

Question 3

(Assuming a block size is 8 bytes.)

$$SIZE = 4 \times 1 \times n.$$

$$n = \frac{4 \times 1 \times n}{4}.$$

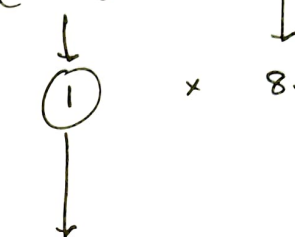
$n = n$ direct-mapping.

$$SIZE = (\#sets) \times (ASSOC) \times (BLOCKSIZE).$$

$$SIZE = (\#sets) \times (\#ways) \times (\#bytes/block).$$

$$SIZE = 4.$$

$$SIZE = 32$$



As the given example has 1 way it is direct-mapped Cache

Question-4

Assume each block is 8 bytes.

	way 0	way 1	way 2
Set 0			
Set 1			
Set 2			
Set 3			

$$SIZE = (\#sets) \times (ASSOC) \times (BLOCKSIZE).$$

$$(\#sets) \times (\#ways) \times (\#bytes/block)$$

$$SIZE = 4 \times 3 \times 8.$$

$$12 \times 8 = 96 \text{ bytes.}$$

$$\#ways = 3$$

Question - 5

	way0	way1	way2
Set 0	Block	Block	Block

We know Direct-mapped & fully-associative are extremes where

Direct-mapped
has a single (1)
Way.

f.

fully-associative
has a single set
in a cache.

Question 6 -

Number of Block offset bits

Number of index bits.

Number of tag bits.

(memory address = 32 bit = 8 bytes)

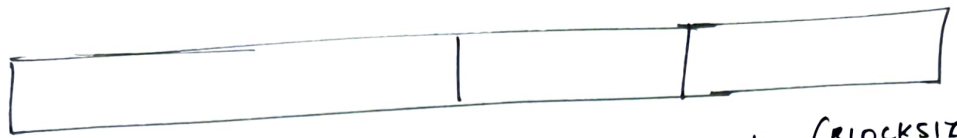
	SIZE	ASSOC	BLOCKSIZE
i.	32 B	1	8 B.

$$SIZE = (\#sets) \times ASSOC \times (BLOCKSIZE)$$

$$32 = (\#sets) \times 1 \times 8$$

$$\#sets = \underline{4}$$

Set 0	Block
Set 1	Block
Set 2	Block
Set 3	Block



$$(\# \text{ address bits}) - \log_2(\# \text{ sets}) - \log_2(\text{BLOCKSIZE}) \quad \log_2(\# \text{ sets}) \quad \log_2(\text{BLOCKSIZE}).$$

$$\# \text{ Block offset bits} = \log_2(\text{BLOCKSIZE})$$

$$\log_2(8) = 3$$

$$\log_2(2^3)$$

$$\underline{\underline{3 \log_2 2 = 3}}$$

$$\# \text{ index bits} = \log_2(\# \text{ sets})$$

$$\log_2(2^2) = \underline{\underline{2 \log_2 2 = 2}}$$

$$\# \text{ tag bits} = (\# \text{ address bits}) - \log_2(\# \text{ sets}) - \log_2(\text{BLOCKSIZE})$$

$$= 32 - \log_2(2^2) - \log_2(2^3)$$

$$32 - 2 - 3 = \underline{\underline{32 - 5 = 27}}$$

(ii) Given $\text{SIZE} = 4 \text{ KB} = 4 \times 2^{10} = \underline{2^{12} \text{ B.}}$
 $\text{ASSOC} = 4\text{-way-set-Associative} = 4.$
 $\text{BLOCKSIZE} = 32. \text{ (Bytes / block)} \rightarrow 2^5.$

	way 0	way 1	way 2	way 3
Set 0				
Set 1				
...				
Set 30				
Set 31				

$$\text{SIZE} = (\# \text{ sets}) \times (\text{ASSOC}) \times (\text{BLOCKSIZE})$$

$$2^{12} = \# \text{ sets} \times 2^2 \times 2^5$$

$$\# \text{ sets} = \frac{2^{12}}{2^7} =$$

$$2^5 = 32 \text{ sets}$$

$$\begin{aligned}\# \text{Block offset Bits} &= \log_2 (\text{BLOCKSIZE}) \\ &= \log_2 (2^5) = 5 \log_2 2 \\ &= \boxed{5}\end{aligned}$$

$$\begin{aligned}\# \text{index Bits} &= \log_2 (\# \text{sets}) \\ &= \log_2 (2^5) \\ &= 5 \log_2 2 = \boxed{5}\end{aligned}$$

$$\begin{aligned}\# \text{tag bits} &= \left(\# \text{ address Bits} \right) - \left(\# \text{ index Bits} \right) - \left(\# \text{ block offset Bits} \right) \\ &= 32 - 5 - 5 = \boxed{22}\end{aligned}$$

iii) $\text{SIZE} = 12 \text{ KB} = 2^3 \times 2^3 \times 2^2 \times 2^{10}$
 $= 3 \times 2^2 \times 2^{10}$
 $= 3 \times 2^{12} \text{ B.}$

$$\text{ASSOC} = 3.$$

$$\text{BLOCKSIZE} = 32 \text{ B.} = 2^5 \text{ B.}$$

$$\text{SIZE} = (\# \text{sets}) \times (\text{ASSOC}) \times (\text{BLOCKSIZE})$$

$$3 \times 2^{12} = (\# \text{sets}) \times 3 \times 2^5$$

$$\# \text{sets} = \frac{3 \times 2^{12}}{3 \times 2^5} = \underline{\underline{2^7}}$$

$$\begin{aligned}\# \text{sets} &= 32 \times 4 \\ &= \underline{\underline{128}}\end{aligned}$$

$$\begin{aligned} \# \text{ Block offsets} &= \log_2(\text{BLOCKSIZE}) \\ &= \log_2(2^5) = \boxed{5} \text{ bits.} \end{aligned}$$

$$\begin{aligned} \# \text{ Index bits} &= \log_2(\# \text{ sets}) \\ &= \log_2(2^7) = \boxed{7} \text{ bits.} \end{aligned}$$

$$\begin{aligned} \# \text{ tag bits} &= \# \text{ address bits} - \# \text{ index bits} - \# \text{ Block offset bits.} \\ &= 32 - 5 - 7 = \boxed{20 \text{ bits}} \end{aligned}$$

	way0	way1	way2
Set 0			
Set 1			
...			
Set 126			
Set 127			

$\boxed{\text{iv}} \rightarrow \text{SIZE} = 128 = 2^7 \cdot B.$

$\text{ASSOC} = 8$

$\text{BLOCKSIZE} = 16 = 2^4 \cdot B.$

$$\text{SIZE} = (\# \text{ sets}) \times (\text{ASSOC}) \times (\text{BLOCKSIZE})$$

$$2^7 = (\# \text{ sets}) \times 8 \times 2^4.$$

$$\# \text{ sets} = \frac{2^7}{2^3 \times 2^4} = 1.$$

$\# \text{ sets} = 1$ (fully-associative).

	way0	way1	way2	way3	way4	...	way7
Set 0							

~~# index hits~~

$$\begin{aligned}\# \text{ Block offset hits} &= \log_2(\text{BLOCKSIZE}) \\ &= \log_2(16) = \log_2(2^4) \\ &= \boxed{4 \text{ hits}}.\end{aligned}$$

$$\# \text{ index hits} = \log_2(1) = 0 \text{ hits}.$$

$$\begin{aligned}\# \text{ Tag hits} &= \left(\# \text{ address hits} \right) - \left(\# \text{ index hits} \right) - \left(\# \text{ Block offset hits} \right) \\ &= 32 - 0 - 4 = \boxed{28 \text{ hits}}\end{aligned}$$

