# Multi-peak emission of In<sub>2</sub>O<sub>3</sub> induced by oxygen vacancy aggregation

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Yin-Hui Peng, Chang-Chun He, 🗓 Yu-Jun Zhao, et al.







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Yin-Hui Peng, Chang-Chun He, Yu-Jun Zhao, (10) and Xiao-Bao Yang (11)

## **AFFILIATIONS**

School of Physics and Optoelectronics, South China University of Technology, Guangzhou 510640, China

<sup>a)</sup>Author to whom correspondence should be addressed: scxbyang@scut.edu.cn

## **ABSTRACT**

Oxygen vacancy is crucial to the optical properties in  $In_2O_3$ , however, the single oxygen vacancy model fails to explain the observed multi-peak emission in the experiment. Herein, we have theoretically investigated the diversity of oxygen vacancy distribution, revealing the relationship between the defect configurations and the optical properties. Combining the first-principles calculations and bayesian regularized artificial neural networks, we demonstrate that the structural stability can be remarkably enhanced by multi-oxygen vacancy aggregation, which will evolve with the defect concentration and temperature. Notably, our results indicate that the single oxygen vacancy will induce the emission peaks centered at  $1.35 \, \text{eV}$ , while multi-peak emission near  $2.35 \, \text{eV}$  will be attributed to the distribution of aggregated double oxygen vacancies. Our findings provide a comprehensive understanding of multi-peak emission observed in  $In_2O_3$ , and the rules of the vacancy distribution may be extended for other metal oxides to modulate the optical properties in practice.

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## I. INTRODUCTION

Due to excellent photoelectronic properties, wide bandgap oxide semiconductors have been widely applied in flat-panel displays, solar cells, emerging flexible, and transparent electronics. 1-3 As an n-type semiconductor with high conductivity and good optical transparency, indium oxide (In2O3) has attracted extensive attention.4 It has long been suspected that the oxygen vacancies are the origin of n-type conductivity in  $In_2O_3$  because the oxygen partial pressure during growth or post-growth processing can affect the optical properties of In<sub>2</sub>O<sub>3</sub>. <sup>5,6</sup> In<sub>2</sub>O<sub>3</sub> films have exhibited the optical bandgap of 3.62 eV and optical transmittance of 87% at an oxygen partial pressure of  $2 \times 10^{-3}$  mbar. With the increasing oxygen partial pressure, the optical bandgap of the In2O3 thin film was also observed to increase gradually.8 Also, oxygen partial pressure percentage would induce the morphology difference of In2O3 by modulating the spatial distribution of In and O atoms, further affecting the defect concentration, electron density, and Fermi level

In the experiment, the synthesis temperature has played a significant role in the photoluminescence (PL) peak of  $In_2O_3$ . There is emission at 475 nm in the PL spectra of high-density and well-aligned  $In_2O_3$  nanotubes synthesized at lower temperatures, indicating a deep defect level introduced by oxygen vacancy  $(V_O)$ .

The blue emission peaks at 420 and 470 nm have been observed in the thermally oxidizing indium nanohillock at  $500^{\circ}$ C, and the high oxygen vacancies density has been detected in these  $In_2O_3$  nanostructures. For the  $In_2O_3$  nanowires grown in the temperature of  $1050^{\circ}$ C, there are three deep defect level emission peaks in PL spectra, corresponding to the visible region centered at 423, 436, and 487 nm. In the recent study, three main PL peaks, including 485, 505, and 795 nm, have been observed in the  $In_2O_3$  thin layers annealed at 250 and 450 °C during 1 and 2 h. Therefore, the multi-peak emission in the spectra might be attributed to the complex distributions of  $V_O$ , which will evolve as a function of synthesis temperature.

Theoretically, researchers have believed that the treatments of the first-principles calculations should be most important to the effect of  $V_{\rm O}$  on optical properties, employing various methods such as the local density approximation (LDA), LDA+U, generalized gradient approximations (GGAs), GGA+U, and Heyd–Scuseria–Ernzerhof (HSE). Based on the calculated by HSE06 with higher accuracy, the defect energy level induced by single  $V_{\rm O}$  is about 2.25 eV above the valence band maximum (VBM). Furthermore, when the Hartree–Fock mixing parameter is 0.28, the single  $V_{\rm O}$  structure only gives rise to one emission peak at 2.3 eV. In most theoretical studies, a supercell with 80 atoms is adopted to

model  $\rm In_2O_3$  with single oxygen vacancy because this system has been characterized by a large 1% O-deficient nonstoichiometry. <sup>18–21</sup> However, regardless of the change in calculation methods, the single vacancy model can only induce one peak emission of  $\rm In_2O_3$ . Recent studies have shown that the distribution of oxygen vacancies in  $\rm TiO_2$ ,  $\rm SiO_2$ , and  $\rm HfO_2$  can affect the electronic structure properties, while our recent progress has shown that the configuration with double vacancies will be more stable than that with single vacancy in  $\rm In_2O_3$ . <sup>22–25</sup> Thus, the effect of  $\rm V_O$  distribution should be considered, which will provide a reasonable explanation of the multi-peak emission.

In this paper, we have systematically studied the structural stability of In2O3 with various distributions of oxygen vacancies based on the first-principles calculations, employing the HSE06 hybrid functional to obtain accurate optical properties. To give a good estimation of structural stability, we use bayesian regularized artificial neural networks (BRANNs) to get the relationship between oxygen vacancy distance and defect formation energy from the first-principles calculations. 26 The stable structures are determined based on the formation of energies, and the evolution of vacancy distribution is demonstrated as a function of temperature by considering the contribution of configuration entropy. In optical properties, we have confirmed the emission centers for single and double oxygen vacancies based on the simulation of excited states, which indicates that the multi-peak emission are attributed to multi-oxygen vacancy aggregation.

## **II. METHODS**

The first-principles calculations based on density-functional theory were performed with Vienna *Ab initio* Simulation Package (VASP). The Perdew–Burke–Ernzerhof (PBE) generalized gradient approximation was used to describe the exchange–correlation interaction. The Brillouin zone was sampled with allowed spacing between points in 0.3 Å $^{-1}$ . Cutoff energy of 520 eV and residual atomic forces criteria of 0.02 eV/Åwere selected in all simulations. To avoid the underestimation of bandgap for traditional metal oxide semiconductors, the HSE06 hybrid functional was adopted to improve the description of band structure and density of state (DOS). The  $\Delta$ SCF method was employed to simulate excited states. The  $\Delta$ SCF method was employed to simulate excited states. Sent In this way, we will construct the different electronic configurations by a set of orbitals occupation. Based on the electronic ground-state configuration with a set of occupied orbitals, an excited state of  $In_2O_3$  can be obtained by emptying one of the occupied orbitals and filling one of the unoccupied orbitals.

It is known that the  $V_{\rm O}$  concentration will reach 1% in the experiments under the O-poor condition. <sup>18–21</sup> The supercells of  $80 \times n$  ( $n=1 \sim 7$ ) atoms were generated with the Hermite normal form matrices, and n oxygen vacancies were introduced in the supercell with  $80 \times n$  atoms, respectively. <sup>35,36</sup> Based on the Structures of Alloy Generation and Recognition (SAGAR), <sup>36</sup> the structural multiplicity will be obtained. With such concentrations, the  $V_{\rm O}$  is generally in a neutral charge state under the charge neutrality restriction. <sup>25</sup> Therefore, we give priority to the neutral  $V_{\rm O}$  as the main defect. The formation energy of neutral defect  $\alpha$  can be

calculated as follows:37

$$\Delta H_D^{(\alpha)} = E(\alpha) - E(0) + \sum_{\alpha} n_{\alpha} (\Delta \mu_{\alpha} + \mu_{\alpha}), \tag{1}$$

where  $E(\alpha)$  is the total energy of the supercell containing the defect  $\alpha$ ; E(0) is the total energy of perfect supercell;  $n_{\alpha}$  is the number of atoms corresponding to defect  $\alpha$ ; a positive or negative value of  $n_{\alpha}$  indicates the atoms are removed or added.  $\Delta\mu_{\alpha}$  is the chemical potentials of defect  $\alpha$ ;  $\mu_{\alpha}$  is total energy of the most stable phase corresponding to defect  $\alpha$ .

The average formation energy with the different number of oxygen vacancies ( $\Delta E_{V_O}$ ) is used to describe the structural stability of supercells, and the formula is given by

$$\Delta E_{V_O} = \Delta H_D^{(\alpha)}/n_\alpha. \tag{2}$$

To consider the temperature effect on structural stability, the Gibbs free energy F for a solid system ignoring volume changes is calculated by the following equation:<sup>38</sup>  $F = kT \ln Z$ . The partition function Z is expressed as  $Z = \sum_i \omega_i e^{-\beta E_i}$ , where  $\omega$  is the structural multiplicity for the system. The occurrence probability of structure  $p_i$  with defect  $\alpha$  can be shown as

$$p_i = \omega_i e^{-\beta \Delta E_{V_O}^i} / Z, \tag{3}$$

where  $\Delta E_{V_O}^i$  is the average formation energy of structure  $p_i$ .

The concentration of oxygen vacancies in  $In_2O_3$  has been reported to affect the optical properties,  $^{21}$  so we first exclude the contribution of defect concentration during the calculation process. We construct the structures with the same concentration and focus on the defect concentration  $(c_d)$  with  $c_d=1/48$ , which is generally adopted by previous studies.  $^{13-17}$  In the supercell of proper size, the  $V_O$  interaction from the periodic images is small enough to be neglected, and those perfect supercells are shown in supplementary material, Fig. S1.

## III. RESULTS AND DISCUSSION

## A. The stable distribution of oxygen vacancies

According to the enumeration with structural recognition, we obtain the formation energies of all structures with single vacancy and double vacancies. When the supercell reaches 240 atoms, there are 40 621 nonequivalent structures with triple vacancies. As the supercell grows larger, there are more than one hundred million structures, and the computational cost becomes over expensive. Thus, the BRANNs are employed to predict the relationship between oxygen vacancy distance and  $\Delta E_{V_0}$ . Our dataset contains all structures for 40 and 80 atoms with triple oxygen vacancies, and 150 structures are selected in the supercells with 120, 160, 200, and 240 atoms, respectively. We obtain the first nearest neighbor distances between the  $V_O$  in supercells with triple oxygen vacancies and the 150 structures are selected uniformly for each supercell according to the average distance. The relationship between the average distances of triple oxygen vacancies and the formation energy is shown in supplementary material, Fig. S2. We observe that with the increase of the average distance,  $\Delta E_{V_O}$  first increases,

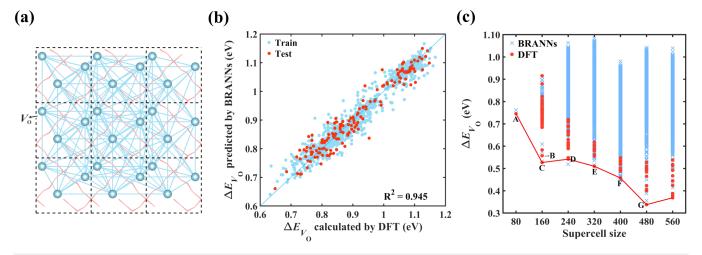
then decreases, and, finally, converges. The structures are more stable when the oxygen vacancies overall tend to be aggregated. We describe the configurations by the distances among all oxygen defects under the periodic boundary conditions, as shown in Fig. 1(a). Based on BRANNs, the error is smaller and the correlation coefficient  $\mathbb{R}^2$  of the model is 0.945, as shown in Fig. 1(b).

Figure 1(c) shows the relationship between supercell size and average defect formation energy under O-poor condition  $(\mu_{_{O}}=-2.74\,\mathrm{eV}$  and  $\mu_{_{\mathrm{In}}}=0\,\mathrm{eV})$  . There is only one type of O site according to the Wyckoff position in the In<sub>2</sub>O<sub>3</sub> bixbyite structure. The structure of 80 atoms with single V<sub>O</sub> has only one configuration, and  $\Delta E_{V_0}$  is 0.745 eV. For double oxygen vacancies in the supercell of 160 atoms, we calculated all the configurations by DFT, and evaluated the  $\Delta E_{V_0}$  by BRANNs for comparison. The most stable supercells predicted by model and DFT are the same configuration, and the lowest  $\Delta E_{V_O}$  calculated by DFT is 0.527 eV. Thus, the model evaluation with BRANNs is found to be accurate and efficient. Similarly, we used the trained model to predict oxygen vacancy defects in supercells with  $80 \times n$  (n = 3-7) atoms. Due to the large number of defect configurations in supercell sizes ranging from 320 to 480, the 100 000 defect configurations were randomly selected to predict  $\Delta E_{V_0}$ . In addition, the ten of most stable structures under each type of supercell were confirmed by the DFT calculation, determining the most stable defect configurations in the corresponding supercells. The lowest  $\Delta E_{V_O}$  decreases from 0.548 to 0.338 eV in supercell sizes ranging from 240 to 480. Interestingly, there is a magic structure with aggregated six-oxygen vacancy in the supercell of 480 atoms as shown in structure G of Fig. 2.

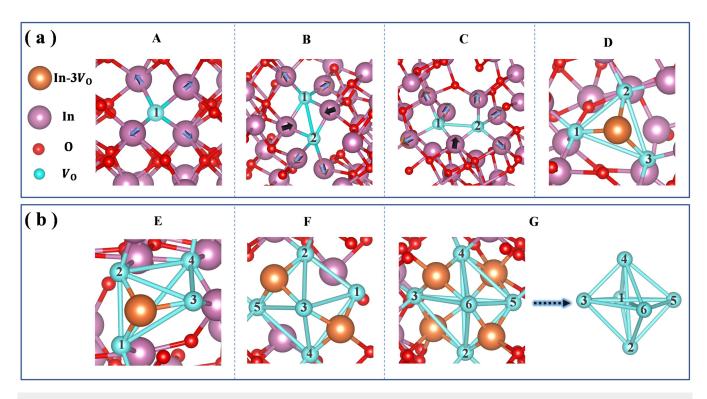
Figure 2 shows the distributions of oxygen vacancies for the stable configurations in supercells with  $80 \times n$  (n = 1-6) atoms. In structure A, the introduction of single  $V_O$  gives rise to the repulsion of In atoms near  $V_O$ , shortening of bond length. The average distance among the In atoms increases by 0.15 Å, as shown in

supplementary material, Fig. S3(a). For two stable double V<sub>O</sub> configurations (B and C) in the supercell of 160 atoms, we employ  $In-2V_O$  to mark one In atom losing two oxygen atoms. There are two In-2V<sub>O</sub> in structure B, and only one In-2V<sub>O</sub> in structure C. Both In-2 $V_0$  in structure B and C move toward the center of double oxygen vacancies, while the other neighboring In atoms are repulsed. The distances between In-In bonds are given in supplementary material, Fig. S3, and we find that the repulsion for In-In bonds around double oxygen vacancies is stronger than those around single vacancy. With shortening, the distance between double oxygen vacancies, the stronger repulsive Coulomb forces of In-In bonds can strengthen In-O bonds near V<sub>O</sub>, enhancing the structural stability. In the most stable structure D with triple oxygen vacancies, the aggregation structure is also energetically preferable. Furthermore, the stable structure of the triple vacancy can be considered the introduction of an additional oxygen vacancy around the In-2VO. Interestingly, the structures D, E, F, and G contain 1, 1, 2, and 4 In-3 $V_{\rm O}$  respectively. The lowest  $\Delta E_{V_0}$  is the structure G with six-vacancy, and the distribution of  $V_{\rm O}$  is an octahedron. There are four In-3 $V_{\rm O}$  near the octahedron, and those are not on adjacent octahedral surfaces. Each additional V<sub>O</sub> repels a set of In atoms, strengthening a set of In-O bonds around vacancies. However, when the seven vacancies are aggregated, the weakened repulsive force of In atoms around the vacancy can be obviously observed. The distances of In atoms in those structures are shown in supplementary material, Fig. S3. Thus, six vacancies will form a magic cluster of aggregated oxygen vacancies, and the structural stability is attributed to the repulsion between the In atoms near oxygen vacancies. The aggregation of oxygen vacancies can increase the number of strengthened In-O bonds, improving structural stability.

In order to determine the effect of aggregated  $V_{\rm O}$  on structural stability from the perspective of electronic structure, we use crystal



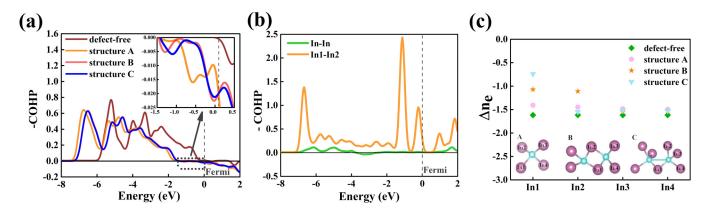
**FIG. 1.** (a) One wireframe graphic structure with the triple oxygen vacancies for  $\ln_2 O_3$ . A black box represents one lattice period, and the blue ball shows the  $V_0$ . The blue line shows the distance between oxygen vacancies, while the red background box shows the line between the ln and O atoms. (b) Comparison of  $\Delta E_{V_0}$  predicted by the BRANNs and DFT.  $R^2$  is the correlation coefficient. (c)  $\Delta E_{V_0}$  varies with the supercell size under O-poor condition at 1/48 vacancy concentration.  $\Delta E_{V_0}$  represented by letters corresponds to the structures in Fig. 2.



**FIG. 2.** Vacancy distribution of stable configurations at different supercell sizes. (a) 80, 160, 240 atoms. (b) 320, 400, 480 atoms. In- $3V_{\rm O}$  represents the orange In atom losing three oxygen atoms. The arrows show the direction of movement for the In atoms after relaxation.

orbital Hamilton populations (COHP) to discuss bonding between atom pairs. <sup>39,40</sup> The positive value of -COHP indicates bonding states, whereas the negative value indicates antibonding states. As shown in Fig. 3(a), the -COHP shows that the In-O interactions are mainly bonding states in the defect-free In<sub>2</sub>O<sub>3</sub>. The In-O

bonds form the antibonding states below the Fermi level in the structures with vacancy, whereas it can be attributed to the structural distortion caused by the introduction of  $V_{\rm O}$ . Thus, the expelling O atoms immediately weaken In–O bonding states and are energetically unfavorable. Note that the In–O antibonding states



**FIG. 3.** (a) Negative crystal orbital Hamilton population of ln–O bond in the structure of A, B, C, and defect-free. (b) Negative crystal orbital Hamilton population of average ln–ln bonds and single ln1–ln2 bond in structure B. (c) The Bader charges of ln atoms around the oxygen vacancies in the structure of A, B, C, and defect-free. The negative value of  $\Delta n_e$  represents the number of electrons lost by one ln atom.

for expelling two adjacent O atoms is weaker than expelling single O atom. On structural relaxation, the structures for aggregated oxygen vacancies are more stable. Furthermore, there is a pair of In–In bonds in structure B as shown in Fig. 3(b), which is consistent with the two In atoms moving towards each other. Compared with structure C, the pair of In–In bonds will enhance In–O antibonding, thus slightly reducing structural stability. Figure 3(c) shows that In atoms in structures B and C lose less charge than that in structure A, based on the charge transfer by the Bader analysis. The In- $2V_O$  of structure C has more charge than the In- $2V_O$  of structure B with the absence of In–In bond. The number of paired electrons between the In and the O atoms around the double oxygen vacancies increases, strengthening the stability of the In–O bond.

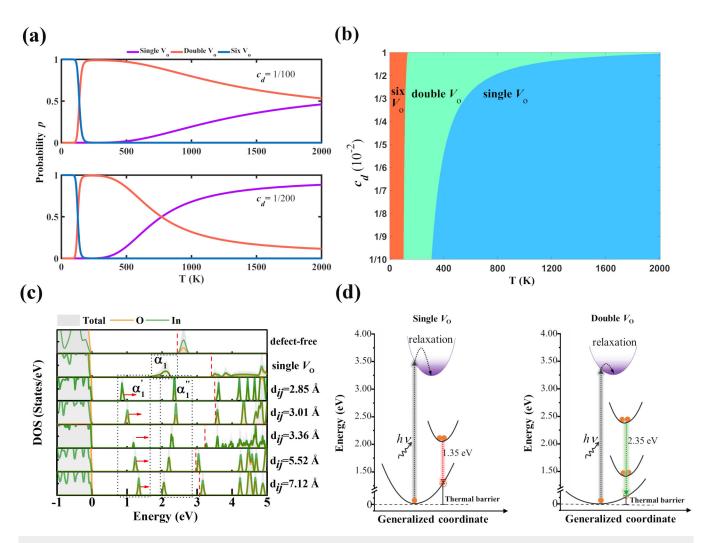
## B. The optical properties modulated by the distributions of double oxygen vacancies

Due to the diversity of experimental synthesis conditions, there may be a variety of defects in the preparation of In<sub>2</sub>O<sub>3</sub>. Based on the Boltzmann distribution, the vacancy concentration under thermodynamic equilibrium at growth temperature  $T_g$  is estimated as:25 The oxygen vacancy concentration of single and double are 0.57%, 2.58%, respectively at  $T_g = 1673 \,\mathrm{K}^{20}$  The  $\mathrm{In}_2\mathrm{O}_3$  is characterized by a non-stoichiometric ratio of 1% O-deficient at this growth temperature  $T_g$ , indicating a mixed distribution of single and double vacancies with different probabilities. Therefore, we study the free energy variation of defect structure with the temperature by considering the configuration entropy attributed to structural multiplicity. The system with given concentration of vacancy is considered the canonical ensemble, and the number of possible configurations is estimated by combination. Taking the structure with six oxygen vacancies as an example, the structural multiplicity of single vacancy is represented by the number of combinations formed by six oxygen vacancies that are not close to each other. When facing the aggregated double oxygen vacancies, we regard the adjacent double oxygen vacancy as a local structure, and the three local structures are far away from each other. The structural multiplicity with aggregated double oxygen vacancies is given by the number of combinations, and changes with the defect concentration. Similarly, the combination of aggregated triple, four, five, and six oxygen vacancies are given correspondingly. For a given defect concentration and temperature, we estimate the probability of these  $V_{\rm O}$  configurations according to the Eq. (3), as shown in Fig. 4(a). The probability for the structure with triple, four, and five oxygen vacancies are small enough to be neglected, and only the probability for structures with single, double, and six oxygen vacancies are shown in Fig. 4(a). When the  $V_{\rm O}$  concentration is 1/100, the probability of structure with the six-vacancy aggregation is the highest at low temperatures. With the increase in temperature, the probability of the structure of a double vacancy configuration is obviously superior. However, when the  $V_{\rm O}$  concentration is 1/200 and the experimental temperature exceeds 800 K, the defect configuration of single vacancy is obviously more likely to appear, rather than double vacancies. The detailed phase diagram as a function of defect concentration and temperature is given in Fig. 4(b). Considering the defect concentration from 0.1% to 1%, the six-vacancy aggregation will energetically preferable at low temperatures, which will evolve into double vacancies and, finally, single vacancy as the temperature increases. The critical temperature of the transition from aggregated six vacancies to aggregated double vacancies is almost the same, while the temperature of transition from double vacancies to single vacancy depends on the concentration dramatically. At the synthesis temperature (450–1050°C) of  $\rm In_2O_3,^{9-12}$  the phase diagram indicates that aggregated double oxygen vacancies will appear when the synthesis concentration of oxygen vacancies is higher than 1/150. Note that,  $\rm In_2O_3$  is characterized by a non-stoichiometric ratio of 1% O-deficient in experiments.  $^{\rm 18-21}$  Therefore, double oxygen vacancies should be the majority of defects under common conditions.

Besides the structural stability, the optical properties will be dominated by the aggregation of multi-oxygen vacancy. The HSE06 was used to overcome the problem of underestimating the bandgap, and the electronic band in the reciprocal space is shown in supplementary material, Fig. S4. The calculated bandgap of In<sub>2</sub>O<sub>3</sub> given by PBE is 0.90 eV, while the one by HSE06 is 2.57 eV, which is in good agreement with the previous result.<sup>15</sup>

In Fig. 4(c), we have shown the DOS of In<sub>2</sub>O<sub>3</sub> with and without  $V_0$ , focusing on the variation with the distance of double oxygen vacancies. The O atoms are surrounded by four In nearest neighbors in In<sub>2</sub>O<sub>3</sub>, with four slightly different In–O bond lengths. The formation of V<sub>O</sub> induces four In dangling bonds, which consist of a lower energy  $\alpha_1$  state in bandgap and three higher energy states in the conduction band. The  $\alpha_1$  state is located at 2.1 eV above the VBM in single  $V_{\rm O}$ , whereas the double oxygen vacancies introduce two energy states in the bandgap, and the deeper state is marked as  $\alpha_{1}^{'}$  state. Interestingly, the  $\alpha_{1}^{'}$  state gradually moves toward the conduction band minimum (CBM) with the distance of the double oxygen vacancies increasing, while the  $\alpha_1^n$  state first moves toward the CBM and then moves toward the VBM. Owing to the weakened interaction between the oxygen vacancies , the two energy states in the gap become almost degenerate, eventually forming a single energy state. As shown in Fig. S5 of the supplementary material, we have obtained structures A, C, and G with partial charge densities from defect states, corresponding to single-, double-, and six-vacancy, respectively. The charge distribution in the gap state is mainly localized around the defect. The variation of defect states induced by the spatial distribution of oxygen vacancies will effectively modulate the optical properties.

The multi-peak emission of  $\rm In_2O_3$  have been observed in the recent experiment, including 485, 505, and 795 nm. <sup>12</sup> In order to understand these emission centers caused by defect states, we employed  $\Delta SCF$  method to simulate excited states, and focusing on the optical properties of single and double neutral oxygen vacancies based on the results discussed in Fig. 4(b). <sup>32–34</sup> The schematic diagram of electron-hole pairs induced by oxygen vacancies under external field excitation is shown in Fig. 4(d). When the electron of VBM is excited above the CBM, the system is in excited state. After lattice relaxation, the electron in the defect state falls back to the VBM accompanied by a luminescence process. In view of the higher thermal barrier induced by the instability of the single  $V_O$ , we predict a broad emission peak centered at 1.35 eV. In the structure of double oxygen vacancies, the emission peak centered at 2.35 eV is significantly higher than that of single  $V_O$ . Since the



**FIG. 4.** (a) The probability of configurations with aggregated n (n=1,2,6) oxygen vacancies under the Boltzmann distribution at defect concentration of 1/100 and 1/200. (b) The structural stability with n (n=1,2,6) oxygen vacancies in  $\ln_2 O_3$  as a function of concentration  $c_d$  and temperature T. In a certain concentration and temperature, the structure for specific defect is dominant in the given area. (c) The total and atom-projected DOS for the defect-free, single  $V_0$ , and different double oxygen vacancies in  $\ln_2 O_3$ . The zero position is VBM, and the red dashed lines represent the CBM. The  $\alpha_1$  state represents the defect state induced by the single  $V_0$ , while the  $\alpha_1'$  and  $\alpha_1''$  states circled by the black dashed lines respectively refer to the deeper and shallower defect states induced by double oxygen vacancies. The  $d_{ij}$  is the relative position between the oxygen vacancies i and j. (d) Calculated configuration coordinate diagram of the optical transition for single oxygen vacancy (structure A) and double oxygen vacancies (structure C).

bandgap is slightly  $0.1\,\mathrm{eV}$  lower than the experimental gap of  $2.67\,\mathrm{eV}$ , we infer that the two calculated emission peaks, respectively, correspond to emission peaks near 795 and 505 nm. Note that the thermal barrier of double oxygen vacancies is significantly lower than that of the single  $V_{\mathrm{O}}$ , which is in agreement with the experimental observation that the PL intensity near 795 nm is evidently weaker than the intensity near  $505\,\mathrm{nm}$ . As shown in Fig. 4(c), the position of the  $\alpha_1''$  state will change with the distance between the oxygen vacancies. The double oxygen vacancies with different distributions may lead to various emission peaks near  $2.35\,\mathrm{eV}$ , corresponding to the multi-peak emission of  $\mathrm{In}_2\mathrm{O}_3$ . Thus,

the peaks at 485 and 505 nm are attributed to double oxygen vacancies, rather than the single  $V_{\rm O}$ .

## IV. CONCLUSION

In summary, we have demonstrated that the aggregation of oxygen vacancies will be energetically preferable combining the BRANNs and the first-principles calculations. The aggregated six-oxygen vacancy is an octahedral defect, and the four  $\text{In-}3V_{\text{O}}$  are distributed on non-adjacent octahedral surfaces. The calculated free energy shows that the double oxygen vacancies are dominant at the

common condition due to the contribution of configuration entropy. In addition, the structural distortion induced by  $V_{\rm O}$  will lead to charge redistribution, and form many localized defect states, resulting in the multi-peak emission in  $\rm In_2O_3$ . The experimentally observed peaks at 485 and 505 nm are attributed to double oxygen vacancies, while the single vacancy mainly induces an emission peak at 795nm. Our calculation results fully illustrate that different oxygen vacancy distributions will affect the structural stabilities and optical properties, which is of great significance to the study of other non-stoichiometric oxides.

## SUPPLEMENTARY MATERIAL

The supplementary material includes supercell structure corresponding to the 80, 160, 240, 320, 400, and 480 atoms (Fig. S1),  $\Delta E_{V_O}$  varies with the average distances of triple oxygen vacancies under O-poor conditions (Fig. S2), the relative positions of In atoms before and after optimization of defect structures with oxygen vacancies (Fig. S3), the electronic band dispersion diagram for  $\rm In_2O_3$  calculated at the PBE and HSE06 level of the theory (Fig. S4), the partial charge densities from defect states of structures A, C, and G (Fig. S5).

### **ACKNOWLEDGMENTS**

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## **AUTHOR DECLARATIONS**

## **Conflict of Interest**

The authors have no conflicts to disclose.

## **Authors Contribution**

Y.-H.P. and C.-C.H. contributed equally to this work.

Yin-Hui Peng: Methodology (equal); Writing – original draft (equal). Chang-Chun He: Formal analysis (equal); Software (equal). Yu-Jun Zhao: Investigation (equal); Methodology (equal); Writing – original draft (equal). Xiao-Bao Yang: Supervision (equal); Writing – review & editing (equal).

## **DATA AVAILABILITY**

The data that support the findings of this study are available from the corresponding author upon reasonable request.

## **REFERENCES**

- M. Katayama, "TFT-LCD technology," Thin Solid Films 341, 140–147 (1999).
   E. Fortunato, D. Ginley, H. Hosono, and D. C. Paine, "Transparent conducting oxides for photovoltaics," MRS Bull. 32, 242–247 (2007).
- <sup>3</sup>O. Bierwagen, "Indium oxide—A transparent, wide-band gap semiconductor for (opto)electronic applications," Semicond. Sci. Technol. **30**, 024001 (2015).

- <sup>4</sup>J. Shi, J. Z. nad Lu Yang, M. Qu, D.-C. Qi, and K. H. L. Zhang, "Wide bandgap oxide semiconductors: From materials physics to optoelectronic devices," Adv. Mater. 33, 2006230 (2021).
- $^{5}$ O. Bierwagen and J. S. Speck, "High electron mobility  $In_{2}O_{3}(001)$  and (111) thin films with nondegenerate electron concentration," Appl. Phys. Lett. **97**, 072103 (2010).
- <sup>6</sup>A. Chen, K. Zhu, H. Zhong, Q. Sha, and G. Ge, "A new investigation of oxygen flow influence on ito thin films by magnetron sputtering," Sol. Energy Mater. Sol. Cells **120**, 157–162 (2013).
- <sup>7</sup>S. Kaleemullaa, A. S. Reddyc, S. Uthannab, and P. S. Reddy, "Physical properties of In<sub>2</sub>O<sub>3</sub> thin films prepared at various oxygen partial pressures," J. Alloy. Compd. 479, 589–593 (2009).
- <sup>8</sup>A. V. M. Ali and D. Kekuda, "Thickness and oxygen partial pressure dependence on optical band gap of indium oxide by reactive evaporation method," IOP Conf. Ser.: Mater. Sci. Eng. 73, 012027 (2015).
- <sup>9</sup>X. ping Shen, H. jiang Liu, X. Fan, Y. Jiang, J. ming Hong, and Z. Xu, "Construction and photoluminescence of In<sub>2</sub>O<sub>3</sub> nanotube array by CVD-template method," J. Cryst. Growth **276**, 471–477 (2005).
- $^{10}$ H.-L. Wei, L. Zhang, Z.-L. Liu, and K.-L. Yao, "Fabrication and photoluminescence characteristics of  $In_2O_3$  nanohillocks," Chin. Phys. B **20**, 118102 (2011).
- <sup>11</sup>P. Wu, Q. Li, C.-X. Zhao, D.-L. Zhang, L. fei Chi, and T. Xiao, "Synthesis and photoluminescence property of indium oxide nanowires," Appl. Surf. Sci. 255, 3201–3204 (2008).
- $^{12}$ N. Beji, M. Reghima, M. Souli, and N. Kamoun Turki, "Effect of nitrogen annealing on the structural, optical and photoluminescence properties of  $In_2O_3$  thin films," J. Alloy. Compd. 675, 231–235 (2016).
- <sup>13</sup>S. Lany and A. Zunger, "Dopability, intrinsic conductivity, and nonstoichiometry of transparent conducting oxides," Phys. Rev. Lett. 98, 045501 (2007).
- <sup>14</sup>P. Agoston, P. Erhart, A. Klein, and K. Albe, "Geometry, electronic structure and thermodynamic stability of intrinsic point defects in indium oxide," J. Phys.: Condens. Matter 21, 455801 (2009).
- <sup>15</sup>P. Ágoston, K. Albe, R. M. Nieminen, and M. J. Puska, "Intrinsic *n*-type behavior in transparent conducting oxides: A comparative hybrid-functional study of In<sub>2</sub>O<sub>3</sub>, SnO<sub>2</sub>, and ZnO," Phys. Rev. Lett. **103**, 245501 (2009).
- <sup>16</sup>S. Limpijumnong, P. Reunchan, A. Janotti, and C. G. Van de Walle, "Hydrogen doping in indium oxide: An *ab initio* study," Phys. Rev. B **80**, 193202 (2009).
- <sup>17</sup>I. Chatratin, F. P. Sabino, P. Reunchan, S. Limpijumnong, J. B. Varley, C. G. Van de Walle, and A. Janotti, "Role of point defects in the electrical and optical properties of In<sub>2</sub>O<sub>3</sub>," Phys. Rev. Mater. 3, 074604 (2019).
- 18 J. H. W. De Wit, G. Van Unen, and M. Lahey, "Electron concentration and mobility in In<sub>2</sub>O<sub>3</sub>," J. Phys. Chem. Solids 38, 819–824 (1977).
- $^{19}$ J. H. W. De Wit, "The high temperature behavior of  $In_2O_3$ ," J. Solid State Chem. 13, 192–200 (1975).
- $^{20}$ J. H. W. De Wit, "Structural aspects and defect chemistry in  $In_2O_3$ ," J. Solid State Chem. 20, 143–148 (1977).
- $^{21}$ J.-Y. Gan, X.-H. Lu, J.-H. Wu, S.-L. Xie, T. Zhai, M.-H. Yu, Z.-S. Zhang, Y.-C. Mao, and Y.-X. Tong, "Oxygen vacancies promoting photoelectrochemical performance of  $In_2O_3$  nanocubes," Sci. Rep. 3, 1021 (2013).
- **22**T. Li, F. Hong, K. Yang, B. Yue, N. Tamura, H. Wu, Z. Cheng, and C. Wang, "Metastable oxygen vacancy ordering state and improved memristive behavior in TiO<sub>2</sub> crystals," Sci. Bull. **65**, 631–639 (2020).
- $^{23}$ M. C. Sahu, S. K. Mallik, S. Sahoo, S. K. Gupta, R. Ahuja, and S. Sahoo, "Effect of charge injection on the conducting filament of valence change anatase  ${\rm TiO_2}$  resistive random access memory device," J. Phys. Chem. Lett. 12, 1876–1884 (2021).
- $^{\bf 24}$  D. Z. Gao, J. Strand, M. S. Munde, and A. L. Shluger, "Mechanisms of oxygen vacancy aggregation in SiO  $_2$  and HfO  $_2$ ," Front. Phys. 7, 43 (2019).
- <sup>25</sup>L. Liu, C.-C. He, J. Zeng, Y.-H. Peng, W.-Y. Chen, Y.-J. Zhao, and X.-B. Yang, "Theoretical study of oxygen-vacancy distribution in In<sub>2</sub>O<sub>3</sub>," J. Phys. Chem. C 125, 7077–7085 (2021).
- <sup>26</sup>D. J. MacKay, "Bayesian neural networks and density networks," Nucl. Instrum. Methods Phys. Res., Sect. A 354, 73–80 (1995).

- <sup>27</sup>G. Kresse and J. Furthmüller, "Efficient iterative schemes for ab initio total-energy calculations using a plane-wave basis set," Phys. Rev. B **54**, 11169–11186 (1996). <sup>28</sup>G. Kresse and D. Joubert, "From ultrasoft pseudopotentials to the projector
- augmented-wave method," Phys. Rev. B 59, 1758-1775 (1999).
- <sup>29</sup>P. E. Blöchl, "Projector augmented-wave method," Phys. Rev. B **50**, 17953-17979 (1994).
- 30 J. P. Perdew, K. Burke, and M. Ernzerhof, "Generalized gradient approximation made simple," Phys. Rev. Lett. 77, 3865-3868 (1996).
- 31 J. Heyd, G. E. Scuseria, and M. Ernzerhof, "Erratum: 'Hybrid functionals based on a screened coulomb potential," J. Chem. Phys. 124, 219906 (2006).
- 32 A. Hellman, B. Razaznejad, and B. I. Lundqvist, "Potential-energy surfaces for
- excited states in extended systems," J. Chem. Phys. 120, 4593–4602 (2004).

  33R. J. Maurer and K. Reuter, "Excited-state potential-energy surfaces of metaladsorbed organic molecules from linear expansion Δ-self-consistent field density-functional theory (\Delta SCF-DFT)," J. Chem. Phys. 139, 014708 (2013).
- 34X. Jiang, Z. Xu, Y. Zheng, J. Zeng, K.-Q. Chen, and Y. Feng, "Origin of broadband emission and large Stokes shift in antimony trisulfide," J. Phys. Chem. Lett. 13, 8026-8032 (2022).

- 35G. L. W. Hart and R. W. Forcade, "Algorithm for generating derivative structures," Phys. Rev. B 77, 224115 (2008).
- <sup>36</sup>C.-C. He, J.-H. Liao, S.-B. Qiu, Y.-J. Zhao, and X.-B. Yang, "Biased screening for multi-component materials with Structures of Alloy Generation and Recognition (SAGAR)," Comput. Mater. Sci. 193, 110386 (2021).
- 37S. B. Zhang, S.-H. Wei, and A. Zunger, "Stabilization of ternary compounds via ordered arrays of defect pairs," Phys. Rev. Lett. 78, 4059-4062
- 38 L. D. Landau, Statistical Physics (Butterworth-Heinemann, 1980).
- 39 S. Maintz, V. L. Deringer, A. L. Tchougréeff, and R. Dronskowski, "LOBSTER: A tool to extract chemical bonding from plane-wave based DFT," J. Comput. Chem. 37, 1030-1035 (2016).
- <sup>40</sup>R. Nelson, C. Ertural, J. George, V. L. Deringer, G. Hautier, and R. Dronskowski, "Lobster: Local orbital projections, atomic charges, and chemical-bonding analysis from projector-augmented-wave-based densityfunctional theory," J. Comput. Chem. 41, 1931-1940 (2020).
- <sup>41</sup>M. Yu and D. R. Trinkle, "Accurate and efficient algorithm for Bader charge integration," J. Chem. Phys. 134, 064111 (2011).