Assignment 9

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Outline

- Question
- 2 Definitions
- Probability
- Graph

Question

CBSE 12 13.5 Q 1

A die is thrown 6 times. If 'getting an odd number' is a success, what is the probability of

- 5 successes ?
- at least 5 successes ?
- at most 5 successes ?

Definitions

Let $X \in \{0, 1, 2, 3, 4, 5, 6\}$ be a random variable denoting the number of successes (getting an odd number) in an experiment of 6 trials.

Event	Probability
Getting an odd no. (Success)	$p=\frac{1}{2}$
Getting an even no. (Failure)	$q=\frac{1}{2}$

Table: Outcomes of the Experiment

Throwing a die is a Bernoulli trail. So, X has a binomial distribution

$$\Pr(X = x) = \frac{n!}{x!(n-x)!} (1-p)^{n-x} p^x$$
 (1)

5 successes

$$\Pr(X=5) = \frac{6!}{5!(6-5)!}p^5q^1 \tag{2}$$

$$=6\times\left(\frac{1}{2}\right)^5\times\left(\frac{1}{2}\right)^1\tag{3}$$

$$=6\times\frac{1}{32}\times\frac{1}{2}\tag{4}$$

$$=\frac{3}{32}\tag{5}$$

at least 5 successes

$$\Pr(X \ge 5) = \Pr(X = 5) + \Pr(X = 6)$$

$$= \frac{6!}{5!(6-5)!} p^5 q^1 + \frac{6!}{6!(6-6)!} p^5 q^0$$
(7)

$$= 6 \times \left(\frac{1}{2}\right)^5 \times \left(\frac{1}{2}\right)^1 + 1 \times \left(\frac{1}{2}\right)^6 \times \left(\frac{1}{2}\right)^0 \tag{8}$$

$$= \frac{6}{64} \times \frac{1}{64}$$
 (9)
= $\frac{7}{64}$ (10)

$$=\frac{7}{64}\tag{10}$$



at most 5 successes

$$Pr(X \le 5) = 1 - Pr(X = 6)$$
 (11)

$$=1-\frac{6!}{6!(6-6)!}p^6q^0\tag{12}$$

$$= 1 - 1 \times \left(\frac{1}{2}\right)^6 \times \left(\frac{1}{2}\right)^0 \tag{13}$$

$$=1-\frac{1}{64}$$
 (14)

$$=\frac{63}{64}$$
 (15)

PMF Graph

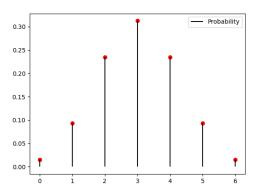


Figure: Probability Mass Function

CDF Graph

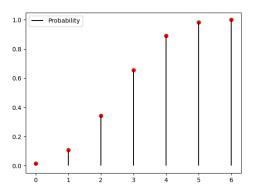


Figure: Cummulative Distribution Function

