

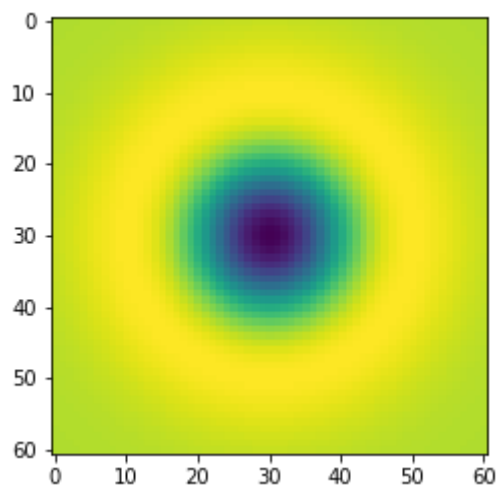
```
In [ ]: import numpy as np
import cv2 as cv
import matplotlib.pyplot as plt
```

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In [ ]: sigma = 10
hw = 3*sigma
X, Y = np.meshgrid(np.arange(-hw,hw+1,1), np.arange(-hw,hw+1,1))

log = 1/(2*np.pi*sigma**2)*(X**2/(sigma**2) + Y**2/(sigma**2) - 2)*np.exp(-(X**2 + Y**2)/(2*sigma**2))

plt.imshow(log)
```

```
Out[ ]: <matplotlib.image.AxesImage at 0x1c0b12140a0>
```

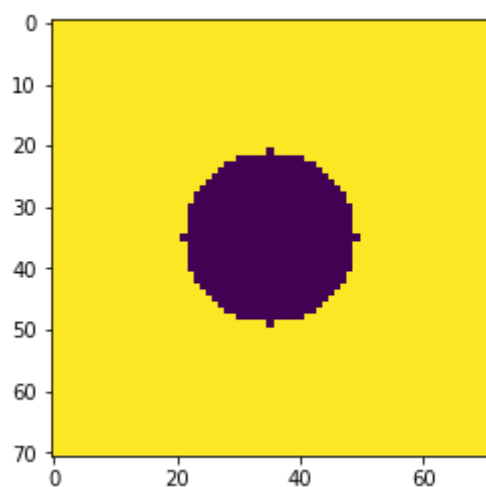


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In [ ]: w, h = 71 , 71
hw = w//2
hh = h//2

f = np.ones((h,w), dtype= np.float32)* 255
X, Y = np.meshgrid(np.arange(-hw,hw+1,1), np.arange(-hw,hw+1,1))

r = w//5
f *= X**2 + Y**2 > r** 2
plt.imshow(f)
```

```
Out[ ]: <matplotlib.image.AxesImage at 0x1c0b1176f40>
```



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In [ ]: s = 11
fig, ax = plt.subplots(2, s, figsize = (20,5))
scale_space = np.empty((h,w,s), dtype= np.float32)
sigmas = np.arange(5,16,1)
for i , sigma in enumerate(np.arange(5,16,1)):
    log_hw = 3*np.max(sigmas)
    X, Y = np.meshgrid(np.arange(-hw,hw+1,1), np.arange(-hw,hw+1,1))
```

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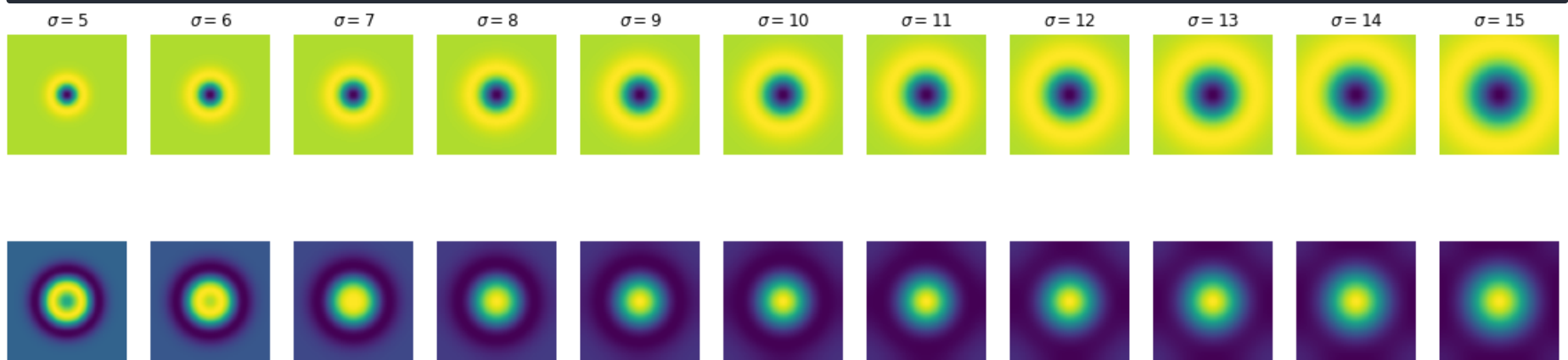
log = 1/(2*np.pi*sigma**2)*(X**2/(sigma**2) + Y**2/(sigma**2) - 2)*np.exp(-(X**2 +
Y**2)/(2*sigma**2))
f_log = cv.filter2D(f,-1, log)
scale_space[:, :, i] = f_log
ax[0,i].imshow(log)
ax[0,i].axis('off')
ax[0,i].set_title(r'$\sigma = {}$'.format(sigma))
ax[1,i].imshow(f_log)
ax[1,i].axis('off')
indices = np.unravel_index(np.argmax(scale_space, axis = None), scale_space.shape)
print(indices)
print(sigmas[indices[2]])

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(35, 35, 5)
10

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In [ ]: m = 2 # Line equation : y = m*x + c . m is the slope . c is the intercept .
c = 1
x = np.arange (1 , 1000 , 1)
sigma = 50
np.random.seed(45)
noise = sigma * np.random.randn(len(x))
o = np.zeros(x.shape)
y = m*x + c + noise + o

n = len(x)
X = np.concatenate([x.reshape(n,1), np.ones((n, 1))], axis = 1)
B = np.linalg.pinv(X.T @ X) @ X.T @ y
mstar = B[0]
cstar = B[1]

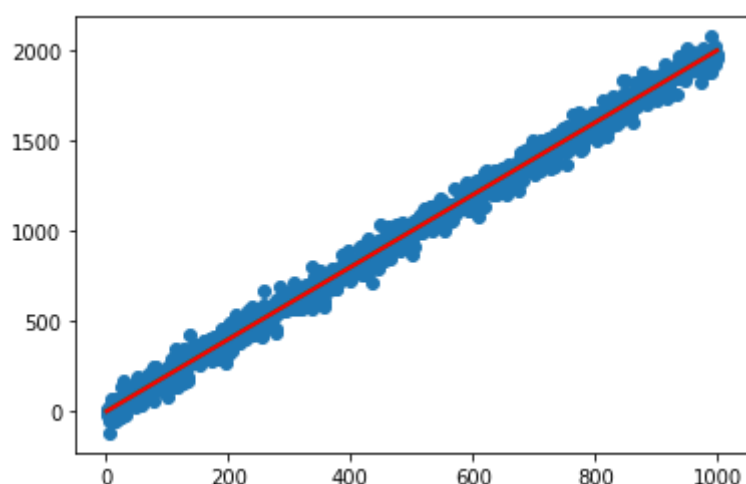
plt.plot(x,y,'o', label='noise points')
plt.plot([x[0], x[-1]], [m*x[0] + c, m*x[-1] + c], color = 'g', linewidth = 2, label="True Line")
plt.plot([x[0], x[-1]], [mstar*x[0] + cstar, mstar*x[-1] + c], color = 'r', linewidth = 2,
label="Estimated Line")

```

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Out [ ]: [ <matplotlib.lines.Line2D at 0x1c0b411ee50> ]

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In [ ]: m = 2
c = 1

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x = np.arange (1 , 1000 , 1)
sigma = 50
np.random.seed(45)
noise = sigma * np.random.randn(len(x))
o = np.zeros(x.shape)
y = m*x +c +noise + o

n = len(x)
u11 = np.sum((x - np.mean(x))**2)
u12 = np.sum((x - np.mean(x))*(y- np.mean(y)))
u21 = u12
u22 = np.sum((y - np.mean(y))**2)

U = np.array([[u11, u12], [u21, u22]])
W, V = np.linalg.eig(U)
ev_corresponding_to_smallest_ev = V[:, np.argmin(w)]

a = ev_corresponding_to_smallest_ev[0]
b = ev_corresponding_to_smallest_ev[1]
d = a*np.mean(x) + b*np.mean(y)

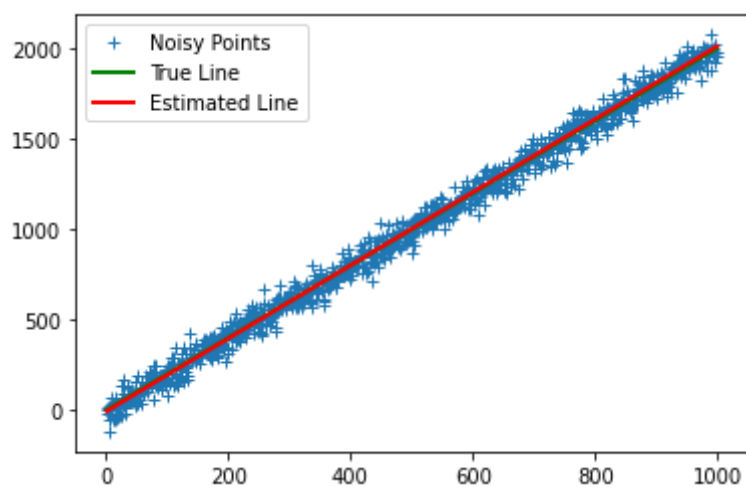
mstar = -a/b
cstar = d/b

plt.plot(x,y, '+', label = 'Noisy Points')
plt.plot([x[0], x[-1]], [m*x[0] + c, m*x[-1] + c], color = 'g', linewidth = 2, label="True Line")
plt.plot([x[0], x[-1]], [mstar*x[0] + cstar, mstar*x[-1] + c], color = 'r', linewidth = 2,
label="Estimated Line")

plt.legend(loc = 'best')

```

Out[ ]: <matplotlib.legend.Legend at 0x1c0b25a6f70>



In [ ]: