

Correctness of Selection Sort: (By loop invariant)

Initialization

At the beginning of the i th iteration of outer loop, the subarray contains $i-1$ elements of the original array in sorted order i.e. $A[1 \dots i-1]$ in sorted order.

Initialization:

Before the first iteration where $i=1$, we have the subarray $A[1 \dots i-1]$ is empty. The loop invariant holds trivially, before the first iteration of the loop.

Maintenance: Now, we tackle the second property: showing that each iteration maintains the loop invariant. Let's assume that our loop invariant holds at the beginning of the i th iteration.

$\Rightarrow A[1 \dots i-1]$ contains the $i-1$ elements in sorted order.

\Rightarrow In the i th iteration:

- The inner loop finds the minimum element index in the unsorted portion.
- And the minimum element is swapped with $arr[i]$ and now $A[1 \dots i]$ contains the i elements in sorted order and the loop invariant is maintained.

Termination: Now, we examine what happens when the loop terminates.

\Rightarrow The outer loop terminates when i reaches n where n is length of array.

\Rightarrow The loop invariant states that $A[1 \dots n]$ elements are sorted which represent our entire array.

Hence the algorithm is correct.