzahl Intervalle auf der x-Achse
   # ny = Anzahl Intervalle auf der y-Achse
   # approx = approximationsfaktor. Je größer, desto mehr ähnelt die Oberfläche einem
Barplot (Achtung bei großen Zahlen Rechenintensiv! approx *nx/10 und approx*ny/10
sollte bei ca. 100 bleiben.
   xlim = range(x),
   vlim = range(y),
   zlim = c(0, length(x)),
   xlab = "x".
   vlab = "y",
   zlab = "z".
   main = NULL
   sub = NULL.
   theta = 20.
   phi = 20.
   r = sart(3),
   d = 1,
   scale = TRUE,
   expand = 1,
   col = "white"
   border = NULL.
   Itheta = -135,
   lphi = 0,
   shade = NA
   box = TRUE.
   axes = TRUE
   nticks = 5.
   ticktype = "simple",
   # persp - Argumente
   cex.lab = par("cex.lab").
   font.lab= par("font.lab"),
   cex.axis= par("cex.axis").
   font.axis= par("font.axis")
   #par - Argumente
#x-Achse nach vorne:
tempy=y:tempx=x;
```

```
# Aufteilung des Definitionsbereichs in Intervalle bzw. Rechtecke
 I <- seg(min(x), max(x), length.out=nx+1)
 b <- seg(min(y), max(y), length.out=ny+1)
 #Haufigkeit = Anzahl von (x.v)-Pärchen pro Intervall bzw. Rechteck
 Haufigkeit <- matrix(0,ny,nx)
 for (u in 1:nx-1) {
    Haufigkeit[v.u] <- sum( (x>=l[u] & x<l[u+1])+(y>=b[v] & y<b[v+1])==2 ) #Zählen
der (x,y)-Päärchen pro halboffenem Intervall/Rechteck, bis auf Rand
for (u in 1:nx-1) {
                                                       # oberer Rand (ohne rechte
Ecke), nach rechts offenes Hufeisen
  Haufigkeit[nv.u] <- sum((x>=|[u] & x<|[u+1])+(y>=b[nv] & y<=b[ny+1])==2)
 for (v in 1:ny-1) {
  Haufigkeit[v,nx] <- sum((x>=l[nx] & x<=l[nx+1])+(y>=b[v] & y<b[v+1])==2) #rechter
Rand (ohne obere Ecke), nach oben offenes Hufeisen
 \label{eq:haufigkeit[ny.nx] <- sum((x>=|[nx] & x<=|[nx+1])+(y>=b[ny] & y<=b[ny+1])==2) \#Ecke} \\
rechts oben, abgeschlossen
 f \leftarrow function(x1,y1) {
 #Haufigkeit big = Große Matrix, Blöcke mit Werten von Häufigkeit, entspricht einer
Verfeinerung des Gitters
 Haufigkeit_big <- matrix(0,length(y1)-1,length(x1)-1)
 for (p in 1: (lenath(x1)-2)) {
  for (q in 1:(length(y1)-2)) {
   for (k \text{ in } 1:nx) \{ if (x1[p] > = I[k] \& x1[p] < I[k+1]) \{ i < -k \} \}
entsprechenden Wert von Haufigkeit für den passenden Bereich in Haufigkeit big
   for (k \text{ in } 1:ny) \{ if (y1[q] >= b[k] \& y1[q] < b[k+1]) \{ j <- k \} \}
   Haufigkeit big[g.p] <- Haufigkeit[i.i]
```

```
for (p in 1: (lenath(x1)-2)) {
                                             # oberer Rand (ohne rechte Ecke), nach
rechts offenes Hufeisen
  for (k in 1:nx) {
  if(x1[p]>=|[k] & x1[p]<|[k+1]) {i <-k}
  Haufigkeit_big[length(y1)-1,p]<- Haufigkeit[ny.i]
                                             # rechter Rand (ohne obere Ecke), nach
for (q in 1: (lenath(y1)-2)) {
oben offenes Hufeisen
  for (k in 1:ny) {
   if (y1[q]>=b[k] & y1[q]<b[k+1]) {j <-k}
  Haufigkeit_big[q.length(x1)-1]<- Haufigkeit[j.nx]
Haufigkeit_big[length(y1)-1,length(x1)-1]<-Haufigkeit[ny.nx] #rechte obere Ecke
 return(Haufigkeit_big)
#Vorgabe des feineres Gitters
xnew <- seg(min(x), max(x), length=1+ approx*nx/10)
vnew <- seg(min(y), max(y), length=1+ approx*ny/10)
z <- f(xnew.ynew)
 y2 <- seg(min(xnew), max(xnew), length.out=nrow(z)) # Intervalle
 x2 <- seq(min(vnew), max(vnew), length.out=ncol(z))
persp(x2,y2,z,
   xlim = range(x2), ylim = range(y2),
   zlim = range(z, na.rm = TRUE).
   xlab = xlab, ylab = ylab, zlab = zlab,
   main = main, sub = sub,
   theta = theta, phi = phi, r = r, d = d,
   scale = scale, expand = expand.
   col = col, border = border, ltheta = ltheta, lphi = lphi,
   shade = shade, box = box, axes = axes, nticks = nticks.
   ticktype = ticktype,
   cex.lab = cex.lab , font.lab = font.lab,
   cex axis=cex axis, font axis=font axis
```



The Code – step by step

```
nist3d <- function(x,y, nx=10, ny=10, approx=75,
  # x = Wert x-Achse
  # y = Wert y-Achse
  # nx = Anzahl Intervalle auf der x-Achse
  # ny = Anzahl Intervalle auf der y-Achse
  # approx = approximationsfaktor. Je größer, desto mehr ähnelt die Oberfläche einem
 Barplot (Achtung bei großen Zahlen Rechenintensiv! approx *nx/10 und approx*ny/10
sollte bei ca. 100 bleiben.
  xlim = range(x),
   vlim = range(y).
  zlim = c(0, length(x)),
  xlab = "x"
   vlab = "y",
   zlab = "z".
  main = NULL.
   sub = NULL,
   theta = 20.
  phi = 20,
   r = sart(3),
   scale = TRUE,
   expand = 1,
   col = "white"
  border = NULL
   Itheta = -135.
   lphi = 0,
  shade = NA
  box = TRUE
   axes = TRUE
   nticks = 5.
  ticktype = "simple",
   # persp - Argumente
   cex.lab = par("cex.lab"),
   font.lab= par("font.lab"),
   cex.axis= par("cex.axis").
  font.axis= par("font.axis")
   #par - Argumente
#x-Achse nach vorne:
tempy=y:tempx=x;
```

```
# Aufteilung des Definitionsbereichs in Intervalle bzw. Rechtecke
 I <- seg(min(x), max(x), length.out=nx+1)
 b <- seg(min(y), max(y), length.out=ny+1)
  #Haufigkeit = Anzahl von (x.v)-Pärchen pro Intervall bzw. Rechteck
 Haufigkeit <- matrix(0,ny,nx)
 for (u in 1:nx-1) {
     Haufigkeit[v.u] <- sum( (x>=l[u] & x<l[u+1])+(y>=b[v] & y<b[v+1])==2 ) #Zählen
der (x, y)-Päärchen pro halboffenem Intervall/Rechteck, bis auf Rand
                                                      # oberer Rand (ohne rechte
for (u in 1:nx-1) {
Ecke), nach rechts offenes Hufeisen
  Haufigkeit[nv.u] <- sum((x>=|[u] & x<|[u+1])+(y>=b[nv] & y<=b[ny+1])==2)
 for (v in 1:ny-1) {
  Haufigkeit[v,nx] <- sum((x>=l[nx] & x<=l[nx+1])+(y>=b[v] & y<b[v+1])==2) #rechter
Rand (ohne obere Ecke), nach oben offenes Hufeisen
 Haufigkeit[ny,nx] < -sum((x>=l[nx] & x<=l[nx+1])+(y>=b[ny] & y<=b[ny+1])==2) #Ecke
rechts oben, abgeschlossen
 f \leftarrow function(x1,y1) {
 #Haufigkeit big = Große Matrix, Blöcke mit Werten von Häufigkeit, entspricht einer
Verfeinerung des Gitters
 Haufigkeit_big <- matrix(0,length(y1)-1,length(x1)-1)
 for (p in 1: (lenath(x1)-2)) {
  for (q in 1:(length(y1)-2)) {
    for (k \text{ in } 1:nx) \{ if (x1[p]>=|[k] & x1[p]<|[k+1]) \{ i <-k \} \}
entsprechenden Wert von Haufigkeit für den passenden Bereich in Haufigkeit big
    for (k \text{ in } 1:ny) \{ if (y1[q] >= b[k] \& y1[q] < b[k+1]) \{ j <- k \} \}
    Haufigkeit big[g.p] <- Haufigkeit[i.i]
```

```
for (p in 1: (lenath(x1)-2)) {
                                             # oberer Rand (ohne rechte Ecke), nach
rechts offenes Hufeisen
  for (k in 1:nx) {
  if(x1[p]>=l[k] & x1[p]<l[k+1]) {i <-k}
  Haufigkeit_big[length(y1)-1,p]<- Haufigkeit[ny.i]
                                             # rechter Rand (ohne obere Ecke), nach
for (q in 1: (length(y1)-2)) {
oben offenes Hufeisen
  for (k in 1:ny) {
   if (y1[q]>=b[k] & y1[q]<b[k+1]) {j <-k}
  Haufigkeit_big[q.length(x1)-1]<- Haufigkeit[j.nx]
Haufigkeit_big[length(y1)-1,length(x1)-1]<-Haufigkeit[ny.nx] #rechte obere Ecke
 return(Haufigkeit_big)
#Vorgabe des feineres Gitters
xnew <- seq(min(x), max(x), length=1+ approx*nx/10)
vnew <- seg(min(y), max(y), length=1+ approx*ny/10)
z <- f(xnew.ynew)
 y2 <- seg(min(xnew), max(xnew), length.out=nrow(z)) # Intervalle
 x2 <- seq(min(vnew), max(vnew), length.out=ncol(z))
persp(x2,y2,z,
   xlim = range(x2), ylim = range(y2),
   zlim = range(z, na.rm = TRUE).
   xlab = xlab, ylab = ylab, zlab = zlab
   main = main, sub = sub,
   theta = theta, phi = phi, r = r, d = d,
   scale = scale, expand = expand.
   col = col, border = border, ltheta = ltheta, lphi = lphi,
   shade = shade, box = box, axes = axes, nticks = nticks.
   ticktype = ticktype,
   cex.lab = cex.lab , font.lab = font.lab,
   cex axis=cex axis, font axis=font axis
```

Calling the function





Calling the function

```
hist3d <- function(x, y, nx=10, ny=10, approx=75,
   # x = Wert x-Achse
   # y = Wert y-Achse
   # nx = Anzahl Intervalle auf der x-Achse
   # ny = Anzahl Intervalle auf der y-Achse
   # approx = approximationsfaktor. Je größer, desto mehr ähnelt die Oberfläche einem
Barplot (Achtung bei großen Zahlen Rechenintensiv! approx *nx/10 und approx*ny/10
sollte bei ca. 100 bleiben.
   xlim = range(x),
   vlim = range(y).
   zlim = c(0, length(x)),
   xlab = "x",
   vlab = "y",
   zlab = "z",
   main = NULL,
   sub = NULL,
   theta = 20,
   phi = 20,
   r = sart(3),
   d = 1,
   scale = TRUE,
   expand = 1,
   col = "white",
   border = NULL
   Itheta = -135.
   lphi = 0,
   shade = NA.
   box = TRUE.
   axes = TRUE,
   nticks = 5,
   ticktype = "simple",
   # persp - Argumente
   cex.lab = par("cex.lab"),
   font.lab= par("font.lab"),
   cex.axis= par("cex.axis").
   font axis= par("font axis")
   #par - Argumente
```



Calling the function

There are several parameters when calling the new "hist3d" fct.:

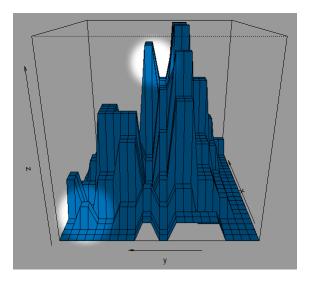
x / y	The data you want to plot
nx / ny	The number of bars you want on the axes Right now: Use nx = ny to avoid malfunction
approx	Sets the size of the fine grid. The higher the more the fct. Will look like a barplot, the lower, the more like a surface
persp	All persp() parameters such as "xlim" or "theta" are handed through the function. All defaults are persp's defaults.
par	You may use cex.lab, font.lab,cex.axis and font.axis

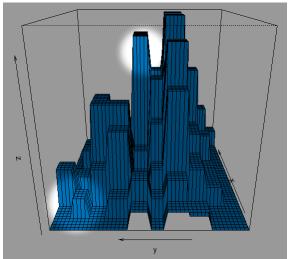


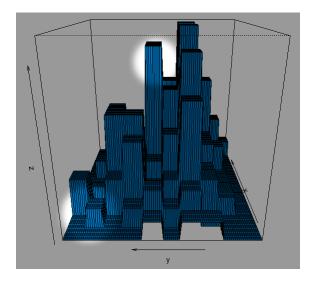
Calling the function: The approx-parameter

$$approx = 25 \qquad \Box \Box \Rightarrow$$

$$approx = 50 \implies$$











```
hist3d <- function(x,y, nx=10, ny=10, approx=75
   # x = Wert x-Achse
   # y = Wert y-Achse
   # nx = Anzahl Intervalle auf der x-Achse
   # ny = Anzahl Intervalle auf der y-Achse
   # approx = approximationsfaktor: Je größer, desto mehr ähnelt die Oberfläche einem
Barplot (Achtung bei großen Zahlen Rechenintensiv! approx *nx/10 und approx*ny/10
sollte bei ca. 100 bleiben.
   xlim = range(x),
   vlim = range(y),
   zlim = c(0, length(x)),
   xlab = "x".
   vlab = "y",
   zlab = "z".
   main = NULL
   sub = NULL.
   theta = 20.
   phi = 20.
   r = sart(3),
   d = 1,
   scale = TRUE,
   expand = 1.
   col = "white"
   border = NULL.
   Itheta = -135,
   lphi = 0,
   shade = NA
   box = TRUE.
   axes = TRUE
   nticks = 5.
   ticktype = "simple",
   # persp - Argumente
   cex.lab = par("cex.lab").
   font.lab= par("font.lab"),
   cex_axis= par("cex_axis")
   font.axis= par("font.axis")
   #par - Argumente
#x-Achse nach vorne:
tempy=y:tempx=x;
```

```
# Aufteilung des Definitionsbereichs in Intervalle bzw. Rechtecke
I <- seq(min(x), max(x), length.out=nx+1)
b <- seg(min(y), max(y), length.out=ny+1)
#Haufigkeit = Anzahl von (x v)-Pärchen pro Intervall bzw. Rechteck
Haufigkeit <- matrix(0,ny,nx)
 for (u in 1:nx-1) {
    Haufigkeit[v,u] <- sum( (x>=l[u] & x<l[u+1])+(y>=b[v] & y<b[v+1])==2 ) #Zählen
der (x, y)-Päärchen pro halboffenem Intervall/Rechteck, bis auf Rand
                                                      # oberer Rand (ohne rechte
for (u in 1:nx-1) {
Ecke), nach rechts offenes Hufeisen
 Haufigkeit[ny.u] <- sum((x>=l[u] & x<l[u+1])+(y>=b[ny] & y<=b[ny+1])==2)
for (v in 1:ny-1) {
 Haufigkeit[v.nx] <- sum((x>=I[nx] & x<=I[nx+1])+(y>=b[v] & y<b[v+1])==2) #rechter
Rand (ohne obere Ecke), nach oben offenes Hufeisen
\label{eq:haufigkeit[ny.nx] <- sum(x>=l[nx] & x<=l[nx+1])+(y>=b[ny] & y<=b[ny+1])==2) \#Ecke} \\
rechts oben, abgeschlossen
 f \leftarrow function(x1,y1) {
 #Haufigkeit big = Große Matrix, Blöcke mit Werten von Häufigkeit, entspricht einer
Verfeinerung des Gitters
Haufigkeit_big <- matrix(0,length(y1)-1,length(x1)-1)
 for (p in 1: (lenath(x1)-2)) {
  for (q in 1:(length(y1)-2)) {
   for (k \text{ in } 1:nx) \{ if (x1[p] > = I[k] \& x1[p] < I[k+1]) \{ i < -k \} \}
entsprechenden Wert von Haufigkeit für den passenden Bereich in Haufigkeit big
   for (k \text{ in } 1:ny) \{ if (y1[q] >= b[k] \& y1[q] < b[k+1]) \{ j <- k \} \}
   Haufigkeit big[g.p] <- Haufigkeit[i.i]
```

```
for (p in 1: (lenath(x1)-2)) {
                                             # oberer Rand (ohne rechte Ecke), nach
rechts offenes Hufeisen
  for (k in 1:nx) {
   if(x1[p]>=l[k] & x1[p]<l[k+1]) {i <-k}
  Haufigkeit_big[length(y1)-1,p]<- Haufigkeit[ny.i]
                                             # rechter Rand (ohne obere Ecke), nach
 for (q in 1: (lenath(y1)-2)) {
oben offenes Hufeisen
  for (k in 1:ny) {
   if (y1[q]>=b[k] & y1[q]<b[k+1]) {j <-k}
  Haufigkeit_big[q.length(x1)-1]<- Haufigkeit[j.nx]
 Haufigkeit_big[length(y1)-1,length(x1)-1]<-Haufigkeit[ny.nx] #rechte obere Ecke
 return(Haufigkeit_big)
 #Vorgabe des feineres Gitters
 xnew <- seg(min(x), max(x), length=1+ approx*nx/10)
 vnew <- seg(min(y), max(y), length=1+ approx*ny/10)
 z <- f(xnew.ynew)
 y2 <- seg(min(xnew), max(xnew), length.out=nrow(z)) # Intervalle
 x2 <- seq(min(vnew), max(vnew), length.out=ncol(z))
 persp(x2,y2,z,
   xlim = range(x2), ylim = range(y2),
   zlim = range(z, na.rm = TRUE).
   xlab = xlab, ylab = ylab, zlab = zlab
   main = main, sub = sub,
   theta = theta, phi = phi, r = r, d = d,
   scale = scale, expand = expand.
   col = col, border = border, ltheta = ltheta, lphi = lphi,
    shade = shade, box = box, axes = axes, nticks = nticks.
   ticktype = ticktype,
   cex.lab = cex.lab , font.lab = font.lab,
   cex axis=cex axis, font axis=font axis
```





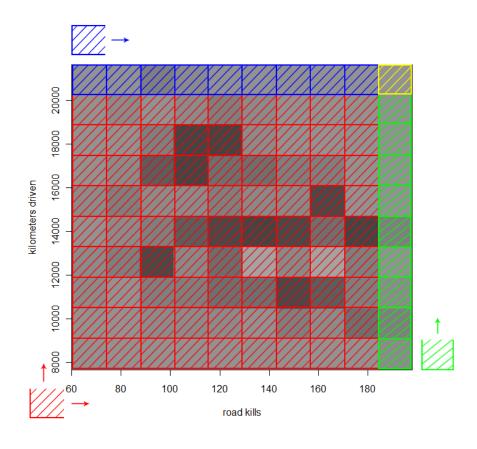
```
# Aufteilung des Definitionsbereichs in Intervalle bzw. Rechtecke
 I <- seg(min(x), max(x), length.out=nx+1)
 b <- seg(min(y), max(y), length.out=ny+1)
 #Haufigkeit = Anzahl von (x,y)-Pärchen pro Intervall bzw. Rechteck
 Haufigkeit <- matrix(0,ny,nx)
 for (u in 1:nx-1) {
  for (v in 1:ny-1) {
    Haufigkeit[v.u] <- sum((x>=l[u] & x<l[u+1])+(y>=b[v] & y<b[v+1])==2) #Zählen
der (x.y)-Päärchen pro halboffenem Intervall/Rechteck, bis auf Rand
for (u in 1:nx-1) {
                                                      # oberer Rand (ohne rechte
Ecke), nach rechts offenes Hufeisen
  Haufigkeit[ny.u] <- sum( (x>=l[u] & x<l[u+1])+(y>=b[ny] & y<=b[ny+1])==2)
 for (v in 1:ny-1) {
  Haufigkeit[v,nx] <- sum( (x>=l[nx] & x<=l[nx+1])+(y>=b[v] & y<b[v+1])==2)
                                                                               #rechter
Rand (ohne obere Ecke), nach oben offenes Hufeisen
 Haufigkeit[ny.nx] <- sum((x>=l[nx] & x<=l[nx+1])+(y>=b[ny] & y<=b[ny+1])==2) #Ecke
rechts oben, abgeschlossen
```





Fakultät Mathematik - M4 - Lehrstuhl für Mathematische Statistik

- 1. Search breakpoints for intervalls (from min(x) to max(x))
- 2. Initialise matrix of #intervals x #intervals
- 3. Fill "inner" with L-shaped squares
- 4. Fill upper margin with C-shaped squares
- 5. Fill right margin with U-shaped squares
- 6. Fill upper right corner with closed box
- ⇒ No datapoint is counted twice!
- → Matrix "Haufigkeit" is filled with frequencie-values of the intervals.







The Code – step by step

```
hist3d <- function(x,y, nx=10, ny=10, approx=75
   # x = Wert x-Achse
   # y = Wert y-Achse
   # nx = Anzahl Intervalle auf der x-Achse
   # ny = Anzahl Intervalle auf der y-Achse
   # approx = approximationsfaktor. Je größer, desto mehr ähnelt die Oberfläche einem
Barplot (Achtung bei großen Zahlen Rechenintensiv! approx *nx/10 und approx*ny/10
sollte bei ca. 100 bleiben.
   xlim = range(x),
   vlim = range(y),
   zlim = c(0, length(x)),
   xlab = "x".
   vlab = "y",
   zlab = "z".
   main = NULL
   sub = NULL.
   theta = 20.
   phi = 20.
   r = sart(3),
   d = 1,
   scale = TRUE,
   expand = 1.
   col = "white"
   border = NULL.
   Itheta = -135,
   lphi = 0,
   shade = NA
   box = TRUE.
   axes = TRUE.
   nticks = 5.
   ticktype = "simple",
   # persp - Argumente
   cex.lab = par("cex.lab").
   font.lab= par("font.lab"),
   cex.axis= par("cex.axis").
   font.axis= par("font.axis")
   #par - Argumente
#x-Achse nach vorne:
tempy=y:tempx=x;
```

```
# Aufteilung des Definitionsbereichs in Intervalle bzw. Rechtecke
 I <- seg(min(x), max(x), length.out=nx+1)
 b <- seg(min(y), max(y), length.out=ny+1)
 #Haufigkeit = Anzahl von (x.v)-Pärchen pro Intervall bzw. Rechteck
 Haufigkeit <- matrix(0,ny,nx)
 for (u in 1:nx-1) {
    Haufigkeit[v.u] <- sum( (x>=l[u] & x<l[u+1])+(y>=b[v] & y<b[v+1])==2 ) #Zählen
der (x,y)-Päärchen pro halboffenem Intervall/Rechteck, bis auf Rand
for (u in 1:nx-1) {
                                                       # oberer Rand (ohne rechte
Ecke), nach rechts offenes Hufeisen
  Haufigkeit[nv.u] <- sum((x>=|[u] & x<|[u+1])+(y>=b[nv] & y<=b[ny+1])==2)
 for (v in 1:ny-1) {
  Haufigkeit[v,nx] <- sum((x>=l[nx] & x<=l[nx+1])+(y>=b[v] & y<b[v+1])==2) #rechter
Rand (ohne obere Ecke), nach oben offenes Hufeisen
 \label{eq:haufigkeit[ny.nx] <- sum((x>=|[nx] & x<=|[nx+1])+(y>=b[ny] & y<=b[ny+1])==2) \#Ecke} \\
rechts oben, abgeschlossen
```

```
for (p in 1:(lenath(x1)-2)) {
                                             # oberer Rand (ohne rechte Ecke), nach
rechts offenes Hufeisen
 for (k in 1:nx) {
 if(x1[p]>=1[k] & x1[p]<1[k+1]) {i <-k}
 Haufigkeit_big[length(y1)-1,p]<- Haufigkeit[ny.i]
for (q in 1:(lenath(y1)-2)) {
                                             # rechter Rand (ohne obere Ecke), nach
oben offenes Hufeisen
 for (k in 1:ny) {
  if(y1[q]>=b[k] & y1[q]<b[k+1]) {i <-k}
 Haufigkeit bio[q.length(x1)-1]<- Haufigkeit[j.nx]
Haufigkeit_big[length(y1)-1,length(x1)-1]<-Haufigkeit[ny.nx] #rechte obere Ecke
return(Haufigkeit_big)
#Vorgabe des feineres Gitters
xnew <- seq(min(x), max(x), length=1+ approx*nx/10)
vnew <- seq(min(y), max(y), length=1+ approx*nv/10)
z <- f(xnew.ynew)
```



```
y2 <- seg(min(xnew), max(xnew), length, out=nrow(z)) # Intervall x2 <- seg(min(xnew), max(xnew), length, out=ncol(z)) # Intervall x2 <- seg(min(xnew), max(xnew), length, out=ncol(z)) # Intervall x2 <- yet, x2 <- yet, x3 <- yet, x3 <- yet, x4 <- yet, x4
```

Computing the finer grid





Computing the finer grid

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```
for (p in 1: (lenath(x1)-2)) {
                                             # oberer Rand (ohne rechte Ecke), nach
rechts offenes Hufeisen
 for (k in 1:nx) {
  if (x1[p]>=|[k] & x1[p]<|[k+1]) {i <-k}
 Haufigkeit_big[length(y1)-1,p]<- Haufigkeit[ny.i]
for (q in 1: (lenath(y1)-2)) {
                                             # rechter Rand (ohne obere Ecke), nach
oben offenes Hufeisen
 for (k in 1:ny) {
  if(y1[q]>=b[k] & y1[q]<b[k+1]) {i <-k}
 Haufigkeit_big[q.length(x1)-1]<- Haufigkeit[j.nx]
Haufigkeit_big[length(y1)-1,length(x1)-1]<-Haufigkeit[ny.nx] #rechte obere Ecke
return(Haufigkeit_big)
#Vorgabe des feineres Gitters
xnew <- seq(min(x), max(x), length=1+ approx*nx/10)
vnew <- seq(min(y), max(y), length=1+ approx*ny/10)
z <- f(xnew.ynew)
```

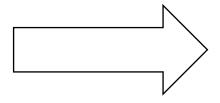




Computing the finer grid

- Create more breakpoints (length.out= 1 * approx/10 * nx)
- Start same procedure...
- 3. ...but fill new, larger matrix with values from old, smaller matrix









The Code – step by step

```
hist3d <- function(x,y, nx=10, ny=10, approx=75
   # x = Wert x-Achse
   # y = Wert y-Achse
   # nx = Anzahl Intervalle auf der x-Achse
   # ny = Anzahl Intervalle auf der y-Achse
   # approx = approximationsfaktor. Je größer, desto mehr ähnelt die Oberfläche einem
Barplot (Achtung bei großen Zahlen Rechenintensiv! approx *nx/10 und approx*ny/10
sollte bei ca. 100 bleiben.
   xlim = range(x),
   vlim = range(y),
   zlim = c(0, length(x)),
   xlab = "x".
   vlab = "y",
   zlab = "z".
   main = NULL
   sub = NULL.
   theta = 20.
   phi = 20.
   r = sart(3),
   d = 1,
   scale = TRUE,
   expand = 1,
   col = "white"
   border = NULL.
   Itheta = -135,
   lphi = 0,
   shade = NA
   box = TRUE.
   axes = TRUE
   nticks = 5.
   ticktype = "simple",
   # persp - Argumente
   cex.lab = par("cex.lab").
   font.lab= par("font.lab"),
   cex.axis= par("cex.axis").
   font.axis= par("font.axis")
   #par - Argumente
#x-Achse nach vorne:
tempy=y:tempx=x;
```

```
# Aufteilung des Definitionsbereichs in Intervalle bzw. Rechtecke
 I <- seg(min(x), max(x), length.out=nx+1)
 b <- seg(min(y), max(y), length.out=ny+1)
 #Haufigkeit = Anzahl von (x.v)-Pärchen pro Intervall bzw. Rechteck
 Haufigkeit <- matrix(0,ny,nx)
 for (u in 1:nx-1) {
    Haufigkeit[v.u] <- sum( (x>=l[u] & x<l[u+1])+(y>=b[v] & y<b[v+1])==2 ) #Zählen
der (x,y)-Päärchen pro halboffenem Intervall/Rechteck, bis auf Rand
for (u in 1:nx-1) {
                                                       # oberer Rand (ohne rechte
Ecke), nach rechts offenes Hufeisen
  Haufigkeit[nv.u] <- sum((x>=|[u] & x<|[u+1])+(y>=b[nv] & y<=b[ny+1])==2)
 for (v in 1:ny-1) {
  Haufigkeit[v,nx] <- sum((x>=l[nx] & x<=l[nx+1])+(y>=b[v] & y<b[v+1])==2) #rechter
Rand (ohne obere Ecke), nach oben offenes Hufeisen
 \label{eq:haufigkeit[ny.nx] <- sum((x>=|[nx] & x<=|[nx+1])+(y>=b[ny] & y<=b[ny+1])==2) \#Ecke} \\
rechts oben, abgeschlossen
 f \leftarrow function(x1,y1) {
 #Haufigkeit big = Große Matrix, Blöcke mit Werten von Häufigkeit, entspricht einer
Verfeinerung des Gitters
 Haufigkeit_big <- matrix(0,length(y1)-1,length(x1)-1)
 for (p in 1: (lenath(x1)-2)) {
  for (q in 1:(lenath(y1)-2)) {
   for (k \text{ in } 1:nx) \{ if (x1[p] > = I[k] \& x1[p] < I[k+1]) \{ i < -k \} \}
entsprechenden Wert von Haufigkeit für den passenden Bereich in Haufigkeit big
   for (k \text{ in } 1:ny) \{ if (y1[q] >= b[k] \& y1[q] < b[k+1]) \{ j <- k \} \}
   Haufigkeit big[g.p] <- Haufigkeit[i.i]
```

```
for (p in 1: (lenath(x1)-2)) {
                                            # oberer Rand (ohne rechte Ecke), nach
rechts offenes Hufeisen
  for (k in 1:nx) {
  if(x1[p]>=l[k] & x1[p]<l[k+1]) {i <-k}
  Haufigkeit_big[length(y1)-1,p]<- Haufigkeit[ny.i]
                                            # rechter Rand (ohne obere Ecke), nach
for (q in 1: (lenath(y1)-2)) {
oben offenes Hufeisen
  for (k in 1:ny) {
   if (y1[q]>=b[k] & y1[q]<b[k+1]) {j <-k}
  Haufigkeit_big[q.length(x1)-1]<- Haufigkeit[j.nx]
Haufigkeit_big[length(y1)-1,length(x1)-1]<-Haufigkeit[ny.nx] #rechte obere Ecke
 return(Haufigkeit_big)
#Vorgabe des feineres Gitters
xnew <- seq(min(x), max(x), length=1+ approx*nx/10)
vnew <- seg(min(y), max(y), length=1+ approx*ny/10)
z <- f(xnew.ynew)
 y2 <- seq(min(xnew), max(xnew), length.out=nrow(z)) # Intervalle
x2 <- seg(min(vnew), max(vnew), length.out=ncol(z))
persp(x2,y2,z,
   xlim = range(x2), ylim = range(y2),
   zlim = range(z, na.rm = TRUE).
   xlab = xlab, ylab = ylab, zlab = zlab
   main = main, sub = sub,
   theta = theta, phi = phi, r = r, d = d,
   scale = scale, expand = expand.
   col = col, border = border, ltheta = ltheta, lphi = lphi,
   shade = shade, box = box, axes = axes, nticks = nticks,
   ticktype = ticktype,
   cex.lab =cex.lab , font.lab =font.lab.
   cex axis=cex axis, font axis=font axis
```

Plotting with persp()





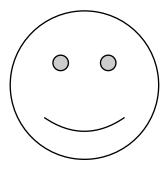
Plotting with persp()

```
persp(x2,y2,z,
xlim = range(x2), ylim = range(y2),
zlim = range(z, na.rm = TRUE),
xlab = xlab, ylab = ylab, zlab = zlab,
main = main, sub = sub,
theta = theta, phi = phi, r = r, d = d,
scale = scale, expand = expand,
col = col, border = border, ltheta = ltheta, lphi = lphi,
shade = shade, box = box, axes = axes, nticks = nticks,
ticktype = ticktype,
cex.lab = cex.lab, font.lab = font.lab,
cex.axis = cex.axis, font axis = font axis
)
```



Plotting with persp()

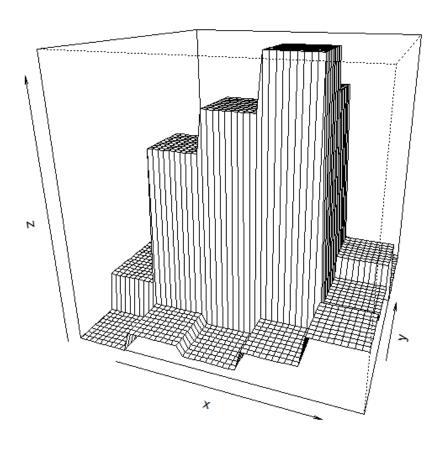
- Plot the fine grid, respectively the new, large matrix
- ...and use all handed-through parameters

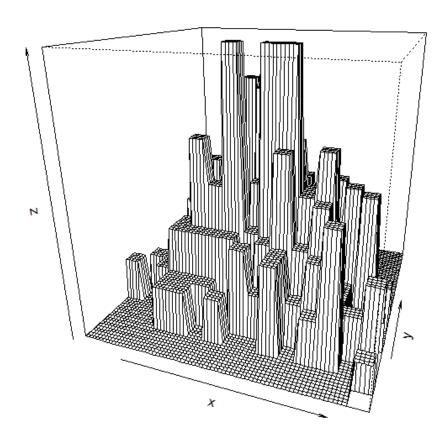


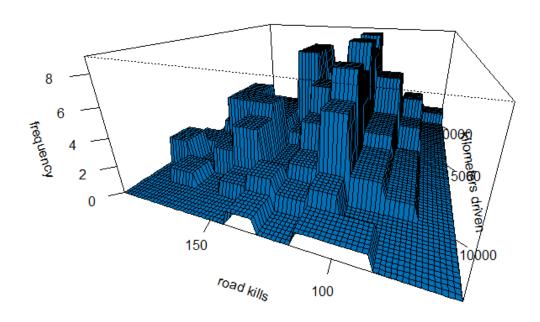
II. 3-dimensional barplots: hist3d

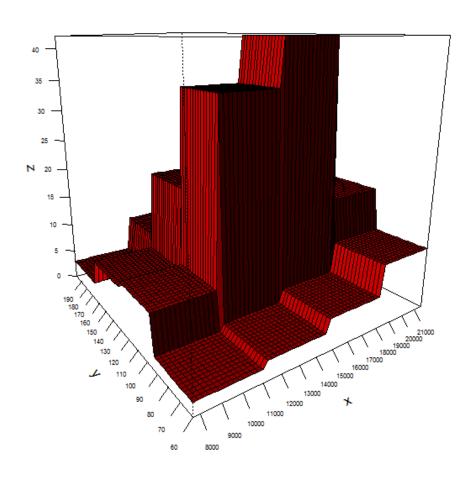
- i. Motivation
- ii. Implementation
- iii. The Code step by step
 - iv. Results
 - v. hist3drot
 - vi. Alternatives

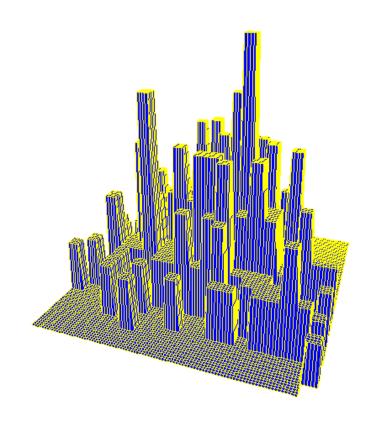
iv. Results

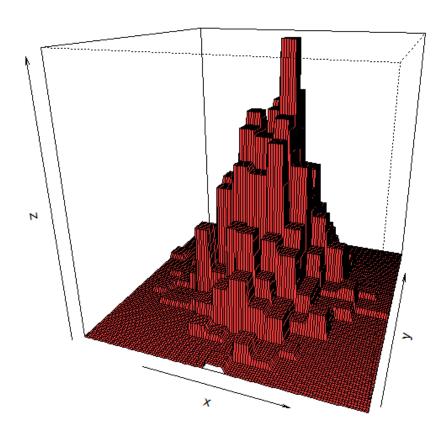












II. 3-dimensional barplots: hist3d

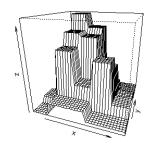
- i. Motivation
- ii. Implementation
- iii. The Code step by step
 - iv. Results
 - v. hist3drot
 - vi. Alternatives

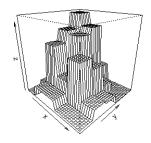
v. hist3drot

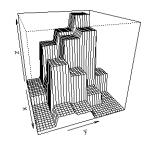
hist3d's little sister

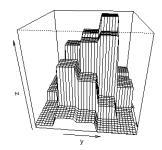
hist3drot

- No rotation in R graphic-window possible
- => hist3drot does that for you









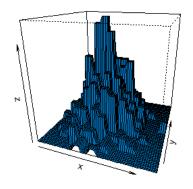
hist3drot

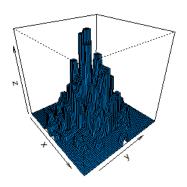
- Two additional parameters:
 - dphi
 - dtheta
- ...specify phi and theta rotation in each new plot
- Four plots alltogether (par(mfrow=c(2,2)))

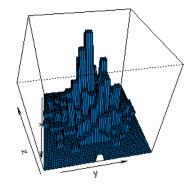
Code

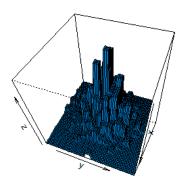
```
par(mfrow=c(2,2))
persp(x2,y2,z,theta=theta, phi=phi, ...
persp(x2,y2,z,theta=theta+dtheta, phi=phi+dphi, ...
persp(x2,y2,z,theta=theta+2*dtheta, phi=phi+2*dphi, ...
persp(x2,y2,z,theta=theta+3*dtheta, phi=phi+3*dphi, ...
par(mfrow=c(1,1))
```

hist3drot









II. 3-dimensional barplots: hist3d

- i. Motivation
- ii. Implementation
- iii. The Code step by step
 - iv. Results
 - v. hist3drot
 - vi. Alternatives

vi. Alternatives

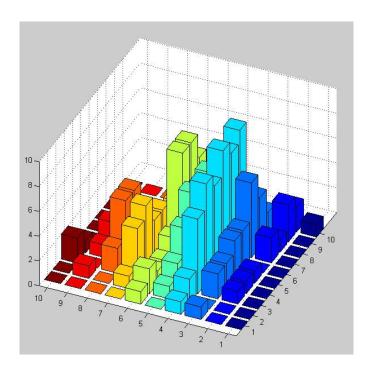
Plotting 3-dimensional bars

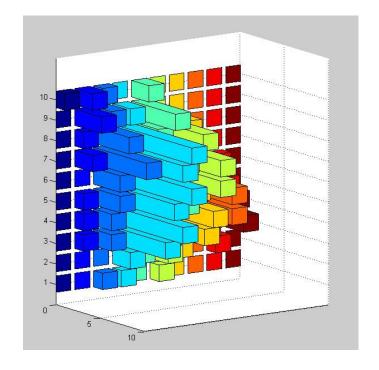




Alternatives: Matlab

- Matlab does provide 3-dimensional barplots
- "bar3" function

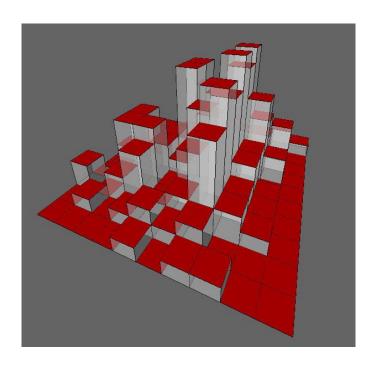


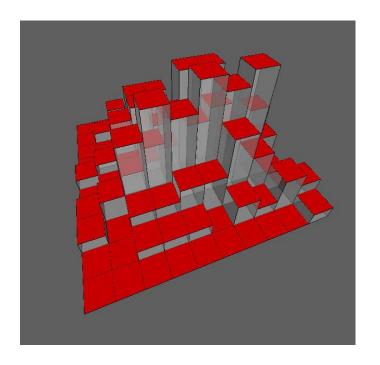






- Rgl package provides a sophisticated plotting engine
- "hist3d" function





III. Plotting maps with R

- i. The "map" and "mapproj" package
 - ii. The "drawmap()" function
 - iii. Alternatives

i. The "map" and "mapproj" package

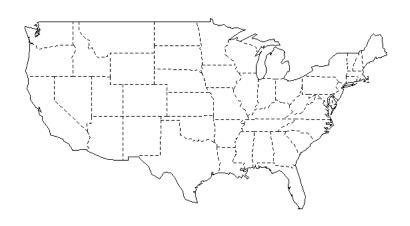
Plotting maps

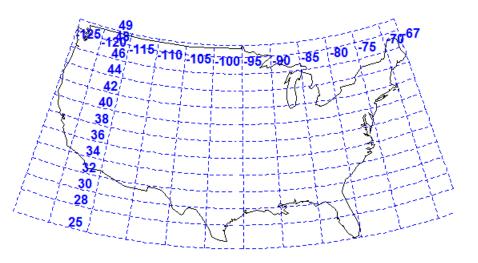


The "map" and "mapproj" package

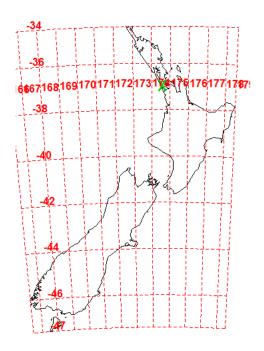
- Includes "map()" function that plots maps
- Includes "mapproj()" function that projects maps on spheres etc.
- Documentation of maps package: http://cran.r-project.org/web/packages/maps/maps.pdf
- Documentation of mapproj package: http://cran.r-project.org/web/packages/mapproj/mapproj.pdf

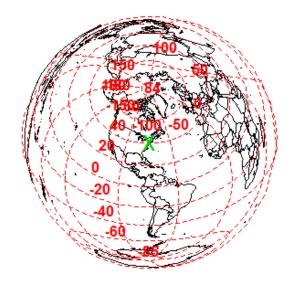
[Source: R documentation]





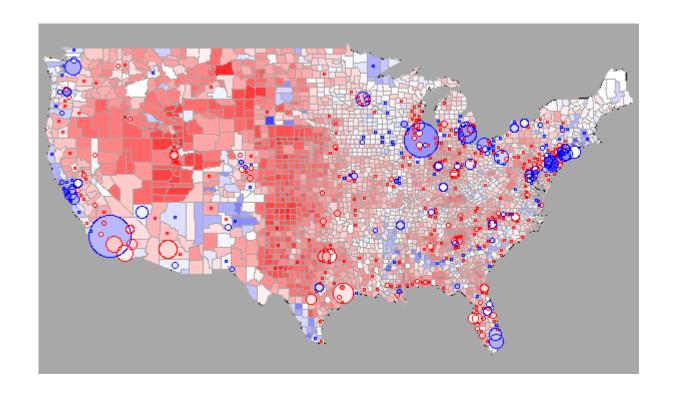
[Source: R documentation]





[Source: http://www.ai.rug.nl/~hedderik/R/US2004/map.r]

Plotting a colour-based "histogram" with "map()" is possible…





[Source: http://www.ai.rug.nl/~hedderik/R/US2004/map.r]

...however code-intensive

Rijn, 041105 ## hedderik@ai.rug.nl, Artificial Intelligence Groningen ## ## http://www.ai.rug.nl/~hedderik/R/election2004map ## ## Written for R 2.0.0+ (because of use of transparancy in plotting) ## ## -- ## ## Code to plot a map of the US elections with, apart from just coloring ## almost each country red, colored circles reflecting the number of voters ## in each county. (I *do* know about the perceptual problems with circles - ## but this way it at least looks like Kerry was close :-)). ## ## Plot is based on the excellent plots found on the New York Times election ## website. plotting code and databases. Library "maps" is not installed by ## default in R 2+ so, if necessary, install maps first (using something ## like install.packages("maps",lib="~/Library/R/R-2.0.0") and setting ## R_LIBS="\$HOME/Library/R" in .Renviron. library("maps") ## --- ## bluered constructs a color based on the number of votes for B(ush), ## K(erry). If graded==F, color is either blue or red, otherwise color ## ranges from blue to red, reflecting the proportion of votes for either ## candidate. S (originally for Size) is transparancy of the color. Only ## useful when plotting to an OS X quartz device or to ## pdf(...,version="1.4"). Values other than 1 won't show on X11 or other ## devices. bluered <function(B.K.S=1,graded=F) { if (graded) { ## Purple plot rgb(B/(B+K),0,K/(B+K),S); } else { ## All or none ifelse(B>K,rgb(1,0,0,S),rgb(0,0,1,S)) } } ## map.center returns a dataframe with the name and coordinates of the ## center of each map region. Code is based on map.text, can probably be ## improved as often the map database is already available. map.center <- function (database, regions = ".") { cc = match.call(expand.dots = TRUE) cc[[1]] = as.name("map") cc\$fill = TRUE cc\$plot = FALSE cc\$move = cc\$add = cc\$cex = cc\$labels = NULL cc\$resolution = 0 m <-counties <- map('county',plot=F) ## List of states and abbreviations states <c("ALABAMA"."AL"."ALASKA"."AK"."AMERICAN SAMOA","AS","ARIZONA","AZ","ARKANSAS","AR","CALIFORNIA","CA","COLOR ADO", "CO", "CONNECTICUT", "CT", "DELAWARE", "DE", "DISTRICT OF COLUMBIA", "DC", "FEDERATED STATES OF MICRONESIA", "FM", "FLORIDA", "FL", "GEORGIA", "GA", "GUAM", "GU", "HAWAII", " HI"."IDAHO"."ID"."ILLINOIS"."IL"."INDIANA"."IN"."IOWA"."IA"."KANSAS"."KS"."KE NTUCKY" "KY". "LOUISIANA" "LA". "MAINE". "ME". "MARSHALI ISLANDS","MH","MARYLAND","MD","MASSACHUSETTS","MA","MICHIGAN","MI " "MINNESOTA" "MN" "MISSISSIPPI" "MS" "MISSOLIRI" "MO" "MONTANA" "MT" "NEBRASKA" "NE" "NEVADA" "NV" "NEW HAMPSHIRE" "NH" "NEW

JERSEY","NJ","NEW MEXICO","NM","NEW YORK","NY","NORTH

CAROLINA", "NC", "NORTH DAKOTA", "ND", "NORTHERN MARIANA ISLANDS", "MP",

NIA" "PA" "PUERTO RICO" "PR" "RHODE ISLAND" "RI" "SOUTH CAROLINA". "SC". "SOUTH DAKOTA". "SD". "TENNESSEE". "TN". "TEXAS", "TX", "UTAH", "UT", "VERMONT", "VT", "VIRGIN ISI ANDS" "VI" "VIRGINIA" "VA" "WASHINGTON" "WA" "WEST VIRGINIA","WV","WISCONSIN","WI","WYOMING","WY"); states <data.frame(name=states[(1:(length(states)/2))*2-1],abbrev=states[(1:(length(states)/2))*2]) states\$name <tolower(as character(states\$name)) states\$abbrev <as.character(states\$abbrev) ## Code used to download data files, files needed some tweaking. Data files are ## available separately, if (F) { URL < "http://www.usatoday.com/news/politicselections/yote2004/PresidentialByCounty aspx?oi=P&rti=G&sp=XX&tf=I" for (S in states\$abbrev) { URL.s <sub("XX",S,URL) cmdLine <- sprintf("/sw/bin/lynx -dump \"%s\" | /sw/bin/gawk '{if (\$1==\"County\") output=1; if (\$1==\"Updated:\") output=0; if (output) print \$0; }' > %s.dat",URL.s,S) cat("Working on ",S,"\n"); system(cmdLine) } ## Removed from .dat files ## Removed extra "County" names from NV.dat } ## Remove states for which we don't have any data states <states[sapply(states\$abbrev,function(X){file.exists(sprintf("%s.dat",X))}),] ## Prepare and read in data election <- NULL for (S in states\$abbrev) { ## calls to gawk not necessary if csy files are downloaded, if (F) { cmdLine < sprintf("/sw/bin/gawk -f prep.awk %s.dat > %s.csv",S,S); system(cmdLine) } tmp <- read.table(sprintf("%s.csv",S),header=T,sep=";") tmp\$State <states\$name[states\$abbrev==S] tmp\$X <- NULL if (is.null(election)) { election <tmp; } else { election <- rbind(election,tmp) } } ## Create a column in which state and county is combined, as in the map database election\$stcounty < tolower(paste(election\$State election\$County.sen=".")) ## Add a column (order) to the election df representing the order of ## counties in the map database countyOrder <- data.frame(stcounty = counties\$names,order=1:length(counties\$names)) election <merge(election,countyOrder) ## Determine size of county. (N.B., size is determined by number of voters, ## not by real number of inhabitants.) election\$size <- election\$Bush+election\$Kerry+election\$Nader election\$sizeR <election\$size/max(election\$size) ## Create a vector of colors, counties for which we don't have any data will ## be colored grey, others blue or red depending on who "won" that county, col <- rep("grev".length(counties\$names)) col[tmp\$order] <- ifelse((tmp\$Bush>tmp\$Kerry),"red","blue") ## Add the county center coordinates to the election data. county.coord <- map.center("county") names(county.coord)[1] <- "stcounty"; election <- merge(election,county.coord)

"OHIO", "OH", "OKLAHOMA", "OK", "OREGON", "OR", "PALAU", "PW", "PENNSYLVA

And finally, the actual plotting ## ## -- ## Real plot, only works when exporting to a recent enough version of PDF or ## Quartz. If you're using a device that can't handle transparancy, change ## the .4 and the .6 in the bluered function to 1 pdf("US04Election-PopGraded.pdf", version="1.4", width=10, height=6.5) ## Draw the USA outline map('usa'.fill=T.col="white".bg="darkgray") ## Create the colors for the states col <- rep(rgb(.1,.1,.1,.2),length(counties\$names)) col[election\$order] <- bluered(election\$Bush,election\$Kerry,.4,graded=T) ## Plot states without borders (should work with map, see help for fill ## argument, but cannot get it working) m <- map('county',fill=T,plot=F) polygon(m\$x.m\$v.col=col.border=NA) ## Draw county borders map('county' col="darkgrey" add=T) ## Draw state borders map('state',col="black",add=T,lwd=1) ## Color for circles col < bluered(election\$Bush,election\$Kerry,.6) ## Symbols is the easiest way to draw circles that have the right aspect ratio symbols(election\$x, election\$y,circles=log(election\$sizeR+1)*3,fg=col,bg=col,add=T,inches=F) ',col="darkgrey",add=T) ## Color for circles col < bluered(election\$Bush.election\$Kerry.1.graded=T) ## Symbols is the easiest way to draw circles that have the right aspect ratio symbols(election\$x election\$y,circles=log(election\$sizeR+1)*3,fg=col,bg=col,add=T,inches=F) ## col <- bluered(election\$Bush.election\$Kerry.1.graded=F) ## Symbols is the easiest</p> way to draw circles that have the right aspect ratio symbols(election\$x election\$y,circles=log(election\$sizeR+1)*3,fg=col,bg=NA,add=T,inches=F) ## Not sure which version I like more, the previous (with purple counties) ## or the next one, with blue/red counties, ## Real plot, only works when exporting to a recent enough version of PDF or Quartz, pdf("US04Flection-PopBin.pdf",version="1.4",width=10,height=6.5) ## Draw the USA outline map('usa',fill=T,col="white",bg="darkgray") ## Create the colors for the states co <- rep(rgb(.1,.1,.1,.2),length(counties\$names)) col[election\$order] <bluered(election\$Bush,election\$Kerry,.4,graded=F) ## Plot states without borders (should work with map, see help for fill ## argument, but cannot get i working) m <- map('county'.fill=T.plot=F) polygon(m\$x.m\$v.col=col.border=NA) ## Draw county borders map('county',col="darkgrey",add=T) ## Draw state borders man('state' col="black" add=T lwd=2) ## Color for circles col < bluered(election\$Bush.election\$Kerry..6) ## Symbols is the easiest way to draw circles that have the right aspect ratio symbols(election\$x, election\$y,circles=log(election\$sizeR+1)*3,fg=col,bg=col,add=T,inches=F) dev.off() ## Plot without transparancy, but neutral states colored white. Made with ## help from Gregoire Thomas. bluered <- function(B,K,S=1,graded=F) { if (graded) { ## Suggested by Gregoire Thomas: Kn <- K/(B+K) red <ifelse(Kn<0.5, 1, 2-2*Kn) blue <- ifelse(Kn<0.5, 2*Kn, 1) green <- ifelse(Kn<0.5, blue, red) rgb(red, green, blue, S) } else { ## All or none ifelse(B>K,rgb(1,0,0,S),rgb(0,0,1,S)) } } png("map3.png",width=600,height=400) map('usa',fill=T,col="white",bg="darkgray") ## Create the colors for the states col <- rep(rgb(.1,.1,.1,.2),length(counties\$names)) col[election\$order] <bluered(election\$Bush,election\$Kerry,1,graded=T) ## Plot states without borders (should work with map, see help for fill ## argument, but cannot get it working) m <- map('county',fill=T,plot=F) polygon(m\$x,m\$y,col=col,border=NA) ## Draw county borders map('county

III. Plotting maps with R

- The "map" and "mapproj" package
 - ii. The "drawmap()" function
 - iii. Alternatives

ii. The "drawmap()" function

Plotting maps with colour-based histograms



Motivation

- We want to plot a map with coloured areas...
- ...where the colour is correspondent with the value of an area
- Example:
 - Election map
 - Number of doctors in an area
- Example:
 - The higher the number, the more red the colour is
 - The lower the number, the more green it is



Solution

- The "drawmap()" function
- By Thomas Kneib
- Available here:

http://www.statistik.lmu.de/~semwiso/raeumliche-statistik0809/uebungen/rcode/blatt6/drawmap.r

 By not it is included in a software package called "BayesX": http://www.stat.uni-muenchen.de/~bayesx/bayesx.html

Input data

- "drawmap()" basically builds on the "polygon()" function
- Map input therefore is list of coordinates...
- ...where each list-item is named
- Names may occur twice

Thus:

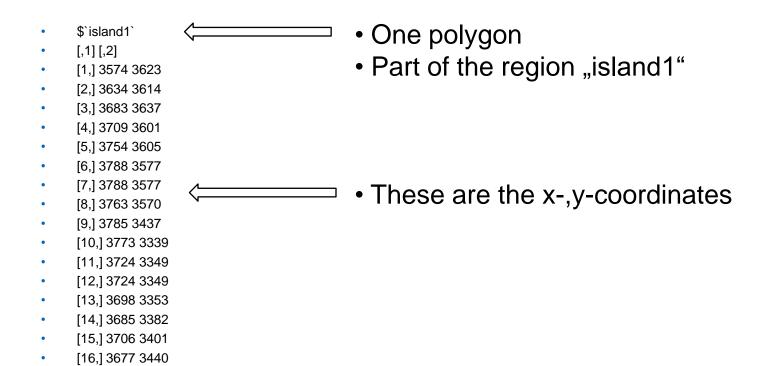
- ⇒ Map consists of polygons
- ⇒ Multiple polygons are grouped to so called "regions" by their name
- ⇒ "regions" may be coloured or their name may be drawn



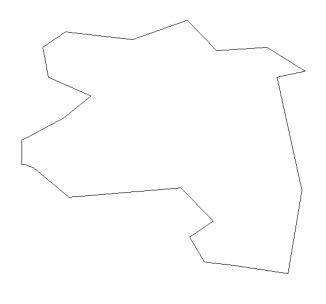


Input data: Example file

[17,] 3577 3429 [18,] 3546 3463



Input data







Data file

- "drawmap()" supports an input file-path...
- ...to a (txt-)file that maps each region-name to a value
- Note: This file is later processed with: ",read.table(FILEPATH, header = T, row.names = NULL)
- ...so be sure to include a header
- Example:

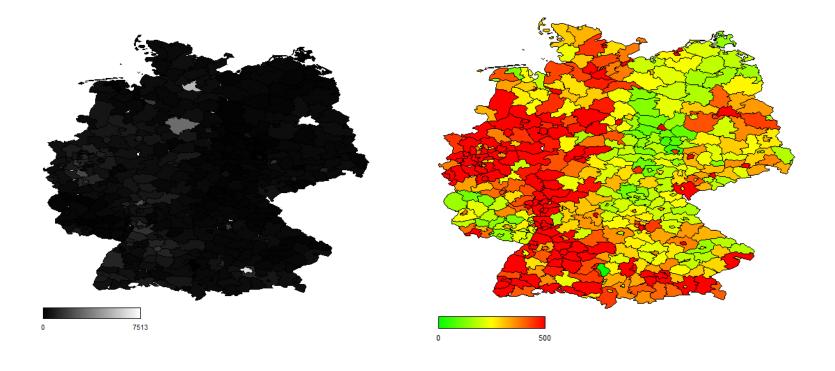
```
"Group.1" "x"
1001 218
1002 703
1003 545
1004 173
```

...maps the region "1001" to the value 218 and so on



Data file

- These values are then computed into a gradient of colour or grays
- ...and the polygons filled with the corresponding colour







"drawmap()" parameters

map The map data needed to plot the map. Expects a list.

dfile The file that links regions' names with values. Expects a path.

regionvar Specifies which column in the dfile contains the regions' names

plotvar Specifies which columns in the "dfile" contains the values.

outfile Specifies the file the map is saved to (in .ps-format).

If left blank, the map is drawn to a window.

lowerlimit Lower limit where to start color-scaling (to avoid outliers)

upperlimit Upper limit where to start color-scaling (to avoid outliers)





"drawmap()" parameters

nrcolors Sets the number of colors for scaling. The more the smoother.

swapcolors Invert the color scaling. Expects logical value.

pcat Simplifies values to -1,0,1 (nrcolors=3). Expects a logical value.

hcl Makes use of the hcl color scaling. Expects a logical value.

h / c / I Sets start and end color for colorscaling if hcl =T

legend Specifies whether to plot legend or not. Expects a logical value.

cex.legend Scales legend's size.

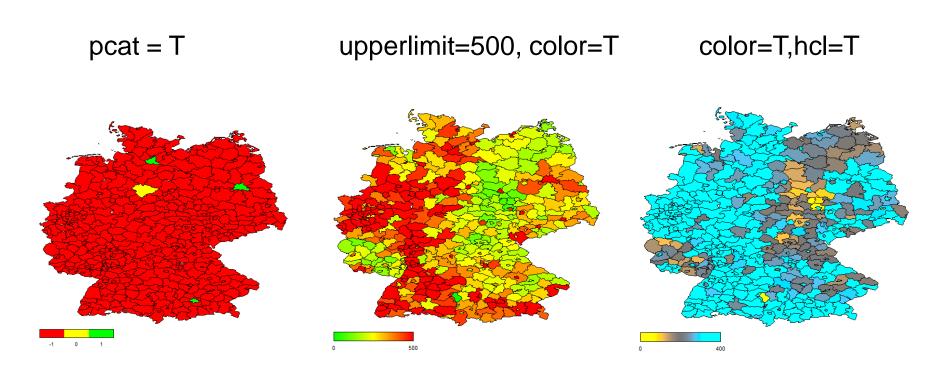
drawnames Draws the regions names. Expects a logical value.

pstitle Sets the title (equivalent to "main" parameter)





Some examples



III. Plotting maps with R

- i. The "map" and "mapproj" package
 - ii. The "drawmap()" function
 - iii. Alternatives

iii. Alternatives

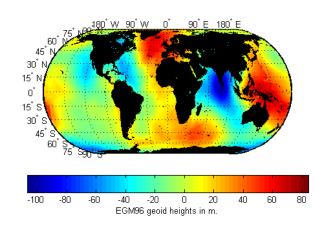
What else is there?

Maps in Matlab: Mapping Toolbox

- Commercial addin for Matlab called "Mapping Toolbox"
- Distributed by "MathWorks"
- Homepage:

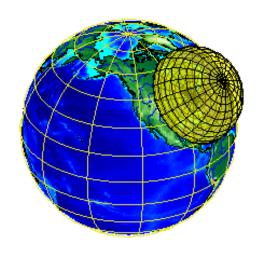
http://www.mathworks.com/products/mapping/

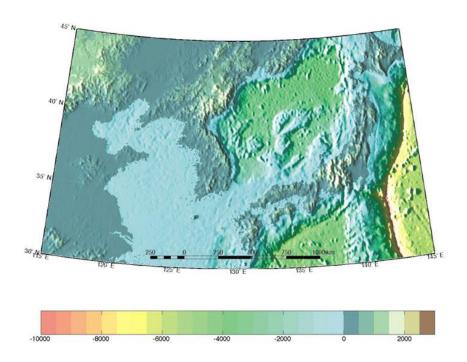






Maps in Matlab: Mapping Toolbox





Thanks to:

Vizenz Erhard - for support!
Prof. Czado - for Proseminar!
You all - for your attention!