

## Unit = 3

### 1. Structure of a Wireless Communication Link

A **wireless communication link** is the path through which information travels from a **transmitter** to a **receiver** over the air. It's more complex than a wired link due to **fading, noise, interference, and mobility**.

#### Basic Components:

##### 1. Transmitter

- Converts the information signal (voice, data, video) into a suitable form for transmission.
- Components include:
  - **Source encoder:** Compresses and formats data.
  - **Channel encoder:** Adds redundancy for error correction.
  - **Modulator:** Maps bits to signal waveforms (e.g., QPSK, MSK).
- Example: In a mobile phone, the microphone signal is digitized, encoded, and modulated.

##### 2. Channel

- The medium through which the signal propagates. In wireless, this is **air**.
- Characteristics:
  - **Path loss:** Signal power decreases with distance.
  - **Shadowing:** Signal blocked or attenuated by obstacles.
  - **Fading:** Rapid fluctuations in amplitude/phase due to multipath propagation.
    - **Flat fading:** All frequencies affected equally.
    - **Frequency-selective fading:** Different frequencies affected differently.
  - **Noise and interference:** Thermal noise, other transmissions.

##### 3. Receiver

- Converts the received waveform back into the original information.
- Components include:

- **Demodulator:** Extracts the transmitted symbols from the waveform.
  - **Channel decoder:** Corrects errors introduced by noise/fading.
  - **Source decoder:** Reconstructs the original data (voice, text, video).
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### Flow of a Wireless Link:

Information → Source Encoder → Channel Encoder → Modulator → Transmitter

→ Wireless Channel (fading, noise, interference)

→ Receiver → Demodulator → Channel Decoder → Source Decoder → Information

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### Challenges in Wireless Communication:

1. **Fading** – Causes signal fluctuations; needs techniques like diversity, equalization, or adaptive modulation.
  2. **Interference** – Signals from other users degrade performance.
  3. **Noise** – Adds random errors; affects BER (Bit Error Rate).
  4. **Doppler Effect** – Relative motion between transmitter and receiver changes frequency.
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### Summary:

The wireless communication link is a chain: **Transmitter → Channel → Receiver**, with **fading, noise, and interference** being the main challenges. Proper modulation, coding, and diversity techniques help maintain reliable communication.

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## 2. Principles of Offset-QPSK (OQPSK)

**Offset Quadrature Phase Shift Keying (OQPSK)** is a type of **phase modulation** used in digital communication to improve performance in fading channels.

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### Basic Concept:

- **QPSK (Quadrature Phase Shift Keying):** Transmits 2 bits per symbol by shifting the phase of a carrier among 4 values ( $0^\circ$ ,  $90^\circ$ ,  $180^\circ$ ,  $270^\circ$ ).
- **Problem with QPSK:** Phase can jump by  $180^\circ$  instantaneously, causing large amplitude fluctuations. This is a problem for **non-linear amplifiers**.

**OQPSK solves this problem** by **offsetting the timing of the in-phase (I) and quadrature (Q) signals by half a symbol period ( $T/2$ )**.

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### How It Works:

1. The data stream is split into **I (In-phase)** and **Q (Quadrature)** components.
  2. Q component is **delayed by  $T/2$** , where T is the symbol duration.
  3. Result: **No two bits change simultaneously**, so the **phase change is never  $180^\circ$** , only  $\pm 90^\circ$  at most.
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### Advantages of OQPSK:

- **Reduced amplitude fluctuations**  $\rightarrow$  less distortion in non-linear amplifiers.
  - **Better performance in fading channels** compared to standard QPSK.
  - **Widely used in mobile and satellite communication.**
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### Constellation Diagram:

- Standard QPSK: Points at  $0^\circ$ ,  $90^\circ$ ,  $180^\circ$ ,  $270^\circ$ ; abrupt jumps possible.
- OQPSK: Points are the same, but the **transitions are smoother** because only one component changes at a time.

I-axis: In-phase

Q-axis: Quadrature

Symbols change along one axis at a time → smoother transitions

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#### Summary:

- OQPSK is a **modified QPSK** to reduce sudden phase shifts.
  - Achieves **better power efficiency** and **less distortion**.
  - Common in **satellite links, GSM, and other wireless systems**.
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### 3. $\pi/4$ -DQPSK ( $\pi/4$ -Differential QPSK)

$\pi/4$ -DQPSK is a **phase modulation technique** used in wireless communication that combines **differential encoding** with **QPSK**, but with a  **$\pi/4$  phase shift** to improve performance in fading channels.

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#### Basic Concept:

1. **QPSK:** Transmits 2 bits per symbol using 4 possible phases ( $0^\circ$ ,  $90^\circ$ ,  $180^\circ$ ,  $270^\circ$ ).
  2. **Problem with QPSK:** Phase transitions can be abrupt (up to  $180^\circ$ ), leading to signal amplitude fluctuations.
  3. **Solution ( $\pi/4$ -DQPSK):**
    - Introduces a  **$\pi/4$  ( $45^\circ$ ) offset between successive constellations**.
    - Each symbol is **differentially encoded** with respect to the previous symbol.
    - Maximum phase change is  **$\pm 135^\circ$**  instead of  $180^\circ$ , which **reduces envelope variations**.
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#### Differential Encoding:

- Instead of encoding the absolute phase, the **change in phase** from the previous symbol represents the data.

- This allows the receiver to **detect data without exact carrier phase reference**, making it **robust to phase shifts in fading channels**.
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#### Constellation Diagram:

- Uses **two QPSK constellations**, rotated by  $\pi/4$  (**45°**) relative to each other.
- Symbols alternate between these constellations, making **phase transitions smoother**.

Constellation 1: 0°, 90°, 180°, 270°

Constellation 2: 45°, 135°, 225°, 315°

- Only **one axis changes at a time**, reducing sudden amplitude changes.
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#### Advantages of $\pi/4$ -DQPSK:

1. **Reduced amplitude fluctuations** → better for non-linear power amplifiers.
  2. **Differential detection** → avoids the need for exact phase synchronization.
  3. **Better performance in fading channels** than standard QPSK.
  4. Commonly used in **GSM mobile communication**.
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#### Summary:

- $\pi/4$ -DQPSK = **Differential QPSK +  $\pi/4$  rotation**.
  - Smooth transitions, lower amplitude variations, robust in fading channels.
  - Ideal for **mobile and wireless communication systems**.
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## 4. Minimum Shift Keying (MSK)

**MSK** is a type of **continuous phase frequency shift keying (CPFSK)** that is **highly spectrally efficient** and commonly used in digital wireless communications.

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### Basic Concept:

#### 1. Frequency Shift Keying (FSK):

- Represents digital data by **changing the frequency** of the carrier signal.
- Binary FSK uses two frequencies for 0 and 1.

#### 2. MSK Characteristics:

- Special case of **binary FSK** where the **frequency separation ( $\Delta f$ ) =  $1 / (2T)$** , where **T = symbol duration**.
  - This is the **minimum frequency spacing** to maintain **orthogonality** between symbols → hence the name **Minimum Shift Keying**.
  - Ensures **continuous phase transitions**, reducing sudden changes in the signal.
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### Mathematical Representation:

The MSK signal can be written as:

$$s(t) = \sqrt{\frac{2E_b}{T}} \cos[2\pi f_c t + \phi(t)]$$
$$s(t) = \sqrt{\frac{2E_b}{T}} \cos[2\pi f_c t + \phi(t)]$$

Where:

- $f_c$  = carrier frequency
  - $E_b$  = energy per bit
  - $\phi(t)$  = continuous phase term
  - Phase continuity ensures **smooth transitions** between symbols.
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### Key Features of MSK:

#### 1. Constant envelope:

- Amplitude does not change, suitable for **non-linear power amplifiers**.

## 2. Continuous phase:

- Phase changes **gradually**, reducing spectral side lobes.

## 3. Spectral efficiency:

- Bandwidth =  $1.5/T$  (narrower than standard FSK).

## 4. Error performance:

- Similar to QPSK in **AWGN channels**.
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### Waveform of MSK:

- MSK can be seen as **OQPSK with sinusoidal pulse shaping**.
  - In the I-Q plane:
    - I and Q components are **offset by  $T/2$** , like OQPSK.
    - Each bit corresponds to a **half-cycle of a sine wave**.
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### Advantages of MSK:

- **High spectral efficiency** → fits more data in a given bandwidth.
  - **Good power efficiency** → constant envelope allows use of non-linear amplifiers.
  - **Smooth waveform** → less interference with adjacent channels.
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### Applications:

- GSM mobile communication (precursor to GMSK)
  - Satellite and military communications
  - Low-power wireless devices
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### ✅ Summary:

MSK is a **continuous phase, minimum frequency shift keying** scheme. It's **power-efficient, spectrally efficient, and smooth**, making it ideal for fading channels and non-linear amplifiers.

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## 5. Gaussian Minimum Shift Keying (GMSK)

**GMSK** is an **enhanced version of MSK** where the data signal is **shaped by a Gaussian filter** before frequency modulation. It is widely used in **GSM mobile communication**.

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### Basic Concept:

#### 1. MSK recap:

- MSK is a continuous-phase FSK with minimum frequency spacing.
- Smooth phase transitions → constant envelope → efficient for non-linear amplifiers.

#### 2. Enhancement in GMSK:

- MSK is passed through a **Gaussian low-pass filter** before modulation.
- Gaussian filter **reduces the signal bandwidth**, making it **more spectrally efficient**.

#### 3. Key idea:

- Smooth transitions in phase and **bandwidth limitation** → lower interference with adjacent channels.
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### Mathematical Representation:

$$s(t) = \sqrt{\frac{2E_b}{T}} \cos \left[ 2\pi f_c t + 2\pi h \int_0^t m(\tau) d\tau \right]$$
$$s(t) = \sqrt{\frac{2E_b}{T}} \cos \left[ 2\pi f_c t + 2\pi h \int_0^t m(\tau) d\tau \right]$$

Where:

- $m(t)$  = filtered digital data (after Gaussian shaping)
  - $h = 0.5$  for MSK/GMSK
  - Gaussian filter **reduces high-frequency components**, lowering side lobes.
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### Key Features of GMSK:

#### 1. Constant envelope:

- Can use **non-linear power amplifiers** → energy efficient.

#### 2. Bandwidth-efficient:



- Gaussian filter compresses spectrum → **narrow bandwidth**.

### 3. Continuous phase:

- Smooth phase transitions → lower interference.

### 4. Parameter BT (Bandwidth × Time):

- Determines **filter width**:
  - Small BT → narrower bandwidth, smoother signal, slightly slower rise time.
  - Typical GSM value: **BT = 0.3**.

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### Advantages:

- **High spectral efficiency** → supports more channels in limited spectrum.
- **Power-efficient** → suitable for mobile phones with battery constraints.
- **Robust in fading channels** → good BER performance.

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### Applications:

- **GSM cellular systems** (most common)
- **Satellite communication**
- **Military and low-power wireless systems**

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### ✅ Summary:

GMSK = **MSK + Gaussian filtering**.

- Reduces bandwidth
  - Maintains constant amplitude
  - Smooth phase transitions
  - Widely used in GSM due to spectral and power efficiency.
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## 6. Error Performance in Fading Channels

In wireless communication, the **channel is not ideal**. Signals undergo **fading**, which affects their amplitude and phase, leading to errors. Understanding **error performance** is critical for designing reliable systems.

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### 1. Fading in Wireless Channels

**Fading** is the **variation of signal strength** over time or space due to **multipath propagation**.

Types of fading:

#### 1. Flat Fading

- Bandwidth of transmitted signal < channel coherence bandwidth.
- **All frequencies affected equally.**
- Causes **signal amplitude variations** → affects SNR and BER.

#### 2. Frequency-Selective Fading

- Bandwidth of transmitted signal > channel coherence bandwidth.
- **Different frequency components experience different fading.**
- Causes **inter-symbol interference (ISI)**.

#### 3. Slow vs. Fast Fading

- **Slow fading:** Channel changes slowly compared to symbol duration.
  - **Fast fading:** Channel changes quickly → rapid fluctuations within symbol duration.
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## 2. Error Performance Metrics

### 1. Bit Error Rate (BER)

- Probability that a received bit is incorrect.
- Depends on modulation type, SNR, and channel characteristics.

### 2. Symbol Error Rate (SER)

- Probability of a symbol being incorrectly detected.
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### 3. BER in Fading Channels

- Fading increases BER compared to **AWGN (Additive White Gaussian Noise) channels**.
- Example: For BPSK in Rayleigh fading:

• Example: For BPSK in Rayleigh fading:

$$P_b = \frac{1}{2} \left( 1 - \sqrt{\frac{\gamma}{1 + \gamma}} \right)$$

Where:

- $\gamma$  = average SNR per bit
- Rayleigh fading → no line-of-sight component
- BER for QPSK/MSK/OQPSK in fading channels is generally **worse than AWGN** because of random amplitude variations.

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### 4. Techniques to Improve Error Performance

#### 1. Diversity Techniques

- Use multiple antennas, frequencies, or time slots to **combat fading**.
- Types:
  - **Time diversity:** Repeat signal at different times
  - **Frequency diversity:** Transmit on different frequencies
  - **Spatial diversity:** Multiple antennas (MIMO)

#### 2. Equalization

- Compensates for **ISI caused by multipath**.

#### 3. Adaptive Modulation & Coding

- Modulation order and coding rate adapt according to **channel conditions**.

#### 4. Forward Error Correction (FEC)

- Adds redundancy to correct errors at the receiver.

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### Summary:

- **Fading** significantly affects wireless signal reliability.

- **BER in fading channels** is worse than in AWGN channels.
  - **Techniques like diversity, equalization, and adaptive coding** help improve error performance.
  - Understanding fading and error performance is essential for choosing **modulation schemes** like OQPSK, MSK, or GMSK.
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## 7. OFDM (Orthogonal Frequency Division Multiplexing) Principle

**OFDM** is a **multicarrier modulation technique** used to efficiently transmit data over **frequency-selective fading channels**. It is widely used in **4G, 5G, Wi-Fi, and LTE systems**.

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### Basic Concept:

#### 1. Problem with Single-Carrier Systems:

- In frequency-selective fading, different frequencies of the signal experience different attenuation.
- This causes **inter-symbol interference (ISI)** and limits data rates.

#### 2. OFDM Solution:

- Splits the high-rate data stream into **multiple low-rate streams**.
  - Each low-rate stream modulates a **separate subcarrier**.
  - Subcarriers are **orthogonal** to each other → no interference between them.
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### Key Features of OFDM:

#### 1. Orthogonality:

- Subcarriers are spaced such that **peak of one aligns with nulls of others**.
- Allows **overlapping in frequency** → high spectral efficiency.

#### 2. Parallel Transmission:

- Data is transmitted in **parallel** across multiple subcarriers.
- Reduces the **symbol rate** per subcarrier → mitigates ISI.

### 3. Robustness Against Fading:

- Frequency-selective fading affects only some subcarriers.
- Easy to recover data using **equalization**.

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#### Mathematical Representation:

- An OFDM signal with N subcarriers:

$$s(t) = \sum_{k=0}^{N-1} X_k \cos(2\pi f_k t)$$

Where:

- $X_k$  = symbol on k-th subcarrier
- $f_k$  = frequency of k-th subcarrier
- Subcarriers satisfy **orthogonality**:  $f_k = f_0 + k/T$

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#### Advantages of OFDM:

1. **ISI reduction** due to low symbol rate per subcarrier.
2. **Efficient bandwidth usage** due to overlapping subcarriers.
3. **Simple equalization** using frequency-domain techniques.
4. **Adaptable to channel conditions** → supports adaptive modulation per subcarrier.

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#### Applications:

- 4G LTE, 5G NR
  - Wi-Fi (IEEE 802.11a/g/n/ac)
  - Digital TV (DVB-T)
  - Power-line communications
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### ✓ Summary:

OFDM divides a high-rate data stream into **many low-rate substreams**, transmits them over **orthogonal subcarriers**, and is **highly robust against frequency-selective fading**.

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## 8. Cyclic Prefix (CP) in OFDM

**Cyclic Prefix (CP)** is a key technique in OFDM systems to **combat inter-symbol interference (ISI)** caused by **multipath propagation**.

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### Problem: Inter-Symbol Interference (ISI)

- In wireless channels, signals reflect from buildings, walls, and other objects → **multipath propagation**.
  - Multipath causes **delayed copies** of the transmitted symbol to arrive at the receiver.
  - If these delayed copies overlap with the next symbol, **ISI** occurs → errors in detection.
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### Solution: Cyclic Prefix

#### 1. Definition:

- A **cyclic prefix** is a **copy of the last part of an OFDM symbol**, prepended to the symbol before transmission.

#### 2. How it works:

- If the OFDM symbol is  $x[n]$  of length  $N$ , the last  $L$  samples are copied and added at the beginning.
- This ensures that **linear convolution with the channel becomes circular convolution**.
- Circular convolution allows **simple frequency-domain equalization** using FFT.

### 3. Length of CP:

- Must be **longer than the maximum delay spread** of the channel.
- Too short → ISI not fully eliminated
- Too long → **reduces spectral efficiency**

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#### Mathematical Illustration:

- Transmitted OFDM symbol with CP:

$$x_{CP}[n] = [x[N - L], x[N - L + 1], \dots, x[N - 1], x[0], x[1], \dots, x[N - 1]]$$

- At the receiver, after removing CP:

$$y[n] = h[n] * x[n] + noise$$

- Circular convolution ensures **simple division in frequency domain** for equalization.

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#### Advantages of Cyclic Prefix:

1. **ISI elimination** if  $CP \geq$  channel delay spread.
2. **Simplifies equalization** → FFT can recover transmitted symbols.
3. **Maintains orthogonality** of subcarriers.

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#### Disadvantages:

- Reduces **data rate** slightly (overhead from CP).
- Longer CP → more spectral inefficiency.

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#### Summary:

- **Cyclic Prefix = Guard interval** in OFDM to combat ISI.
  - Converts **linear convolution** → **circular convolution** → easy frequency-domain equalization.
  - Must be **longer than channel delay spread** to be effective.
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## 9. Windowing in OFDM

**Windowing** is a technique used in OFDM systems to **reduce spectral leakage** and **improve signal quality**.

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### Problem: Spectral Leakage

- OFDM uses **rectangular pulses** in time domain for each symbol.
  - Rectangular pulses have a **sinc-shaped spectrum**, which causes **side lobes** → interference with adjacent channels.
  - High side lobes reduce **spectral efficiency** and can violate regulatory limits.
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### Solution: Windowing

#### 1. Definition:

- Windowing multiplies the OFDM signal with a **smooth window function** (like Hanning, Hamming, or Raised Cosine) before transmission.

#### 2. How it Works:

- Smoothly ramps up and ramps down the symbol at the edges.
- Reduces abrupt transitions in time domain → **reduces side lobes in frequency domain**.

#### 3. Mathematical Representation:

- Let  $x[n]$  be an OFDM symbol of length  $N$ .
- Windowed signal:

$$x_w[n] = x[n] \cdot w[n], \quad 0 \leq n \leq N - 1$$

- Where  $w[n]$  = window function (e.g., Hanning, Hamming).
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### Common Window Functions:

#### Window Type    Characteristics

Hanning            Smooth, reduces side lobes significantly



## Window Type Characteristics

Hamming      Slightly higher main lobe, lower side lobes

Raised Cosine Controlled roll-off, widely used in OFDM

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### Advantages of Windowing:

1. **Reduces spectral leakage** → less interference to adjacent channels.
  2. **Improves signal quality** → lower bit error rate.
  3. **Maintains orthogonality** of subcarriers.
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### Disadvantages:

- Slight **increase in symbol duration** → reduces throughput slightly.
  - **Additional complexity** in implementation.
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### Summary:

- Windowing is used to **smooth OFDM symbol edges**, reducing **side lobes** in the frequency domain.
  - Improves **spectral efficiency** and **signal quality**, making it essential for practical OFDM systems.
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## 10. PAPR (Peak-to-Average Power Ratio) in OFDM

**PAPR** is a critical parameter in OFDM systems that measures the **ratio of the peak power to the average power** of the transmitted signal.

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### Problem: High PAPR in OFDM

- OFDM combines **many subcarriers** in the time domain.
  - When multiple subcarriers **constructively add**, the instantaneous signal power can become very high.
  - This leads to **high PAPR**, causing issues like:
    1. **Non-linear distortion** in power amplifiers.
    2. **Reduced power efficiency**.
    3. Increased **out-of-band radiation**.
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#### Definition:

$$\text{PAPR} = \frac{P_{\text{peak}}}{P_{\text{avg}}} = \frac{\max |x(t)|^2}{\mathbb{E}[|x(t)|^2]}$$

Where:

- $x(t)$  = OFDM signal in time domain
- $P_{\text{peak}}$  = maximum instantaneous power
- $P_{\text{avg}}$  = average signal power
- PAPR is usually expressed in **dB**:

$$\text{PAPR(dB)} = 10 \log_{10} \frac{P_{\text{peak}}}{P_{\text{avg}}}$$

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### Why PAPR is a Problem

- High PAPR requires **linear amplifiers with large dynamic range**.
- Linear amplifiers are **less power-efficient**, which is critical for **battery-powered devices**.
- Non-linear amplifiers cause **signal distortion** → higher **BER**.

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## Techniques to Reduce PAPR

### 1. Clipping and Filtering:

- Clip peaks of the signal → reduces PAPR, but may cause **in-band distortion**.

### 2. Coding Techniques:

- Special codes reduce peak occurrences in the OFDM signal.

### 3. Selective Mapping (SLM):

- Generate multiple versions of OFDM symbols → choose the one with **lowest PAPR**.

### 4. Partial Transmit Sequence (PTS):

- Divide OFDM symbol into sub-blocks → phase rotate to reduce PAPR.

### 5. Tone Reservation / Tone Injection:

- Reserve certain subcarriers or inject signals to **cancel peaks**.

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## Summary:

- **PAPR** measures the ratio of the **highest peak power to average power** in OFDM.
- High PAPR is a major issue for **power efficiency and amplifier linearity**.
- **Techniques like clipping, coding, and SLM** help reduce PAPR in practical OFDM systems.