

## 2. A\* Algorithm using misplaced tiles.

**Code:**

```
class Puzzle:
    def __init__(self, initial_state, goal_state):
        self.board = initial_state
        self.goal = goal_state
        self.n = len(initial_state)

    # To find the index of '0' (blank tile)
    def find_blank(self, board):
        for i in range(self.n):
            for j in range(self.n):
                if board[i][j] == 0:
                    return (i, j)

    # Heuristic function: h(n) - number of misplaced tiles
    def misplaced_tiles(self, board):
        misplaced = 0
        for i in range(self.n):
            for j in range(self.n):
                if board[i][j] != 0 and board[i][j] != self.goal[i][j]:
                    misplaced += 1
        return misplaced

    # Generate possible moves (neighbors) from the current state
    def get_neighbors(self, board):
        neighbors = []
        blank_pos = self.find_blank(board)
        x, y = blank_pos
        # Possible moves (up, down, left, right)
        moves = [(x-1, y), (x+1, y), (x, y-1), (x, y+1)]
        for move in moves:
            new_x, new_y = move
            if 0 <= new_x < self.n and 0 <= new_y < self.n:
                new_board = [row[:] for row in board] # Copy the board
                # Swap the blank with the adjacent tile
                new_board[x][y], new_board[new_x][new_y] = new_board[new_x][new_y],
new_board[x][y]
                neighbors.append(new_board)
        return neighbors

    # A* Search Algorithm
    def a_star(self):
        start = self.board
        goal = self.goal
        open_list = [(start, 0)] # List of tuples (board, g(n))
        closed_list = set()
        iteration = 0

        while open_list:
            # Sort open list by f(n) = g(n) + h(n)
            open_list.sort(key=lambda x: x[1] + self.misplaced_tiles(x[0])) # Sort by f(n)
            current_board, g = open_list.pop(0) # Get the board with the lowest f(n)
```

```

        iteration += 1
        print(f"\nIteration {iteration}:")
        self.print_board(current_board)
        print(f"g(n): {g}, h(n): {self.misplaced_tiles(current_board)}, f(n): {g + self.misplaced_tiles(current_board)}")

        # If we reach the goal, return the solution
        if current_board == goal:
            print("\nGoal reached!")
            return g

        # Add the current state to the closed list
        closed_list.add(tuple(map(tuple, current_board)))

        # Get all possible moves (neighbors)
        for neighbor in self.get_neighbors(current_board):
            if tuple(map(tuple, neighbor)) in closed_list:
                continue
            # g(n) is the depth (number of moves from the start)
            g_new = g + 1
            # Add neighbor to the open list
            open_list.append((neighbor, g_new))

        return -1 # If no solution is found

# Print the 3x3 board
def print_board(self, board):
    for row in board:
        print(" ".join(str(tile) if tile != 0 else "_" for tile in row))

# Helper function to take input from the user
def take_input():
    print("Enter the initial state (3x3 grid) row by row, use '0' for the blank tile:")
    initial_state = []
    for _ in range(3):
        row = list(map(int, input().split()))
        initial_state.append(row)

    print("Enter the goal state (3x3 grid) row by row, use '0' for the blank tile:")
    goal_state = []
    for _ in range(3):
        row = list(map(int, input().split()))
        goal_state.append(row)

    return initial_state, goal_state

# Main
if __name__ == "__main__":
    initial_state, goal_state = take_input()

    puzzle = Puzzle(initial_state, goal_state)
    moves = puzzle.a_star()

    if moves != -1:

```

```
    print(f"\nNumber of moves to solve: {moves}")
else:
    print("\nNo solution found.")
```

**Output:**

Enter the initial state (3x3 grid) row by row, use '0' for the blank tile:

```
2 8 3
1 6 4
0 7 5
```

Enter the goal state (3x3 grid) row by row, use '0' for the blank tile:

```
1 2 3
8 0 4
7 6 5
```

Iteration 1:

```
2 8 3
1 6 4
_ 7 5
```

$g(n): 0$ ,  $h(n): 5$ ,  $f(n): 5$

Iteration 2:

```
2 8 3
1 6 4
7 _ 5
```

$g(n): 1$ ,  $h(n): 4$ ,  $f(n): 5$

Iteration 3:

2 8 3

1 \_ 4

7 6 5

$g(n): 2, h(n): 3, f(n): 5$

Iteration 4:

2 8 3

\_ 6 4

1 7 5

$g(n): 1, h(n): 5, f(n): 6$

Iteration 5:

2 \_ 3

1 8 4

7 6 5

$g(n): 3, h(n): 3, f(n): 6$

Iteration 6:

2 8 3

\_ 1 4

7 6 5

$g(n): 3, h(n): 3, f(n): 6$

Iteration 7:

\_ 2 3

1 8 4

7 6 5

$g(n): 4, h(n): 2, f(n): 6$

Iteration 8:

1 2 3

\_ 8 4

7 6 5

$g(n): 5, h(n): 1, f(n): 6$

Iteration 9:

1 2 3

8 \_ 4

7 6 5

$g(n): 6, h(n): 0, f(n): 6$

Goal reached!

Number of moves to solve: 6