Homework 4 Spring 2022

Due 04/18 23:59

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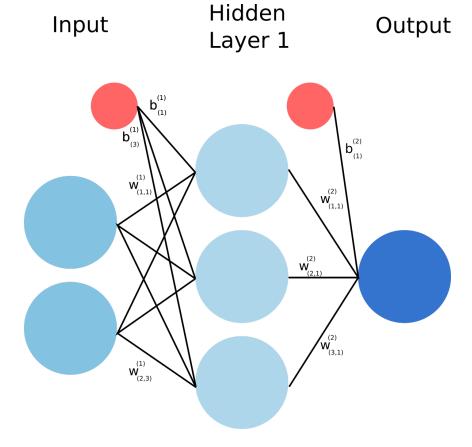
```
import numpy as np
import matplotlib.pyplot as plt

import pprint
pp = pprint.PrettyPrinter(indent=4)
```

Part 1: Feed forward network from scratch!

For this part, you are not allowed to use any library other than numpy.

In this part, you will will implement the forward pass and backward pass (i.e. the derivates of each parameter wrt to the loss) for the following neural network:



The weight matrix for the hidden layer is W1 and has bias b1.

The weight matrix for the ouput layer is W2 and has bias b2.

Activatation function is sigmoid for both hidden and output layer

Loss function is the MSE loss

$$L(y,y_t) = rac{1}{2N} \sum_{n=1}^{N} (y^n - y_t^n)^2$$

Refer to the below dictionary for dimensions for each matrix

```
In [2]:
    np.random.seed(0) # don't change this

weights = {
        'W1': np.random.randn(3, 2),
        'b1': np.zeros(3),
        'W2': np.random.randn(3),
        'b2': 0,
}

X = np.random.rand(1000,2)
Y = np.random.randint(low=0, high=2, size=(1000,))
```

```
In [3]:
         def sigmoid(z):
             return 1/(1 + np.exp(-z))
In [4]:
         #Implement the forward pass
         def forward_propagation(X, weights):
             # Z1 -> output of the hidden layer before applying activation
             # H -> output of the hidden layer after applying activation
             # Z2 -> output of the final layer before applying activation
             # Y -> output of the final layer after applying activation
             Z1 = np.dot(X, weights['W1'].T) + weights['b1']
             H = sigmoid(Z1)
             Z2 = np.dot(H, weights['W2'].T) + weights['b2']
             Y = sigmoid(Z2)
             return Y, Z2, H, Z1
In [5]:
         # Implement the backward pass
         # Y T are the ground truth labels
         def back propagation(X, Y T, weights):
             N_points = X.shape[0]
             # forward propagation
             Y, Z2, H, Z1 = forward_propagation(X, weights)
             L = (1/(2*N points)) * np.sum(np.square(Y - Y T))
             # back propagation
             dLdY = 1/N points * (Y - Y_T)
             dLdZ2 = np.multiply(dLdY, (sigmoid(Z2)*(1-sigmoid(Z2))))
             dLdW2 = np.dot(H.T, dLdZ2)
             dLdb2 = np.sum(dLdZ2, axis = 0)
```

```
# forward propagation
Y, Z2, H, Z1 = forward_propagation(X, weights)
L = (1/(2*N_points)) * np.sum(np.square(Y - Y_T))

# back propagation
dLdY = 1/N_points * (Y - Y_T)
dLdZ2 = np.multiply(dLdY, (sigmoid(Z2)*(1-sigmoid(Z2))))
dLdW2 = np.dot(H.T, dLdZ2)
dLdb2 = np.sum(dLdZ2, axis = 0)

dLdH = np.dot(dLdZ2[:, np.newaxis], weights['W2'][np.newaxis, :])
dLdZ1 = np.multiply(dLdH, (sigmoid(Z1)*(1-sigmoid(Z1))))
dLdW1 = np.dot(X.T, dLdZ1)
dLdb1 = np.sum(dLdZ1, axis = 0)

gradients = {
    'W1': dLdW1,
    'b1': dLdb1,
    'W2': dLdb2,
    'b2': dLdb2,
}

return gradients, L
```

Your answers should be close to L=0.133 and 'b1': array([0.00492, -0.000581, -0.00066]). You will be graded based on your implementation and outputs for L, W1, W2 b1, and b2

You can use any library for the following questions.

Part 2: Fashion MNIST dataset

The Fashion-MNIST dataset is a dataset of Zalando's article images—consisting of a training set of 60,000 examples and a test set of 10,000 examples. Each example is a 28x28 grayscale image, associated with a label from 10 classes. It's commonly used as a direct drop-in replacement for the original MNIST dataset for benchmarking machine learning models. You can read more about the dataset at the Fashion-MNIST homepage.

We will utilize tensorflow to import the dataset, however, feel free to use any framework (TF/PyTorch) to answer the assignment questions.

```
from tensorflow.keras.datasets import fashion_mnist

# load data
(xdev, ydev), (xtest, ytest) = fashion_mnist.load_data()
```

```
Downloading data from https://storage.googleapis.com/tensorflow/tf-keras-datas
ets/train-labels-idx1-ubyte.gz
Downloading data from https://storage.googleapis.com/tensorflow/tf-keras-datas
ets/train-images-idx3-ubyte.gz
Downloading data from https://storage.googleapis.com/tensorflow/tf-keras-datas
ets/t10k-labels-idx1-ubyte.gz
======] - 0s Ous/step
Downloading data from https://storage.googleapis.com/tensorflow/tf-keras-datas
ets/t10k-images-idx3-ubyte.gz
```

2.1 Plot the first 25 samples from both development and test sets on two separate 5×5 subplots.

Each image in your subplot should be labelled with the ground truth label. Get rid of the plot axes for a nicer presentation. You should also label your plots to indicate if the plotted data is from development or test set. You are given the expected output for development samples.

```
def plot_sampled_images(X_data, Y_data, num_rows, num_cols, title):
    num_images_to_sample = num_rows * num_cols
    images_ls = X_data[:num_images_to_sample]

    fig, axes = plt.subplots(num_rows, num_cols, figsize = (2 * num_rows, 2 *
        fig.suptitle(title)
    for curr_idx, image in enumerate(images_ls):
        ax = axes[curr_idx//num_cols, curr_idx%num_cols]
        ax.imshow(image)
        ax.set_title(f"Label: {Y_data[curr_idx]}")
        ax.axis('off')

    plt.show()
```

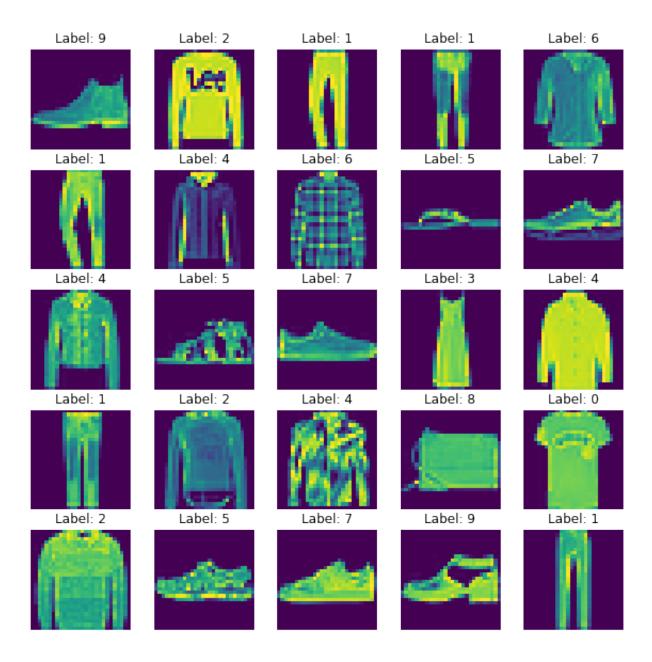
```
In [10]: # Plot dev samples
    plot_sampled_images(xdev, ydev, 5, 5, "Development Set Image Sample")
```

Development Set Image Sample



In [11]: # Plot test samples
 plot_sampled_images(xtest, ytest, 5, 5, "Test Set Image Sample")

Test Set Image Sample



Part 3: Feed Forward Network

In this part of the homework, we will build and train a deep neural network on the Fashion-MNIST dataset.

3.1.1 Print their shapes - $x_{
m dev}, y_{
m dev}, x_{
m test}, y_{
m test}$

```
In [12]: # Print
    print(f"X Development Shape: {xdev.shape}")
    print(f"Y Development Shape: {ydev.shape}")
    print(f"X Test Shape: {xtest.shape}")
    print(f"Y Test Shape: {ytest.shape}")

X Development Shape: (60000, 28, 28)
Y Development Shape: (60000,)
X Test Shape: (10000, 28, 28)
Y Test Shape: (10000,)
```

3.1.2 Flatten the images into one-dimensional vectors. Again, print out the shapes of $x_{ m dev}, x_{ m test}$

```
In [13]:
          I am going to use the reshape as that is faster!
          import time
          start time = time.time()
          xdev_images = np.array([dev_image.flatten() for dev_image in xdev])
          end_time = time.time()
          print(f"Time taken: {end_time - start_time}")
          start_time = time.time()
          xdev images = xdev.reshape(xdev.shape[0], xdev.shape[1] * xdev.shape[2])
          end time = time.time()
          print(f"Time taken: {end_time - start_time}")
         Time taken: 0.2842710018157959
         Time taken: 0.0004353523254394531
In [14]:
          # Flatten and print
          xdev = xdev.reshape(xdev.shape[0], xdev.shape[1] * xdev.shape[2])
          xtest = xtest.reshape(xtest.shape[0], xtest.shape[1] * xtest.shape[2])
          print(f"X Development Shape: {xdev.shape}")
          print(f"X Test Shape: {xtest.shape}")
         X Development Shape: (60000, 784)
         X Test Shape: (10000, 784)
```

3.1.3 Standardize the development and test sets.

Note that the images are 28x28 numpy arrays, and each pixel takes value from 0 to 255.0. 0 means background (white), 255 means foreground (black).

```
In [15]: # Standardize
    xdev = xdev / 255.0
    xtest = xtest / 255.0
```

3.1.4 Assume your neural network has softmax activation as the last layer activation. Would you consider encoding your target variable? Which encoding would you choose and why? The answer depends on your choice of loss function too, you might want to read 3.2.1 and 3.2.5 before answering this one!

Encode the target variable else provide justification for not doing so. Supporting answer may contain your choice of loss function.

```
In [16]: # answer
    from tensorflow.keras import utils

    num_classes = 10
    ydev = utils.to_categorical(ydev, num_classes)
    ytest = utils.to_categorical(ytest, num_classes)

    print(f"Development Labels Shape: {ydev.shape}")
    print(f"Test Labels Shape: {ytest.shape}")
```

Development Labels Shape: (60000, 10) Test Labels Shape: (10000, 10)

Reasons for the encoding:

- 1. Because we know the target classes beforehand and it's uniformly distributed, we can use encoding for the categorical target variable here. Furthermore, as the number of classes is just 10 and not very large, it wouldn't increase the dimensionality of the data by a lot, thus, I am using one-hot encoding here using the "to_categorical" function in the utils package.
- 2. Usage of Loss Function: "Categorical Cross Entropy": Also, as we will be using this loss function which computes losses across all the categories and is generally used for multi-class classification which is the case here, I have to do one-hot encoding here for the target variable. The losses using this function are computed as the differences in the one-hot encoded target vector and the probabilities (logits) generated at the end of the network.

Thus, I have to encode the target variable as one-hot vectors here.

3.1.5 Train-test split your development set into train and validation sets (8:2 ratio).

Note that splitting after encoding does not causes data leakage here because we know all the classes beforehand.

```
# split
from sklearn.model_selection import train_test_split
xtrain, xval, ytrain, yval = train_test_split(xdev, ydev, test_size = 0.2)
```

3.2.1 Build the feed forward network

Using Softmax activation for the last layer and ReLU activation for every other layer, build the following model:

- 1. First hidden layer size 128
- 2. Second hidden layer size 64
- 3. Third and last layer size You should know this

```
In [18]:  # build model
    from tensorflow.keras.models import Sequential
    from tensorflow.keras.layers import Dense

model = Sequential()

#Hidden Layers
model.add(Dense(units = 128, activation = "relu", input_shape = (xtrain.shape model.add(Dense(units = 64, activation = "relu"))

# Output Layer
model.add(Dense(units = 10, activation = "softmax"))

# Building the model network
model.build()
```

3.2.2 Print out the model summary

```
In [19]: # print summary
model.summary()
```

Model: "sequential"

Layer (type)	Output Shape	Param #
dense (Dense)	(None, 128)	100480
dense_1 (Dense)	(None, 64)	8256
dense_2 (Dense)	(None, 10)	650
Total params: 109,386 Trainable params: 109,386 Non-trainable params: 0		

3.2.3 Report the total number of trainable parameters. Do you think this number is dependent on the image height and width? Only Yes/No required.

```
# answer
from keras.utils.layer_utils import count_params
trainable_count = count_params(model.trainable_weights)
print(f"Number of Trainable Parameters in the model is: {trainable_count}")
```

Number of Trainable Parameters in the model is: 109386

The number of trainable parameters in the model is 109386.

Yes the number of Trainable parameters in the model depends on the image height and width in a way that it depends on the pixels in the image (total number of nodes required in the input layer). If for some other height and width, the number of nodes/pixels remains the same, then this won't impact the number of trainable parameters and thus, not affect the model training.

3.2.4 Print out your model's output on first train sample. This will confirm if your dimensions are correctly set up. Is the sum of this output equal to 1 upto two decimal places?

Yes, the sum of the ouputs equals 1 as the sum of all the probabilities should be 1.

3.2.5 Considering the output of your model and overall objective, what loss function would you choose and why? Choose a metric for evaluation and explain the reason behind your choice.

I would choose "Categorical Cross Entropy" here because:

- 1. This loss function is generally used for Multi-class classification which is our objective here as we want to classify 10 classes.
- 2. Also, as the outputs generated from our model are probabilities for each of the classes and this function computes the difference between two probability distributions, one being the probabilities computed at the end of the network and other is the encoding from the target variable, we need this loss function to compute the loss across all the categories.
- 3. Also, as the activation for our last/output layer is "softmax" which basically works really well with the formulation for cross entropy, I am choosing my loss function to be "Categorical Cross Entropy".

Also, I would chooose "Categorical Accuracy" as the metric here: Since the dataset is balanced (6000 for each class), a metric related to accuracy would suffice. Also, as we need to match the predictions with the one-hot labels for multiple categories (10 class labels), we are using "Categorical Accuracy" as the metric here.

3.2.6 Using the metric and loss function above, with Adam as the optimizer, train your model for 20 epochs with batch size 128.

Make sure to save and print out the values of loss function and metric after each epoch for both train and validation sets.

Note - Use appropriate learning rate for the optimizer, you might have to try different values

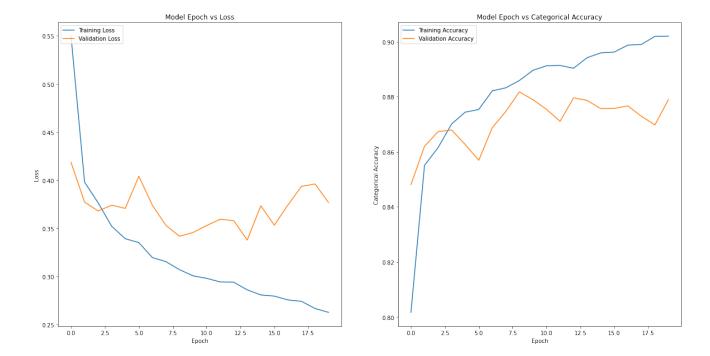
```
In [23]:
       # train
       from tensorflow.keras.losses import CategoricalCrossentropy
       from tensorflow.keras.optimizers import Adam
       from tensorflow.keras.metrics import CategoricalAccuracy
      model.compile(loss = CategoricalCrossentropy(),
                optimizer = Adam(learning rate = 1e-2),
                metrics = [CategoricalAccuracy()])
      history = model.fit(xtrain, ytrain, batch_size = 128, epochs = 20, validation
      Epoch 1/20
      rical accuracy: 0.8017 - val loss: 0.4185 - val categorical accuracy: 0.8481
      rical_accuracy: 0.8551 - val_loss: 0.3773 - val_categorical_accuracy: 0.8620
      Epoch 3/20
      rical accuracy: 0.8615 - val loss: 0.3680 - val categorical accuracy: 0.8673
      Epoch 4/20
      375/375 [============] - 1s 3ms/step - loss: 0.3521 - catego
      rical_accuracy: 0.8701 - val_loss: 0.3741 - val_categorical_accuracy: 0.8679
      Epoch 5/20
      rical accuracy: 0.8744 - val loss: 0.3708 - val categorical accuracy: 0.8627
      Epoch 6/20
      375/375 [=============] - 1s 3ms/step - loss: 0.3352 - catego
      rical_accuracy: 0.8754 - val_loss: 0.4042 - val_categorical_accuracy: 0.8569
      Epoch 7/20
      375/375 [=============] - 1s 3ms/step - loss: 0.3196 - catego
      rical accuracy: 0.8821 - val loss: 0.3740 - val categorical accuracy: 0.8687
      Epoch 8/20
      rical accuracy: 0.8832 - val loss: 0.3531 - val categorical accuracy: 0.8747
      Epoch 9/20
      rical_accuracy: 0.8859 - val_loss: 0.3418 - val_categorical_accuracy: 0.8817
      Epoch 10/20
      rical accuracy: 0.8896 - val loss: 0.3457 - val categorical accuracy: 0.8789
      Epoch 11/20
      rical_accuracy: 0.8912 - val_loss: 0.3529 - val_categorical_accuracy: 0.8754
```

Epoch 12/20

```
rical accuracy: 0.8913 - val loss: 0.3595 - val categorical accuracy: 0.8711
Epoch 13/20
rical accuracy: 0.8903 - val loss: 0.3580 - val categorical accuracy: 0.8796
Epoch 14/20
375/375 [=============] - 1s 3ms/step - loss: 0.2861 - catego
rical accuracy: 0.8942 - val loss: 0.3378 - val categorical accuracy: 0.8787
Epoch 15/20
rical accuracy: 0.8959 - val loss: 0.3735 - val categorical accuracy: 0.8757
Epoch 16/20
rical_accuracy: 0.8962 - val_loss: 0.3533 - val_categorical accuracy: 0.8758
Epoch 17/20
rical_accuracy: 0.8987 - val_loss: 0.3742 - val_categorical_accuracy: 0.8767
Epoch 18/20
rical accuracy: 0.8990 - val loss: 0.3936 - val categorical accuracy: 0.8729
Epoch 19/20
rical accuracy: 0.9019 - val loss: 0.3962 - val categorical accuracy: 0.8698
Epoch 20/20
rical accuracy: 0.9020 - val loss: 0.3768 - val categorical accuracy: 0.8790
```

3.2.7 Plot two separate plots displaying train vs validation loss and train vs validation metric scores over each epoch

```
In [24]:
          # plot
          plt.rcParams["figure.figsize"] = (20, 10)
          figure , axes = plt.subplots(1, 2)
          axes[0].plot(history.history['loss'])
          axes[0].plot(history.history['val loss'])
          axes[0].set xlabel('Epoch')
          axes[0].set ylabel('Loss')
          axes[0].set_title('Model Epoch vs Loss')
          axes[0].legend(['Training Loss', 'Validation Loss'], loc='upper left')
          axes[1].plot(history.history['categorical accuracy'])
          axes[1].plot(history.history['val_categorical_accuracy'])
          axes[1].set_xlabel('Epoch')
          axes[1].set ylabel('Categorical Accuracy')
          axes[1].set title('Model Epoch vs Categorical Accuracy')
          axes[1].legend(['Training Accuracy', 'Validation Accuracy'], loc='upper left'
          plt.show()
```



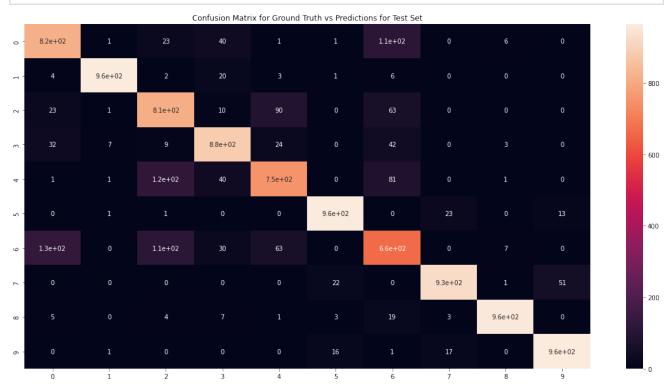
3.3.1 Report metric score on test set

3.3.2 Plot confusion matrix on the test set and label the axes appropriately with true and predicted labels.

Labels on the axes should be the original classes (0-9) and not one-hot-encoded. To achieve this, you might have to reverse transform your model's predictions. Please look into the documentation of your target encoder. Sample output is provided

In [26]:

```
# confusion matrix
from sklearn.metrics import confusion_matrix
import seaborn as sns
# Getting the predictions on the test set.
test preds = list()
test gts = list()
ypreds = model.predict(xtest)
for idx, ypred in enumerate(ypreds):
  class pred = np.argmax(ypred)
  class gt = np.argmax(ytest[idx])
  test preds.append(class pred)
  test_gts.append(class_gt)
cf_matrix = confusion_matrix(test_gts, test_preds)
sns.heatmap(cf_matrix, annot = True)
plt.title("Confusion Matrix for Ground Truth vs Predictions for Test Set")
plt.show()
```



3.3.3 Plot the first 25 samples of test dataset on a 5×5 subplot and this time label the images with both the ground truth (GT) and predicted class (P).

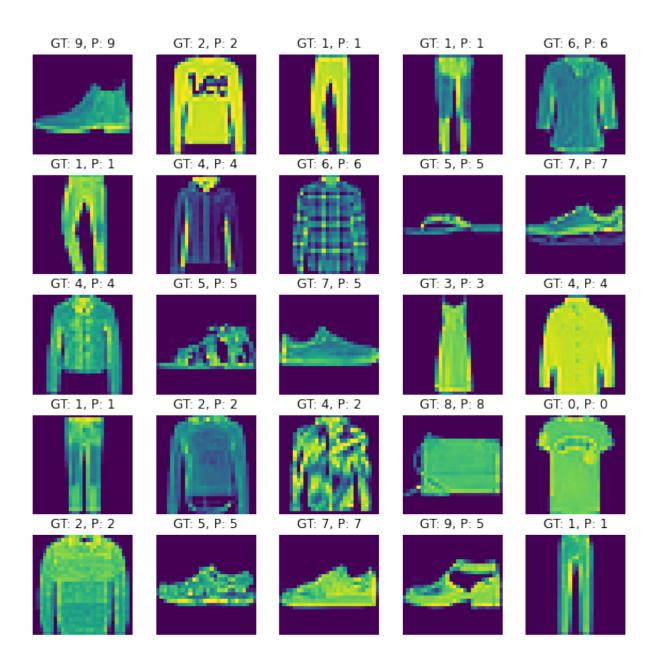
For instance, an image of class 3, with predicted class 7 should have the label GT:3, P:7. Get rid of the plot axes for a nicer presentation.

```
In [27]: # Plot with predictions
num_images_to_sample = 25
images_ls = xtest[:num_images_to_sample].reshape((num_images_to_sample, 28, 2)

fig, axes = plt.subplots(5, 5, figsize = (10, 10))
fig.suptitle("GT (Ground Truths) and P (Predictions) for Test Dataset as Image
for curr_idx, image in enumerate(images_ls):
    ax = axes[curr_idx//5, curr_idx%5]
    ax.imshow(image)
    ax.set_title(f"GT: {test_gts[curr_idx]}, P: {test_preds[curr_idx]}")
    ax.axis('off')

plt.show()
```

GT (Ground Truths) and P (Predictions) for Test Dataset as Image Labels



Part 4: Convolutional Neural Network

In this part of the homework, we will build and train a classical convolutional neural network, LeNet-5, on the Fashion-MNIST dataset.

```
In [28]:
    from tensorflow.keras.datasets import fashion_mnist
    # load data again
    (xdev, ydev), (xtest, ytest) = fashion_mnist.load_data()
```

4.1 Preprocess

- 1. Standardize the datasets
- 2. Encode the target variable.
- 3. Split development set to train and validation sets (8:2).

```
In [29]:
          # TODO: Standardize the datasets
          xdev = xdev/255.0
          xtest = xtest/255.0
          # TODO: Encode the target labels
          ydev = utils.to_categorical(ydev, 10)
          ytest = utils.to categorical(ytest, 10)
          print(f"Shape of y-dev: {ydev.shape}")
          print(f"Shape of y-test: {ytest.shape}")
          # Split
          xtrain, xval, ytrain, yval = train test split(xdev, ydev, test size = 0.2)
          print(f"Shape of xtrain: {xtrain.shape}")
          print(f"Shape of xval: {xval.shape}")
          print(f"Shape of ytrain: {ytrain.shape}")
          print(f"Shape of yval: {yval.shape}")
         Shape of y-dev: (60000, 10)
         Shape of y-test: (10000, 10)
         Shape of xtrain: (48000, 28, 28)
         Shape of xval: (12000, 28, 28)
         Shape of ytrain: (48000, 10)
         Shape of yval: (12000, 10)
```

4.2.1 LeNet-5

We will be implementing the one of the first CNN models put forward by Yann LeCunn, which is commonly referred to as LeNet-5. The network has the following layers:

- 1. 2D convolutional layer with 6 filters, 5x5 kernel, stride of 1 padded to yield the same size as input, ReLU activation
- 2. Maxpooling layer of 2x2
- 3. 2D convolutional layer with 16 filters, 5x5 kernel, 0 padding, ReLU activation
- 4. Maxpooling layer of 2x2
- 5. 2D convolutional layer with 120 filters, 5x5 kernel, ReLU activation. Note that this layer has 120 output channels (filters), and each channel has only 1 number. The output of this layer is just a vector with 120 units!
- 6. A fully connected layer with 84 units, ReLU activation
- 7. The output layer where each unit respresents the probability of image being in that category. What activation function should you use in this layer? (You should know this)

```
In [30]:
          # TODO: build the model
          from tensorflow.keras.layers import Conv2D, MaxPooling2D, Dense, Flatten
          lenet5 model = Sequential()
          lenet5_model.add(Conv2D(filters = 6, kernel_size = (5, 5),
                           strides = (1, 1), padding = "same",
                           activation = "relu",
                           input_shape = (xtrain.shape[1], xtrain.shape[1], 1)))
          lenet5 model.add(MaxPooling2D((2, 2)))
          lenet5 model.add(Conv2D(filters = 16, kernel size = (5, 5),
                           strides = (1, 1), padding = "valid",
                           activation = "relu"))
          lenet5 model.add(MaxPooling2D((2, 2)))
          lenet5 model.add(Conv2D(filters = 120, kernel size = (5, 5), activation = "re
          lenet5 model.add(Flatten())
          lenet5_model.add(Dense(84, activation = "relu"))
          # I am using Softmax function in the last layer
          lenet5 model.add(Dense(10, activation = "softmax"))
          lenet5 model.build()
```

4.2.2 Report layer output

Report the output dimensions of each layers of LeNet-5. **Hint:** You can report them using the model summary function that most frameworks have, or you can calculate and report the output dimensions by hand (It's actually not that hard and it's a good practice too!)

```
In [31]: # TODO: report model output dimensions
lenet5_model.summary()
```

Model: "sequential 1"

Layer (type)	Output Shape	Param #
conv2d (Conv2D)	(None, 28, 28, 6)	156
<pre>max_pooling2d (MaxPooling2D)</pre>	(None, 14, 14, 6)	0
conv2d_1 (Conv2D)	(None, 10, 10, 16)	2416
<pre>max_pooling2d_1 (MaxPooling 2D)</pre>	(None, 5, 5, 16)	0
conv2d_2 (Conv2D)	(None, 1, 1, 120)	48120
flatten (Flatten)	(None, 120)	0
dense_3 (Dense)	(None, 84)	10164
dense_4 (Dense)	(None, 10)	850
		=======

Total params: 61,706

Trainable params: 61,706 Non-trainable params: 0

4.2.3 Model training

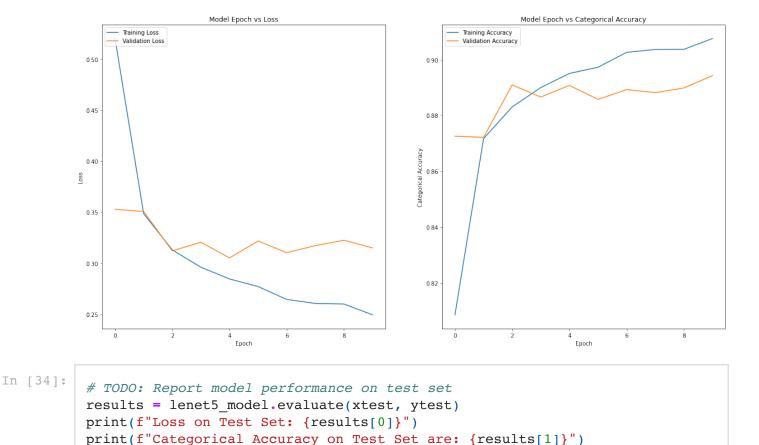
Train the model for 10 epochs. In each epoch, record the loss and metric (chosen in part 3) scores for both train and validation sets. Use two separate plots to display train vs validation metric scores and train vs validation loss. Finally, report the model performance on the test set. Feel free to tune the hyperparameters such as batch size and optimizers to achieve better performance.

```
In [32]:
```

```
Epoch 1/10
orical_accuracy: 0.8087 - val_loss: 0.3528 - val_categorical_accuracy: 0.8726
Epoch 2/10
rical accuracy: 0.8717 - val loss: 0.3506 - val categorical accuracy: 0.8722
Epoch 3/10
rical_accuracy: 0.8831 - val_loss: 0.3120 - val_categorical_accuracy: 0.8909
Epoch 4/10
rical accuracy: 0.8900 - val loss: 0.3205 - val categorical accuracy: 0.8866
Epoch 5/10
rical_accuracy: 0.8950 - val_loss: 0.3051 - val_categorical_accuracy: 0.8907
Epoch 6/10
rical_accuracy: 0.8972 - val_loss: 0.3217 - val_categorical_accuracy: 0.8857
Epoch 7/10
rical accuracy: 0.9026 - val loss: 0.3102 - val categorical accuracy: 0.8892
Epoch 8/10
rical_accuracy: 0.9036 - val_loss: 0.3172 - val_categorical_accuracy: 0.8882
Epoch 9/10
rical accuracy: 0.9036 - val loss: 0.3224 - val categorical accuracy: 0.8898
Epoch 10/10
rical_accuracy: 0.9075 - val_loss: 0.3149 - val_categorical_accuracy: 0.8942
```

```
In [33]:
          # TODO: Plot accuracy and loss over epochs
          plt.rcParams["figure.figsize"] = (20, 10)
          figure , axes = plt.subplots(1, 2)
          figure.suptitle("For LeNet-5 Model")
          axes[0].plot(history.history['loss'])
          axes[0].plot(history.history['val loss'])
          axes[0].set xlabel('Epoch')
          axes[0].set_ylabel('Loss')
          axes[0].set title('Model Epoch vs Loss')
          axes[0].legend(['Training Loss', 'Validation Loss'], loc='upper left')
          axes[1].plot(history.history['categorical_accuracy'])
          axes[1].plot(history.history['val_categorical_accuracy'])
          axes[1].set_xlabel('Epoch')
          axes[1].set ylabel('Categorical Accuracy')
          axes[1].set title('Model Epoch vs Categorical Accuracy')
          axes[1].legend(['Training Accuracy', 'Validation Accuracy'], loc='upper left'
          plt.show()
```

For LeNet-5 Model



What do you see from the plots? Are there signs of overfitting? If so, what are the signs and what techniques can we use to combat overfitting?

From the plot involving losses above, we can see that the training loss shows a downward trend till the end but the validation loss decreases till epoch 4 and starts increasing after that, albeit slowly. Also, from the plot involving accuracies (metric) above, we see that the training accuracies show an upward trend, but the validation accuracy plateaus after some epochs.

Signs of Overfitting:

- 1. As the Validation loss starts showing an upward trend while the training loss is going down (after the 4th epoch), this clearly shows that our model starts to overfit at the end.
- 2. As the Validation Accuracy increases but then plateaus and starts showing some downward trend while the training accuracy goes up, this also bolsters the fact that the model is surely overfitting.

Common techniques to prevent overfitting are Dropout and Batch Normalization

4.2.4 Report metric score on test set

4.3 Overfitting

4.3.1 Drop-out

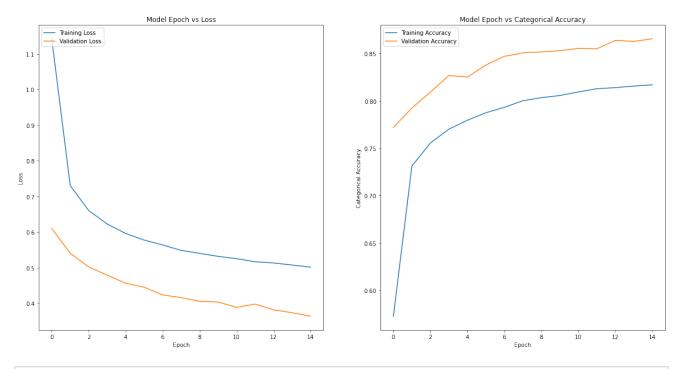
To overcome overfitting, we will train the network again with dropout this time. For hidden layers use dropout probability of 0.5. Train the model again for 15 epochs, use two plots to display train vs validation metric scores and train vs validation loss over each epoch. Report model performance on test set. What's your observation?

```
In [36]:
          # TODO: build the model with drop-out layers
          from tensorflow.keras.layers import Conv2D, MaxPooling2D, Dense, Flatten, Dro
          lenet5 model dropout = Sequential()
          lenet5 model dropout.add(Conv2D(filters = 6, kernel size = (5, 5),
                                          strides = (1, 1), padding = "same",
                                          activation = "relu",
                                          input_shape = (xtrain.shape[1],
                                                         xtrain.shape[1], 1)))
          lenet5 model dropout.add(MaxPooling2D((2, 2)))
          lenet5 model dropout.add(Dropout(0.5))
          lenet5_model_dropout.add(Conv2D(filters = 16, kernel_size = (5, 5),
                                          strides = (1, 1), padding = "valid",
                                          activation = "relu"))
          lenet5_model_dropout.add(MaxPooling2D((2, 2)))
          lenet5 model dropout.add(Dropout(0.5))
          lenet5_model_dropout.add(Conv2D(filters = 120, kernel_size = (5, 5),
                                          activation = "relu"))
          lenet5 model dropout.add(Flatten())
          lenet5 model dropout.add(Dropout(0.5))
          lenet5 model dropout.add(Dense(84, activation = "relu"))
          lenet5 model dropout.add(Dropout(0.5))
          # I am using Softmax function in the last layer
          lenet5_model_dropout.add(Dense(10, activation = "softmax"))
          lenet5 model dropout.build()
In [37]:
          # TODO: train the model
          from tensorflow.keras.losses import CategoricalCrossentropy
          from tensorflow.keras.optimizers import Adam
          from tensorflow.keras.metrics import CategoricalAccuracy
          lenet5_model_dropout.compile(loss = CategoricalCrossentropy(),
                        optimizer = Adam(learning rate = 1e-3),
                        metrics = [CategoricalAccuracy()])
          history = lenet5_model_dropout.fit(xtrain, ytrain, batch_size = 128, epochs =
```

```
Epoch 1/15
rical_accuracy: 0.5729 - val_loss: 0.6100 - val_categorical accuracy: 0.7719
Epoch 2/15
rical accuracy: 0.7313 - val loss: 0.5402 - val categorical accuracy: 0.7924
rical accuracy: 0.7555 - val loss: 0.5018 - val categorical accuracy: 0.8092
Epoch 4/15
rical accuracy: 0.7701 - val loss: 0.4788 - val categorical accuracy: 0.8267
Epoch 5/15
rical accuracy: 0.7795 - val loss: 0.4559 - val categorical accuracy: 0.8251
rical accuracy: 0.7875 - val loss: 0.4449 - val categorical accuracy: 0.8378
Epoch 7/15
rical accuracy: 0.7932 - val loss: 0.4233 - val categorical accuracy: 0.8470
Epoch 8/15
375/375 [=============] - 2s 5ms/step - loss: 0.5483 - catego
rical accuracy: 0.8001 - val loss: 0.4156 - val categorical accuracy: 0.8507
Epoch 9/15
rical accuracy: 0.8034 - val loss: 0.4052 - val categorical accuracy: 0.8516
Epoch 10/15
rical accuracy: 0.8056 - val_loss: 0.4033 - val_categorical_accuracy: 0.8529
Epoch 11/15
rical accuracy: 0.8094 - val loss: 0.3882 - val categorical accuracy: 0.8553
Epoch 12/15
rical accuracy: 0.8128 - val_loss: 0.3975 - val_categorical_accuracy: 0.8549
Epoch 13/15
rical accuracy: 0.8139 - val loss: 0.3812 - val categorical accuracy: 0.8638
Epoch 14/15
rical accuracy: 0.8156 - val loss: 0.3732 - val categorical accuracy: 0.8627
Epoch 15/15
rical accuracy: 0.8169 - val loss: 0.3635 - val categorical accuracy: 0.8655
```

```
In [38]:
          # TODO: plot
          plt.rcParams["figure.figsize"] = (20, 10)
          figure , axes = plt.subplots(1, 2)
          figure.suptitle("For LeNet-5 Model with Dropout")
          axes[0].plot(history.history['loss'])
          axes[0].plot(history.history['val loss'])
          axes[0].set xlabel('Epoch')
          axes[0].set_ylabel('Loss')
          axes[0].set title('Model Epoch vs Loss')
          axes[0].legend(['Training Loss', 'Validation Loss'], loc='upper left')
          axes[1].plot(history.history['categorical_accuracy'])
          axes[1].plot(history.history['val_categorical_accuracy'])
          axes[1].set_xlabel('Epoch')
          axes[1].set ylabel('Categorical Accuracy')
          axes[1].set title('Model Epoch vs Categorical Accuracy')
          axes[1].legend(['Training Accuracy', 'Validation Accuracy'], loc='upper left'
          plt.show()
```

For LeNet-5 Model with Dropout



```
In [39]: # TODO: Report model performance on test set
    results = lenet5_model_dropout.evaluate(xtest, ytest)
    print(f"Loss on Test Set: {results[0]}")
    print(f"Categorical Accuracy on Test Set are: {results[1]}")
```

What's your observation?

Answer: Depending on the loss curve above, the trend for the validation loss is a downward one and at the same time the training loss decreases as well.

Also, depending on the accuracy curve above, the trend for the validation accuracy is a upward one, and the training accuracy is also increasing continuously till the end. Interestingly, we can also see that initially, the training accuracy increases more rapidly as compared to before.

From the analysis above, it's clear that our model is not overfitting in this case. However, the accuracy for the lenet-5 model has decreased by 88.279 - 85.549 = 2.73% in comparison to the original lenet-5 model. This can be considered as a significant accuracy drop and might be attributed to the fact that we are not overfitting at all but we have lost

4.3.2 Batch Normalization

accuracy points.

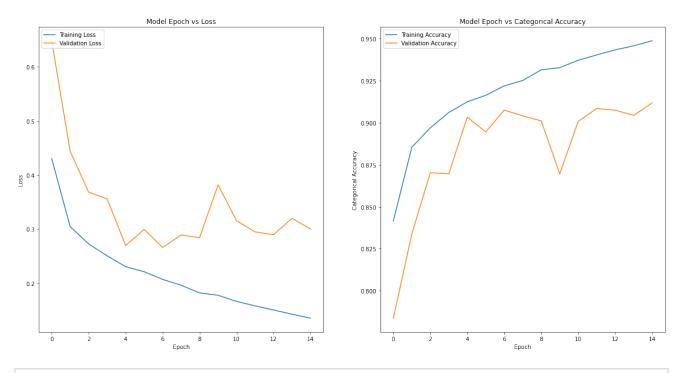
This time, let's apply a batch normalization after every hidden layer, train the model for 15 epochs, plot the metric scores and loss values, and report model performance on test set as above. Compare this technique with the original model and with dropout, which technique do you think helps with overfitting better?

```
In [40]:
          # TODO: build the model with batch normalization layers
          from tensorflow.keras.layers import Conv2D, MaxPooling2D, Dense, Flatten, Bat
          lenet5_model_bn = Sequential()
          lenet5 model bn.add(Conv2D(filters = 6, kernel size = (5, 5),
                           strides = (1, 1), padding = "same",
                           input shape = (xtrain.shape[1], xtrain.shape[1], 1)))
          lenet5 model bn.add(Activation("relu"))
          lenet5 model bn.add(MaxPooling2D((2, 2)))
          lenet5 model bn.add(BatchNormalization())
          lenet5 model bn.add(Conv2D(filters = 16, kernel size = (5, 5),
                           strides = (1, 1), padding = "valid"))
          lenet5 model bn.add(Activation("relu"))
          lenet5_model_bn.add(MaxPooling2D((2, 2)))
          lenet5_model_bn.add(BatchNormalization())
          lenet5 model bn.add(Conv2D(filters = 120, kernel size = (5, 5)))
          lenet5_model_bn.add(Activation("relu"))
          lenet5 model bn.add(Flatten())
          lenet5 model bn.add(BatchNormalization())
          lenet5 model bn.add(Dense(84))
          lenet5 model bn.add(Activation("relu"))
          lenet5 model bn.add(BatchNormalization())
          # I am using Softmax function in the last layer
          lenet5_model_bn.add(Dense(10, activation = "softmax"))
          lenet5 model bn.build()
In [41]:
          # TODO: train the model
          from tensorflow.keras.losses import CategoricalCrossentropy
          from tensorflow.keras.optimizers import Adam
          from tensorflow.keras.metrics import CategoricalAccuracy
          lenet5_model_bn.compile(loss = CategoricalCrossentropy(),
                        optimizer = Adam(learning rate = 1e-2),
                        metrics = [CategoricalAccuracy()])
          history = lenet5_model_bn.fit(xtrain, ytrain, batch_size = 128, epochs = 15,
```

```
Epoch 1/15
rical accuracy: 0.8416 - val loss: 0.6481 - val categorical accuracy: 0.7837
Epoch 2/15
rical accuracy: 0.8854 - val loss: 0.4439 - val categorical accuracy: 0.8338
rical accuracy: 0.8969 - val loss: 0.3681 - val categorical accuracy: 0.8702
Epoch 4/15
rical accuracy: 0.9061 - val loss: 0.3558 - val categorical accuracy: 0.8696
Epoch 5/15
rical accuracy: 0.9124 - val loss: 0.2695 - val categorical accuracy: 0.9032
rical accuracy: 0.9163 - val loss: 0.2992 - val categorical accuracy: 0.8945
Epoch 7/15
rical accuracy: 0.9219 - val loss: 0.2659 - val categorical accuracy: 0.9075
Epoch 8/15
375/375 [==============] - 2s 5ms/step - loss: 0.1961 - catego
rical accuracy: 0.9251 - val loss: 0.2891 - val categorical accuracy: 0.9040
Epoch 9/15
rical accuracy: 0.9314 - val_loss: 0.2840 - val_categorical_accuracy: 0.9011
Epoch 10/15
rical accuracy: 0.9327 - val_loss: 0.3818 - val_categorical_accuracy: 0.8695
Epoch 11/15
rical accuracy: 0.9371 - val loss: 0.3153 - val categorical accuracy: 0.9007
Epoch 12/15
rical accuracy: 0.9403 - val_loss: 0.2948 - val_categorical_accuracy: 0.9084
Epoch 13/15
rical accuracy: 0.9433 - val loss: 0.2896 - val categorical accuracy: 0.9074
Epoch 14/15
rical accuracy: 0.9457 - val loss: 0.3198 - val categorical accuracy: 0.9043
Epoch 15/15
rical accuracy: 0.9487 - val loss: 0.3001 - val categorical accuracy: 0.9118
```

```
In [42]:
          # TODO: plot
          plt.rcParams["figure.figsize"] = (20, 10)
          figure , axes = plt.subplots(1, 2)
          figure.suptitle("For LeNet-5 Model with Batch Normalization")
          axes[0].plot(history.history['loss'])
          axes[0].plot(history.history['val loss'])
          axes[0].set xlabel('Epoch')
          axes[0].set ylabel('Loss')
          axes[0].set title('Model Epoch vs Loss')
          axes[0].legend(['Training Loss', 'Validation Loss'], loc='upper left')
          axes[1].plot(history.history['categorical_accuracy'])
          axes[1].plot(history.history['val_categorical_accuracy'])
          axes[1].set_xlabel('Epoch')
          axes[1].set ylabel('Categorical Accuracy')
          axes[1].set title('Model Epoch vs Categorical Accuracy')
          axes[1].legend(['Training Accuracy', 'Validation Accuracy'], loc='upper left'
          plt.show()
```

For LeNet-5 Model with Batch Normalization



```
In [43]:
# TODO: Report model performance on test set
results = lenet5_model_bn.evaluate(xtest, ytest)
print(f"Loss on Test Set: {results[0]}")
print(f"Categorical Accuracy on Test Set are: {results[1]}")
```

Observation, comparison with Dropout:

Answer: As we can see above, the plot for the losses shows the validation loss with a generic downward trend with some spikes and increases a little at the end (showing an upward trend), while the training loss shows a strong downward trend till the end. Also, from the accuracy curves, we can see that the validation accuracy plateaus at the end while the training accuracy shows a strong upward trend. Also, as the accuracy for the model with batch normalization (90.219%) has increased from the lenet-5 model (88.279%). This shows us that the model with batch normalization performs quite better in comparison to the original lenet model and also the model with dropout. However, this model overfits a lot. Furthermore, the accuracy is 90.219% which is quite larger, albeit a little, with that of the original lenet model which has an accuracy of 88.279%. Also, the accuracy for the model with batch normalization is more than the accuracy for the model with dropout.

Looking at the trends and the performance metric, we can deduce that the model with batch normalization helps little with overfitting in comparison to the dropout in this case. Although, this model (with BN) reaches the highest accuracy but overfits a lot. Thus, the model with dropout in this case helps us in preventing the overfitting of the model (better than batch normalization) but at the cost of the accuracy drop.

PLEASE NOTE: I went to Angad's OH and I asked him the same and he suggested me to do the Dropout and Batch Normalization in this way. Thank You!