

Assignment - 4

Iteration - 1 sample - 1

x_i	y_i
7.6	157
7.1	174

Step 1: $[7.6, 157]$, $\eta = 0.01$, $m = 1$, $c = -1$

Step 2: $\frac{\partial E}{\partial m} \Big|_{m=1} = -(y_i^a - mx_i^a - c)(-x_i^a)$
 $= (157 - 7.6 - (-1))(7.6)$
 $= (150.4)(7.6)$
 $= 1143.04$

$$\frac{\partial E}{\partial c} \Big|_{c=-1} = -(y_i^a - mx_i^a - c)$$
$$= -(157 - (1)(7.6) - (-1))$$
$$= -(158 - 7.6) = -150.4$$

Step 3: $\Delta m = -\eta \frac{\partial E}{\partial m} = -(0.01)(1143.04)$
 $= -11.430$

$$\Delta c = -\eta \frac{\partial E}{\partial c} = -(0.01)(-150.4)$$
$$= 1.504$$

Step 4: $m = m + \Delta m = 1 + (-11.43)$
 $= -10.43$

$$c = c + \Delta c = -1 + (1.504)$$
$$= 0.504$$

Iteration - 2

Step 1: $[7.6, 157]$, $\eta = 0.01$, $m = -10.43$, $c = 0.504$

Step 2: $\frac{\partial E}{\partial m} \Big|_{m=-10.43} = (157 + (10.43)(7.6) - 0.504)(7.6)$

$$= (156.496 + 79.372)(7.61)$$

$$= 1794.955$$

$$\left. \frac{\partial E}{\partial c} \right|_c = 0.504 = -(157 - (-10.43)(7.61) - 0.84)$$

$$= -235.868$$

$$\text{Step 3: } \Delta m = -\eta \frac{\partial E}{\partial c} = (-0.01 \times 1794.955) = -17.949$$

$$\Delta c = -\eta \frac{\partial E}{\partial c} = (-0.01)(-235.868)$$

$$= 2.358$$

$$\text{Step 4: } m = m + \Delta m = -10.43 + (-17.943)$$

$$= -28.379$$

$$c = c + \Delta c = 0.504 + 2.358$$

$$= 2.862$$

Sample-2 Iteration 1.

$$\text{Step 1: } (7.1, 174) \quad \eta = 0.01, m = 1, c = 1$$

$$\text{Step 2: } \left. \frac{\partial E}{\partial m} \right|_{m=1} = -(y_i^a - mx_i^a - c) - x_i^a$$

$$= (174 - (7.1) - (-1)) + 7.1$$

$$= (175 - 7.1)(7.1)$$

$$\left. \frac{\partial E}{\partial c} \right|_{c=1} = -(y_i^a - mx_i^a - c)$$

$$= -(174 - (7.1)) - (-1)$$

$$= -167.9$$

$$\text{Step 3: } \Delta m = -\eta \frac{\partial E}{\partial m} = -(0.01) 1192.09$$

$$= -11.920$$

$$\Delta c = -\eta \frac{\partial E}{\partial c} = -(0.01)(-167.9)$$

$$= 1.679$$

$$\text{Step 4: } m = m + \Delta m = 1 + (-11.920) = -10.920$$

$$c = c + \Delta c = -1 + 1.679 = 0.679$$

Iteration -2:

$$\text{Step 1: } [7.1, 174] \quad \eta = 0.01, \quad m = -10.92, \quad c = 0.679$$

$$\begin{aligned} \text{Step 2: } \frac{\partial E}{\partial m} \Big|_m &= -10.92 = (174 - (-10.92)(7.1) - 0.679(7.1)) \\ &= (173.321 + (10.92 + 7.1))(7.3) \\ &= 1781.056 \end{aligned}$$

$$\begin{aligned} \frac{\partial E}{\partial c} \Big|_c &= 0.679 = -(174 - (-10.92)(7.1) - 0.679(7.1)) \\ &= -250.853 \end{aligned}$$

$$\begin{aligned} \text{Step 3: } \Delta m &= -\eta \frac{\partial E}{\partial m} = (-0.01) \times (1781.056) \\ &= -17.810 \end{aligned}$$

$$\begin{aligned} \Delta c &= -\eta \frac{\partial E}{\partial c} = -(0.01)(-250.853) \\ &= 2.508 \end{aligned}$$

$$\begin{aligned} \text{Step 4: } m &= m + \Delta m = -10.92 - 17.81 \\ &= -28.73 \end{aligned}$$

$$\begin{aligned} c &= c + \Delta c = 0.679 + 2.508 \\ &= 3.187 \end{aligned}$$