

Assignment 02-QMM

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The Problem has been solved under the following basis.

1. Objective

Maximize the profit = $(420 \times y_{\text{no of Large}}) + (360 \times y_{\text{no of Medium}}) + (300 \times y_{\text{no of small}})$

2. Constraints and Assumptions

Capacity constraints (per plant) - Each plant has a maximum capacity

- Plant 1: $y_{\text{Large}} + y_{\text{Medium}} + y_{\text{Small}} \leq 750$
- Plant 2: $y_{\text{Large}} + y_{\text{Medium}} + y_{\text{Small}} \leq 900$
- Plant 3: $y_{\text{Large}} + y_{\text{Medium}} + y_{\text{Small}} \leq 450$

Storage constraints - Storage space per plant

- $20 \times y_{\text{Large}} + 15 \times y_{\text{Medium}} + 12 \times y_{\text{Small}} \leq 13,000$ for Plant 01
- $20 \times y_{\text{Large}} + 15 \times y_{\text{Medium}} + 12 \times y_{\text{Small}} \leq 12,000$ for Plant 02
- $20 \times y_{\text{Large}} + 15 \times y_{\text{Medium}} + 12 \times y_{\text{Small}} \leq 5,000$ for Plant 03

Sales constraints - The maximum number of each size that can be sold

- $y_{\text{Large plant 1}} + y_{\text{Large plant 2}} + y_{\text{Large plant 3}} \leq 900$ for large
- $y_{\text{Medium plant 1}} + y_{\text{Medium plant 2}} + y_{\text{Medium plant 3}} \leq 1,200$ for medium
- $y_{\text{Small plant 1}} + y_{\text{Small plant 2}} + y_{\text{Small plant 3}} \leq 750$ for small

Equal capacity usage: Each plant uses the same percentage of its total capacity

```
# Load the lpSolve Library  
library(lpSolve)
```

```
# Coefficients of the objective function (profit per unit)  
objective <- c(420, 360, 300, 420, 360, 300, 420, 360, 300) # Large, Medium,  
Small for 3 plants
```

```

# Constraints matrix
constraints <- matrix(c(
  # Capacity constraints
  1, 1, 1, 0, 0, 0, 0, 0, 0, # Plant 1 (<= 750)
  0, 0, 0, 1, 1, 1, 0, 0, 0, # Plant 2 (<= 900)
  0, 0, 0, 0, 0, 0, 1, 1, 1, # Plant 3 (<= 450)

  # Storage constraints
  20, 15, 12, 0, 0, 0, 0, 0, 0, # Plant 1 (<= 13000 sq ft)
  0, 0, 0, 20, 15, 12, 0, 0, 0, # Plant 2 (<= 12000 sq ft)
  0, 0, 0, 0, 0, 0, 20, 15, 12, # Plant 3 (<= 5000 sq ft)

  # Sales constraints
  1, 0, 0, 1, 0, 0, 1, 0, 0, # Large sizes (<= 900)
  0, 1, 0, 0, 1, 0, 0, 1, 0, # Medium sizes (<= 1200)
  0, 0, 1, 0, 0, 1, 0, 0, 1, # Small sizes (<= 750)
), nrow = 9, byrow = TRUE)

# RHS of the constraints
rhs <- c(750, 900, 450, 13000, 12000, 5000, 900, 1200, 750)

# Constraint direction
direction <- c("<=", "<=", "<=", "<=", "<=", "<=", "<=", "<=", "<=")

# Solve the linear programming problem
solution <- lp("max", objective, constraints, direction, rhs)

# Display the results
solution$objval # The maximum profit

## [1] 708000

solution$solution # The optimal production plan

## [1] 350.0000 400.0000 0.0000 0.0000 400.0000 500.0000 0.0000
133.3333
## [9] 250.0000

```