proj2

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```
library(AlgDesign)
desFull <- gen.factorial( levels=c(3,3,2,2), nVars=4, varNames=c("attr1", "attr2", "feat1", "feat2"), cent</pre>
print(desFull)
##
      attr1 attr2 feat1 feat2
## 1
          1
                1
## 2
          2
                1
                      1
                            1
## 3
          3
                1
                      1
## 4
          1
                2
                      1
## 5
          2
                2
## 6
          3
                2
                      1
                            1
## 7
          1
                3
## 8
          2
                3
                      1
                            1
## 9
          3
                3
                      1
                            1
                      2
## 10
          1
                1
                            1
## 11
          2
                1
                      2
                            1
                      2
## 12
          3
                1
                            1
## 13
          1
                2
                      2
                            1
## 14
          2
                2
                      2
                            1
## 15
          3
                2
                      2
## 16
          1
                3
                      2
                      2
## 17
          2
                3
                            1
## 18
          3
                3
                      2
                            1
## 19
          1
                1
                      1
                            2
## 20
          2
                            2
## 21
          3
                1
                      1
                            2
                            2
## 22
          1
                2
## 23
          2
                2
                            2
                      1
## 24
          3
                2
## 25
          1
                3
                            2
                      1
                            2
## 26
          2
                3
                      1
## 27
          3
                3
                      1
                            2
## 28
          1
                1
                      2
                            2
                      2
## 29
          2
                            2
                1
## 30
          3
                1
                      2
                            2
## 31
                2
                      2
                            2
          1
## 32
          2
                2
                      2
                            2
                2
                      2
                            2
## 33
          3
## 34
                3
                      2
                            2
          1
## 35
          2
                3
                      2
                            2
## 36
          3
                3
fml = ~ factor(attr1) + factor(attr2) + factor(feat1) + factor(feat2)
desDummies = model.matrix(fml, data=desFull)
colnames(desDummies) = paste0("D",(1:dim(desDummies)[2]))
print(desDummies)
```

```
D1 D2 D3 D4 D5 D6 D7
##
## 1
          0 0 0 0
## 2
## 3
       1
             1
                0
                   0
                      0
## 4
             0
## 5
             0
                   0
       1
          1
                1
## 6
       1
## 7
                0
                      0
       1
          0
             0
                   1
## 8
       1
          1
             0
                0
                   1
## 9
          0
       1
             1
                   1
## 10
       1
             0
## 11
       1
          1
             0
                0
                   0
   12
          0
             1
## 13
          0
             0
## 14
       1
             0
                   0
          1
                1
## 15
       1
          0
             1
                   0
                      1
                         0
##
  16
       1
          0
             0
                0
                      1
## 17
## 18
          0
       1
             1
## 19
          0
             0
                0
##
  20
          1
             0
                0
## 21
## 22
          0
             0
                   0
                      0
       1
                1
## 23
          1
             0
                1
## 24
       1
          0
             1
                1
  25
       1
          0
             0
                0
## 26
       1
          1
             0
                0
                   1
   27
             1
          0
## 28
      1
          0
             0
                0
## 29
       1
             0
                0
                   0
## 30
       1
          0
             1
                0
                   0
                      1
##
  31
       1
          0
             0
                1
                      1
  32
##
       1
             0
## 33
          0
       1
             1
               1
## 34
       1
          0
             0
               0
## 35
       1 1 0 0 1 1
## 36
      1 0 1 0 1 1 1
## attr(,"assign")
## [1] 0 1 1 2 2 3 4
## attr(,"contrasts")
## attr(,"contrasts")$`factor(attr1)`
## [1] "contr.treatment"
## attr(,"contrasts")$`factor(attr2)`
## [1] "contr.treatment"
##
## attr(,"contrasts")$`factor(feat1)`
## [1] "contr.treatment"
## attr(,"contrasts")$`factor(feat2)`
## [1] "contr.treatment"
desFract = optFederov(~ . -1,data=desDummies,nTrials=12)
print(desFract)
```

```
## $D
## [1] 0.2576402
##
## $A
## [1] 5.914286
##
## $Ge
## [1] 0.897
##
## $Dea
## [1] 0.892
##
## $design
##
     D1 D2 D3 D4 D5 D6 D7
## 3
     1 0 1 0 0 0
## 5
      1
        1
           0 1
                 0
                    0
## 7
      1 0 0 0 1 0
## 11 1 1 0 0 0 1
## 15 1 0 1 1 0 1
## 16
     1
        0 0 0 1 1
## 19 1 0 0 0 0 0
## 23 1
        1
           0 1 0 0
## 27
     1 0 1 0 1 0 1
## 30 1 0 1 0 0 1
## 31 1 0 0 1 0 1 1
## 35 1 1 0 0 1 1 1
##
## $rows
## [1] 3 5 7 11 15 16 19 23 27 30 31 35
eval.design(~.-1, desFract$design)
## $determinant
## [1] 0.2576402
## $A
## [1] 5.914286
##
## $diagonality
## [1] 0.588
##
## $gmean.variances
## [1] 5.756168
#Check dummies for model with just main effects
desD1 = model.matrix(~factor(attr1) + factor(attr2), data=desFull)
print(desD1)
##
     (Intercept) factor(attr1)2 factor(attr1)3 factor(attr2)2 factor(attr2)3
## 1
                             0
## 2
                                          0
                                                        0
                                                                      0
              1
                            1
## 3
              1
                             0
                                          1
                                                        0
                                                                      0
## 4
                                          0
                                                                       0
              1
                             0
                                                         1
```

```
## 5
                                                                                  0
                                 1
                                                  0
                                                                  1
## 6
                 1
                                 0
                                                  1
                                                                  1
                                                                                  0
## 7
                 1
                                 0
                                                  0
                                                                  0
                                                                                  1
## 8
                                 1
                                                  0
                                                                  0
                                                                                  1
                 1
## 9
                 1
                                 0
                                                  1
                                                                  0
                                                                                  1
## 10
                 1
                                 0
                                                  0
                                                                  0
                                                                                  0
## 11
                 1
                                 1
                                                  0
                                                                  0
                                                                                  0
## 12
                                 0
                                                                  0
                                                                                  0
                 1
                                                  1
## 13
                 1
                                 0
                                                  0
                                                                  1
                                                                                  0
## 14
                                                  0
                                                                                  0
                 1
                                 1
                                                                  1
## 15
                 1
                                 0
                                                  1
                                                                  1
                                                                                  0
                                 0
                                                  0
                                                                  0
## 16
                 1
                                                                                  1
## 17
                                                                  0
                 1
                                 1
                                                  0
                                                                                  1
## 18
                 1
                                 0
                                                                  0
                                                  1
                                                                                  1
## 19
                 1
                                 0
                                                  0
                                                                  0
                                                                                  0
## 20
                 1
                                 1
                                                  0
                                                                  0
                                                                                  0
## 21
                 1
                                 0
                                                                  0
                                                                                  0
                                                  1
## 22
                                                                                  0
                 1
                                 0
                                                  0
                                                                  1
## 23
                 1
                                 1
                                                  0
                                                                  1
                                                                                  0
## 24
                                 0
                 1
                                                  1
                                                                  1
                                                                                  0
## 25
                 1
                                 0
                                                  0
                                                                  0
                                                                                  1
## 26
                                                  0
                                                                  0
                                                                                  1
## 27
                                 0
                                                                  0
                                                                                  1
                 1
                                                  1
## 28
                 1
                                 0
                                                  0
                                                                  0
                                                                                  0
                                                                  0
                                                                                  0
## 29
                 1
                                 1
                                                  0
## 30
                 1
                                 0
                                                  1
                                                                  0
                                                                                  0
## 31
                 1
                                 0
                                                  0
                                                                  1
                                                                                  0
## 32
                 1
                                 1
                                                  0
                                                                  1
                                                                                  0
## 33
                                 0
                                                                                  0
                 1
                                                  1
                                                                  1
## 34
                                                  0
                                                                  0
                                                                                  1
                 1
## 35
                 1
                                 1
                                                  0
                                                                  0
                                                                                  1
## 36
                 1
                                 0
                                                  1
                                                                  0
                                                                                  1
## attr(,"assign")
## [1] 0 1 1 2 2
## attr(,"contrasts")
## attr(,"contrasts")$`factor(attr1)`
## [1] "contr.treatment"
##
## attr(,"contrasts")$`factor(attr2)`
## [1] "contr.treatment"
y = desD1*c(1,.2,.3,.4)+rnorm(6,sd=.1)
res1a = lm(y~factor(attr1) + factor(attr2), data=desFull)
print(summary(res1a))
## Response (Intercept) :
##
## Call:
## lm(formula = `(Intercept)` ~ factor(attr1) + factor(attr2), data = desFull)
##
## Residuals:
##
       Min
                 1Q Median
                                  ЗQ
                                          Max
## -0.3134 -0.2211 -0.0769 0.1442 0.4671
##
```

```
## Coefficients:
##
                   Estimate Std. Error t value Pr(>|t|)
                  4.726e-01 1.084e-01
## (Intercept)
                                        4.361 0.000133 ***
## factor(attr1)2 2.226e-02 1.187e-01
                                         0.188 0.852444
## factor(attr1)3 -1.425e-03 1.187e-01 -0.012 0.990501
## factor(attr2)2 3.738e-17 1.187e-01
                                       0.000 1.000000
## factor(attr2)3 4.532e-17 1.187e-01
                                        0.000 1.000000
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.2908 on 31 degrees of freedom
## Multiple R-squared: 0.001613, Adjusted R-squared:
## F-statistic: 0.01252 on 4 and 31 DF, p-value: 0.9997
##
##
## Response factor(attr1)2 :
##
## Call:
## lm(formula = `factor(attr1)2` ~ factor(attr1) + factor(attr2),
      data = desFull)
##
## Residuals:
##
       Min
                 1Q
                    Median
                                   3Q
                                           Max
## -0.23286 -0.13835 -0.06223 0.11508 0.46714
##
## Coefficients:
##
                   Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                 -2.399e-03 7.712e-02 -0.031
                                                  0.975
## factor(attr1)2 4.973e-01 8.448e-02
                                        5.886 1.7e-06 ***
## factor(attr1)3 -1.425e-03 8.448e-02
                                       -0.017
                                                  0.987
## factor(attr2)2 5.701e-17 8.448e-02
                                         0.000
                                                  1.000
## factor(attr2)3 4.532e-17 8.448e-02
                                         0.000
                                                  1.000
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.2069 on 31 degrees of freedom
## Multiple R-squared: 0.5991, Adjusted R-squared: 0.5474
## F-statistic: 11.58 on 4 and 31 DF, p-value: 7.235e-06
##
##
## Response factor(attr1)3 :
##
## Call:
## lm(formula = `factor(attr1)3` ~ factor(attr1) + factor(attr2),
      data = desFull)
##
## Residuals:
       Min
                 1Q
                     Median
                                   3Q
                                           Max
## -0.31335 -0.10732 0.00000 0.07434 0.38665
##
## Coefficients:
                   Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                 -2.399e-03 6.658e-02 -0.036
                                                  0.971
## factor(attr1)2 2.226e-02 7.294e-02 0.305
```

```
## factor(attr1)3 4.736e-01 7.294e-02
                                         6.493 3.04e-07 ***
## factor(attr2)2 1.831e-17 7.294e-02
                                         0.000
                                                  1.000
## factor(attr2)3 1.700e-17 7.294e-02
                                         0.000
                                                  1.000
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.1787 on 31 degrees of freedom
## Multiple R-squared: 0.634, Adjusted R-squared: 0.5867
## F-statistic: 13.42 on 4 and 31 DF, p-value: 1.858e-06
##
##
## Response factor(attr2)2 :
## Call:
## lm(formula = `factor(attr2)2` ~ factor(attr1) + factor(attr2),
##
      data = desFull)
##
## Residuals:
      Min
               1Q Median
                               3Q
                                      Max
## -0.3134 -0.1371 -0.0375 0.1073 0.4671
##
## Coefficients:
##
                   Estimate Std. Error t value Pr(>|t|)
                 -2.399e-03 7.164e-02 -0.033
## (Intercept)
                                                  0.974
## factor(attr1)2 2.226e-02 7.848e-02
                                         0.284
                                                  0.779
## factor(attr1)3 -1.425e-03 7.848e-02 -0.018
                                                  0.986
## factor(attr2)2 4.750e-01 7.848e-02
                                        6.052 1.06e-06 ***
## factor(attr2)3 2.266e-17 7.848e-02
                                         0.000
                                                  1.000
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.1922 on 31 degrees of freedom
## Multiple R-squared: 0.6123, Adjusted R-squared: 0.5623
## F-statistic: 12.24 on 4 and 31 DF, p-value: 4.392e-06
##
##
## Response factor(attr2)3:
##
## Call:
## lm(formula = `factor(attr2)3` ~ factor(attr1) + factor(attr2),
      data = desFull)
##
## Residuals:
               1Q Median
                               3Q
      Min
                                      Max
## -0.3134 -0.1371 -0.0375 0.1073 0.4671
##
## Coefficients:
##
                   Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                 -2.399e-03 7.164e-02 -0.033
                                                  0.974
## factor(attr1)2 2.226e-02 7.848e-02
                                         0.284
                                                  0.779
## factor(attr1)3 -1.425e-03 7.848e-02 -0.018
                                                  0.986
## factor(attr2)2 3.925e-17 7.848e-02 0.000
                                                  1.000
## factor(attr2)3 4.750e-01 7.848e-02 6.052 1.06e-06 ***
## ---
```

```
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.1922 on 31 degrees of freedom
## Multiple R-squared: 0.6123, Adjusted R-squared: 0.5623
## F-statistic: 12.24 on 4 and 31 DF, p-value: 4.392e-06
# Now draw randomly a "half" random fractional factorial design
sampl = sample.int(n=6,size=3,replace=TRUE)
desHalf = desFull[sampl,]
print(desHalf)
     attr1 attr2 feat1 feat2
##
## 4
       1
             2
                    1
        2
              2
## 5
                     1
                           1
## 3
         3
res1b=lm(y[sampl]~factor(attr1)+factor(attr2), data=desHalf)
print(summary(res1b))
##
## lm(formula = y[sampl] ~ factor(attr1) + factor(attr2), data = desHalf)
##
## Residuals:
## ALL 3 residuals are 0: no residual degrees of freedom!
## Coefficients: (1 not defined because of singularities)
                 Estimate Std. Error t value Pr(>|t|)
##
                   0.5049
                                          NA
## (Intercept)
                                  NA
## factor(attr1)2 0.4571
                                  NA
                                          NA
                                                   NA
## factor(attr1)3 -0.3471
                                  NA
                                          NA
                                                   NA
## factor(attr2)2
                       NΑ
                                  NA
                                          NA
## Residual standard error: NaN on O degrees of freedom
## Multiple R-squared:
                           1, Adjusted R-squared:
## F-statistic: NaN on 2 and 0 DF, p-value: NA
# Now take a random draw of conditions, still 6 observations, but some conditions will be double counte
sampl = sample.int(n=6,size=6,replace=TRUE)
desRandom = desFull[sampl,]
print(desRandom)
##
       attr1 attr2 feat1 feat2
## 3
           3
               1
                      1
## 1
           1
                 1
                       1
                             1
                 2
## 4
           1
                       1
## 1.1
                      1
                            1
           1
                1
## 3.1
           3
                            1
```

2

1

1

1

2

```
# compute some optimal fractional factorial designs
formulaMainEffects1 = ~ attr1 + attr2 + feat1 +feat2
desConjointFract1 = AlgDesign::optFederov(formulaMainEffects1, data=desFull, nTrials=24)
eval.design(formulaMainEffects1,desConjointFract1$design)
## $determinant
## [1] 0.5339536
##
## $A
## [1] 7.8
## $diagonality
## [1] 0.304
##
## $gmean.variances
## [1] 2.19089
\# now with interaction between feat1 and feat2
formulaIntEffects2 = ~ attr1 + attr2 + feat1 + feat2 + feat1*feat2
desConjointFract2<- optFederov(formulaIntEffects2,data=desFull,nTrials=24)
print(desConjointFract2)
## $D
## [1] 0.3734504
##
## $A
## [1] 34.66667
##
## $Ge
## [1] 0.937
## $Dea
## [1] 0.936
##
## $design
##
      attr1 attr2 feat1 feat2
## 1
         1
              1
                      1
## 3
         3
                1
                      1
                            1
## 4
         1
                2
                      1
                            1
## 6
         3
                2
                      1
                            1
## 7
         1
                3
                      1
                            1
## 9
          3
                3
                      1
                            1
## 10
                      2
         1
                1
                            1
## 11
          2
                      2
                1
## 12
          3
                1
                      2
                            1
                      2
## 16
          1
                3
## 17
          2
                3
                      2
                            1
## 18
          3
                3
                      2
## 19
         1
                      1
                            2
                1
## 21
          3
                1
                      1
                            2
## 22
                2
                            2
          1
                      1
## 24
                2
```

25

3

1

1

2

```
## 27
        3
            3
                  1
## 28
        1
             1
                  2
                       2
                       2
## 29
        2
                  2
## 30
        3
             1
                  2
                       2
                  2
                       2
## 34
        1
             3
                  2
## 35
        2
            3
                       2
        3
            3
## 36
##
## $rows
## [1] 1 3 4 6 7 9 10 11 12 16 17 18 19 21 22 24 25 27 28 29 30 34 35
## [24] 36
```

eval.design(formulaIntEffects2,desConjointFract2\$design)

```
## $determinant
## [1] 0.3734504
##
## $A
## [1] 34.66667
##
## $diagonality
## [1] 0.201
##
## $gmean.variances
## [1] 8.19069
```