

# Banker's Algorithm

Scenario:

Process	Allocation			Max			Available			Need		
	A	B	C	A	B	C	A	B	C	A	B	C
P <sub>0</sub>	0	1	0	7	5	3	3	3	2	7	4	3
P <sub>1</sub>	2	0	0	3	2	2				1	2	2
P <sub>2</sub>	3	0	2	9	0	2				6	0	0
P <sub>3</sub>	2	1	1	2	2	2				0	1	1
P <sub>4</sub>	0	0	2	4	3	3				4	3	1

$$\text{Work} = \text{Available} = [3 \ 3 \ 2]$$

Finish[i] = false for  $i = 0, 1, \dots, n-1$

$$\text{Finish}[0] = \text{false}$$

$$\text{Need}_0 = [7 \ 4 \ 3] \leq [\overset{\text{Work}}{3 \ 3 \ 2}] \quad \text{false}$$

$$\text{Need}_1 = [1 \ 2 \ 2] \leq [3 \ 3 \ 2] \quad \text{True} \checkmark$$

$$\# \text{Work} = \text{Work} + \text{Allocation}_1$$

$$= [3 \ 3 \ 2] + [2 \ 0 \ 0]$$

$$= [5 \ 3 \ 2]$$

$$\text{Finish}_1 = \text{True}$$

$$\text{Need}_2 = [6 \ 0 \ 0] \leq [5 \ 3 \ 2] \quad \text{false}$$

$$\text{Need}_3 = [0 \ 1 \ 1] \leq [5 \ 3 \ 2] \quad \text{True} \checkmark$$

$$\text{Work} = \text{Work} + \text{Allocation}_3$$

$$= [5 \ 3 \ 2] + [2 \ 1 \ 1]$$

$$= [7 \ 4 \ 3]$$

$$\text{Need}_4 = [4 \ 3 \ 1] \leq \begin{matrix} \text{Work} \\ [7 \ 4 \ 3] \end{matrix} \text{ True}$$

$$\text{Work} = \text{Work} + \text{Allocation}_4$$

$$= [7 \ 4 \ 3] + [0 \ 0 \ 2]$$

$$= [7 \ 4 \ 5]$$

$$\text{Finish}[4] = \text{True}$$

$$\text{Need}_2 = [6 \ 0 \ 0] \leq \begin{matrix} \text{Work} \\ [7 \ 4 \ 5] \end{matrix} \text{ True}$$

$$\text{Work} = \text{Work} + \text{Allocation}_2$$

$$= [7 \ 4 \ 5] + [3 \ 0 \ 2]$$

$$= [10 \ 4 \ 7]$$

$$\text{Finish}[2] = \text{True}$$

$$\text{Need}_0 = [7 \ 4 \ 3] \leq \begin{matrix} \text{Work} \\ [10 \ 4 \ 7] \end{matrix} \text{ True}$$

$$\text{Work} = \text{Work} + \text{Allocation}_0$$

$$= [10 \ 4 \ 7] + [0 \ 1 \ 0]$$

$$= [10 \ 5 \ 7]$$

$$\text{Finish}[0] = \text{True}$$

$$\text{Finish}[i] = \text{True}, \text{ for } i = 0 \text{ to } 4$$

Hence there is a safe sequence.

The safe sequence is  $\langle P_1, P_3, P_4, P_2, P_0 \rangle$

Hence the system is in a safe state.

Now, suppose process  $P_1$  requests one additional instance of resource type A and two instances of resource type C.

$$\text{Request}_1 = (1, 0, 2)$$

Check whether this request can be granted.  
To check this, use the resource request algorithm.

$$\text{Request}_i \leq \text{Need}$$

$$[1 \ 0 \ 2] \leq [1 \ 2 \ 2] \quad \text{True}$$

$$\text{Request}_i \leq \text{Available}$$

$$[1 \ 0 \ 2] \leq [3 \ 3 \ 2] \quad \text{True}$$

Pretend that the request is granted

$$\begin{aligned} \text{Available}_i &= \text{Available} - \text{Request}_i \\ &= [3 \ 3 \ 2] - [1 \ 0 \ 2] \\ &= [2 \ 3 \ 0] \end{aligned}$$

$$\begin{aligned} \text{Allocation}_i &= \text{Allocation}_i + \text{Request}_i \\ &= [2 \ 0 \ 0] + [1 \ 0 \ 2] \\ &= [3 \ 0 \ 2] \end{aligned}$$

$$\begin{aligned} \text{Need}_i &= \text{Need}_i - \text{Request}_i \\ &= [1 \ 2 \ 2] - [1 \ 0 \ 2] \\ &= [0 \ 2 \ 0] \end{aligned}$$

The state of the system becomes like this

Process	Allocation			Max			Available			Need		
	A	B	C	A	B	C	A	B	C	A	B	C
P <sub>0</sub>	0	1	0	7	4	3	2	3	0	7	4	3
P <sub>1</sub>	3	0	2	0	2	0				0	2	0
P <sub>2</sub>	3	0	2	6	0	0				6	0	0
P <sub>3</sub>	2	1	1	0	1	1				0	1	1
P <sub>4</sub>	0	0	2	4	3	1				4	3	1

Now apply the safety algorithm

$$\text{Work} = \text{Available} = [2 \ 3 \ 0]$$

$$\text{Finish}[i] = \text{False, for } i = 0, 1, 2, \dots, 4$$

$$\text{Finish}[0] = \text{False}$$

$$\text{Need}_0 = [7 \ 4 \ 3] \leq [2 \ 3 \ 0] \quad \text{false}$$

$$\text{Finish}[1] = \text{false}$$

$$\text{Need}_1 = [0 \ 2 \ 0] \leq [2 \ 3 \ 0] \text{ True } \checkmark$$

$$\text{Work} = [2 \ 3 \ 0] + [3 \ 0 \ 2]$$

$$= [5 \ 3 \ 2]$$

$$\text{Finish}[1] = \text{True}$$

$$\text{Need}_2 = [6 \ 0 \ 0] \leq [5 \ 3 \ 2] \text{ false}$$

$$\text{Finish}[3] = \text{false}$$

$$\text{Need}_3 = [0 \ 1 \ 1] \leq [5 \ 3 \ 2] \text{ True } \checkmark$$

$$\text{Work} = [5 \ 3 \ 2] + [2 \ 1 \ 1] = [7 \ 4 \ 3]$$

$$\text{Finish}[3] = \text{True}$$

$$\text{Finish}[4] = \text{false}$$

$$\text{Need}_4 = [4 \ 3 \ 1] \leq [7 \ 4 \ 3] \text{ True } \checkmark$$

$$\text{Work} = [7 \ 4 \ 3] + [0 \ 0 \ 2]$$

$$= [7 \ 4 \ 5]$$

$$\text{Finish}[4] = \text{True}$$

$$\text{Finish}[0] = \text{false}$$

$$\text{Need}_0 = [7 \ 4 \ 3] \leq [7 \ 4 \ 5] \text{ True } \checkmark$$

$$\text{Work} = [7 \ 4 \ 5] + [0 \ 1 \ 0]$$

$$= [7 \ 5 \ 5]$$

$$\text{Finish}[0] = \text{True}$$

$$\text{Need}_2 = [6 \ 0 \ 0] \leq [7 \ 5 \ 5] \text{ True } \checkmark$$

$$\text{Work} = [7 \ 5 \ 5] + [3 \ 0 \ 2]$$

$$= [10 \ 5 \ 7]$$

$$\text{Finish}[2] = \text{True}$$

Safe sequence is  $\langle P_1, P_3, P_4, P_0, P_2 \rangle$

Hence the system will be in a safe state.

Hence the request can be granted.