

Binary Search Tree

Questions.

M	T	W	T	F	S	S
Page No.:	YOUVA					
Date:						

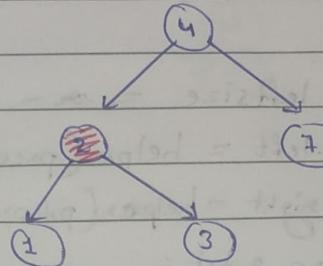
- ① LeetCode Q.No. (700) { Search in a Binary Search Tree }

→ If we search the entire tree, then T.C is $O(n)$.

→ In BST, we do not need to search the entire tree.

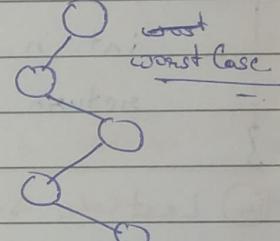
⇒ Code :-

```
public TN searchBST(TN root, int val){
    if (root == null) return null;
    if (root.val == val) return root;
    if (val < root.val){
        return searchBST(root.left, val);
    }
    else {
        return searchBST(root.right, val);
    }
}
```



T.C $\Rightarrow O(\log n)$.

Best Case - $O(\log n)$ / $O(h)$
 [Balanced Binary Tree]



Avg. & Worst Case : - $O(h)$

$O(n)$

height / levels of a Tree.

- ② LeetCode Q.No. (838) { Range Sum of BST }

high $\Rightarrow 15$
 low $\Rightarrow 7$

Code :- public int rangeSumBST(TN root, int low, int high){
 if (root == null) return 0;

int sum = 0;

if (root.val > low){

sum += rangeSumBST(root.left, low, high);

if (root.val < high)

sum += rangeSumBST(root.right, low, high);

if (root.val <= high && root.val >= low)

sum += root.val;

return sum;

Ans $\Rightarrow 32$

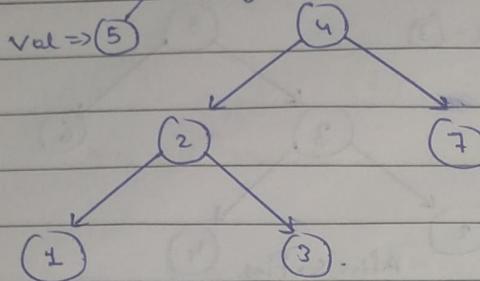
$10 + 15 + 7 \Rightarrow 32$

M	T	W	T	F	S	S
Page No.:	YOUVA					
Date:						

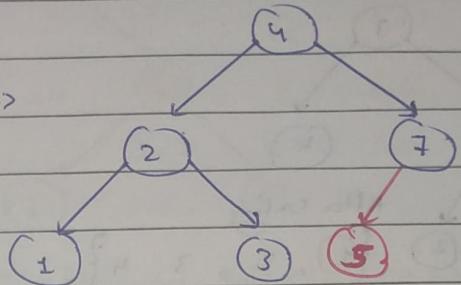
M	T	W	T	F	S	S
Page No.:	YOUVA					
Date:						

(3) Leetcode Q.No. (701) Insert Into A Binary Tree.

Ex 1:- Need to insert with following BST Rules



Ans.



M-1

p TN insertIntoBST(TN root, int val){

if (root == null) return new TN(val);

insert(root, val);

return root;

=> Code :-

p v insert(TN root, int val){

if (val < root.val){ // Attach to Left.

if (root.left == null){ }

root.left = new TreeNode(val);

return;

}

else{ }

insert(root.left, val);

}

else if (val > root.val){ // Attach to Right.

if (root.right == null){ }

root.right = new TreeNode(val);

return;

else

insert(root.right, val);

}

M-2.

=> Code :- p TN insertIntoBST(TreeNode root, int val){

if (root == null) return new TreeNode(val);

if (val < root.val)

root.left = insertIntoBST(root.left, val);

else

root.right = insertIntoBST(root.right, val);

return root;

}

M	T	W	T	F	S	S
Page No.:						
Date:	YOUVA					

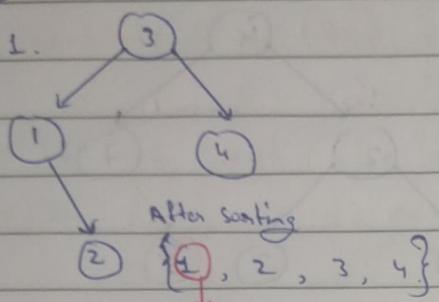
Hint :- Use Inorder

M	T	W	F	S	S
Page No.:				YOUVA	

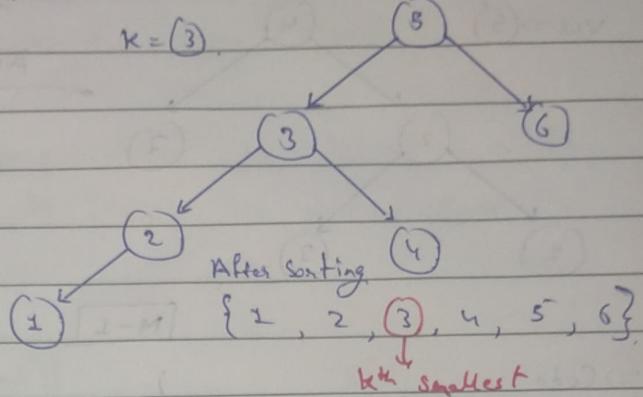
Q) LeetCode Q.No. (230) { Kth Smallest Elements in a BST.

~~1 based indexing.~~

Ex ① :-



Ex ② :-



=> Code :- public int kthSmallest (TN root, int k) {

Stack<TN> st = new Stack<>();

TN temp = root;

~~while (temp != null)~~

while (true) {

if (temp != null) {

st.push(temp);

temp = temp.left;

}

else { // temp == null.

if (st.size() == 0) break;

TN top = st.pop();

if (k == 1) return top.val;

else k--;

temp = top.right;

}

return 0;

M-2

public int kthSmallest (TN root, int k) {

List<Integer> ans = helper(root, k, new ArrayList<>());

return ans.get(k-1);

}

public List<Integer> helper (TN root, int k, List<Integer> ans) {

if (root == null) return ans;

helper (root.left, k, ans);

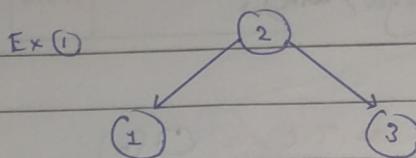
ans.add (root.val);

helper (root.right, k, ans);

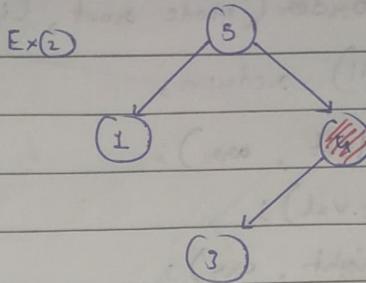
return ans;

⑤ LeetCode Qs. No. 98 } Validate Binary Search Tree. }

M	T	W	T	F	S	S
Page No.:	YOUVA					
Date:						



Ans :- True.



Ans :- False.

$$\boxed{M-L} \rightarrow \{ \min(RST) > \text{root.val} > \max(LST) \}$$

=> Code :-

```

ps long min( Node root){
|   if( root == null) return Long.MAX_VALUE;
|   Long a = root.val;
|   Long minLST = min( root.left);
|   Long minRST = min( root.right);
|   return Math.min( a , Math.min( minLST, minRST));
}
  
```

```

ps long max( Node root){
|   if( root == null) return Long.MIN_VALUE;
|   Long a = root.val;
|   Long maxLST = max( root.left);
|   Long maxRST = max( root.right);
|   return Math.max( a , Math.max( maxLST, maxRST));
}
  
```

```

ps boolean isValidBST( Node root) {
|   if( root == null) return true;
|   if( root.val <= max( root.left)) return false;
|   if( root.val >= min( root.right)) return false;
|   return isValidBST( root.left) && isValidBST( root.right);
}
  
```

T.C $\Rightarrow O(n \cdot \log n)$ } \rightarrow Best Case

T.C $\Rightarrow O(n^2)$ } \rightarrow Worst Case

M-2 → {Using Inorder Traversal}

M	T	W	T	F	S	S
Page No.:						YOUVA

⇒ Code 1 - PS void inorder(Node root, List<Integer> arr){

```
if(root == null) return;
inorder(root.left, arr);
arr.add(root.val);
inorder(root.right, arr);
```

T.C :- O(n)
S.C :- O(6).

PS boolean isValidBST(Node root){

```
List<Integer> arr = new ArrayList<>();
inorder(root, arr);
for(int i = 1; i < arr.size(); i++){
    if(arr.get(i) <= arr.get(i-1)) return false;
}
return true;
}
```

M-3 → Similar to [M-1]

{ Global variable flag = true }

⇒ Code 1 - static boolean flag;

PS long min(Node root){

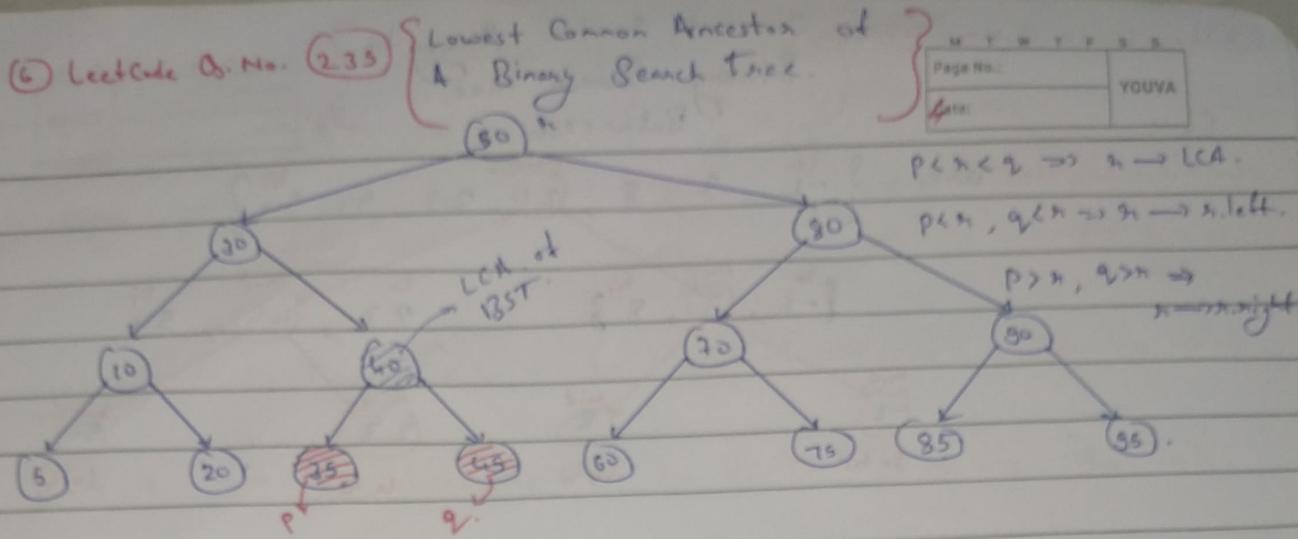
```
if(root == null) return Long.MAX_VALUE;
long a = root.val;
long minLST = min(root.left);
long minRST = min(root.right);
if(minRST <= root.val) flag = false;
return Math.min(a, Math.min(minLST, minRST));
```

PS long max(Node root){

```
if(root == null) return Long.MIN_VALUE;
long a = root.val;
long maxLST = max(root.left);
if(maxLST <= max(root.left)) flag = false;
long maxRST = max(root.right);
return Math.max(a, Math.max(maxLST, maxRST));
```

PS boolean isValidBST(Node root){

```
flag = true;
max(root);
min(root);
return flag;
```



⇒ Code :- p TN lowestCommonAncestor(TN root, TN p, TN q){

if (root == null) return null;

if (p.val < root.val && q.val < root.val)

return lowestCommonAncestor(root.left, p, q);

if (p.val > root.val && q.val > root.val)

return lowestCommonAncestor(root.right, p, q);

return root;

⑦ LeetCode Q. No. 1038 }

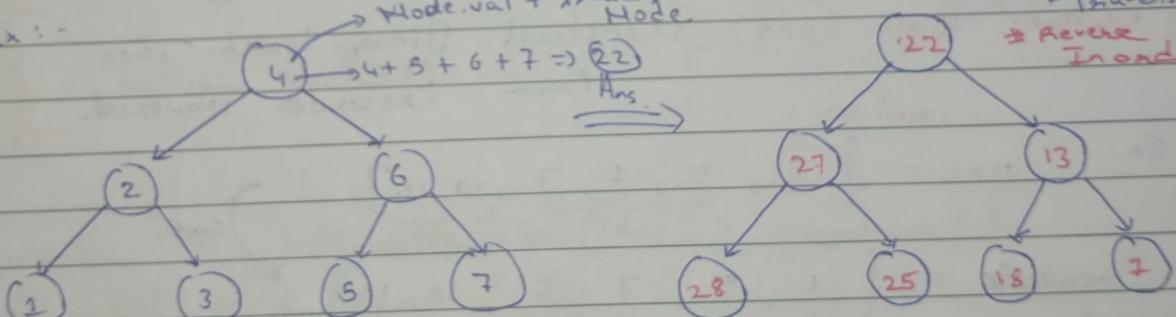
} Binary Search Tree To Greater Sum Tree

Sum of Greater Value of Node.

Use Inorder Traversal.

Reverse Inorder.

Ex:-



⇒ Code:-

Static int sum;

public void reverseInorder(TN root){

if (root == null) return;

reverseInorder(root.right);

root.val += sum;

sum += root.val;

reverseInorder(root.left);

Tc :- O(n)

Sc :- O(h) (h is levels / height on tree.)

p TN bstToGst(TN root){

sum = 0;

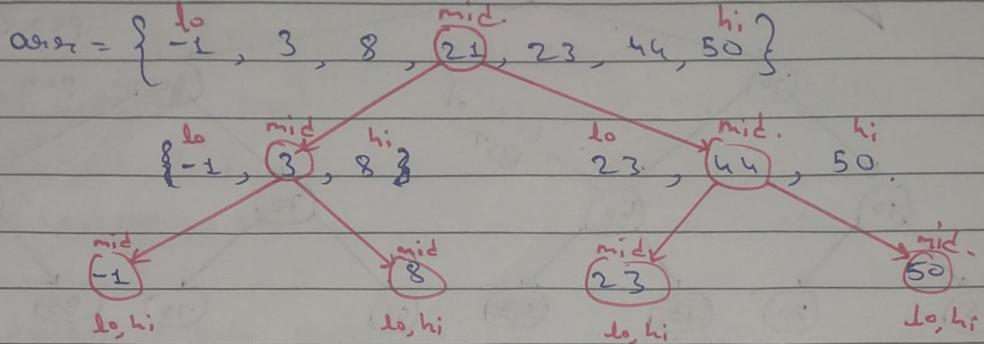
reverseInorder(root);

return root;

7 LeetCode Q.No. 108

Convert Sorted Array to
Binary Search Tree.

Ex :-



Code :-

```

P TN helper(int[] arr, int lo, int hi) {
    if (lo > hi) return null;
    int mid = (lo + hi) / 2;
    TN root = new TN(arr[mid]);
    root.left = helper(arr, lo, mid - 1);
    root.right = helper(arr, mid + 1, hi);
    return root;
}

```

P TN sortedArrayToBST(int[] nums){

return helper(nums, 0, nums.length - 1);

8 LeetCode Q.No. 1008

Construct Binary Search Tree
from Preorder Traversal.

Ex:-

$\text{pre} = \{8, 5, 1, 7, 10, 12\}$.

sort.

$\text{inorder} = \{1, 5, 7, 8, 10, 12\}$.

LST

$\text{pre} = \{5, 1, 7\}$.

root of LST

$\text{in} = \{1, 5, 7\}$.

LST

$\text{pre} = \{1\}$

root of LST

$\text{in} = \{\}$

n

$\text{pre} = \{7\}$

root of RST

$\text{in} = \{\}$

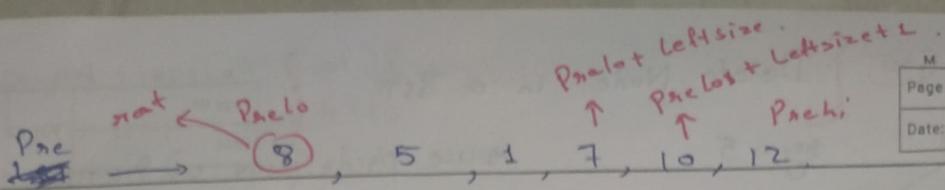
n

$\text{pre} = \{12\}$

$\text{in} = \{\}$

n

M	T	W	T	F	S	S
Page No.:	YOUVA					
Date:						



~~Pre~~ → ~~in.~~ → 1, 5, 7, 10, 12. $\Rightarrow 3 - 0 \Rightarrow 3$

LST → Prelo + 1 to Prelo + leftsize, inlo to $n-1$.

RST → Prelo + leftsize + 1 to Prehi, $n+1$ to inhi

⇒ Code:-

```

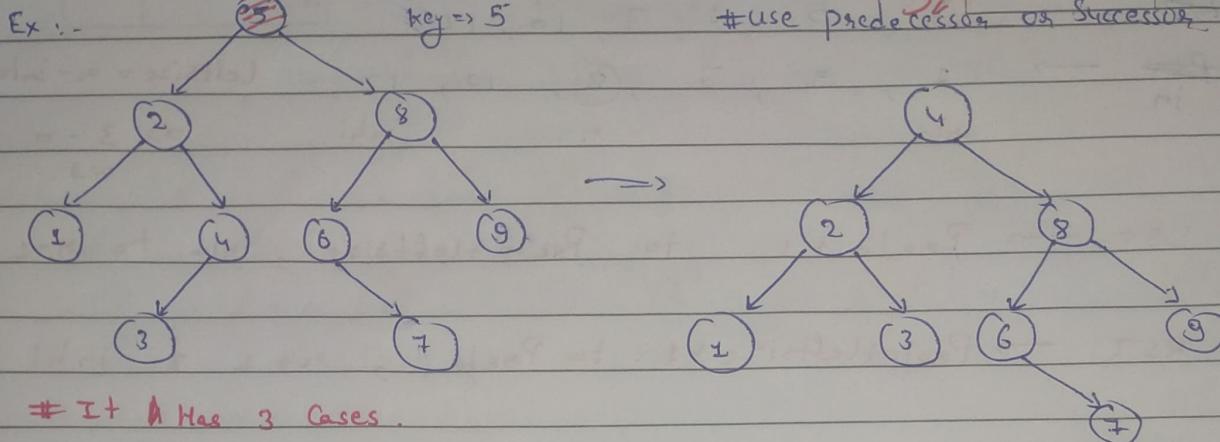
p TN helper(int[] preorder, int[] inorder, int prelo, int prehi,
           int inlo, int inhi) {
    if (prelo > prehi || inlo > inhi) return null;
    TN root = new TN(preorder[prelo]);
    int n = 0;
    while (inorder[n] != preorder[prelo]) n++;
    int leftsize = n - inlo;
    root.left = helper(preorder, inorder, prelo + 1, prelo + leftsize, inlo, n - 1);
    root.right = helper(preorder, inorder, prelo + leftsize + 1, prehi, n + 1, inhi);
    return root;
}
  
```

```

public TN bstFromPreorder(int[] preorder) {
    int n = preorder.length;
    int[] inorder = Array.copyOf(preorder, n);
    Arrays.sort(inorder);
    return helper(preorder, inorder, 0, n - 1, 0, n - 1);
}
  
```

9 LeetCode Q.No. (650) { Delete Node in a BST. }

M	T	W	T	F	S	S
Page No.:	YOUVA					
Date:						



→ Code :-

```

public TN deleteNode(TN root, int key){
    if(root == null) return null;
    if(root.val == key){ // Deletion
        if(root.left == null && root.right == null) } Case(1): 0 Child
        Nodes.
        return null;
        else if(root.left == null || root.right == null){ } Case(2): 1 Child
        Nodes.
        if(root.left == null) return root.right;
        else
            return root.left;
    }
    else{
        TN pred = iop(root);
        TN predParent = parent(root, pred);
        if(pred == predParent){ } Case(3): 2 Child Nodes.
            predParent.pred.right = root.right;
            return pred;
        }
        predParent.right = pred.left;
        pred.left = root.left;
        pred.right = root.right;
        return pred;
    }
    else if(root.val > key) root.left = deleteNode(root.left, key);
    else root.right = deleteNode(root.right, key);
    return root;
}

```

```

p TN iop (TN root) {
    TN temp = root.left;
    while (temp.right != null)
        temp = temp.right;
    return temp;
}

```

M	T	W	T	F	S	S
Page No.:						YOUVA
Date:						

```

p TN parent (TN root, TN pred) {
    if (root.left == pred || root.right == pred) return root;
    TN temp = root.left;
    while (temp.right != pred) {
        temp = temp.right;
    }
    return temp;
}

```

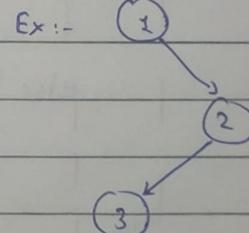
⑩ LeetCode #94. { Binary Tree Inorder Traversal } # Using Morris Traversal . ↴ Left Root Right.

```

=> Code :- p. List<Integer> inorderTraversal (TN root) {
    List<Integer> ans = new ArrayList<>();
    TN curr = root;
    while (curr != null) {
        if (curr.left != null) {
            TN pred = curr.left;
            while (pred.right != null && pred.right != curr)
                pred = pred.right;
            if (pred.right == null) {
                pred.right = curr;
                curr = curr.left;
            }
        }
    }
}

```

if (pred.right == null) {
 pred.right = curr;
 curr = curr.left;
}



else {
 ans.add(curr.val);
 curr = curr.right;
 pred.right = null;
}

Ans = [1, 3, 2]

else {
 ans.add(curr.val);
 curr = curr.right;
}
return ans;
}

11 LeetCode Qs. No. (98) { Validate Binary Search Tree }.

M	T	W	T	F	S	S
Page No.:	YOUVA					
Date:						

[M-4] → Morris Traversal.

⇒ Code :-

```

public boolean isValidBST(TreeNode root) {
    TreeNode prev = null;
    TreeNode curr = root;
    while (curr != null) {
        if (curr.left != null) {
            TreeNode pred = curr.left;
            while (pred.right != null & pred.right != curr) {
                pred = pred.right;
            }
            if (pred.right == null)
                pred.right = curr;
            curr = curr.left;
        }
        else {
            if (prev != null & prev.val >= curr.val)
                return false;
            prev = curr;
            curr = curr.right;
        }
    }
    if (prev != null & prev.val >= curr.val)
        return false;
    return true;
}

```

(12) LeetCode Q.No. (230)

Kth Smallest Element
in a BST.

M	T	W	T	F	S	S
Page No.:						
Date:	YOUVA					

M-3 → Morris Traversal

⇒ Code:-

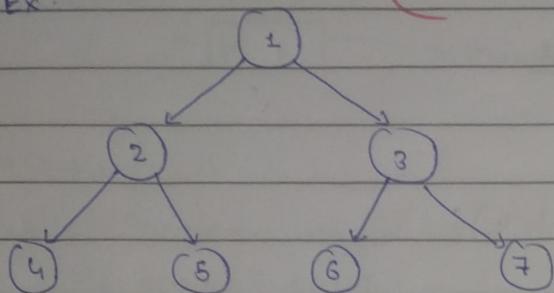
```
public int kthSmallest(TreeNode root, int k){  
    TreeNode curr = root;  
    while(curr != null){  
        if(curr.left != null){  
            TreeNode pred = curr.left;  
            while(pred.right != null & pred.right != curr){  
                pred = pred.right;  
            }  
            if(pred.right == null){  
                pred.right = curr;  
                curr = curr.left;  
            }  
            else{  
                if(k == 1) return curr.val;  
                else k--;  
                curr = curr.right;  
                pred.right = null;  
            }  
        }  
        else{  
            if(k == 1) return curr.val;  
            else k--;  
            curr = curr.right;  
        }  
    }  
    return 0;
```

Ques No. 114

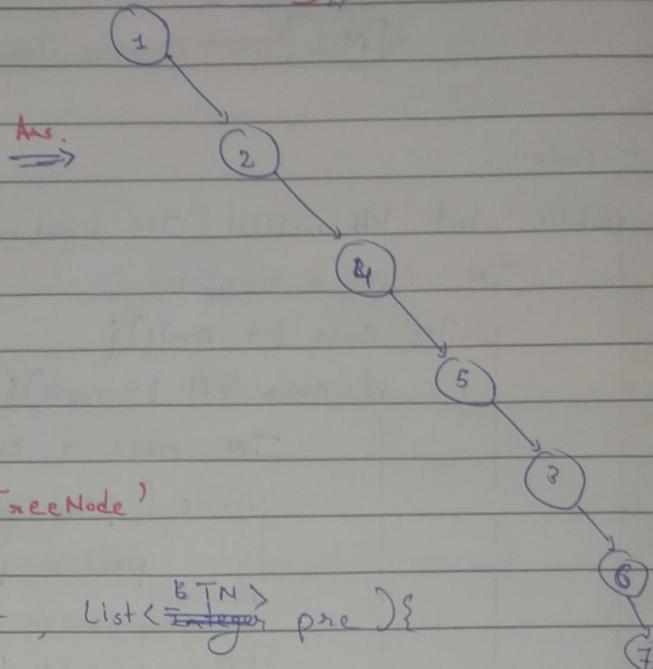
Flatten Binary Tree to
Linked List

M	T	W	T	F	S	S
Page No.:	YOUVA					
Date:						

Ex:-



Ans :- 1 2 4 5 3 6 7.



[M - 1]

Create Preorder Array of 'TreeNode'

⇒ Code:-

```
public void preorder (TN root , List<TN> pre ) {  
    if( root == null) return ;  
    pre.add (root);  
    preorder (root.left , pre );  
    preorder (root.right , pre );  
}
```

```
public void flatten (TN root) {  
    List<TN> pre = new ArrayList<>();  
    preorder (root , pre );  
    int n = pre.size ();  
    for( int i = 0 ; i < n ; i++ ) {  
        if( i != n-1)  
            pre.get(i).right = pre.get(i+1);  
        pre.get(i).left = null;  
    }  
}.
```

(1) Put Null in left of every Node.

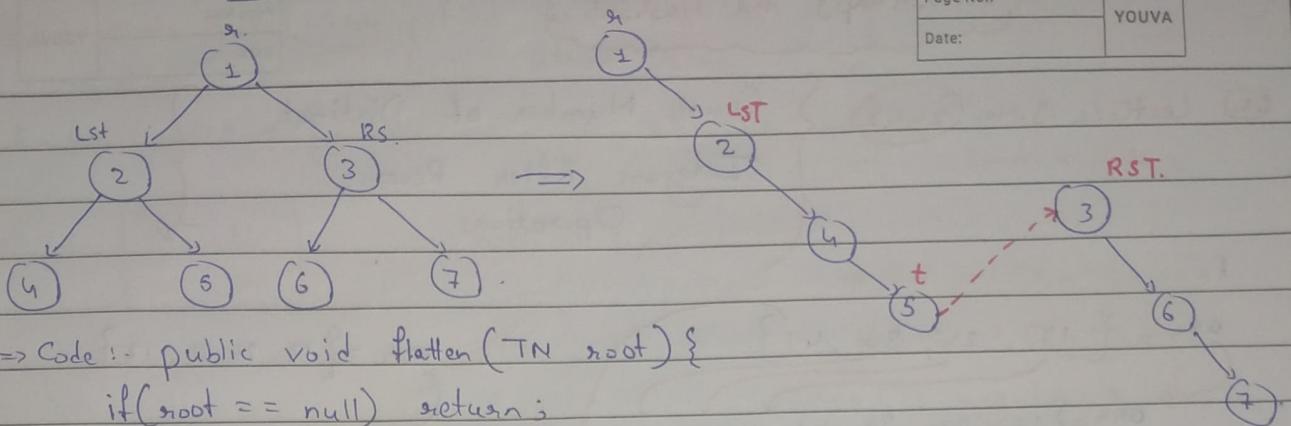
(2) $\text{ans}[i].right = \text{ans}[i+1]$

T.C = $O(n)$

S.C = $O(n)$

M-2 Recursion

M	T	W	T	F	S	S
Page No.:	YOUVA					
Date:						



```

Code :- public void flatten(TN root){
    if(root == null) return;
    if(root.left == null & root.right == null) return;
    TN lst = root.left;
    TN rst = root.right;
    flatten(lst);
    flatten(rst);
    root.left = null;
    root.right = lst;
    TN temp = root;
    while(temp.right != null)
        temp = temp.right;
    temp.right = rst;
}
    
```

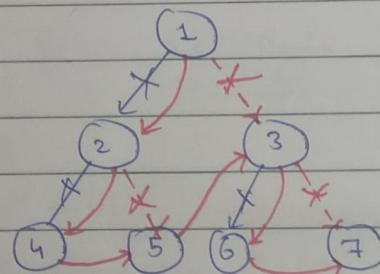
T.C $\Rightarrow O(n)$

S.C $\Rightarrow O(n)$ Recursive stack space.

M-3 Something like Morris traversal.

T.C $\Rightarrow O(n)$

S.C $\Rightarrow O(1)$



Bonus :- Pre/In/Post

$O(n)$ Space Recursive soln.

In \Rightarrow Morris $\rightarrow O(1)$ space

Pre \Rightarrow Morris $\rightarrow O(1)$ space

[But Structure of tree is]
permanently changed

Code :- public void flatten(TN root){

TN curr = *root;

while(curr != null){

if(curr.left != null){

TN r = curr.right;

curr.right = curr.left;

TN pred = curr.left;

while(pred.right != null)

pred = pred.right;

pred.right = r;

curr.left = null; // IMPORTANT

curr = curr.right;

} else {

curr = curr.right;