

Lecture 1: Computer architecture

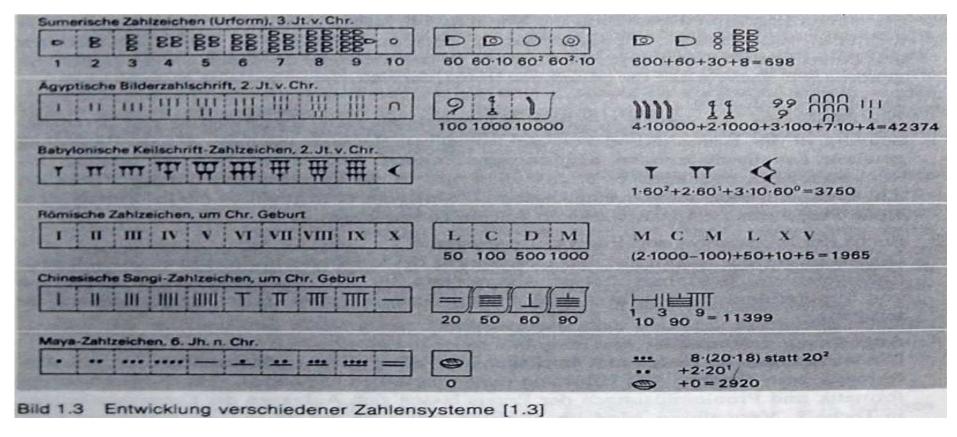
- Numeral systems
- History
- Von-Neumann- architecture
- Boolean Algebra and logic gates



Computer architecture – numeral systems

It all begun with the number systems, which are a set of number representations together with simple operations like addition, subtraction, multiplication and division:

- There are systems with different signs to represent the rating (e.g. Egyptian or Roman)
- There are systems with positional values of the numbers for the rating (e.g. our decimal system which came from India and the nearer east to us)





Computer architecture – numeral system: decimal

- Based on the human experiences with the 10-finger-systems (Chinese and Hindu-Arabic, 3. century BC)
- Positional numeral system which represents each number just with 10 symbols, called digits (base-10 system)
- The simple numbers took a long journey until now (Arabic numerals/Indian numerals)
- It supports mathematical operations very easily
- Fractional parts can be represented by a decimal separator dot
- Positive and negative values can be

represented

7			¥	7	6	7	4	5		Indisch (Brahmi) 3. Jh. v. Chr.
7	2	3	8	4	4	2	1	9	0	Indisch (Gwalior) 8. Jh. n. Chr.
1	6	z	عـد	4	5	2	3	2	0	Westarabisch (Gobär) 11. Jh.
1	?	3	e	4	6	1	8	9	0	Europäisch 15. Jh.
7	2	3	4	5	6	7	8	9	0	Europäisch (Dürer) 16. Jh.
1	2	3	4	5	6	7	8	9	0	Neuzeit (Grotesk) 20, Jh.



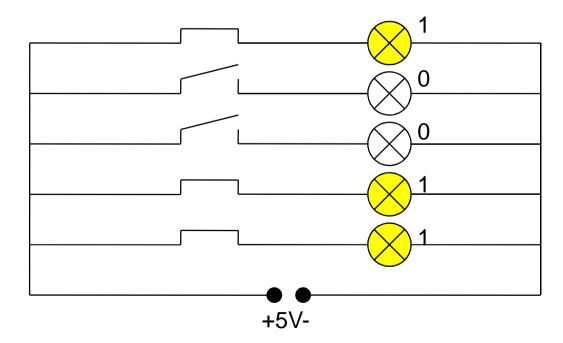
Computer architecture – numeral system: decimal

e.g.



Computer architecture – numeral system: binary

- Origins at China and also developed by the mathematician Leibniz (17th century AD)
- Positional numeral system which represents each number just with 2 symbols,
 0 and 1
- These values can be represented by voltage levels in electronic circuits
- For human use very inefficient but with electronic circuits it is possible to create very efficient arithmetic and logic units (ALUs) for the basic operations addition, subtraction, multiplication and division

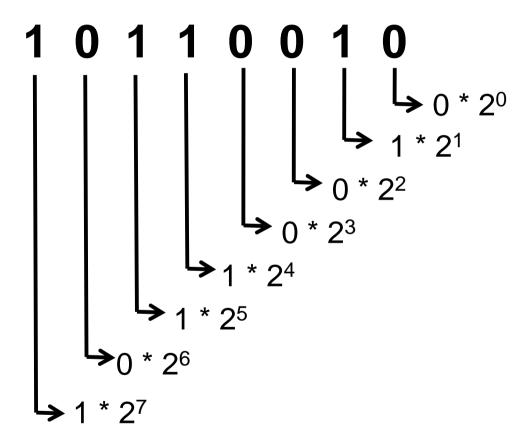






Computer architecture – numeral system: binary

e.g.



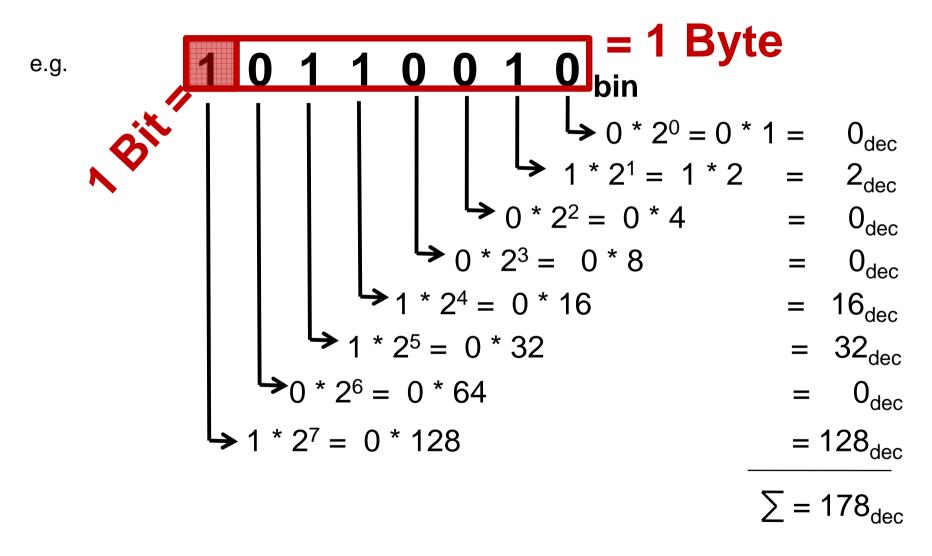


Computer architecture – numeral system: binary -> decimal

e.g. 16_{dec} 32_{dec} $= 128_{dec}$ $\sum = 178_{\text{dec}}$



Computer architecture – numeral system: binary -> decimal





Computer architecture – numeral system: decimal -> binary

1 7 8 dec e.g. \rightarrow 178 / 2 = 89_{dec} Rest 0_{bin} $89/2 = 44_{dec} Rest 1_{bin}$ $44/2 = 22_{dec} Rest 0_{bin}$ $22/2 = 11_{dec} Rest 0_{bin}$ $11/2 = 5_{dec} Rest 1_{bin}$ $5/2 = 2_{dec} \text{ Rest } 1_{bin}$ $2/2 = 1_{dec} Rest 0_{bin}$ $1/2 = 0_{dec} Rest 1_{bin}$







Computer architecture



How many bytes are needed to represent the decimal number 1024?

Which decimal number is given by the binary representation 11010011 (show calculation)?



Lecture 1: Computer architecture

- - History
 - Von-Neumann- architecture
 - Boolean Algebra and logic gates



A short journey through the history of computer science: calculation equipment

Calculation utilities

(2. cent. BC)Calculation boardsAbacus(2. cent. BC)



(17th cent. AD)
John Napier
of Merchistoun
(Napier's bones,
Rabdology, 1623)
-> rods for mult./div.



Mechanical calculation machines (18th cent. AD)

Wilhelm Schickard (Speeding Clock, 1623)

- -> slide rules for mult./div.
- -> 6 digit add./sub.
- -> carryover-gear
- -> overflow detection



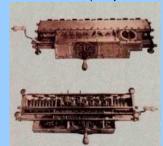
Blaise Pascal (1641)

- -> 8 digit add./sub.
- -> similar to Schickards

Gottfried Wilhelm Freiherr von Leibnitz

(Stepped Reckoner, 1673)

- -> add./sub./mult./div.
- -> Staffelwalze (step reckoner)



Mathäus Hahn (1674)

-> industrial produced calculation machines

See: Rembold, Ulrich et. al.: Einführung in die Informatik für Naturwissenschaftler und Ingenieure. Hanser München Wien 1991

See: http://privat.swol.de/SvenBandel/index.html, Download 01.09.2007 See: http://en.wikipedia.org/wiki/Image:Boulier1.JPG, 01.09.2007



A short journey through the history of computer science: calculation equipment

Programmable, mechanical calculation machines (19th/early 20th cent. AD)

Falcon (1728)

Joseph-Marie Jacquard (1805)

-> punchcard looms for work steps (program)



Charles Babage

(Difference Engine, 1822 Idea of a calculation machined)

-> ideas how they are used in moden computers

Input/Output

Algorithmic unit Control unit

Number memory



Herrmann Hollerith

(Tabulating machine, 1886)

- -> punch cards with personal data (information storage)
- -> counting clocks
- -> sorter machines
- -> punch card writer
- => US-population census 1890

Konrad Zuse

(Z1, 1934)

- -> calculator similar to Babbage's
- -> binary floating point numbers
- -> logic operations

See: Rembold, Ulrich et. al.: Einführung in die Informatik für Naturwissenschaftler und Ingenieure. Hanser München Wien 1991

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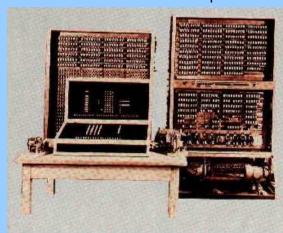
A short journey through the history of computer science: calculation equipment

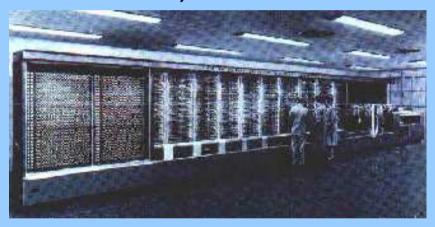
Modern electrical calculation utilities (middle 20th cent. BC)

Konrad Zuse

(Z3, 1941)
-> relaisbased algorithmic

- and logic unit (binary)-> program on punch tapes
- -> instructions consist of address- and operationpart
- -> structure of modern computers





Howard H. Aiken

(Mark 1, 1944)

- -> electromechanical
- -> decimal system based
- instructions consist of address-, control unitand order-part



A short journey through the history of computer science: calculation equipment

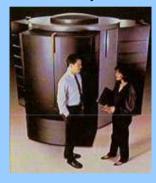
Modern electronic (digital) calculation utilities (Computer) (late 20th cent. BC)

John P. Eckert John W. Mauchly (Electronic Numerical **Integrator and Computer** (ENIAC), 1946)

- -> valvebased algorithmic and logic unit
- -> digital computer (binary)

1953 - 1958

-> valves, core memory, magnetic memory, mainframe



1958 - 1966

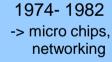
-> transistors, operating systems, prog. languages, computer science





1966 - 1974

-> integrated circuits, structured prog., realtime processing



1982-1990

-> high integrated circuits, parallel computing, home computer



1990 - now

-> personal computer, internet, middleware, object oriented and higher languages







See: Rembold, Ulrich et. al.: Einführung in die Informatik für Naturwissenschaftler und Ingenieure. Hanser München Wien 1991; See: http://privat.swol.de/SvenBandel/index.html, Download 01.09.2007; See: http://en.wikipedia.org/wiki/Eniac, Download 02.09.2007; See: http://renebrossard.com/NetworkingStudy.htm, Download 04.10.2009;

See: http://www.luxist.de/luxist/2008/01/16/it-gadgets-asus-eeepc-4q-ein-weltweit-einmaliges-pc-konzept/, Download 04.10.2009



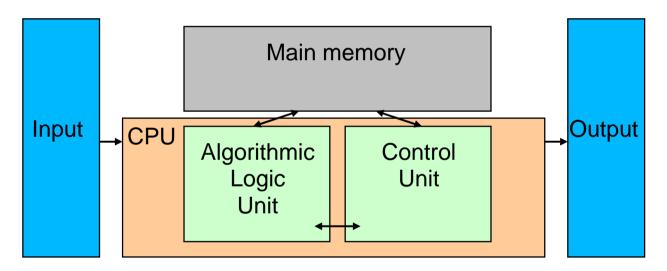
Lecture 1: Computer architecture

- **∀** History
 - Von-Neumann- architecture
- Boolean Algebra and logic gates



Computer architecture – John von Neumann

The heart of a computer: the central processing unit (CPU) or processor

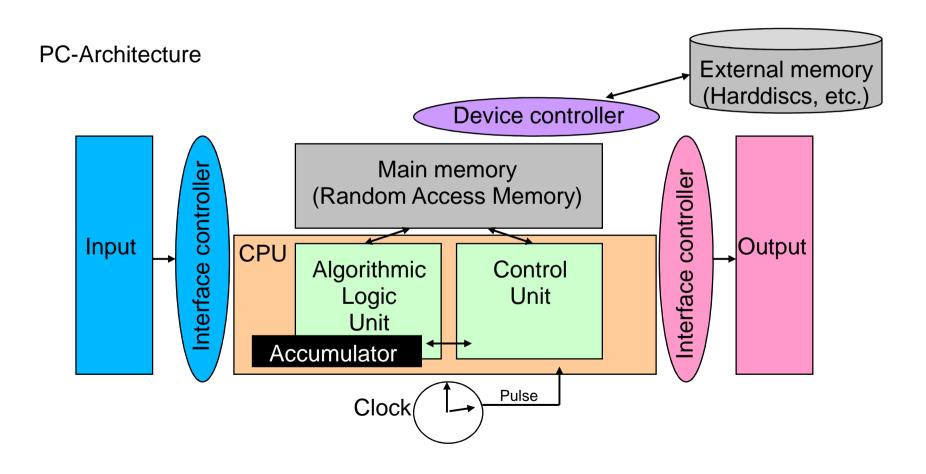


John von Neumann – Architecture (1945)



Computer architecture – Personal Computer

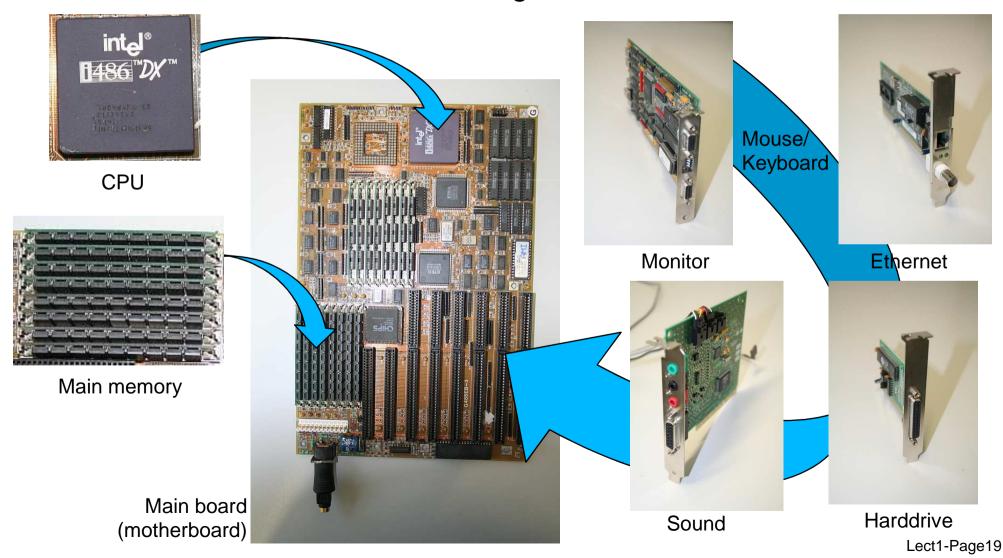
Scheme of a computer





Computer architecture – Personal Computer

PC-architecture, e.g. old main board





Computer architecture – Personal Computer

CPU operations work flow

FETCH: Fetch the binary, numerical representation of an instruction from

memory

DECODE: Break the instruction into ist parts, which are used at the

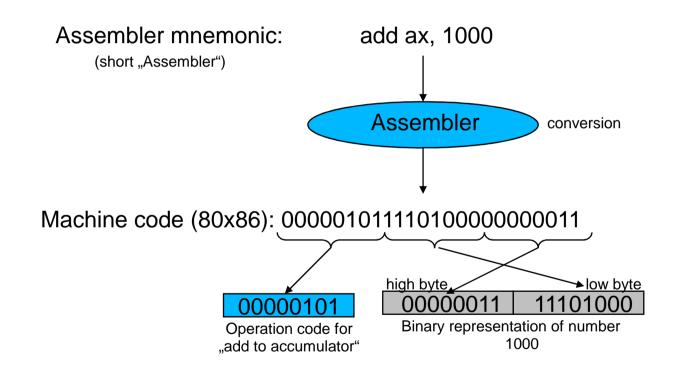
different areas of the CPU

EXECUTE: Performe the operation at the different areas of the CPU

WRITEBACK: Write the result back to memory



Computer architecture – Machine instructions





Computer architecture – Machine instructions sequence

```
Instruction counter

start:
mov ax, data
mov ds, ax

mov dx, hello
mov ah, 09h
int 21h

mov al, 0
mov ah, 4Ch
int 21h

segment data
hello: db 'Hello World!', 13, 10, '$'
```

Prints "Hello World!" to output (monitor)



Lecture 1: Computer architecture

- **∀** History
- ∀Von-Neumann- architecture
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Computer architecture – Boolean algebra

A **Boolean algebra** is a set A, supplied with two elements 0 (called zero) and 1 (called one) and at least one binary operation (AND or OR) and an unary operation (NOT), such that, for all elements a, b and c of set A, the following axioms hold:

$$a \lor (b \lor c) = (a \lor b) \lor c$$

$$a \wedge (b \wedge c) = (a \wedge b) \wedge c$$

associativity

$$a \lor b = b \lor a$$

$$a \wedge b = b \wedge a$$

$$a \lor (a \land b) = a$$

$$a \wedge (a \vee b) = a$$

$$a \lor (b \land c) = (a \lor b) \land (a \lor c) \quad a \land (b \lor c) = (a \land b) \lor (a \land c)$$

$$a \wedge (b \vee c) = (a \wedge b) \vee (a \wedge c)$$

$$a \vee \neg a = 1$$

$$a \wedge \neg a = 0$$

$$a \lor a = a$$

$$a \wedge a = a$$

$$a \lor 0 = a$$

$$a \wedge 1 = a$$

 $a \wedge 0 = 0$

boundedness

$$a \lor 1 = 1$$

$$\neg 1 = 0$$

0 and 1 are complements

$$\neg 0 = 1$$
$$\neg (a \lor b) = \neg a \land \neg b$$

$$\neg(a \land b) = \neg a \lor \neg b$$

De Morgan's laws

$$\neg \neg a = a$$

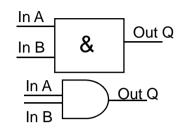
involution

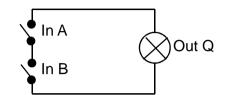


Computer architecture – Boolean algebra and logic gates

AND \wedge , •

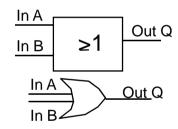
In A	In B	Out Q
0	0	0
0	1	0
1	0	0
1	1	1

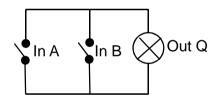




OR \(\sqrt{} , +

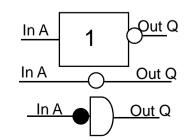
In A	In B	Out Q
0	0	0
0	1	1
1	0	1
1	1	1

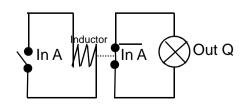




NOT -, -

In A	Out Q
0	1
1	0







Complex gate structures are possible => ALU

e.g.

In A	In B	Out Q
0	0	0
0	1	1
1	0	1
1	1	0

$$\overline{A}$$
 AND \overline{B} A AND \overline{B}

$$Q = (\overline{A} \text{ AND B}) \text{ OR } (A \text{ AND B})$$

Disjunctive normal form



e.g.

In A	In B	Out Q
0	0	1
0	1	1
1	0	0
1	1	1

$$Q = (\overline{A} \text{ AND } \overline{B}) \text{ OR}$$

$$\overline{A} \text{ AND } B$$

$$(\overline{A} \text{ AND } B) \text{ OR}$$

$$(\overline{A} \text{ AND } B)$$
Disjunctive normal for

Simplify (reduce gates)

Mathematical formal solution

Q = (A AND B) OR (A AND B) OR (A AND B) distributivity

= $(\overline{A} \text{ AND } \overline{B}) \text{ OR } (A \text{ OR } A) \text{ AND } B$

= (\overline{A} AND \overline{B}) OR 1 AND B boundedness

= (A AND B) OR B

= (B OR A) AND (B OR B)

complements

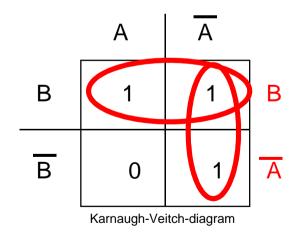
= (B OR \overline{A}) AND 1

boundedness

= (B OR A)

Graphical solution

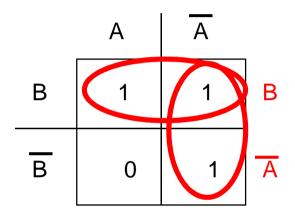
Disjunctive normal form

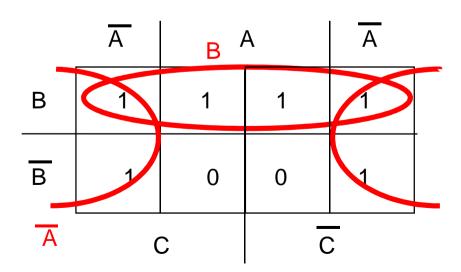


$$Q = (A OR B)$$

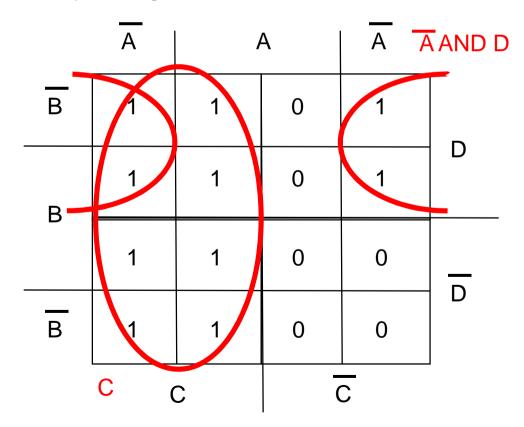


Karnaugh-Veitch-diagram





- Graphical solution
- Reduce number of gates to optimal minimum
- Combine groups with 1, 2, 4 or 8 members
- Combine always max. number of elements
- Border crossing is alowed
- Multiple usage is allowed



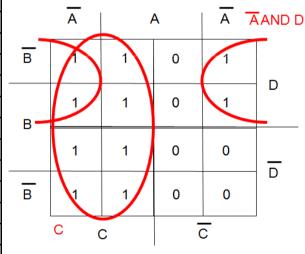


Cross-checking:

Source table:

A	В	C	D	OUT
0	0	0	0	0
0	0	0	1	1
0	0	1	0	1
0	0	1	1	1
0	1	0	0	0
0	1	0	1	1
0	1	1	0	1
0	1	1	1	1
1	0	0	0	0
1	0	0	1	0
1	0	1	0	1
1	0	1	1	1
1	1	0	0	0
1	1	0	1	0
1	1	1	0	1
1	1	1	1	1

Karnaugh-Veitch-diagram:



Check simplification:

A	В	C	D	NOT	D	((NOT A)	C	OUT =
				A		AND D)		C OR ((NOT A) AND D)
0	0	0		1	0	0	0	, ,
0	0	0	0	1	0	0	0	0
0	0	0	1	1	1	1	0	1
0	0	1	0	1	0	0	1	1
0	0	1	1	1	1	1	1	1
0	1	0	0	1	0	0	0	0
0	1	0	1	1	1	1	0	1
0	1	1	0	1	0	0	1	1
0	1	1	1	1	1	1	1	1
1	0	0	0	0	0	0	0	0
1	0	0	1	0	1	0	0	0
1	0	1	0	0	0	0	1	1
1	0	1	1	0	1	0	1	1
1	1	0	0	0	0	0	0	0
1	1	0	1	0	1	0	0	0
1	1	1	0	0	0	0	1	1
1	1	1	1	0	1	0	1	1

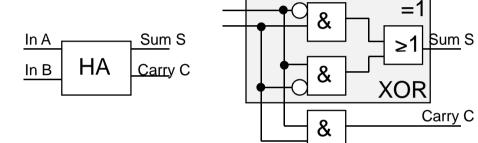
equal?



Addition as basis of all mathematical operations: Half- and Full-Adder

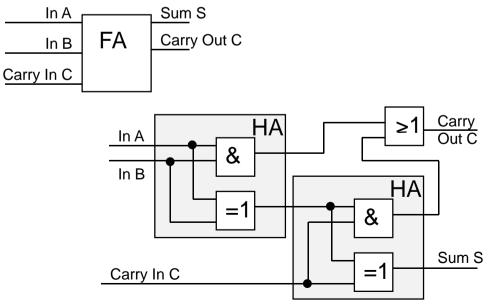
HA

In A	In B	Sum S	Carry C
0	0	0	0
0	1	1	0
1	0	1	0
1	1	0	1



FA

Carry In C	In A	In B	Sum S	Carry Out C
0	0	0	0	0
0	0	1	1	0
0	1	0	1	0
0	1	1	0	1
1	0	0	1	0
1	0	1	0	1
1	1	0	0	1
1	1	1	1	1

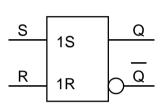


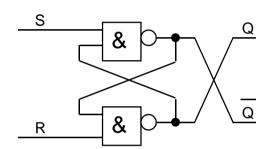


Memory gates: Flip-flops

RS-Flipflop

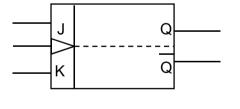
Set	Reset	Out Q _{t+1}
0	0	-
0	1	0
1	0	1
1	1	Q _t

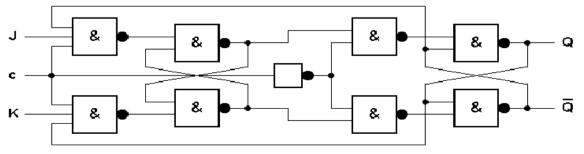




Triggered JK-Master-Slave-Flipflop

J	K	Out Q _{t+1}
0	0	Q_t
0	1	0
1	0	1
1	1	Q _t





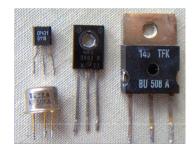


Computer architecture – Modern logic gate design

The modern logic gates: from valves to wafer circuits



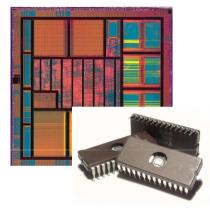
"In electronics, a vacuum tube, electron tube (inside North America), thermionic valve, or just **valve** (elsewhere); is a device used to amplify, switch, otherwise modify, or create an electrical signal by controlling the movement of electrons in a low-pressure space."



"A transistor is a semiconductor device, commonly used as an amplifier or an electrically controlled switch. The transistor is the fundamental building block of the circuitry (intecrated circuits) that governs the operation of computers and all other modern electronics."



"In microelectronics, a wafer is a thin slice of semiconducting material, such as a silicon crystal, upon which microcircuits are constructed by doping (for example, diffusion or ion implantation), chemical edging, and deposition of various materials. Wafers are thus of key importance in the fabrication of semiconductor devices such as integrated circuits."



"In electronics, an **integrated circuit** (also known as IC, microcircuit, microchip, silicon chip, or chip) is a miniaturized electronic circuits (consisting mainly of semiconductor device, as well as passive components) that has been manufactured in the surface of a thin substrate of semiconductor material."







Computer architecture

Simplify the following truth table (define your used signs/pictograms for AND, OR, NOT and use disjunctive normal form; advice for final test: task type could be similar with changed truth table values)

A	В	C	D	OUT
0	0	0	0	0
0	0	0	1	1
0	0	1	0	0
0	0	1	1	0
0	1	0	0	0
0	1	0	1	0
0	1	1	0	1
0	1	1	1	1
1	0	0	0	0
1	0	0	1	1
1	0	1	0	0
1	0	1	1	0
1	1	0	0	0
1	1	0	1	0
1	1	1	0	1
1	1	1	1	1

Use a Karnaugh-Veitch-diagram

Use the mathematical method given by the axioms of Boolean algebra

Draw the logic gate map for simplified table (define the used graphical symbols in a short caption)





Thank you!