

# Applied Machine Learning

Lecture 10 Decision Tree

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## Outline

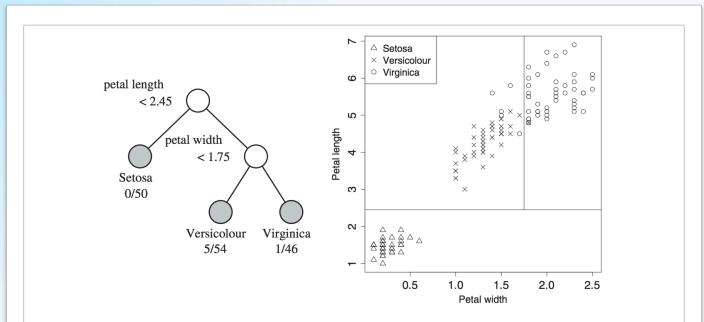
- 1. Introduction
- 2. Classification And Regression Trees (CART)
- 3. Iterative Dichotomiser 3 (ID3)





	Id	SepalLengthCm	SepalWidthCm	PetalLengthCm	PetalWidthCm	Species
0	1	5.1	3.5	1.4		Iris-setosa
1	2	4.9	3.0	1.4	0.2	Iris-setosa
2	3	4.7	3.2	1.3	0.2	Iris-setosa
3	4	4.6	3.1	1.5	0.2	Iris-setosa
4	5	5.0	3.6	1.4	0.2	Iris-setosa
5	6	5.4	3.9	1.7	0.4	Iris-setosa
6	7	4.6	3.4	1.4	0.3	Iris-setosa
7	8	5.0	3.4	1.5	0.2	Iris-setosa
8	9	4.4	2.9	1.4	0.2	Iris-setosa
9	10	4.9	3.1	1.5	0.1	Iris-setosa





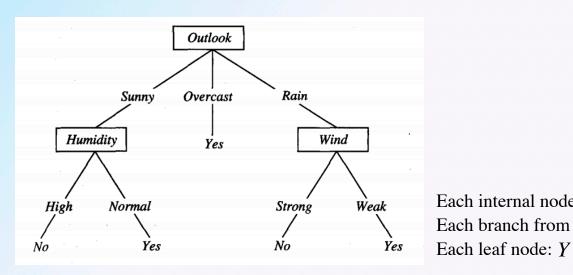
**Figure 1.** Classification tree model for iris data. At each intermediate node, an observation goes to the left child node if and only if the stated condition is true. The pair of numbers beneath each terminal node gives the number misclassified and the node sample size.



Day	Outlook	Temperature	Humidity	Wind	PlayTennis
D1	Sunny	Hot	High	Weak	No
D2	Sunny	Hot	High	Strong	No
D3	Overcast	Hot	High	Weak	Yes
D4	Rain	Mild	High	Weak	Yes
D5	Rain	Cool	Normal	Weak	Yes
D6	Rain	Cool	Normal	Strong	No
D7	Overcast	Cool	Normal	Strong	Yes
D8	Sunny	Mild	High	Weak	No
D9	Sunny	Cool	Normal	Weak	Yes
D10	Rain	Mild	Normal	Weak	Yes
D11	Sunny	Mild	Normal	Strong	Yes
D12	Overcast	Mild	High	Strong	Yes
D13	Overcast	Hot	Normal	Weak	Yes
D14	Rain	Mild	High	Strong	No

Credit: Tom M. Mitchell





Each internal node: attribute  $X_j$ Each branch from a node: selects one value for  $X_j$ 

A decision tree

#### This decision tree is equivalent to:

if  $(Outlook = Sunny) \land (Humidity = Normal)$  then Yes;

if (Outlook = Overcast) then Yes;

if  $(Outlook = Rain) \land (Wind = Weak)$  then Yes;

Credit: Tom M. Mitchell



#### **CART**

- A binary tree classifier
- Gini impurity (index) is a measure of the homogeneity (or "purity") of the nodes. If all data at one node belong to the same class then this node is considered "pure". So by minimising the Gini impurity the decision tree finds the features the separate the data best [quora]
  - Gini index =  $1 \sum_{i=1}^{n} p^2(i|t)$ , where p(i|t) is the proportion of class i observations in node t.



# Example

• https://github.com/ekaratnida/applied-machine-learning/blob/master/Week10-desicion-tree/running.ipynb



# ID3 Algorithm

#### ID3(Examples, Target\_attribute, Attributes)

Examples are the training examples. Target\_attribute is the attribute whose value is to be predicted by the tree. Attributes is a list of other attributes that may be tested by the learned decision tree. Returns a decision tree that correctly classifies the given Examples.

- Create a Root node for the tree
- If all Examples are positive, Return the single-node tree Root, with label = +
- If all Examples are negative, Return the single-node tree Root, with label = -
- If Attributes is empty, Return the single-node tree Root, with label = most common value of Target\_attribute in Examples
- Otherwise Begin
  - $\bullet$  A  $\leftarrow$  the attribute from Attributes that best\* classifies Examples
  - The decision attribute for  $Root \leftarrow A$
  - For each possible value,  $v_i$ , of A,
    - Add a new tree branch below *Root*, corresponding to the test  $A = v_i$
    - Let  $Examples_{v_i}$  be the subset of Examples that have value  $v_i$  for A
    - If  $Examples_{v_i}$  is empty
      - Then below this new branch add a leaf node with label = most common value of Target\_attribute in Examples
      - Else below this new branch add the subtree
         ID3(Examples<sub>vi</sub>, Target\_attribute, Attributes {A}))

- End
- Return Root

Credit: Tom M. Mitchell



## Information Gain

- central choice: Which attribute classifies the examples best?
- ID3 uses the information gain
  - statistical measure that indicates how well a given attribute separates the training examples according to their target classification
  - ID3 uses this **information gain measure** to select among the candidate attributes at each step while growing the tree.



# Entropy

- Entropy is a measure of the impurity in a collection of training examples.

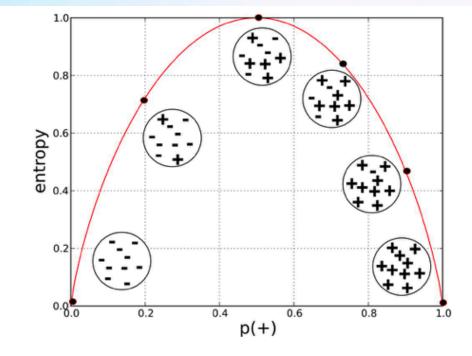
$$Entropy(S) \equiv -p_{\oplus} \log_2 p_{\oplus} - p_{\ominus} \log_2 p_{\ominus}$$

- S: a collection containing positive and negative examples of some target concept.
- p + is the proportion of positive examples in S.
- p is the proportion of negative examples in S.

$$Entropy([9+, 5-]) = -(9/14) \log_2(9/14) - (5/14) \log_2(5/14)$$
$$= 0.940$$



# Entropy



Provost, Foster; Fawcett, Tom. Data Science for Business: What You Need to Know about Data Mining and Data-Analytic Thinking



## Information Gain

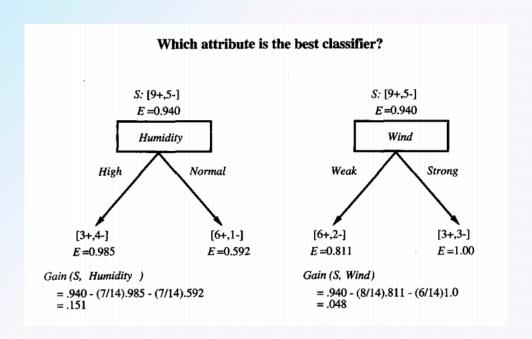
- central choice: Which attribute classifies the examples best?
- ID3 uses the information gain
  - The expected reduction in entropy caused by partitioning the examples according to this attribute

• 
$$Gain(S, A) \equiv Entropy(S) - \sum_{v \in Values(A)} \frac{|S_v|}{|S|} Entropy(S_v)$$
 (3.4)

where Values(A) is the set of all possible values for attribute A, and  $S_v$  is the subset of S for which attribute A has value v (i.e.,  $S_v = \{s \in S | A(s) = v\}$ ). Note the first term in Equation (3.4) is just the entropy of the original collection S, and the second term is the expected value of the entropy after S is partitioned using attribute A. The expected entropy described by this second term is simply the sum of the entropies of each subset  $S_v$ , weighted by the fraction of examples  $\frac{|S_v|}{|S|}$  that belong to  $S_v$ . Gain(S, A) is therefore the expected reduction in entropy caused by knowing the value of attribute A.



### ID3



Credit: Tom M. Mitchell



## ID3

informations gains for the four attributes:

```
Gain(S, Outlook) = 0.246

Gain(S, Humidity) = 0.151

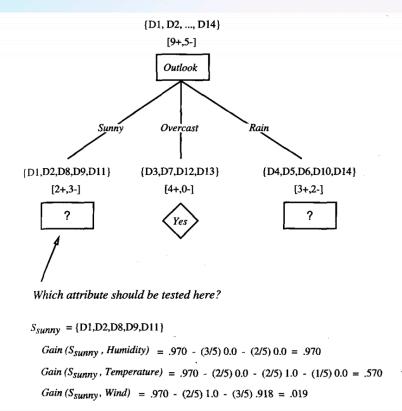
Gain(S, Wind) = 0.048

Gain(S, Temperature) = 0.029
```

- $\Rightarrow Outlook$  is selected as best classifier and is therefore Root of the tree
- ⇒ now branches are created below the root for each possible value
  - ullet because every example for which Outlook = Overcast is positive, this node becomes a leaf node with the classification Yes
  - the other descendants are still ambiguous
  - hence, the decision tree has to be further elaborated below these nodes



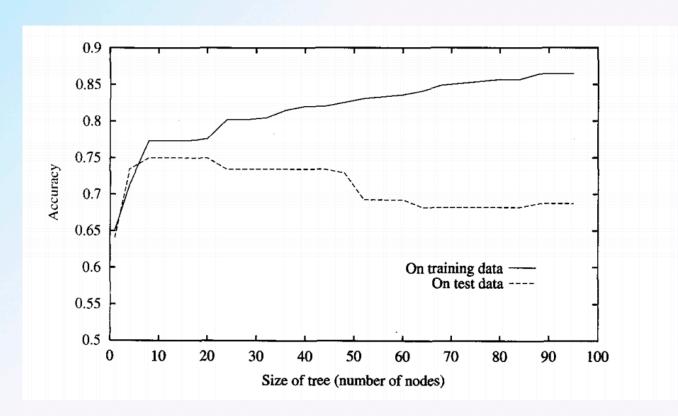
## ID3



Credit: Tom M. Mitchell



# Issue: Overfitting





# Solution: Overfitting

- 1. Limit the number of iterations of ID3
  - Leading to a tree with a bounded number of nodes
- 2. Pruning (after it is built)

#### Generic Tree Pruning Procedure

#### input:

function f(T, m) (bound/estimate for the generalization error of a decision tree T, based on a sample of size m), tree T.

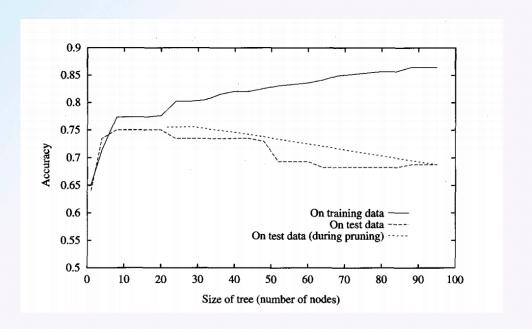
for each node j in a bottom-up walk on T (from leaves to root): find T' which minimizes f(T',m), where T' is any of the following: the current tree after replacing node j with a leaf 1. the current tree after replacing node j with its left subtree. the current tree after replacing node j with its right subtree. the current tree after replacing node j with its right subtree.

let T := T'.



# Solution: Overfitting

#### 1. Effect of reduced error pruning





# Solution: Overfitting

#### 3. Random forests

- A classifier consisting of a collection of decision trees (an ensemble of trees)

The training algorithm for random forests applies the general technique of bootstrap aggregating, or bagging, to tree learners. Given a training set  $X = x_1, ..., x_n$  with responses  $Y = y_1, ..., y_n$ , bagging repeatedly (B times) selects a random sample with replacement of the training set and fits trees to these samples:

For b = 1, ..., B:

- 1. Sample, with replacement, n training examples from X, Y; call these  $X_h$ ,  $Y_h$ .
- 2. Train a classification or regression tree  $f_b$  on  $X_b$ ,  $Y_b$ .

After training, predictions for unseen samples x' can be made by averaging the predictions from all the individual regression trees on x':

$$\hat{f} = rac{1}{B}\sum_{b=1}^B f_b(x')$$

or by taking the majority vote in the case of classification trees.

https://en.wikipedia.org/wiki/Random forest



# Real-case example

#### **Practical Applications:**

Flight simulator: 20 state variables; 90K examples based on expert pilot's actions;

auto-pilot tree

Yahoo Ranking Challenge

Random Forests: Microsoft Kinect Pose Estimation



# Real-case example

เทคโนโลยี (Machine Learning) ที่ใช้ใน Microsoft Kinect

https://www.microsoft.com/.../uploads/2016/02/BodyPartRecogni...

Figure from: Raquel Urtasun

Decision trees are in XBox

