

Superconductivity

①

In 1911, Onnes found that the electrical resistance of some metals, alloys and compounds drops suddenly to zero when the specimen is cooled below a certain temperature. This phenomenon is called "superconductivity" and cooled specimen is called "superconductor".

Temperature dependence of Resistivity in superconducting material.

① In the superconducting state the resistivity of material is zero.

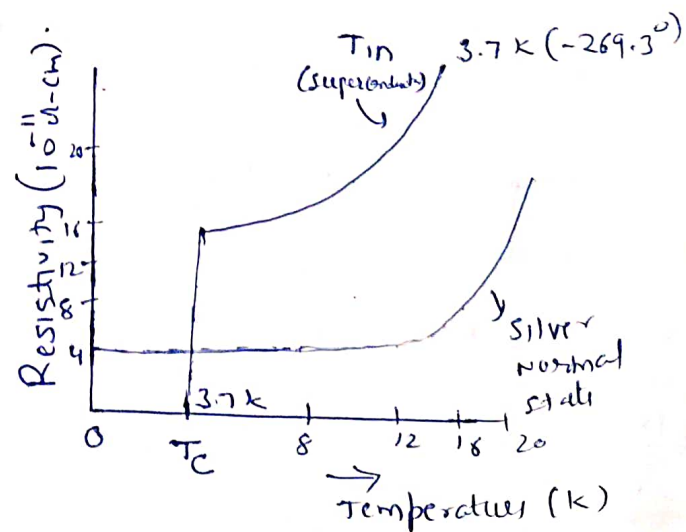
② The temperature called critical temperature (T_c) below which a material undergoes a transition from state of normal conducting to a superconducting state.

③ Critical temperature varies from 23.3 K for the alloy Nb_3Ge to 0.01 K for some semi-conductor.

* In Fig. It has shown that the Tin superconductor shows the resistivity is equal to zero at temperature less than 3.7 K, called critical temperature (T_c).

* Normal metal Silver has residual resistivity at absolute zero kelvin.

So the normal conductor like Cu, Ag, Au, Li does not show superconductivity.



The highest critical temperatures as much as 134 K are found in certain ceramic material.

Oxides of lanthanum, barium and Cu for which $T_c = 30\text{K}$.

Material	T_c
liquid He	4K
liquid N ₂	77K
Mercury (Hg)	4.15K
TiN	3.7K
alloy Pb ₃ Sn	23.3K
Ceramic Ceramic	134K

Note - The electrical resistivity of all the metal and alloys decrease when are cooled.

When the temperature is lowered, the thermal vibration of atoms decreased and conduction electrons are less frequently scattered.

Effect of Magnetic field :-

Super conducting state of material mainly depends on the temperature and magnetic field. It exist only in a particular range of Temperature and field strength.

① Super conducting state disappears if the temperature of specimen is ~~not~~ raised above its critical temperature (T_c).

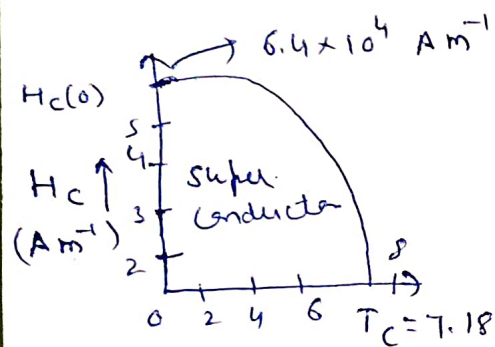
② Critical magnetic field at a given temperature at which super conducting properties are disappears called critical magnetic field (H_c).

* Critical Magnetic field \rightarrow It is the field at which the superconducting properties disappear and denoted as H_c and written as

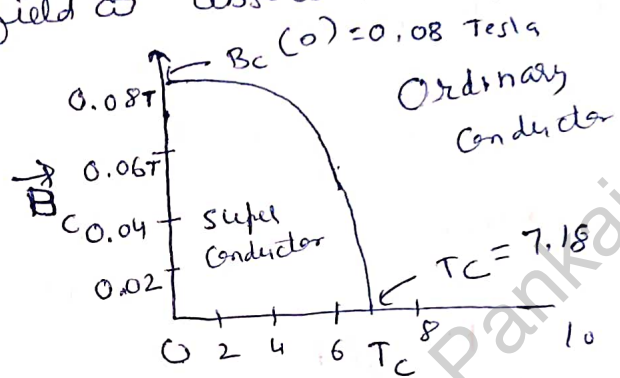
$$H_c = H_0 \left(1 - \left(\frac{T}{T_c} \right)^2 \right)$$

	T_c	$B_c(0)$ Tesla
Al	1.18	0.0105
Hg	4.15	0.0411
Pb	7.18	0.08

H_c is the maximum critical field at temperature T and H_0 is the maximum critical field at absolute temp. T .



variation of critical magnetic field intensity H_c with temperature for Lead

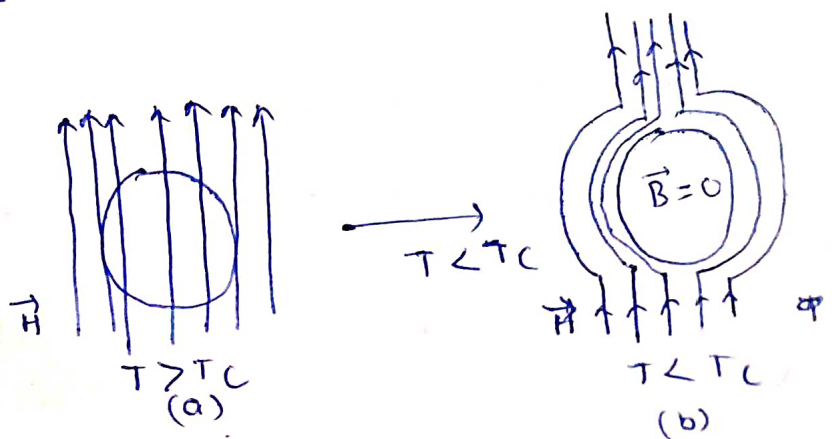


variation of critical field B_c with temperature for Lead.

Meissner effect - (Flux exclusion)

In 1933, Meissner observed that if a superconducting material is placed in a magnetic field and cooled below its critical temperature, it expels all the originally present magnetic flux from its interior it called "Meissner effect".

* Bulk superconductor in weak magnetic field behave as a Diamagnetic in nature



where the magnetic induction (\vec{B}) is zero inside the material.

we know

$$\vec{B} = \mu_0 (\vec{H} + \vec{M}) \rightarrow (1)$$

$$\vec{B} = 0$$

$$\mu_0 (\vec{H} + \vec{M}) = 0$$

$$\vec{M} = -\vec{H} \rightarrow (2)$$

where \vec{M} is the magnetising field intensity

Magnetic susceptibility \rightarrow

we know

$$\vec{M} \propto \vec{H}$$

$$\vec{M} = \chi \vec{H} \rightarrow (3)$$

Now put the value of $\vec{M} = -\vec{H}$ from eq (2) in eq (3)

$$\chi = \frac{\vec{M}}{\vec{H}} = \frac{-\vec{H}}{\vec{H}} = -1$$

Hence susceptibility will be ~~pos~~ -ve (negative) and it is the properties of diamagnetic material.

Hence Super Conductor is a Perfect diamagnetic Material.

Note : Perfect diamagnetism and zero resistivity are two independent and essential properties of superconductor.

Acc. to Ohm law

$$\vec{E} = \rho \vec{J}$$

$$\text{as } \vec{E} = 0$$

$$\text{because } \rho = 0$$

~~So~~

Acc. to Maxwell.

$$\frac{d\vec{B}}{dt} = -\vec{\nabla} \times \vec{E}$$

$$\text{Hence } \frac{d\vec{B}}{dt} = 0$$

$$\vec{B} = \text{Constant.}$$

Critical current →

An electric current flowing through a superconducting specimen itself may be produced for the necessary magnetic field. When magnetic field produced $H_I > H_C$ the super conductivity disappears and material goes to normal state. According to Ampere's law.

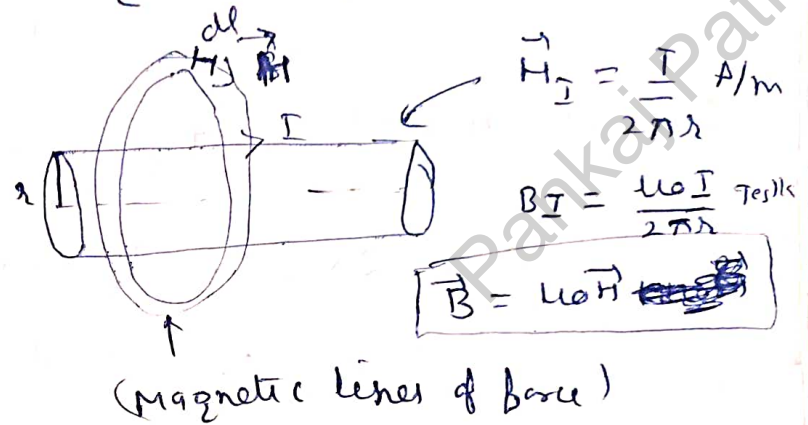
$$\oint \vec{H}_I d\vec{l} = I$$

$$\vec{H}_I \cdot 2\pi r = I$$

$$H_I = H_C$$

$$I = I_c$$

$$\boxed{I_c = 2\pi r H_C} \rightarrow \text{Silber's rule}$$



Hence "minimum current that can be passed in a specimen without destroying its superconductivity is called critical current"

$$\boxed{I_c = 2\pi r H_C}$$

H_C is critical magnetic field.

- Q1 Calculate the critical current, critical current density and critical magnetic field of Lead sample of diameter 1mm at 4.2K. The critical temperature is 7.18K and critical magnetic field at 0K is $6.5 \times 10^4 \text{ A m}^{-1}$.

$$H_c = H_0 \left[1 - \left(\frac{T}{T_c} \right)^2 \right]$$

$$T = 4.2 \text{ K}$$

$$T_c = 7.18 \text{ K}$$

$$H_0 = 6.5 \times 10^4 \text{ Am}^{-1}$$

$$H_c = 6.5 \times 10^4 \left[1 - \left(\frac{4.2}{7.18} \right)^2 \right] = 4.276 \times 10^4 \text{ Am}^{-1}$$

Critical current

$$I_c = 2\pi R H_c$$

$$I_c = 2 \times 3.14 \times \left(\frac{1}{2} \times 10^{-3} \text{ m} \right) \times 4.276 \times 10^4 \text{ Am}^{-1}$$

$$= 134.3 \text{ A}$$

Critical current density

$$J_c = \frac{I_c}{A} = \frac{I_c}{\pi R^2} = \frac{2\pi R H_c}{\pi R^2} = \frac{2H_c}{R}$$

$$J_c = \frac{2 \times 4.276 \times 10^4}{0.5 \times 10^{-3}} = 1.71 \times 10^8 \text{ A/m}^2$$

Persistent current: If current is set up in a perfect superconductor, it can persist for a long time without any applied emf.

A current can be induced in a ring of superconducting material by cooling them in a magnetic field below a transition temperature and then by switching off the field.

(*) When we switch off the field the flux outside the ring disappears, but the inside the ring it will be trapped and leads to current flow for long time up to 10^5 years.

Types of Superconductor - according to behaviour in external magnetic field.

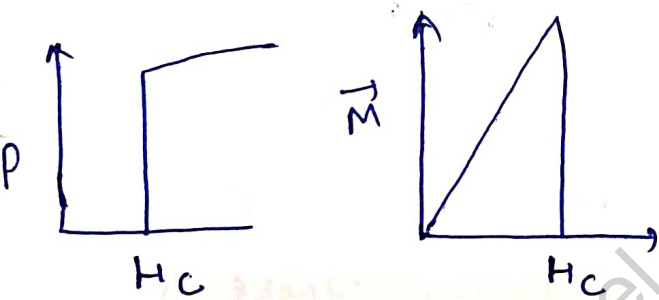
① Type I (soft) superconductor Type II (hard superconductor)

① This type of superconductor is called soft superconductor

② They exhibit complete Meissner effect or they never allow a magnetic flux density to exist in its interior

③ They behave as perfect diamagnetic

④ The critical values of magnetic field H_c at which magnetisation drops are very low.



⑤ The maximum known critical field for type I superconductors are of the order of 0.1 Tesla (1000 Gauss)

⑥ Low value of H_c makes these material unsuitable for use in high field superconducting magnets.

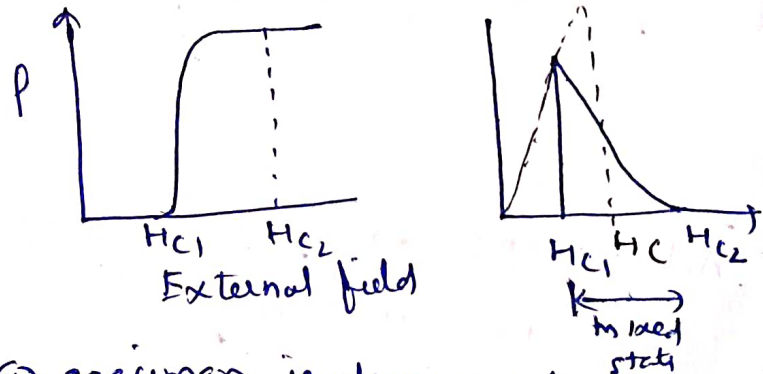
① Type II superconductor are called hard superconductor

② losses magnetization gradually rather than suddenly.

③ They exhibit incomplete (partially) Meissner effect or partially admit magnetic flux density and have zero resistivity.

④ These superconductor have two critical fields called lower or upper critical field called H_{c1} and H_{c2}

Example - Nb-Zr, Nb-Tc alloys
Nb₃Ge - 23.2 (T)



⑤ specimen is diamagnetic below H_c , (magnetic field completely excluded)

⑥ At H_c , the flux begins to penetrate and the penetration of flux increases until the upper critical field H_{c2} is reached.

⑦ The value of H_{c2} for type II material may be 100 times than H_{c1}

High Temperature Superconductor

Those superconductor mainly called metal-alloys having transition temperature above 40K.

In 1987 the compound of yttrium barium copper oxide was found to have a superconductivity temperature nearly 90K.

Most high T_c materials are type II

In $YBa_2Cu_3O_7$ unit cell there will be one atom of a rare earth metal, two barium atoms, three copper atoms and seven oxygen atoms also known as Y_{123} .

Other known High T_c superconductors

$BiSrCaCuO$ - 110 K

$Tl_2Ba_2Cu_3O_{10}$ - 125 K

Advantage \rightarrow High temperature superconductor can be cooled by using liquid nitrogen whereas the previously known superconductors require expensive and hard to handle the coolants like liquid Helium.

Application - Since they retain their superconductivity in higher magnetic field, they are used for constructing superconducting magnets.