



# CLOUD COMPUTING CONCEPTS

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## GOSSIP

Lecture C

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GOSSIP ANALYSIS

# PROPERTIES

Claim that the simple Push protocol

- Is lightweight in large groups
- Spreads a multicast quickly
- Is highly fault-tolerant

# ANALYSIS

From old mathematical branch of *Epidemiology* [Bailey 75]

- Population of  $(n+1)$  individuals mixing homogeneously
- Contact rate between any individual pair is  $\beta$
- At any time, each individual is either uninfected (numbering  $x$ ) or infected (numbering  $y$ )
- Then,  $x_0 = n, y_0 = 1$   
and at all times  $x + y = n + 1$
- Infected–uninfected contact turns latter infected, and it stays infected

# ANALYSIS (CONTD.)

- Continuous time process
- Then

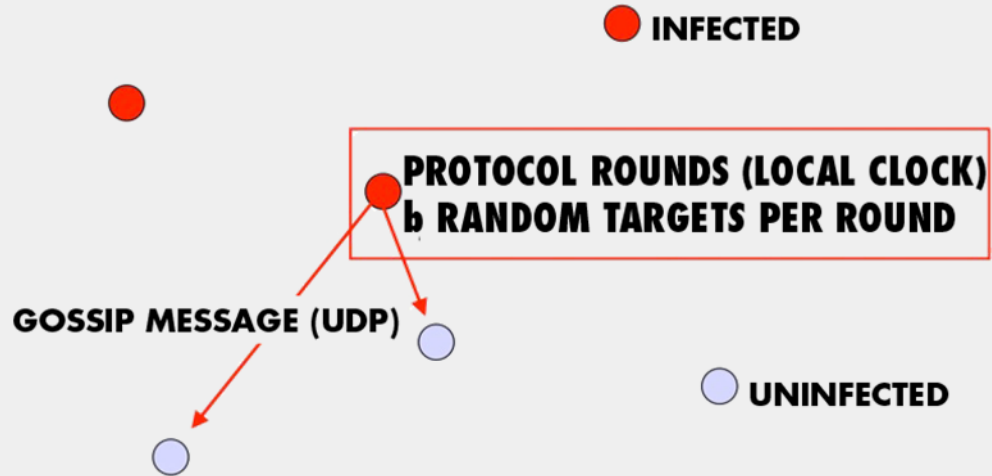
$$\frac{dx}{dt} = -\beta xy \quad (\text{why?})$$

with solution:

$$x = \frac{n(n+1)}{n + e^{\beta(n+1)t}}, \quad y = \frac{(n+1)}{1 + ne^{-\beta(n+1)t}}$$

(can you derive it?)

# EPIDEMIC MULTICAST



# EPIDEMIC MULTICAST ANALYSIS

$$\beta = \frac{b}{n} \quad (\text{why?})$$

Substituting, at time  $t=c\log(n)$ , the number of infected is

$$y \approx (n+1) - \frac{1}{n^{cb-2}}$$

(correct? can you derive it?)

# ANALYSIS (CONTD.)

- Set  $c, b$  to be small numbers independent of  $n$
- Within  $c \log(n)$  rounds, **[low latency]**
  - all but  $\frac{1}{n^{cb-2}}$  number of nodes receive the multicast  
**[reliability]**
- each node has transmitted no more than  $cb \log(n)$  gossip messages **[lightweight]**

# WHY IS LOG(N) LOW?

- $\text{Log}(N)$  is not constant in theory
- But pragmatically, it is a very slowly growing number
- Base 2
  - $\text{Log}(1000) \sim 10$
  - $\text{Log}(1\text{M}) \sim 20$
  - $\text{Log}(1\text{B}) \sim 30$
  - $\text{Log}(\text{all IPv4 address}) = 32$



# FAULT-TOLERANCE

- Packet loss
  - 50% packet loss: analyze with  $b$  replaced with  $b/2$
  - To achieve same reliability as 0% packet loss, takes twice as many rounds
- Node failure
  - 50% of nodes fail: analyze with  $n$  replaced with  $n/2$  and  $b$  replaced with  $b/2$
  - Same as above

# FAULT-TOLERANCE

- With failures, is it possible that the epidemic might die out quickly?
  - Possible, but improbable:
    - Once a few nodes are infected, with high probability, the epidemic will not die out
    - So the analysis we saw in the previous slides is actually behavior *with high probability*
- [Galey and Dani 98]
- Think: Why do rumors spread so fast? Why do infectious diseases cascade quickly into epidemics? Why does a virus or worm spread rapidly?

# PULL GOSSIP: ANALYSIS

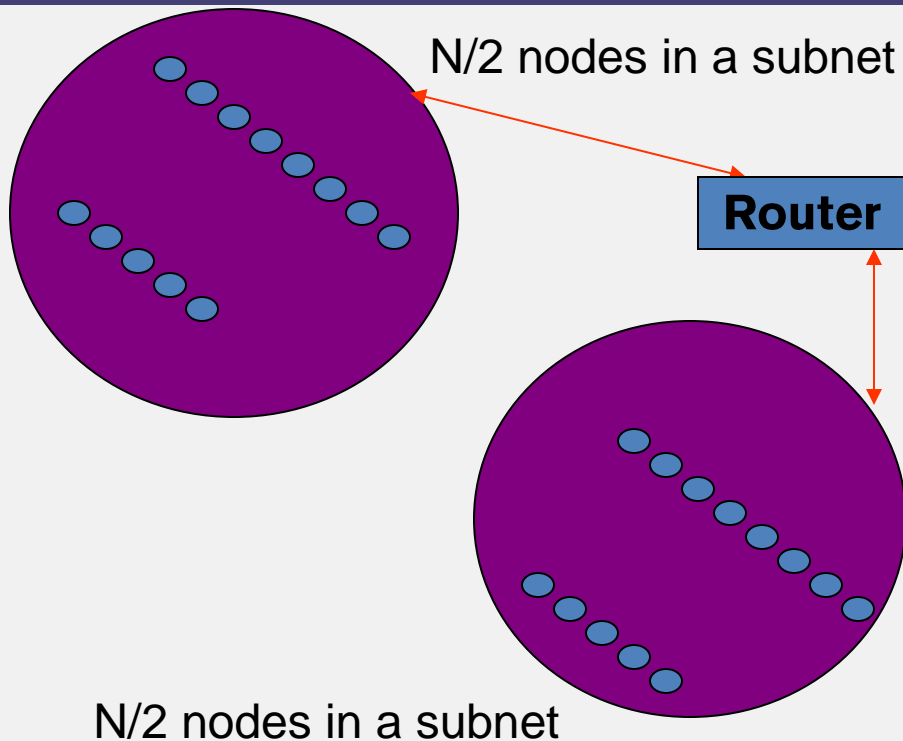
- In all forms of gossip, it takes  $O(\log(N))$  rounds before about  $N/2$  gets the gossip
  - Why? Because that's the fastest you can spread a message – a spanning tree with fanout (degree) of constant degree has  $O(\log(N))$  total nodes
- Thereafter, pull gossip is faster than push gossip
- After the  $i$ th, round let  $p_i$  be the fraction of non-infected processes. Then ( $k$ =number of gossip pulls per round per process)

$$p_{i+1} = (p_i)^{k+1}$$

- This is super-exponential
- Second half of pull gossip finishes in time  $O(\log(\log(N)))$

# TOPOLOGY-AWARE GOSSIP

- Network topology is hierarchical
- Random gossip target selection  $\Rightarrow$  core routers face  $O(N)$  load (Why?)
- **Fix:** In subnet  $i$ , which contains  $n_i$  nodes, pick gossip target in your subnet with probability  $1/n_i$
- Router load  $= O(1)$
- Dissemination time  $= O(\log(N))$
- Why?



# ANSWER – PUSH ANALYSIS (CONTD.)

Using:  $\beta = \frac{b}{n}$

Substituting, at time  $t=c\log(n)$

$$\begin{aligned} y &= \frac{n+1}{1 + ne^{-\frac{b}{n}(n+1)c\log(n)}} \approx \frac{n+1}{1 + \frac{1}{n^{cb-1}}} \\ &\approx (n+1)\left(1 - \frac{1}{n^{cb-1}}\right) \\ &\approx (n+1) - \frac{1}{n^{cb-2}} \end{aligned}$$