Applied Machine Learning

Lecture: 7-1 Model Evaluation

Ekarat Rattagan, Ph.D.

Slides adapted from Andrew NG, Eric Eaton, Raquel Urtasun, and Patrick Winston

Model selection & evaluation

Model Selection

Model selection: estimating the performance of different models in order to choose the best one.

1.
$$h_{\theta}(x) = \theta_0 + \theta_1 x$$

2. $h_{\theta}(x) = \theta_0 + \theta_1 x + \theta_2 x^2$
3. $h_{\theta}(x) = \theta_0 + \theta_1 x + \cdots + \theta_3 x^3$

Which one to choose? how a model generalizes to unseen test data.

10. $h_{\theta}(x) = \theta_0 + \theta_1 x + \dots + \theta_{10} x^{10}$

Model Evaluation

- A part of the model development process to find the best model

- Two methods of evaluating models are

1. Hold-out

2. Cross validation

1. Hold-out method

>>> from sklearn.model_selection import train_test_split

>>> import numpy as np

	_		>>> X, y = np.arange(10).reshape((5, 2)), range(5)
Size	Price		>>> X arrav(If0_11
2104	400	$(x^{(1)},y^{(1)})$	[2, 3],
1600	330	$\left(x^{(2)},y^{(2)} ight)$	[4, 5],
2400	369	\ T	[8, 7], [8, 9]])
1416	232		>>> list(y)
3000	540		[0,1,2,3,4]
1985	300		X, y, test_size=0.30, random_state=42)
1534	315		>>> X_train
1427	199	$(x_{test}^{(1)}, y_{test}^{(1)})$	array([[4, 5], [0, 1]]
1380	212	$(x_{test}^{(2)},y_{test}^{(2)})$	[6, 7]])
1494	243	lest $(x_{test}^{(m_{test})}, y_{test}^{(m_{test})})$	>>> y_train [2, 0, 3]
			>>> X_test

array([[2, 3], [8, 9]])
>>> y_test
[1, 4]

1. Hold-out method

Learn parameter θ from training data (70%)

Compute test set (30%)

$$J_{test}(\theta) = \frac{1}{2m_{test}} \sum_{i=1}^{m_{test}} (h_{\theta}(x_{test}^{(i)}) - y_{test}^{(i)})^2$$

1. Hold-out method

2. Cross-Validation $(20, 20, 10)$	$(x^{(2)},y^{(2)}) \ (x^{(2)},y^{(2)})$	$\langle g, g, g \rangle$	$(x^{(m)},y^{(m)})$	(1) (1)	$(x\overset{\circ}{c}v',y\overset{\circ}{c}v')$	$\langle x_{cv}^{(2)}, y_{cv}^{(2)} \rangle$	\	$\left(x_{cv}^{(m_{cv})},y_{cv}^{(m_{cv})} ight)$			$(x_{test}^{(2)}, y_{test}^{(2)})$		$ig(x_{test}^{(m_{test})},y_{test}^{(m_{test})}ig)$
2. Cross-		Size Price 50	2104 400	1600 330			540	1985 300	1534 315	199	1380 212	1494 243	

Train/validation/test error

Training error:

$$J_{train}(\theta) = \frac{1}{2m} \sum_{i=1}^{m} (h_{\theta}(x^{(i)}) - y^{(i)})^2$$

Cross Validation error:

$$J_{cv}(\theta) = \frac{1}{2m_{cv}} \sum_{i=1}^{m_{cv}} (h_{\theta}(x_{cv}^{(i)}) - y_{cv}^{(i)})^{2}$$

Test error:

$$J_{test}(\theta) = \frac{1}{2m_{test}} \sum_{i=1}^{m_{test}} (h_{\theta}(x_{test}^{(i)}) - y_{test}^{(i)})^2$$

2. Cross Validation (K-fold)

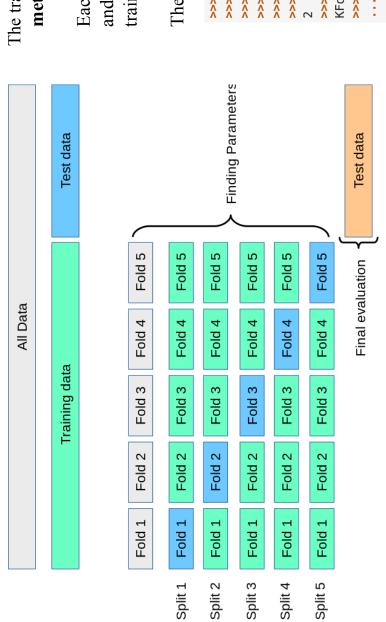


Figure from Hands-on Machine Learning

The training set is divided into k subsets, and the **holdout method** is repeated k times.

Each time, one of the k subsets is used as the test set and the other k-1 subsets are put together to form a training set.

Then the average error across all k trials is computed.

```
print("TRAIN:", train_index, "TEST:", test_index)
                                                                                                                                                                                                                                                                                                                                                                                                                           y_train, y_test = y[train_index], y[test_index]
                                                                                                                                                                                                                                                                                                                                                                                           X_train, X_test = X[train_index], X[test_index]
                                                                                                                                                                                                                                                                                 KFold(n_splits=2, random_state=None, shuffle=False)
                                                                       >>> X = np.array([[1, 2], [3, 4], [1, 2], [3, 4]])
                                                                                                                                                                                                                                                                                                                      >>> for train_index, test_index in kf.split(X):
                                    >>> from sklearn.model_selection import KFold
                                                                                                         >>> y = np.array([1, 2, 3, 4])
                                                                                                                                            >>> kf = KFold(n_splits=2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                              [2 3] TEST: [0 1]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            [0 1] TEST: [2 3]
>>> import numpy as np
                                                                                                                                                                            >>> kf.get_n_splits(X)
                                                                                                                                                                                                                                                 >>> print(kf)
                                                                                                                                                                                                                                                                                                                                                                                                                                                              TRAIN:
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                TRAIN:
```

Evaluation method

Method	Advantage	Disadvantage
1. Holdout	• Simple • Low computation	• Its evaluation can have a high variance
2. Cross validation	• Every data point gets to be in a test set exactly once, and gets to be in a training set k-1 times.	High computation
	• The variance of the resulting estimate is reduced as <i>k</i> is increased	

LOOCV (Leave-one-out Cross Validation)

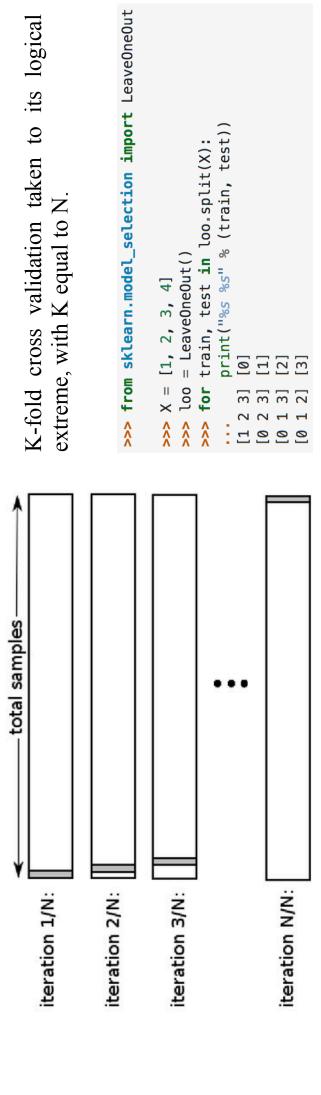


Figure from Hands-on Machine Learning

Machine Learning Methods for Genomic Signature Extraction

Evaluation method

Method	Advantage	Disadvantage
1. Holdout	SimpleLow computation	 Waste data (30% in this slide) Its evaluation can have a high variance
2. Cross validation	 Every data point gets to be in a test set exactly once, and gets to be in a training set k-1 times. The variance of the resulting estimate is reduced as k is increased 	• High computation
3. Leave-One-Out	,	High computation

⁻ Zero randomness - Lower bias as model is trained on the entire dataset

Diagnosing bias vs. variance

Machine learning diagnostic

Suppose you have implemented regularized linear regression to predict housing prices.

$$J(\theta) = \frac{1}{2m} \sum_{i=1}^{m} (h_{\theta}(x^{(i)}) - y^{(i)})^2 + \frac{\lambda}{2} \sum_{j=1}^{n} \theta_j^2$$

However, when you test your hypothesis on a new set of houses, you find that it makes unacceptably large errors in its predictions. What should you try next?

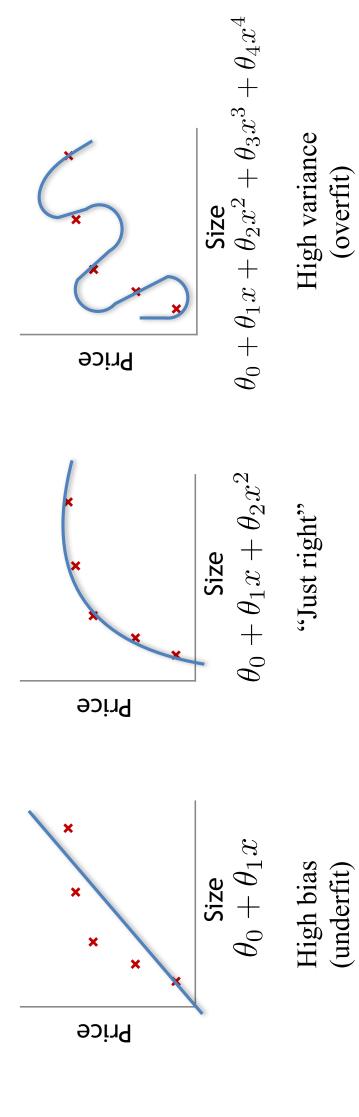
- Get more training examples
- Try smaller sets of features
- Try getting additional features Try adding polynomial features $(x_1^2, x_2^2, x_1x_2, \text{etc.})$
 - Γry decreasing λ
 - Iry increasing λ

Machine learning diagnostic:

Diagnostic:

A test that you can run to gain insight what is/isn't working with a learning algorithm, and gain guidance as to how best to improve its performance. Diagnostics can take time to implement, but doing so can be a very good use of your time.

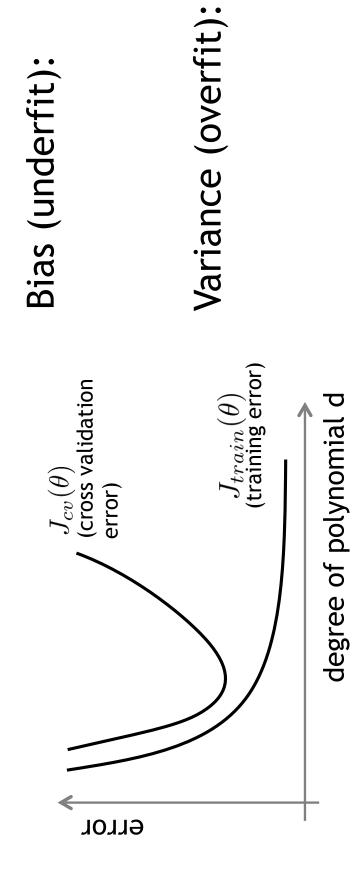
Bias/variance



Credit: Andrew NG

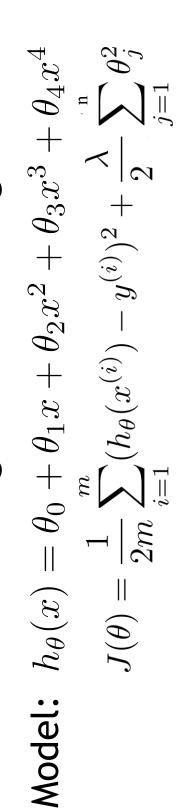
Diagnosing bias vs. variance

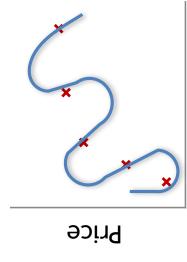
Suppose your learning algorithm is performing less well than you were hoping $(J_{cv}(\theta) \text{ or } J_{test}(\theta) \text{ is high.})$. Is it a bias problem or a variance problem?



Regularization and bias/ variance

Linear regression with regularization





Price

Price

Intermediate λ "Just right"

Size

High variance (overfit) Small \ Size

Credit: Andrew NG

 $\lambda = 100000. \ \theta_1 \approx 0, \theta_2 \approx 0,.$

 $h_{\theta}(x) \approx \theta_0$

High bias (underfit)

Large λ

Size

Choosing the regularization parameter λ

$$h_{\theta}(x) = \theta_{0} + \theta_{1}x + \theta_{2}x^{2} + \theta_{3}x^{3} + \theta_{4}x^{4}$$

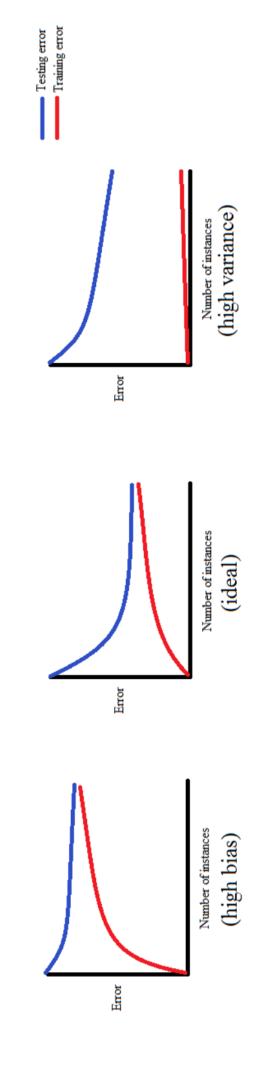
$$J(\theta) = \frac{1}{2m} \sum_{i=1}^{m} (h_{\theta}(x^{(i)}) - y^{(i)})^{2} + \frac{\lambda}{2} \sum_{j=1}^{n} \theta_{j}^{2}$$

$$J_{train}(\theta) = \frac{1}{2m} \sum_{i=1}^{m} (h_{\theta}(x^{(i)}) - y^{(i)})^{2}$$

$$J_{cv}(\theta) = \frac{1}{2m_{cv}} \sum_{i=1}^{m_{cv}} (h_{\theta}(x^{(i)}_{cv}) - y^{(i)}_{cv})^{2}$$

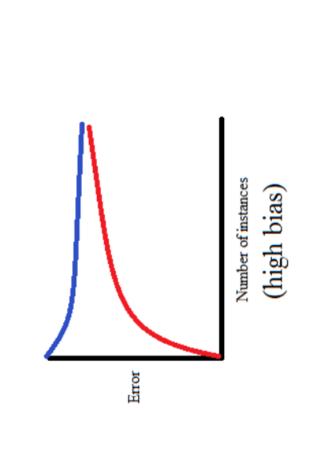
#Training data and bias/variance

Error VS #Training data

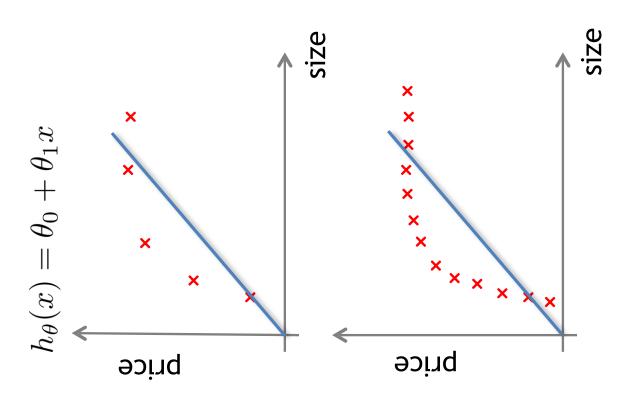


https://rmartinshort.jimdofree.com/2019/02/17/overfitting-bias-variance-and-leaning-curves/

High bias



If a learning algorithm is suffering from high bias, getting more training data will not (by itself) help much.



from high variance, getting more training data is likely to help. If a learning algorithm is suffering

size

Debugging a learning algorithm:

prices. However, when you test your hypothesis in a new set of houses, you find Suppose you have implemented regularized linear regression to predict housing that it makes unacceptably large errors in its prediction. What should you try

Get more training examples

Try smaller sets of features

Try getting additional features Try adding polynomial features $(x_1^2, x_2^2, x_1 x_2, \text{etc})$ Try decreasing λ

Γry increasing λ

Error metrics

Error metrics

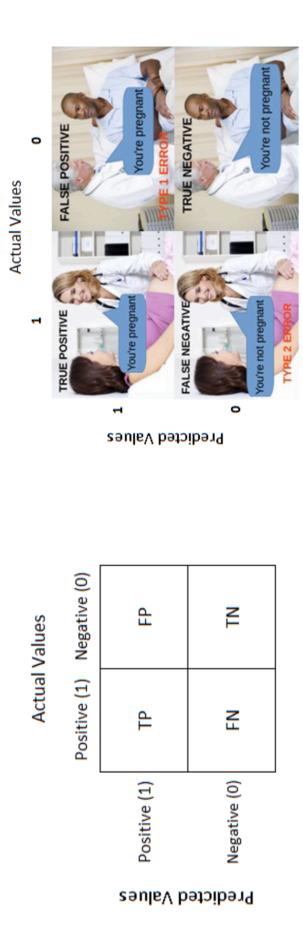
Confusion Matrix

Precision , Recall , and Accuracy

F1-score
ROC AUC Curve and score

Confusion Matrix

A performance measurement for ML classification



https://towardsdatascience.com/understanding-confusion-matrix-a9ad42dcfd62

Confusion Matrix

The Action	Kerall TP+FN MC 100	Post Nog TP+TN	March A A A A A A A A A A A A A A A A A A A		120		
Precision Accuracy				4/7			
Precision				2/3			
Recall				1/2			
output for threshold 0.6 Recall	0	1	1	1	0	0	0
y pred	0.5	6:0	0.7	0.7	0.3	0.4	0.5
٨	0	1	0	1	1	0	1

https://towardsdatascience.com/understanding-confusion-matrix-a9ad42dcfd62

Precision/Recall

y = 1 in presence of rare class that we want to detect

Precision

(Of all patients where we predicted y = 1, what fraction actually has cancer?)

Recall

(Of all patients that actually have cancer, what fraction did we correctly detect as having cancer?)

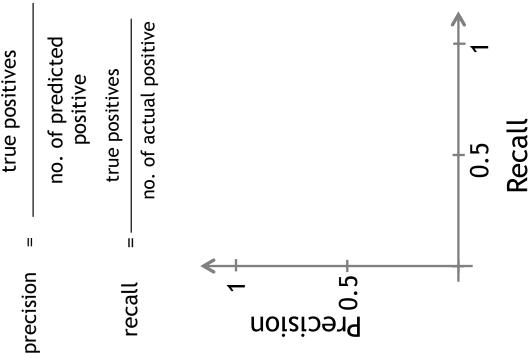
Trading off precision and recall

Logistic regression: $0 \le h_{\theta}(x) \le 1$

Predict 1 if $h_{ heta}(x) \geq 0.5$

Predict 0 if $h_{\theta}(x) < 0.5$

Suppose we want to predict y=1 (cancer) only if very confident. Suppose we want to avoid missing too many cases of cancer (avoid false negatives). More generally: Predict 1 if $h_{\theta}(x) \geq$ threshold.



F₁ Score (F score)

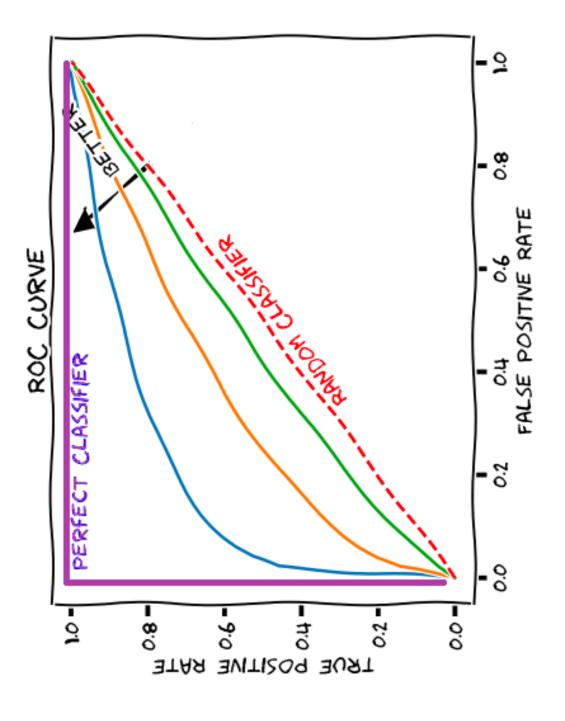
How to compare precision/recall numbers?

	Precision(P)	Recall (R)
Algorithm 1	0.5	0.4
Algorithm 2	0.7	0.1
Algorithm 3	0.02	1.0

Average:

 $\frac{P+R}{2}$

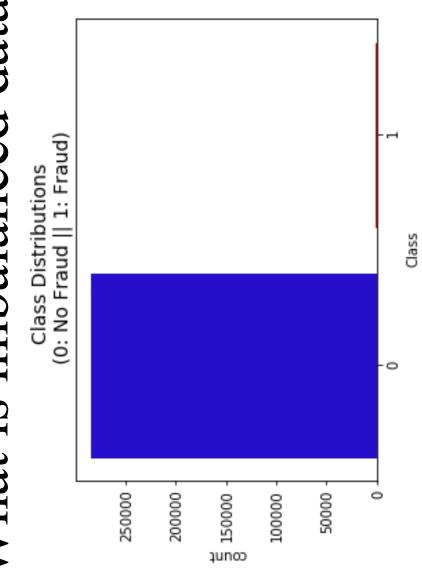
F₁ Score: $2\frac{PR}{P+R}$



https://glassboxmedicine.com/2019/02/23/measuring-performance-auc-auroc/

Imbalanced data

What is imbalanced data



https://www.kaggle.com/janiobachmann/credit-fraud-dealing-with-imbalanced-datasets