In fig. 5.8 finally, the magnetic trap has been switched off and the atoms rest inside the dipole trap, slightly skewed by gravity.

### 5.2 Loading into the hybrid trap

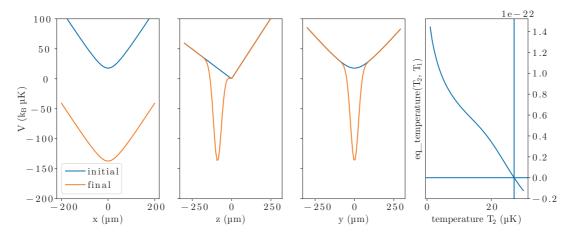
#### 5.2.1 Adiabatic temperature change

Observing the changes in atom density has already hinted at the fact that temperature changes will be expected while changing from one potential to another. These changes will happen adiabatically in the experiment, and since we deal with temperatures  $\sim 5 \,\mu\text{K}$  in this step, classical thermodynamics allows us to consider this process analytically. The following approach is based on the work in [Mel17] and will be used to first calculate the temperature change in a system of N noninteracting particles between two potentials  $V_1(\mathbf{r})$  and  $V_2(\mathbf{r})$ .

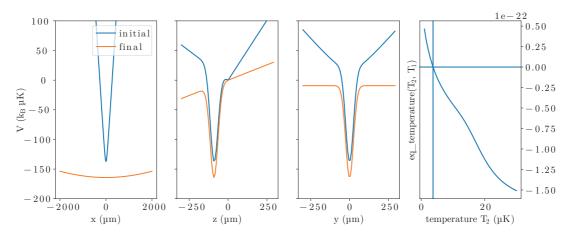
Calculating the entropy from a product of non-interacting single-particle partition functions and equating them, we find

$$0 \stackrel{!}{=} \frac{1}{T_1} \frac{J(T_1)}{I(T_1)} - \frac{1}{T_2} \frac{J(T_2)}{I(T_2)} - k_B \log \left( \frac{T_2^{3/2} I(T_2)}{T_1^{3/2} I(T_1)} \right). \tag{5.10}$$

A full derivation of this is done in the appendix section A.1.4. We have to solve this integral equation in order to obtain the temperature  $T_2$  of the cloud in the new potential  $V_2$ . An example of this is shown in fig. 5.9, where eq. 5.10 in dependence of  $T_2$  is plotted in the rightmost panel. We numerically find its root, which is the desired  $T_2$ .



**Figure 5.9:** Adiabatic change between the magnetic trap and hybrid trap potential (between figures 5.4 and 5.5). The figure shows the potential  $V(\mathbf{r})$  in three cuts around the trap minimum. The cloud heats up from  $10.0\,\mu\mathrm{K}$  to  $27.1\,\mu\mathrm{K}$  during this step, owing to the increased confinement in the hybrid trap. The panel on the very right plots eq. 5.10 and its root.



**Figure 5.10:** Adiabatic change between the hybrid and pure dipole potential (figures 5.5 and 5.8). The cloud cools from  $10.0 \,\mu\text{K}$  to  $3.7 \,\mu\text{K}$  during this, owing to its axial expansion (leftmost panel).

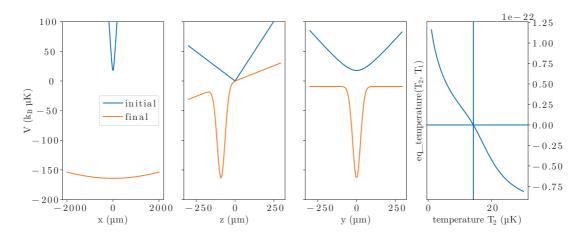


Figure 5.11: Whole transfer cycle: Adiabatic change between the magnetic and pure dipole trap potential (between figures 5.4 and 5.8). The cloud heats from  $10.0\,\mu\mathrm{K}$  to  $14.2\,\mu\mathrm{K}$  during this step due to the combined effects of the two previous figures.

This powerful tool gives us the ability to systematically assess and optimise the effects of different experimental parameters on the heating or cooling of the atom cloud. The most crucial ones for the shape of the potential are the current through the quadrupole coils and the laser power, which are shown in fig. 5.12. We can see that for increasing dipole power, the heating of the cloud changes rather drastically. This is due to the increased confinement within the optical trap, which imparts energy on the atoms. The magnetic field on the other hand appears to have little effect on the temperature change, as it only slightly skews the dipole beam potential.

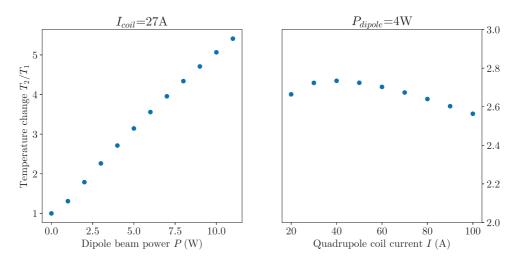


Figure 5.12: Temperature change over the first part of the cycle, for a dipole beam of waists  $w_{y,z} = 50 \, \mu \mathrm{m}$ .

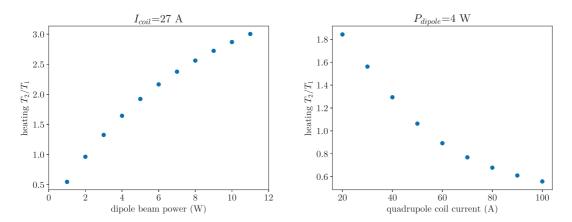


Figure 5.13: Temperature change over the whole cycle, for a dipole beam of waists  $w_{y,z}=50\,\mu\mathrm{m}$ . Note that the dipole beam is the only confining potential after this, such that  $P_{\mathrm{dipole}}\to 0$  approaches an untrapped system.

#### 5.2.2 Fraction of transferred atoms

Another interesting data point is the fraction  $\eta$  of atoms which still remains in the trap after the swift change between two trapping potentials  $V_1(\mathbf{r})$  and  $V_2(\mathbf{r})$ . As is shown in fig. 5.14, we assume a Maxwell–Boltzmann distribution of kinetic energies,

$$f(E_{\rm kin}) = 2\sqrt{\frac{E_{\rm kin}}{\pi}} \left(\frac{1}{k_B T}\right)^{3/2} \exp\left(-\frac{E_{\rm kin}}{k_B T}\right). \tag{5.11}$$

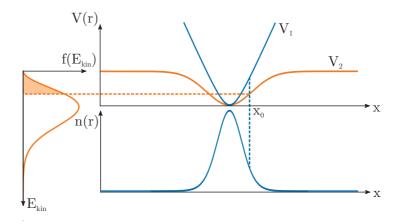
This holds also in the case of an external potential, as the potential does not influence the momentum distribution. We are looking for the fraction of atoms in the initial potential  $V_1$  which has less kinetic energy than the depth of the final potential  $V_2$ . For any given

point **r** in space we find the fraction of atoms with  $E_{\rm kin} < V_2({\bf r})$  to be

$$\eta(\mathbf{r}) \equiv \int_0^{-V_2(\mathbf{r})} f(E) dE. \tag{5.12}$$

As  $V_2$  will be negative, we need to add a sign here. We then have to multiply by the normalised atom density  $n(\mathbf{r})$  from eq. 5.6 and integrate over all space to find the overall transferred fraction

$$\eta = \int d^3 r \, n(\mathbf{r}) \eta(\mathbf{r}). \tag{5.13}$$

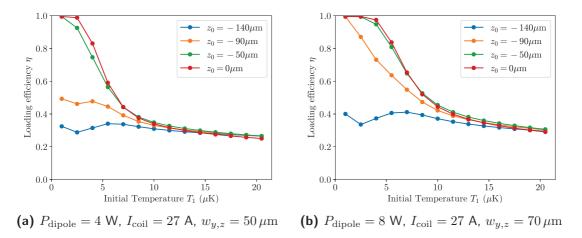


**Figure 5.14:** Schematic depiction of the algorithm to obtain the fraction  $\eta$  of atoms which is still trapped after a transition from  $V_1$  to  $V_2$ . The fraction of the shaded area is  $\eta(\mathbf{r})$  which gets multiplied by the value of the normalised density  $n(\mathbf{r})$ , and we integrate all these values over space.

This was done numerically, the results of which can be found in fig. 5.15 for several initial cloud temperatures  $T_1$ . We can observe that the transfer efficiency strongly decreases with increasing temperature. This effect is not too detrimental though, as this favours colder atoms to be transferred and thereby achieves a net cooling effect. Note that before the transfer efficiency was calculated, the cooling of the cloud due to its axial expansion (see fig. 5.10) was taken into account. Figure 5.15 tells us that if we choose the frequency sweep in the radiofrequency evaporation phase according to a specific final temperature, we can in principle achieve an arbitrary transfer efficiency when loading into the dipole trap.

Due to gravity, the atom cloud tends to be centred vertically below the magnetic field zero, which increases the loading efficiency for small temperatures, as can be seen by comparison with fig. A.2. These results inform our choice of displacement  $z_0$  and trap beam waists  $w_{y,z}$ : where fig. 5.15 suggests that  $z_0 = -50 \,\mu\text{m}$  would be a better choice, this of course results in increased Majorana losses (cf. fig. 5.5). A wider trap with  $w_{y,z} = 70 \,\mu\text{m}$  of course favours loading for all temperatures, but requires a beam of twice the power in order to achieve the same trap depth. Whether this is feasible will mainly be decided by whether the focus-tunable lenses discussed in section 2.5 induce significant aberrations at

these powers, and also whether the increased Rayleigh range  $z_R$  that comes with it still enables efficient transport. This will be the topic of the next section.



**Figure 5.15:** Transfer efficiency for the whole loading cycle (from magnetic trap into pure dipole trap) in dependence of the initial cloud temperature  $T_1$ , for several beam offsets  $z_0$ . This takes into account the cloud heating which this process involves. We can observe the dependence on the trap width: For a slightly wider trap (b), the loading efficiency stays large even for higher  $T_1$ , but to get the same trap depth we require a more powerful beam. Another interesting observation is that a bigger  $z_0$  favours the small temperature loading rate due to gravity. The connecting lines are guides to the eye.

## 5.3 Counterdiabatic driving

After the loading of the hybrid trap is completed and the magnetic quadrupole field is switched off, we want to translate the cloud of atoms from the 3D MOT chamber to the science chamber (see fig. 4.1). The distance between those is approximately d=400 mm, although this value has not been finalised yet. In order to achieve this, the focus tunable lenses from section 2.5 will be utilised to axially shift the focus of the dipole beam. As was discussed there, this does not affect its transversal waist, thereby also conserving the Rayleigh range  $z_{\rm R}$ , i.e. the axial trap frequency. In the following, we want to find the effect of the translation on the trapping potential and point out how to remedy its effect, assuming the trap is approximated in second order by a harmonic potential of frequency  $\omega$ . We further assume the transport of a cloud of thermal (uncondensed) atoms at  $T \sim 10 \,\mu{\rm K}$ . Note that this is only  $\sim 8\%$  of the trap depth and hence allows for a classical treatment of this problem.

For the sake of arriving at an adiabaticity condition for the translation, let us consider the case of a trap that is accelerated with a during the first half (for  $t < t_f/2$ ) and -a during the second half of the protocol (for  $t > t_f/2$ ). In such a protocol, the average velocity has half of its maximal value at  $t = t_f/2$ , i.e.  $d/t_f = \bar{v} = v_{\text{max}}/2$ . We now require that within an oscillation period  $T_{\text{osc}} = 2\pi/\omega$ , the trap move over much less than

# Bibliography

- [Alb15] A. Alberti et al., Super-resolution microscopy of single atoms in optical lattices. New Journal of Physics 18, 053010 (2015) (cit. on p. 27).
- [And73] P. W. Anderson, Resonating valence bonds: A new kind of insulator? Materials Research Bulletin 8, 153 (1973) (cit. on p. 6).
- [And95] M. H. Anderson et al., Observation of Bose-Einstein Condensation in a Dilute Atomic Vapor. Science 269, 198 (1995) (cit. on p. 3).
- [Bak09] W. S. Bakr et al., A quantum gas microscope for detecting single atoms in a Hubbard-regime optical lattice. Nature **462**, 74 (2009) (cit. on p. 4).
- [Bal10] L. Balents, Spin liquids in frustrated magnets. Nature **464**, 199 (2010) (cit. on p. 5).
- [Bol16] M. Boll et al., Spin- and density-resolved microscopy of antiferromagnetic correlations in Fermi-Hubbard chains. Science **353**, 1257 (2016) (cit. on p. 8).
- [Bra13] S. Braun et al., Negative absolute temperature for motional degrees of freedom. Science **339**, 52 (2013) (cit. on pp. 9, 32).
- [Bra15] C. Braun, Implementation of a Raman Sideband Cooling for 87Rb. B.Sc. thesis. Universität Stuttgart, 2015 (cit. on p. 16).
- [Bur97] E. A. Burt et al., Coherence, correlations, and collisions: What one learns about Bose-Einstein condensates from their decay. Physical Review Letters **79**, 337 (1997) (cit. on pp. 51, 52).
- [Cat06] J. Catani et al., Intense slow beams of bosonic potassium isotopes. Physical Review A - Atomic, Molecular, and Optical Physics 73, 033415 (2006) (cit. on p. 36).

[Che14] D. Chen, Anti-Helmholtz magnetic trap Electromagnetism review. 2014. URL: http://publish.illinois.edu/davidchen/files/2012/10/Anti-Helmholtz-magnetic-trap.pdf (cit. on p. 17).

- [Che15] L. W. Cheuk et al., Quantum-Gas Microscope for Fermionic Atoms. Physical Review Letters 114, 193001 (2015) (cit. on p. 4).
- [Chi10] C. Chin et al., Feshbach resonances in ultracold gases. Reviews of Modern Physics 82, 1225 (2010) (cit. on p. 32).
- [Cle76] C. L. Cleveland and R. Medina A., Obtaining a Heisenberg Hamiltonian from the Hubbard model. American Journal of Physics 44, 44 (1976) (cit. on p. 5).
- [Coh90] C. N. Cohen-Tannoudji and W. D. Phillips, New Mechanisms for Laser Cooling. Physics Today 43, 33 (1990) (cit. on p. 13).
- [Dav95] K. B. Davis et al., Observation of Bose-Einstein condensation in a gas of sodium Vapor. Physical Review Letters **75**, 3969 (1995) (cit. on p. 3).
- [De 09] M. A. De Vries et al., Scale-Free Antiferromagnetic Fluctuations in the s=1/2 Kagome Antiferromagnet Herbertsmithite. Physical Review Letters 103, 237201 (2009) (cit. on p. 32).
- [DeM99] B. DeMarco and D. S. Jin, Onset of Fermi Degeneracy in a Trapped Atomic Gas. Science 285, 1703 (1999) (cit. on p. 3).
- [Don99] X. Dong et al., Current-induced guiding and beam steering in active semiconductor planar waveguide. IEEE Photonics Technology Letters 11, 809 (1999) (cit. on p. 47).
- [Duf10] G. Dufour, Etude des collisions entre atomes froids de rubidium et un gaz chaud. Research report. University of British Columbia, Vancouver, 2010 (cit. on p. 34).
- [Ear42] S. Earnshaw, On the Nature of the Molecular Forces which Regulate the Constitution of the Luminiferous Ether. Trans. Camb. Phil. Soc. 7, 97 (1842) (cit. on p. 17).
- [Edg15] G. J. Edge et al., Imaging and addressing of individual fermionic atoms in an optical lattice. Physical Review A - Atomic, Molecular, and Optical Physics 92, 063406 (2015) (cit. on p. 4).
- [Esc03] J. Eschner et al., Laser cooling of trapped ions. Journal of the Optical Society of America B 20, 1003 (2003) (cit. on p. 16).

[Fey82] R. P. Feynman, Simulating Physics with computers. International Journal of Theoretical Physics 21, 467 (1982) (cit. on p. 1).

- [Foo05] C. J. Foot, Atomic Physics. Oxford University Press, USA (2005) (cit. on pp. 11, 13, 17, 19).
- [Fre94] J. K. Freericks and H. Monien, *Phase diagram of the Bose-Hubbard Model*. Europhysics Letters **26**, 545 (1994) (cit. on p. 2).
- [Fuh12] A. Fuhrmanek et al., Light-assisted collisions between a few cold atoms in a microscopic dipole trap. Physical Review A - Atomic, Molecular, and Optical Physics 85, 062708 (2012) (cit. on p. 23).
- [Gre02] M. Greiner et al., Quantum phase transition from a superfluid to a mott insulator in a gas of ultracold atoms. Nature 415, 39 (2002) (cit. on pp. 3, 6).
- [Gri00] R. Grimm, M. Weidemüller, and Y. B. Ovchinnikov, Optical Dipole Traps for Neutral Atoms. Advances in Atomic, Molecular and Optical Physics 42, 95 (2000) (cit. on pp. 19, 20).
- [Hal15] E. Haller et al., Single-atom imaging of fermions in a quantum-gas microscope. Nature Physics 11, 738 (2015) (cit. on p. 4).
- [Han12] T. H. Han et al., Fractionalized excitations in the spin-liquid state of a kagome-lattice antiferromagnet. Nature **492**, 406 (2012) (cit. on p. 9).
- [Ism16] N. Ismail et al., Fabry-Pérot resonator: spectral line shapes, generic and related Airy distributions, linewidths, finesses, and performance at low or frequency-dependent reflectivity. Optics Express 24, 16366 (2016) (cit. on p. 43).
- [Jak98] D. Jaksch et al., Cold bosonic atoms in optical lattices. Physical Review Letters 81, 3108 (1998) (cit. on p. 2).
- [Jo12] G.-B. Jo et al., Ultracold Atoms in a Tunable Optical Kagome Lattice. Physical Review Letters 108, 045305 (2012) (cit. on p. 9).
- [Jör08] R. Jördens et al., A Mott insulator of fermionic atoms in an optical lattice. Nature **455**, 204 (2008) (cit. on p. 3).
- [Kas92] M. Kasevich and S. Chu, Laser cooling below a photon recoil with three-level atoms. Physical Review Letters **69**, 1741 (1992) (cit. on p. 16).

[Ket99] W. Ketterle, D. S. Durfee, and D. M. Stamper-Kurn, Making, probing and understanding Bose-Einstein condensates. arXiv:9904034v2 (1999). URL: http://arxiv.org/abs/cond-mat/9904034 (cit. on p. 18).

- [Kno12] S. Knoop et al., Nonexponential one-body loss in a Bose-Einstein condensate. Physical Review A - Atomic, Molecular, and Optical Physics 85, 025602 (2012) (cit. on pp. 34, 52).
- [Lee06] P. A. Lee, N. Nagaosa, and X. G. Wen, Doping a Mott insulator: Physics of high-temperature superconductivity. Reviews of Modern Physics 78, 17 (2006) (cit. on pp. 3, 5).
- [Léo14] J. Léonard et al., Optical transport and manipulation of an ultracold atomic cloud using focus-tunable lenses. New Journal of Physics 16, 093028 (2014) (cit. on p. 22).
- [Lia17] H. J. Liao et al., Gapless Spin-Liquid Ground State in the S=1 /2 Kagome Antiferromagnet. Physical Review Letters 118, 1 (2017) (cit. on pp. 9, 32).
- [Lin09] Y. J. Lin et al., Rapid production of R 87 b Bose-Einstein condensates in a combined magnetic and optical potential. Physical Review A Atomic, Molecular, and Optical Physics 79, 063631 (2009) (cit. on p. 21).
- [Loh90] E. Y. Loh et al., Sign problem in the numerical simulation of many-electron systems. Physical Review B 41, 9301 (1990) (cit. on p. 32).
- [Maj32] E. Majorana, Atomi orientati in campo magnetico variabile. Nuovo Cimento 9, 43 (1932) (cit. on p. 18).
- [Maz17] A. Mazurenko et al., A cold-atom Fermi-Hubbard antiferromagnet. Nature 545, 462 (2017) (cit. on pp. 5, 8).
- [Mel] M. Melchner, private communication (cit. on p. 36).
- [Mel17] M. Melchner, An optical dipole trap for ultracold atomic gases. M.Sc. thesis. University of Cambridge, 2017 (cit. on pp. 57, 80).
- [Men08] C. Menotti and N. Trivedi, Spectral weight redistribution in strongly correlated bosons in optical lattices. Physical Review B - Condensed Matter and Materials Physics 77, 235120 (2008) (cit. on p. 2).
- [Men10] Z. Y. Meng et al., Quantum spin liquid emerging in two-dimensional correlated Dirac fermions. Nature **464**, 847 (2010) (cit. on p. 9).

[Met99] H. J. Metcalf and P. van der Straten, Laser Cooling and Trapping 1, 1 (1999) (cit. on p. 13).

- [Mir15] M. Miranda et al., Site-resolved imaging of ytterbium atoms in a two-dimensional optical lattice. Physical Review A - Atomic, Molecular, and Optical Physics 91, 1 (2015) (cit. on p. 4).
- [Mit18] D. Mitra et al., Quantum gas microscopy of an attractive Fermi-Hubbard system. Nature Physics 14, 173 (2018) (cit. on pp. 4, 8, 28).
- [Mod01] G. Modugno et al., Bose-Einstein condensation of potassium atoms by sympathetic cooling. Science **294**, 1320 (2001) (cit. on p. 23).
- [Nes08] J. Nes, Cold Atoms and Bose-Einstein Condensates in Optical Dipole Potentials. PhD thesis. Technische Universität Darmstadt, 2008 (cit. on p. 51).
- [Omr15] A. Omran et al., Microscopic Observation of Pauli Blocking in Degenerate Fermionic Lattice Gases. Physical Review Letters 115, 263001 (2015) (cit. on p. 4).
- [Par15] M. F. Parsons et al., Site-Resolved Imaging of Fermionic Li-6 in an Optical Lattice. Physical Review Letters 114, 213002 (2015) (cit. on p. 4).
- [Pet95] W. Petrich et al., Stable, tightly confining magnetic trap for evaporative cooling of neutral atoms. Physical Review Letters 74, 3352 (1995) (cit. on p. 21).
- [Pol10] A. Polkovnikov, *Phase space representation of quantum dynamics*. Annals of Physics **325**, 1790 (2010) (cit. on p. 65).
- [Pri83] D. E. Pritchard, Cooling neutral atoms in a magnetic trap for precision spectroscopy. Physical Review Letters **51**, 1336 (1983) (cit. on p. 21).
- [Sch10] U. Schneider, Interacting Fermionic Atoms in Optical Lattices—A Quantum Simulator for Condensed Matter Physics. PhD thesis. Universität Mainz, 2010. URL: http://ubm.opus.hbz-nrw.de/volltexte/2011/2860/ (cit. on p. 4).
- [Sel] D. Sels, private communication (cit. on p. 65).
- [Sel17] D. Sels and A. Polkovnikov, *Minimizing irreversible losses in quantum systems* by local counter-diabatic driving. Proceedings of the National Academy of Sciences of the United States of America **114**, 3909 (2017) (cit. on p. 82).

[Sel18] D. Sels, Stochastic gradient ascent outperforms gamers in the Quantum Moves game. Physical Review A 97, 040302 (2018) (cit. on pp. 10, 62).

- [She10] J. F. Sherson et al., Single-atom-resolved fluorescence imaging of an atomic Mott insulator. Nature 467, 68 (2010) (cit. on p. 4).
- [Sie86] A. E. Siegman, *Lasers*. University Science Books, 1986, 2. ISBN: 0935702113 (cit. on pp. 41, 42).
- [Sim11] J. Simon et al., Quantum simulation of antiferromagnetic spin chains in an optical lattice. Nature 472, 307 (2011) (cit. on pp. 6, 7).
- [Ste] D. A. Steck, Rubidium 87 D Line Data. URL: http://steck.us/alkalidata (cit. on pp. 13, 79).
- [Ste98] M. J. Steel et al., Dynamical quantum noise in trapped Bose-Einstein condensates. Phys. Rev. A 58, 4824 (1998) (cit. on p. 65).
- [Stö16] F. M. Störtz, Towards quantum simulation with ultracold molecules. B.Sc. thesis. University of Heidelberg, 2016 (cit. on p. 12).
- [Suk97] C. V. Sukumar and D. M. Brink, Spin-flip transitions in a magnetic trap. Physical Review A 56, 2451 (1997) (cit. on p. 18).
- [Tho17] C. K. Thomas, Quantum Simulation of Triangular, Honeycomb and Kagome Crystal Structures using Ultracold Atoms in Lattices of Laser Light. PhD thesis. University of California, Berkeley, 2017 (cit. on pp. 26, 30).
- [Tie11] T. G. Tiecke, *Properties of Potassium*. 2011. URL: http://www.tobiastiecke.nl/archive/PotassiumProperties.pdf (cit. on p. 14).
- [Tor11] E. Torrontegui et al., Fast atomic transport without vibrational heating. Physical Review A Atomic, Molecular, and Optical Physics 83, 013415 (2011) (cit. on p. 63).
- [Tro08] S. Trotzky et al., Time-resolved observation and control of superexchange interactions with ultracold atoms in optical lattices. Science **319**, 295 (2008) (cit. on pp. 7, 8).
- [Ver04] F. Verstraete and J. I. Cirac, Renormalization algorithms for Quantum-Many Body Systems in two and higher dimensions. arXiv:0407066 (2004). URL: https://arxiv.org/abs/cond-mat/0407066 (cit. on p. 9).

[Vie18] K. Viebahn et al., Matter-wave diffraction from a quasicrystalline optical lattice. arXiv:1807.00823v1 (2018). URL: https://arxiv.org/pdf/1807.00823.pdf (cit. on pp. 22, 35, 41).

- [Wan50] G. H. Wannier, Antiferromagnetism. The triangular Ising net. Physical Review 79, 357 (1950) (cit. on pp. 5, 32).
- [Web03] T. Weber et al., Three-body recombination at large scattering lengths in an ultracold atomic gas. Physical Review Letters 91, 123201 (2003) (cit. on p. 51).
- [Wei03] M. Weidemüller and C. Zimmermann, eds., Interactions in Ultracold Gases: From atoms to molecules. Wiley VCH, 2003. ISBN: 3527635076 (cit. on p. 2).
- [Wei09] M. Weidemüller and C. Zimmermann, eds., Cold Atoms and Molecules. Wiley VCH, 2009 (cit. on p. 51).
- [Wei11] C. Weitenberg et al., Single-spin addressing in an atomic Mott insulator. Nature 471, 319 (2011) (cit. on p. 5).
- [Wei17] C. H. Wei and S. H. Yan, Raman sideband cooling of rubidium atoms in optical lattice. Chinese Physics B 26, 080701 (2017) (cit. on p. 16).
- [Wig32] E. Wigner, On the quantum correction for thermodynamic equilibrium. Physical Review 40, 749 (1932) (cit. on p. 65).
- [Wil08] R. A. Williams et al., Dynamic optical lattices: two-dimensional rotating and accordion lattices for ultracold atoms. Optics Express 16, 16977 (2008) (cit. on p. 28).
- [Wis01] E. Wiseman, Degenerate fermion gas heating by hole creation. Physical Review Letters 87, 240403 (2001) (cit. on p. 23).
- [Yam16] R. Yamamoto et al., An ytterbium quantum gas microscope with narrow-line laser cooling. New Journal of Physics 18, 023016 (2016) (cit. on p. 4).
- [Yan11] S. Yan, D. A. Huse, and S. R. White, Spin-Liquid Ground State of the S=1/2 Kagome Heisenberg Antiferromagnet. Science **332**, 1173 (2011) (cit. on p. 9).