hw3

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0.1 Utility functions to facilitate computations

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In [48]: def nand(a, b):
             return not a & b
In [49]: def _and(a, b):
             return a & b
In [50]: def _or(a, b):
             return a | b
In [51]: def nor(a, b):
             return not a | b
0.2 Problem 3
In [52]: inputs = [(0, 0, 0),
                    (0, 0, 1),
                    (0, 1, 0),
                    (0, 1, 1),
                    (1, 0, 0),
                    (1, 0, 1),
                    (1, 1, 0),
                    (1, 1, 1)]
In [53]: for a, b, c in inputs:
             print((a & b) | (b & c) | (a & c))
0
0
0
1
0
1
1
```

1

```
0.3 Problem 4
```

```
In [54]: inputs = [(0, 0),
                    (1, 0),
                    (0, 1),
                    (1, 1)
In [55]: for a, b in inputs:
             print( not ((a & b) | ((not a) & (not b))) )
False
True
True
False
0.4 Problem 5
In [56]: def circuit(s, i3, i2, i1, i0):
             o3 = \_and(not s, i2)
             o2 = \_or(\_and(s, i3), \_and(not s, i1))
             o1 = _{or}(_{and}(i2, s), _{and}(_{not} s, i0))
             o0 = \_and(i1, s)
             return 03, 02, 01, 00
In [57]: circuit(1, 1, 0, 1, 1)
Out [57]: (0, 1, 0, 1)
0.5 Problem 6
In [58]: inputs = [(0, 0),
                    (1, 0),
                    (0, 1),
                    (1, 1)]
In [59]: for a, b in inputs:
             print(nand(nand(a, nand(a, b)), nand(b, nand(a, b))))
False
True
True
False
0.6 Problem 7
In [38]: def circuit(a, b):
              return _or(_and(not a, b), _and(not b, a))
```

```
In [39]: for a, b in inputs:
             for c in [0, 1]:
                 print(circuit(circuit(a, b), c))
0
1
1
0
1
0
0
1
0.7 Problem 8
In [45]: inputs = [(0, 0, 0),
                    (0, 0, 1),
                    (0, 1, 0),
                    (0, 1, 1),
                    (1, 0, 0),
                    (1, 0, 1),
                    (1, 1, 0),
                    (1, 1, 1)]
In [47]: for a, b, c in inputs:
             print(_or(_and(not b, not c), _and(b, c)))
1
0
0
1
1
0
0
1
```