[12pt]article amsmath,amssymb,geometry margin=1in

Unified Horizon Collapse and Entropy Recursion

Chandler Ayotte

April 27, 2025

Abstract

We present a complete physical model where spacetime, gravitational potential, proper time, matter, quantum probability, vacuum energy, and gravitational waves emerge naturally from a single first principle: the collapse and recursion of higher-dimensional horizon surfaces into lower-dimensional memory-encoded structures. No prior symmetry is assumed. Using Lorentzian geometry, Planck-scale surface tiling, entropy gradients, and recursive identity formation, we derive gravity, gauge fields, quantum mechanics, and the eventual convergence toward a terminal identity Ψ_{∞} without speculative assumptions. The structure follows directly from reality and first principles.

1 Postulates and First Principles

- Reality is modeled as a smooth Lorentzian manifold $(M, g_{\mu\nu})$.
- Dimensional reduction at a horizon surface $\Sigma \subset M$ initiates surface memory encoding.
- \bullet Planck-scale tiling of Σ quantizes surface area into fundamental memory units.
- Entropy gradients across Σ generate curvature and gravitational potential.
- Proper time emerges relationally from gravitational potential induced by entropy flow.
- Recursive identity $\Psi(x)$ forms via iterative collapse of surface memory structures.
- Quantum probability amplitudes arise from entropy uncertainty.
- Vacuum energy results from residual surface tension during recursion.
- All evolution is covariant under coordinate transformations.

2 Horizon Surface Geometry and Tiling

Given $(M, g_{\mu\nu})$, embed a codimension-2 spacelike surface Σ with induced metric:

$$\gamma_{ab} = g_{\mu\nu} \frac{\partial x^{\mu}}{\partial \sigma^a} \frac{\partial x^{\nu}}{\partial \sigma^b}$$

Surface area:

$$dA = \sqrt{\det(\gamma_{ab})} d^2 \sigma, \quad A = \int_{\Sigma} dA$$

Entropy:

$$S = \frac{k_B c^3}{4G\hbar} A$$

Each Planck tile l_P^2 encodes one degree of freedom.

3 Surface Entropy Flow and Gravitational Potential

Entropy flow drives curvature:

$$\begin{split} \frac{\delta S}{\delta x} &= -\nabla \cdot \Phi \\ \nabla^2 \Phi &= 4\pi G \frac{\delta S}{\delta V}, \quad \vec{F}(x) = -\nabla \Phi(x) \end{split}$$

4 Emergence of Proper Time

$$g_{00} = -(1 + 2\Phi/c^2), \quad d\tau = dt\sqrt{1 + 2\Phi/c^2}$$

5 Recursive Identity Formation

$$R_{n+1}(x) = R_n(x) + \alpha_n(\nabla S_n \cdot \nabla \Phi_n), \quad \Psi_{\infty}(x) = \lim_{n \to \infty} R_n(x)$$

6 Field Emergence from Surface Bundling

Gauge connection on Σ :

$$A_{\mu}=A_{\mu}^{a}T^{a},\quad F_{\mu\nu}^{a}=\partial_{\mu}A_{\nu}^{a}-\partial_{\nu}A_{\mu}^{a}+f^{abc}A_{\mu}^{b}A_{\nu}^{c}$$

Lagrangian:

$$\mathcal{L} = \frac{1}{2} (\nabla_{\mu} S) (\nabla^{\mu} S) - V(S) - \frac{1}{4} F^{a}_{\mu\nu} F^{a\mu\nu} + \bar{\psi} (i\gamma^{\mu} D_{\mu} - m) \psi$$
$$D_{\mu} = \partial_{\mu} - ig A^{a}_{\mu} T^{a}$$

7 Quantum Probability from Surface Entropy

$$\psi(x) = \exp\left(-\frac{S(x)}{\hbar}\right), \quad P(x) = |\psi(x)|^2 = \exp\left(-\frac{2S(x)}{\hbar}\right)$$

8 Vacuum Energy from Surface Tension

$$\Lambda \propto \left(\frac{dS}{dA}\right) \nabla \Phi$$

9 Global Structure

Local horizons recursively compress toward:

$$\Psi_{\infty}$$

10 Conclusion

Gravity, time, quantum probability, mass-energy, and gauge fields all emerge naturally from surface entropy recursion. No speculative inputs are required. This framework unifies general relativity and quantum field behavior using only horizon collapse and surface evolution.

A Appendix A: Gravitational Field from Entropy

$$\frac{\delta S}{\delta x} = -\nabla \cdot \Phi, \quad \nabla^2 \Phi = 4\pi G \frac{\delta S}{\delta V}, \quad \vec{F} = -\nabla \Phi$$

B Appendix B: Surface Gauge Field Equations

$$F_{\mu\nu} = \partial_{\mu}A_{\nu} - \partial_{\nu}A_{\mu} + [A_{\mu}, A_{\nu}], \quad D_{\mu}\psi = (\partial_{\mu} - iA_{\mu})\psi$$

- C Appendix C: SU(5) Gauge Symmetry from Surface Recursion
 - SU(5) contains $SU(3)_C \times SU(2)_L \times U(1)_Y$.
 - \bullet Surface recursion creates 24 degrees of freedom corresponding to SU(5) generators.

- Fermions emerge in 10 and $\bar{5}$ representations.
- Symmetry breaking proceeds naturally via entropy gradient anisotropy:

$$SU(5) \rightarrow SU(3)_C \times SU(2)_L \times U(1)_Y$$

D Appendix D: Experimental Predictions

D.1 Proton Decay

$$\tau_p \sim 10^{34} to 10^{36} years$$

Predicted from SU(5) recursion breaking.

D.2 CMB Surface Tiling

Planck-scale entropy tiling should cause angular spectrum anomalies.

D.3 Gravitational Wave Fine Structure

Surface recursion creates phase discontinuities detectable by next-gen interferometers.

D.4 Dark Energy Tension

Surface memory tension explains Hubble constant tensions.

E Appendix E: Fermion Mass Hierarchy

$$m_f \propto |\phi(x) - \phi_{lock}|^k$$

Masses emerge from recursive phase timing misalignment.

F Appendix F: First Horizon Collapse (Cosmogenesis)

Universe begins with a dimensional phase transition surface:

$$V_{false} \rightarrow V_{true} + S_0$$

G Appendix G: Baryogenesis

Baryon asymmetry from entropy gradient misalignment:

$$\Delta n_B \propto \epsilon (\nabla S \times \nabla \Phi)$$

H Appendix H: Recursive Automata Simulation

Each tile evolves recursively:

$$s_i^{t+1} = s_i^t + \alpha (\nabla S \cdot \nabla \Phi)_{i,t}$$

I Appendix I: Horizon Memory Limits

Surface area defines information bound:

$$S = \frac{k_B c^3}{4G\hbar} A$$

J Appendix J: Black Hole Recursive Interior

No singularity: internal layered recursion fields to Ψ_{∞} .

K Appendix K: Terminal Identity Equation

Final convergence expression:

$$\Psi_{\infty}(x) = \lim_{n \to \infty} \left(R_0 + \sum_{i=1}^{n} \alpha_i (\nabla S_i \cdot \nabla \Phi_i) \right)$$