

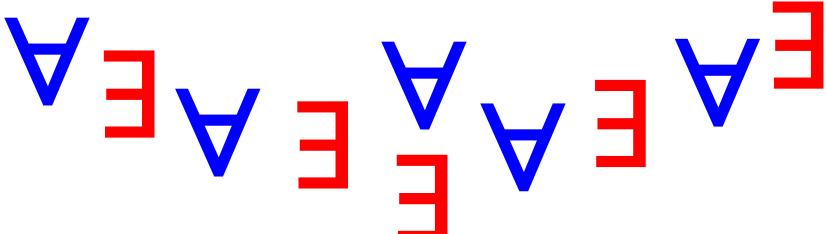
# CS 115 Functional Programming



Lecture 18:

**Existential Types** 









## **Today**

- Existential types
- The Typeable type class
- The cast function
- Applications:
  - "Interfaces" (like in Java)
  - Simulating dynamic typing
  - Extensible exceptions and the Control. Exception module





#### **Motivation**

- Haskell type classes give Haskell programmers great power to express features that many otherwise unrelated types may contain
- Classic example: every instance of Num must be something that can be added, multiplied, negated, etc.
- Often people say that Haskell's type classes are "sort of like Java interfaces" in this respect
- However, they really aren't like Java interfaces in one critical aspect





#### **Motivation**

- Java programmers can express the notion of "a collection of items, each of which implements a particular interface but which may otherwise be of different types"
- This is not possible in basic Haskell!
- You can have a collection all of whose elements are instances of a type class e.g.

```
addList :: Num a => [a] -> a
```

- Here, all elements of type a are instances of Num
- But there is an additional constraint here what?





#### **Motivation**

#### addList :: Num a => [a] -> a

- All elements of the list must have the same type (type a)!
- This is a very severe restriction
- It prevents us from using collections in many situations where we would like to use them
- Any ideas of how we could try to overcome this limitation?





#### List of arbitrary types

 We could define a new datatype where every instance of the datatype is an instance of e.g. the Num type class:

```
data Value =
    IntVal Integer
    | FloatVal Float
    | RationalVal Rational -- from Data.Ratio
    | ComplexVal Complex -- from Data.Complex
    | ...
```

Problems with this approach?





#### List of arbitrary types

```
data Value =
    IntVal Integer
    | FloatVal Float
    | RationalVal Rational -- from Data.Ratio
    | ComplexVal Complex -- from Data.Complex
    | ...
```

 If we want to extend the type, we have to add more constructors and rewrite all code using the datatype!



#### List of arbitrary types

```
data Value =
    IntVal Integer
    | FloatVal Float
    | RationalVal Rational -- from Data.Ratio
    | ComplexVal Complex -- from Data.Complex
    | ...
```

- So this approach is not very flexible
- Existential types provide a much better alternative when you want to write code that will not have to be rewritten when new types are added to the datatype





- Let's start with a simple example: how do we define a datatype which can hold any value as long as it's an instance of type class Show?
  - Note: this used to require a GHC extension called
     ExistentialQuantification
  - Now this extension is enabled by default





Here's our datatype:

data Showable = forall a . Show a => Showable a

- Some points to make about this:
- 1) The name of a constructor of a type can be the same as the name of the type (different namespaces)
- 2) The type variable a found in the datatype is not found outside the constructor (Showable is a type, not a type constructor)





Now we can define our datatype:

```
data Showable = forall a . Show a => Showable a
```

- The forall word is confusing, since it's usually considered to mean universal quantification, not existential quantification
- Intuition: can have any value as an argument to the Showable constructor, as long as its type is an instance of type class Show (it works "for all" types that are instances of type class Show)





data Showable = forall a . Show a => Showable a

- You can also think of it as "a Showable value asserts that there exists a value which is an instance of Show"
- Either way, it allows any value whose type is an instance of Show to be an argument to the Showable constructor



```
data Showable = forall a . Show a => Showable a
```

- Note also the overloading of the dot (.) syntax to mean something other than what we've seen so far:
  - the function composition operator
  - module qualification (e.g. Data.List.init)
- In fact, normal polymorphic types have an implicit forall before the type signature:

```
length :: forall a . [a] -> Int
```

meaning universal quantification in this case





```
data Showable = forall a . Show a => Showable a
```

Here are valid elements of this type:

```
Showable (10 :: Int)
Showable "foo"
Showable '\n'
Showable True
```

We can form lists of Showables:

```
[Showable 10, Showable "foo", Showable '\n']
```

This has the type [Showable]





 We might want to make this type an instance of Show, but this won't work:

```
data Showable = forall a . Show a => Showable a
  deriving (Show)
```

 GHC is not able to automatically derive a Show instance here, so you have to define one manually:

```
instance Show Showable where
  show (Showable s) = "Showable " ++ show s
```





Now you can type Showables into ghci:

```
ghci> Showable 10
Showable 10
ghci> Showable "foo"
Showable "foo"
ghci> [Showable 10, Showable "foo"]
[Showable 10, Showable "foo"]
```





- OK, so now we can put values of different types into a list as long as they are instances of the same type class
- Question: what can we do with this list?
- Answer: all we can do is to show the elements of the list (convert them to strings) because that is all we know about the list elements!



#### Java-like "interfaces"

 This use of existential types is precisely what you get with Java interfaces!



## Java-like "interfaces"

- This use of existential types is precisely what you get with Java interfaces!
- Java:
  - An interface represents a set of operations that a datatype (class) may implement
  - Can have collections of objects implementing a particular interface
  - All you can do with members of these collections is apply the methods of the interface



## Java-like "interfaces"

- This use of existential types is precisely what you get with Java interfaces!
- Haskell with existential types:
  - A type class represents a set of operations that a type may implement
  - Can have collections of objects implementing a particular type class (with existentials)
  - All you can do with members of these collections is apply the methods of the type class



#### Significance

- Although Haskell is not an object-oriented language...
- ...with existentials, you get the most important feature of OO languages (interfaces)
- Note, though, that many uses of interfaces in Java can be handled through normal use of type classes in Haskell (resolved at compile time, not run time)
- But "collections of arbitrary types implementing an interface" requires existential types in Haskell
- Only use this when ordinary uses of type classes are insufficient





#### Beyond interfaces

- In addition to interfaces, Java also has the notion of a base Object class that is a superclass of every other class (i.e. every instance of any class is also an instance of the Object class)
- Java can automatically "cast" an instance of a class to any of its superclasses (guaranteed to succeed)
- Java programmers can also manually cast an instance of a class to any of its subclasses
  - not guaranteed to succeed; get a ClassCastException if not successful
- Can we do these things in Haskell?





#### The Typeable type class

- Haskell is not an OO language, so if we can do these things, the form of the solution will necessarily be different
- The key ingredient is a special type class called
   Typeable
- This is the most general type class of all; it imposes almost no restrictions on its instances!
- It will be possible to cast Haskell values which are Typeable from one type to another (possibly failing)





#### The Typeable type class

 The Typeable type class is defined in the module Data. Typeable as follows:

```
class Typeable a where
typeOf :: a -> TypeRep
```

- TypeRep is a concrete representation of a type that can be compared for equality efficiently (details aren't important)
- This gives Haskell the ability to take two values, compute their TypeReps, and compare them to see if two values are of the same type





#### The Typeable type class

• Example:

```
ghci> import Data.Typeable
ghci> typeOf (10 :: Int) == typeOf (10 :: Integer)
False
ghci> typeOf (10 :: Int) == typeOf (43 :: Int)
True
```

- GHC can also automatically derive instances of the Typeable type class for any new datatype
  - have to add deriving (Typeable) to the data definition





## Casting

 Inside the Data. Typeable module there is this amazing function:

```
cast :: (Typeable a, Typeable b) => a -> Maybe b
```

- Meaning: if a and b are two types that are instances
  of Typeable, then you can try to cast an object of
  type a to an object of type b, and it may or may not
  succeed
- The implementation of this uses an extremely unsafe function called unsafeCoerce that we don't have to worry about
  - cast itself is safe (phew!)





## Application: dynamic typing

- Haskell is a statically-typed language
- Dynamically-typed languages like Scheme or Python can sometimes be more convenient than statically-typed languages
- Good news! With the Typeable class and casting, we can simulate dynamic typing in Haskell!
- Let's define a multiplication function that can work on arbitrary types
  - will be able to multiply Ints and Floats, Ints and Strings, etc.





#### The Dyn existential type

• First, define a dynamic type **Dyn**:

```
data Dyn = forall a . Typeable a => Dyn a
```

 This works, but it's convenient to restrict it to types which also implement Show:

```
data Dyn = forall a . (Show a, Typeable a) => Dyn a
```

 These are existential types, so we need this pragma at the beginning of the file:

```
{-# LANGUAGE ExistentialQuantification #-}
```





#### The Dyn existential type

 We would like our Dyn type to be an instance of Show, but again, GHC can't automatically derive this for existential types, so we write our own instance:

```
instance Show Dyn where
  show (Dyn x) = "Dyn " ++ show x
```

 Now we can enter Dyn values into ghci and see them printed out:

```
ghci> Dyn "foo"
Dyn "foo"
```





#### Type representations

 Let's define some type representations for convenience:

```
int :: TypeRep
int = typeOf (0 :: Integer)

double :: TypeRep
double = typeOf (0 :: Double)

string :: TypeRep
string = typeOf ("a" :: String)
```





#### Dynamic functions

 With what we know now, we can define dynamic functions:

 cast returns a Maybe type, which we convert to a regular type using fromJust (will succeed here)





#### Aside: fromJust

 Here is the definition of fromJust (from the module Data.Maybe):

```
-- The 'fromJust' function extracts the

-- element out of a 'Just' and throws an error

-- if its argument is 'Nothing'.

fromJust :: Maybe a -> a

fromJust Nothing = error "Maybe.fromJust: Nothing"

fromJust (Just x) = x
```





# Simplifying (I)

- This approach works, but it's way too tedious to use in practice
- Let's define some helper functions to make this easier to use

```
get :: (Typeable a, Typeable b) => a -> b
get = fromJust . cast
```

- get is used like cast, except that you only use it when you know that types a and b are the same
  - because their TypeReps are the same!
  - the cast will always succeed, so cast will always return a
     Just value





#### Simplifying (I)

Our previous example now becomes:

```
mul :: Dyn -> Dyn -> Dyn
mul (Dyn i) (Dyn j) =
  let ti = typeOf i
    tj = typeOf j
  in if ti == int && tj == int
    then Dyn (get i * get j :: Integer)
    else ... (other cases)
```



# Simplifying (2)

- We still need to get rid of the nested if statements for multiple cases
- Can't use a case statement with different types
   (can't pattern match on a TypeRep because its data
   representation is not exported (it's an abstract type))
- Instead, we will define a function called cond that behaves like nested if/else forms (like cond in Scheme)



# Simplifying (2)

- We will represent cases of the cond form as pairs of type representations, along with the code to execute if the input types match
- Signature:

```
cond :: (TypeRep, TypeRep) ->
[((TypeRep, TypeRep), Dyn)] -> Dyn
```

 Given a pair of input TypeReps and a list of things to do given matching TypeRep pairs, find the one to execute and return the corresponding Dyn value



- We can take advantage of the lookup function in the Data.List module, which looks for a key in a list of key/value pairs
- Given that, cond is easy to define:

```
cond :: (TypeRep, TypeRep) ->
  [((TypeRep, TypeRep), Dyn)] -> Dyn
cond ts assoc =
  case lookup ts assoc of
    Just d -> d
  Nothing -> Dyn () -- default case
```





 Now our original function can easily be given different cases:

```
mul :: Dyn -> Dyn -> Dyn
mul (Dyn i) (Dyn j) =
  cond (typeOf i, typeOf j) $
    [((int, int), Dyn (get i * get j :: Integer)),
     ((double, double), Dyn (get i * get j :: Double)),
     ((int, double),
      Dyn (fromInteger (get i) * get j :: Double)),
     ((double, int),
      Dyn (get i * fromInteger (get j) :: Double)),
     ((int, string), Dyn (mulString (get i) (get j))),
     ((string, int), Dyn (mulString (get j) (get i)))]
```





Multiply integer \* integer:

```
mul :: Dyn -> Dyn -> Dyn
mul (Dyn i) (Dyn j) =
 cond (typeOf i, typeOf j) $
    [((int, int), Dyn (get i * get j :: Integer)),
     ((double, double), Dyn (get i * get j :: Double)),
     ((int, double),
      Dyn (fromInteger (get i) * get j :: Double)),
     ((double, int),
      Dyn (get i * fromInteger (get j) :: Double)),
     ((int, string), Dyn (mulString (get i) (get j))),
     ((string, int), Dyn (mulString (get j) (get i)))]
```





Multiply double \* double:

```
mul :: Dyn -> Dyn -> Dyn
mul (Dyn i) (Dyn j) =
 cond (typeOf i, typeOf j) $
    [((int, int), Dyn (get i * get j :: Integer)),
     ((double, double), Dyn (get i * get j :: Double)),
     ((int, double),
      Dyn (fromInteger (get i) * get j :: Double)),
     ((double, int),
      Dyn (get i * fromInteger (get j) :: Double)),
     ((int, string), Dyn (mulString (get i) (get j))),
     ((string, int), Dyn (mulString (get j) (get i)))]
```





Multiply int \* double and double \* int:

```
mul :: Dyn -> Dyn -> Dyn
mul (Dyn i) (Dyn j) =
 cond (typeOf i, typeOf j) $
    [((int, int), Dyn (get i * get j :: Integer)),
     ((double, double), Dyn (get i * get j :: Double)),
     ((int, double),
      Dyn (fromInteger (get i) * get j :: Double)),
     ((double, int),
      Dyn (get i * fromInteger (get j) :: Double)),
     ((int, string), Dyn (mulString (get i) (get j))),
     ((string, int), Dyn (mulString (get j) (get i)))]
```





"Multiply" int \* string and string \* int:

```
mul :: Dyn -> Dyn -> Dyn
mul (Dyn i) (Dyn j) =
 cond (typeOf i, typeOf j) $
    [((int, int), Dyn (get i * get j :: Integer)),
     ((double, double), Dyn (get i * get j :: Double)),
     ((int, double),
      Dyn (fromInteger (get i) * get j :: Double)),
     ((double, int),
      Dyn (get i * fromInteger (get j) :: Double)),
     ((int, string), Dyn (mulString (get i) (get j))),
     ((string, int), Dyn (mulString (get j) (get i)))]
```





- "Multiply" int \* string and string \* int
- These use the mulString function defined as:

```
mulString :: Integer -> String -> String
mulString n s = concat (replicate (fromInteger n) s)
```

This concatenates a string with itself n times:

```
ghci> mulString 3 "foo"
"foofoofoo"
```

This is the Python notion of string "multiplication"





## **Testing**

#### Some tests:

```
ghci> mul (Dyn (5 :: Integer)) (Dyn (13 :: Integer))
Dyn 65
ghci> mul (Dyn (5 :: Integer)) (Dyn (13 :: Double))
Dyn 65.0
ghci> mul (Dyn (5 :: Double)) (Dyn (13 :: Double))
Dyn 65.0
ghci> mul (Dyn (5 :: Integer)) (Dyn "foo")
Dyn "foofoofoofoo"
ghci> mul (Dyn (5 :: Int)) (Dyn "foo")
Dyn ()
```





#### Exceptions revisited

- One nice use of existential types in Haskell is to define standard Haskell exceptions
- These can be "thrown" from any code, but can only be caught in the IO monad
  - If you need exceptions that can be caught in functional code, you need error-handling monads (last two lectures)
- These exceptions are called "extensible exceptions" and the code is in the Control. Exception module



- These exceptions are called "extensible" because you can take nearly any type and make it into an exception type
- The only requirements on the type are that it be an instance of the Typeable and Show type classes
- The system will also use the cast function from Data. Typeable to extract exceptions from a generic exception type



- The basic exception type is called SomeException
- It has this definition:

```
data SomeException =
  forall e . Exception e => SomeException e
  deriving Typeable
```

- We can see that it's an existential type
- Any datatype that is an instance of the Exception type class can be made into a SomeException value
- So what is the Exception type class?





Here it is:

```
class (Typeable e, Show e) => Exception e where
    toException :: e -> SomeException
    fromException :: SomeException -> Maybe e
    -- default definitions:
    toException = SomeException
    fromException (SomeException e) = cast e
```

Key points:



Here it is:

```
class (Typeable e, Show e) => Exception e where
    toException :: e -> SomeException
    fromException :: SomeException -> Maybe e
    -- default definitions:
    toException = SomeException
    fromException (SomeException e) = cast e
```

- Key points:
  - Exception instances must be instances of Typeable and Show



Here it is:

```
class (Typeable e, Show e) => Exception e where
    toException :: e -> SomeException
    fromException :: SomeException -> Maybe e
    -- default definitions:
    toException = SomeException
    fromException (SomeException e) = cast e
```

- Key points:
  - To turn a suitable value into an exception, wrap it with the SomeException constructor



Here it is:

```
class (Typeable e, Show e) => Exception e where
    toException :: e -> SomeException
    fromException :: SomeException -> Maybe e
    -- default definitions:
    toException = SomeException
    fromException (SomeException e) = cast e
```

- Key points:
  - To turn an exception back into its constituent value, use the cast function (from Data. Typeable)





We'll define a new exception type called
 MyException that can hold a String value:

```
data MyException = MyException String
  deriving (Show, Typeable)
```

 The default definitions of the Exception type class work fine for this type, so to make it an instance of Exception we only have to do this:

```
instance Exception MyException
```

-- no method definitions!





 Now we can throw and catch exceptions of type MyException:

 The type signature in (e :: MyException) has a very important role: it will cause the function to only catch exceptions of MyException type, but propagate all other exceptions





- Typical case: want to catch more than one kind of exception
- Solution: use a function called catches, with this type signature:

```
catches :: IO a -> [Handler a] -> IO a
```

 Intuition: given an IO computation, and a list of exception handlers, return an IO computation that handles the exceptions corresponding to the handlers





 The Handler type itself is an existential type with this definition:

```
data Handler a =
  forall e . Exception e => Handler (e -> IO a)
```

 When an exception is thrown, catches will try each Handler in turn until it finds one whose exception matches the provided type signature, then it will execute the corresponding IO action



Example use of catches:

```
f = expr `catches`
[Handler (\(ex :: ArithException) -> handleArith ex),
Handler (\(ex :: IOException) -> handleIO ex)]
```

- If expr throws an ArithException exception, then handleArith handler will be called
- If expr throws an IOException exception, then handleIO handler will be called



#### Notice...

- The exception handling system is implemented purely as a Haskell module, not hard-wired into the language
- Haskell's primitive features (type classes,
   Typeable, etc.) are powerful enough to allow users
   to implement many features that would have to be
   written into most languages as primitives



### Summary

- Although Haskell is a statically-typed language, sometimes we might want more dynamism than such languages usually provide
- Existential types provide a big "escape hatch" into more dynamic forms of programming just like the IO monad provides a big "escape hatch" into imperative forms of programming



## Summary

- I would like to claim that "Haskell is the world's best dynamic programming language", but I don't think it's quite true
- What is true is that you don't have to give up all features you enjoyed in dynamically-typed programming languages just because you're using Haskell
- Haskell's type system is very flexible ©





## Coming up

State monads!

