

✓ Consider the following sequence of operations on an empty stack.

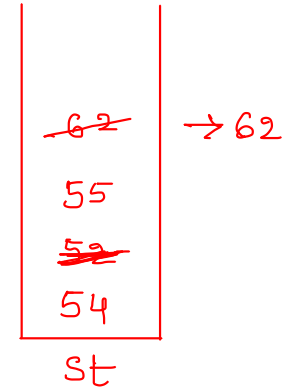
push(54); push(52); pop(); push(55); push(62); s = pop();

← 1000 push(x)/pop(x)

Consider the following sequence of operations on an empty queue.

enqueue(21); enqueue(24); dequeue(  ); enqueue(28); enqueue(32); q = dequeue(  );

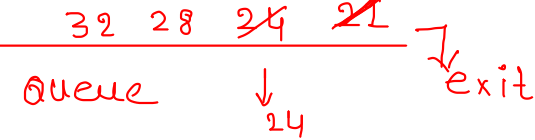
The value of s + q is  $\underline{62} + 24 = \underline{86}$



LIFO

entry

↳



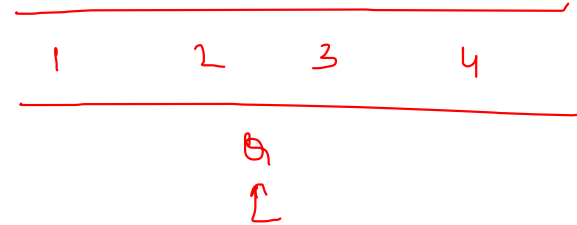
exit

✓ Suppose you are given an implementation of a queue of integers. The operations that can be performed on the queue are:

- ✓ i. isEmpty (Q) — returns true if the queue is empty, false otherwise. ✓
- ii. delete (Q) — deletes the element at the front of the queue and returns its value.
- iii. insert (Q, i) — inserts the integer i at the rear of the queue.

Consider the following function:

```
void f (queue Q) {  
    int i ;  
    if (!isEmpty(Q)) {  
        i = delete(Q);  
        f(Q);  
        insert(Q, i);  
    }  
}
```



10-min's

What operation is performed by the above function f ?

☐ A Leaves the queue Q unchanged

✓ ☒ B Reverses the order of the elements in the queue Q

☐ C Deletes the element at the front of the queue Q and inserts it at the rear keeping the other elements in the same order

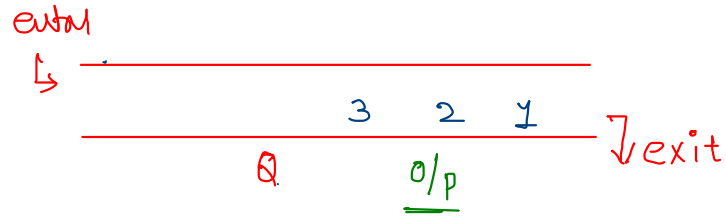
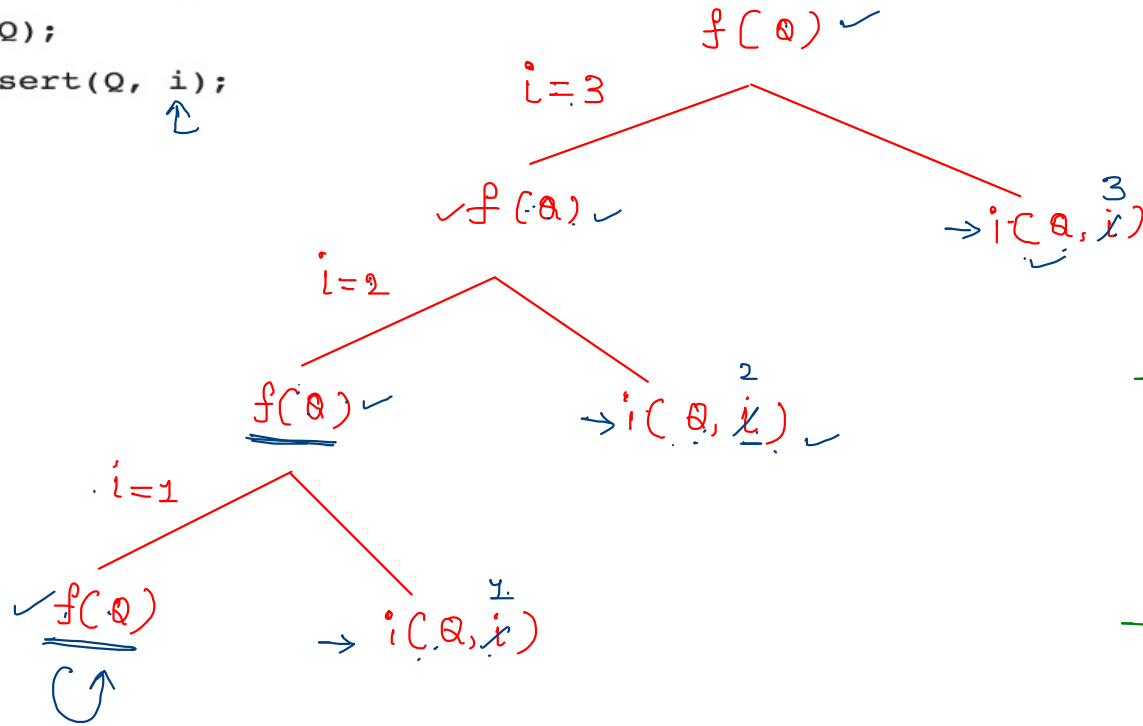
☐ D Empties the queue Q

```

void f (queue Q) {
    int i; ✓
    if (!isEmpty(Q)) {
        i = delete(Q);
        f(Q);
        insert(Q, i);
    }
}

```

! false



1	2	3
i/p		

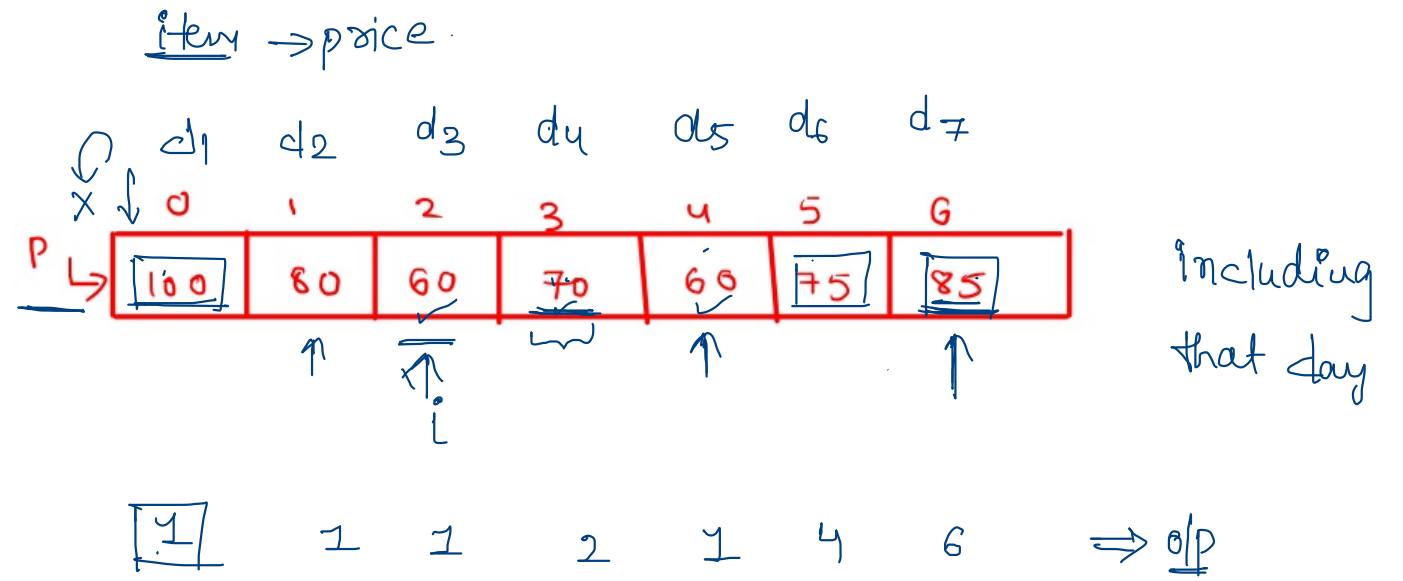
→ Reverse contents of stack, without using extra "

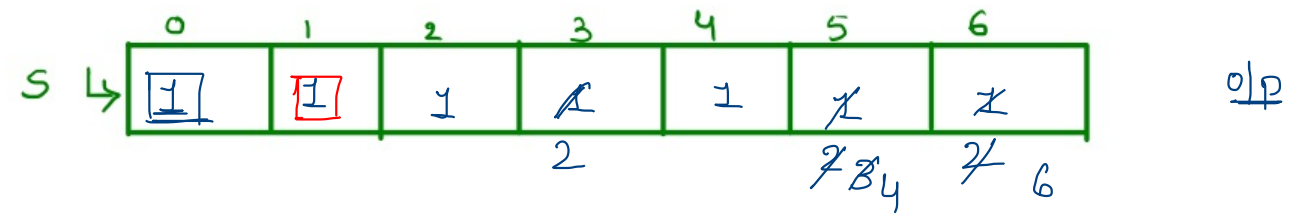
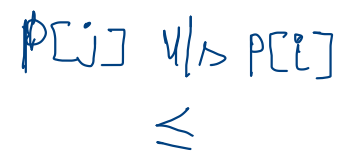
→ Reverse contents of queue without using extra "

→ Implement S using Q

→ Implement Q using S

# \*\*\* stock span problem





function calculateSpan(price[], n, S[])  
 {  
 // Span value of first day is always 1  
 S[0] = 1;

→ empty ✓  
 n → for(int i = 1; i < n; i++) ✓  
 {  
 S[i] = 1; //

for(int j = i - 1; (j >= 0) && (price[j] <= price[i]); j--)  
 S[i]++; ✓  
 }

}

$P[j] \leq P[i]$

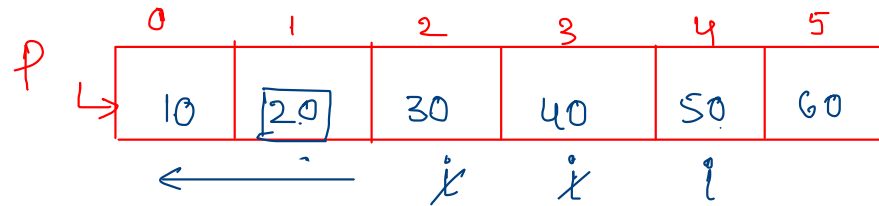
$P[j] \leq P[i]$

⇒ n

n ⇒ ✗

TLE

n = 10<sup>6</sup> ✓



n = 6

↑ worst case i/p ✓

✗

i = 1 → 1

i = 2 → 2

3 → 3

4 → 4

5 → 5

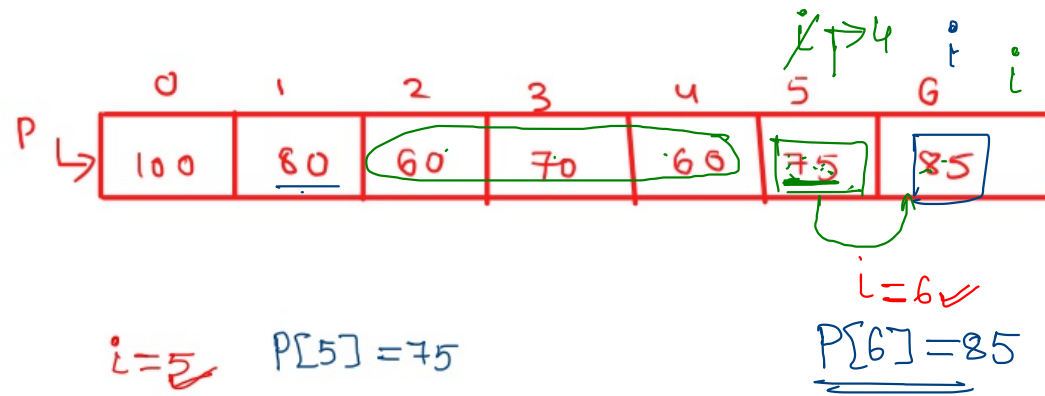
Analysis

$\frac{n(n+1)}{2}$

⇒ O(n<sup>2</sup>)

Brute Force:-  
 $O(n^2)$

10+



$i=5$   $P[5]=75$

60 v/s 75  
 70 v/s 75  
 60 v/s 75  
 80 v/s 75

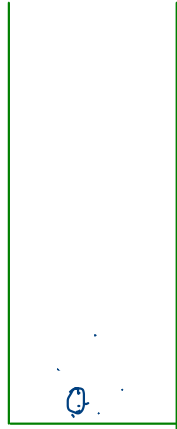
$P[6]=85$

75 v/s 85  
 60 v/s 85  
 70 v/s 85  
 60 v/s 85  
 80 v/s 85  
 100 v/s 85 X

units | 12

BF  $\xrightarrow{?}$  Stack  
 ?  $\rightarrow$  ✓

remember  $\Rightarrow$  stack  
 $75 < 85$   
 $\Rightarrow 0(n^2)$ ?  
 { repetitive calculations  
 $\hookrightarrow$  some how if you can avoid.  
 then  
 T.C  $\Rightarrow$  ↓ reduced

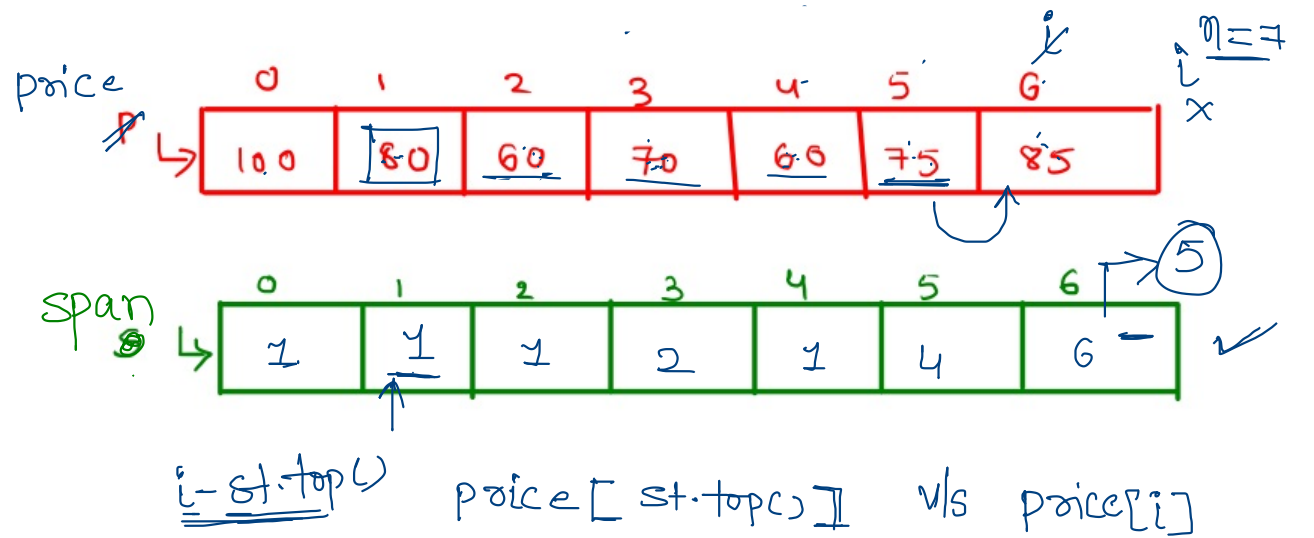


st

↳ can contains all array indices

any value (0 to 6)

$$\underline{100} \leq \underline{80}$$



for (i=1; i<n; i++)  
{

x → while (price[st.top()] ≤ price[i] &&  
{ ! st.isEmpty() )

st.pop()

3  
→  
3



```
findSpan(price[],n,span[])
```

```
{
```

```
Stack st
```

```
st.push(0) ✓
```

```
span[0]=1 ✓
```

```
for(i=1;i<n;i++)
```

```
{
```

```
    while(!isEmpty() && price[st[top]]<=price[i])
```

```
    {
```

```
        stst.pop() ✓
```

```
    }
```

```
    span[i]=isEmpty()? i+1 : i-st[top]
```

```
    st.push(i)
```

```
}
```

```
}
```

st.peek()

st.top()

11:05

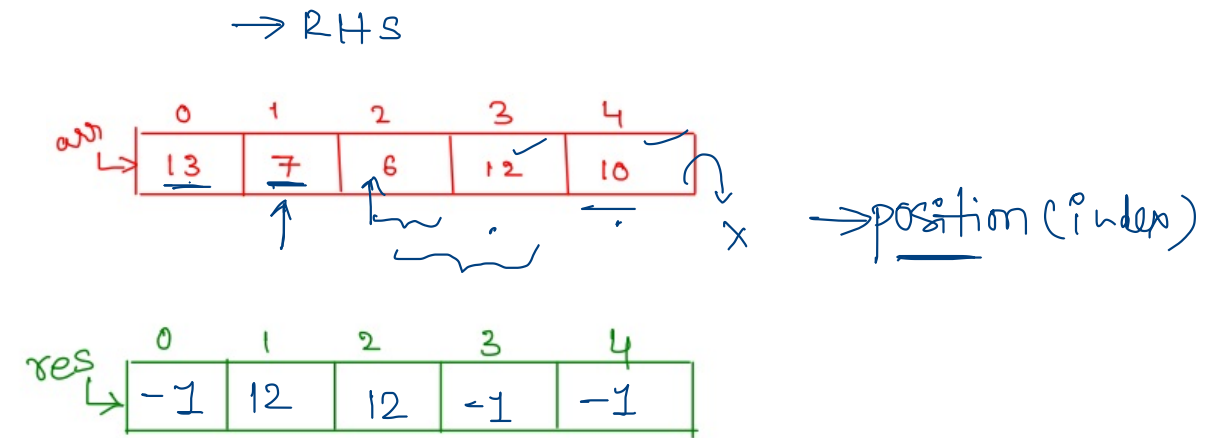
i

0	1	2	3	4	5	6
100	80	60	70	60	75	85

span

0	1	2	3	4	5	6
1						

Next Greater Element to right



Brute Force:

	0	1	2	3	4
arr ↳	13	7	6	12	10

	0	1	2	3	4
res ↳	-1	12	12	-1	-1

$$arr[j] \geq arr[i]$$

$$temp = 12$$

break;

OJ ✓

$O(n^2)$

↳ TLE

⇒ for ( $i=0$ ;  $i \leq n-2$ ;  $i++$ )

{ temp = -1

for ( $j=i+1$ ;  $j < n$ ;  $j++$ )

{

if ( $arr[j] \geq arr[i]$ )

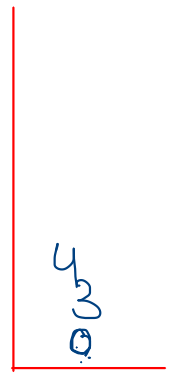
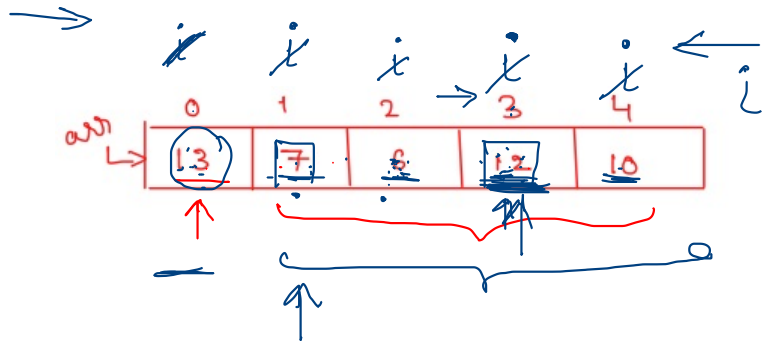
{

temp = arr[j]; break;

}

}

res[i] = temp;

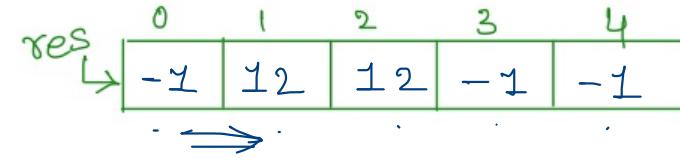


St → push ~~all~~ indices to stack.

curr = 10

$10 \leq 12 \checkmark$

$12 > 13 \times$



$7 \leq 13$

$\times$  if (curr ≤ arr[st.top()])  
 {  
     st.push(i)  
 }

$12 \leq 6$

else ~~6 ≤ 7~~  
 { while (!st.isEmpty() &&  
     curr > arr[st.top()])  
   {  
     index = st.pop() ✓  
     res[index] = curr  
   }  
 }

```
function fun(arr[],n,res[])
```

```
{
```

```
    let st be a stack
```

```
    for(i=0;i<n;i++)
```

```
        res[i]=-1
```

```
    for(i=0;i<n;i++)
```

```
    {
```

```
        curr=arr[i]
```

```
        if(st.isEmpty())
```

```
            st.push(i)
```

```
        else
```

```
        {
```

```
            if(curr<=arr[st.peek()])
```

```
                st.push(i)
```

```
            else
```

```
            {
```

```
                while(!st.isEmpty() && curr>arr[st.peek()])
```

```
                {
```

```
                    index=st.pop()
```

```
                    res[index]=curr
```

```
                }
```

```
                st.push(i)
```

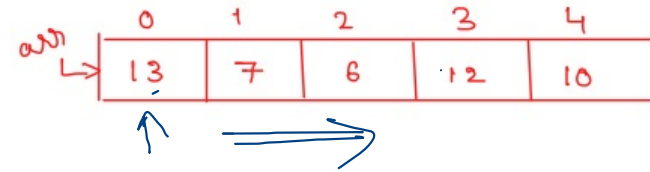
```
            }
```

```
        }
```

```
    }
```

```
    return res
```

```
}
```



Design a stack such that `getMin()` is in  $O(1)$

10, 5, 2, 6, `getMin()`



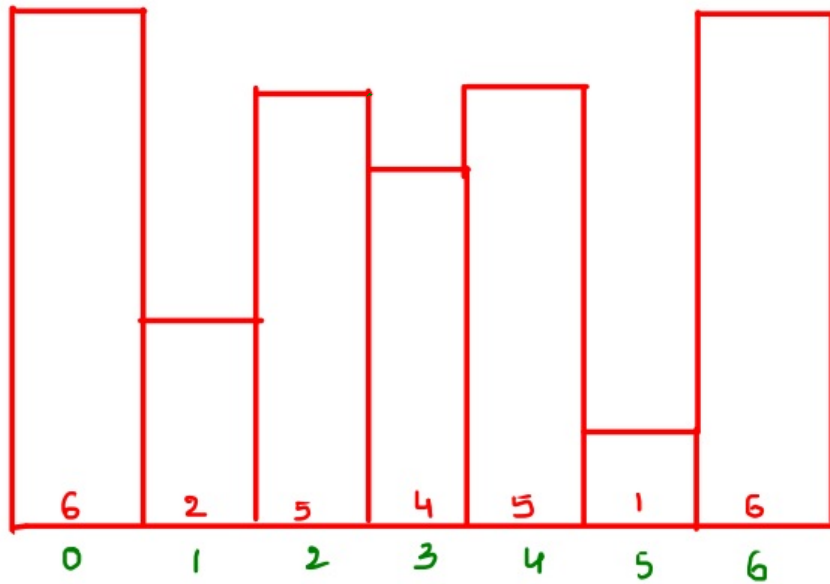
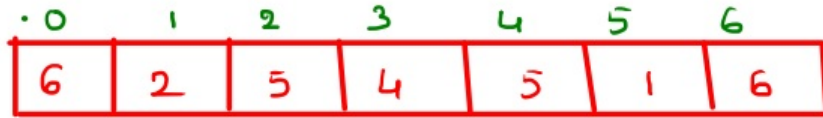
design a stack such that `getMin()` in  $O(1)$   
Let `st` be a global stack

```
add(data)
{
    if(s.isEmpty())
    {
        s.push(data)
        curr_min=data
    }
    else
    {
        if(data<curr_min)
        {
            s.push(data-curr_min)
            curr_min=data
        }
        else
            s.push(data)
    }
}

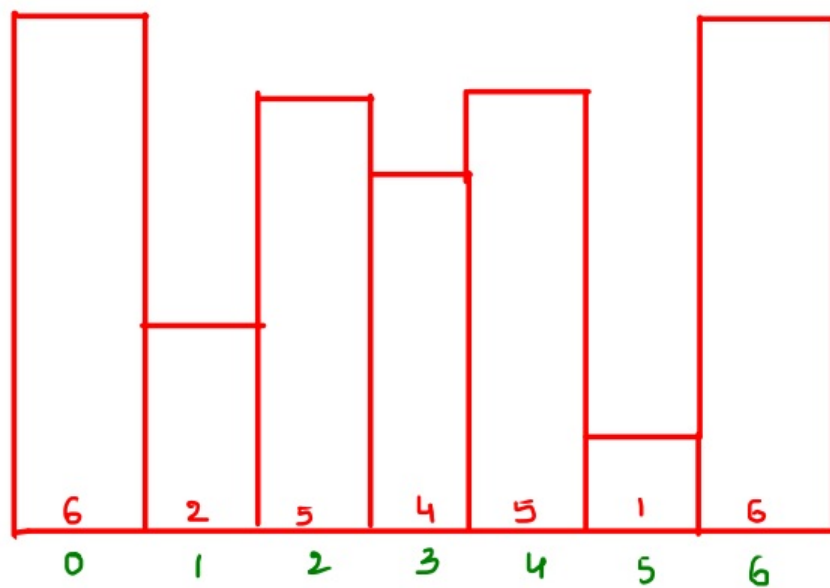
delete()
{
    if(s.peek()<curr_min)
    {
        curr_min=curr_min-s.peek()
    }
    return s.pop()
}
```



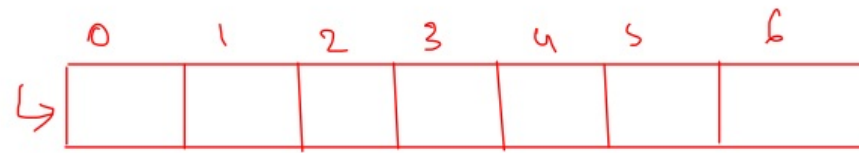
## Largest Rectangle Area in a Histogram



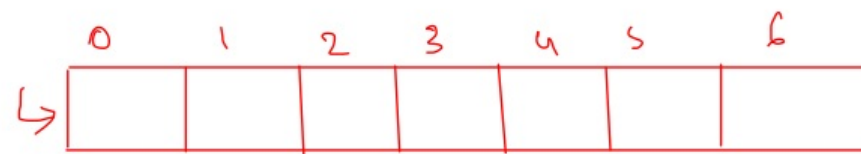
0	1	2	3	4	5	6
6	2	5	4	5	1	6



left



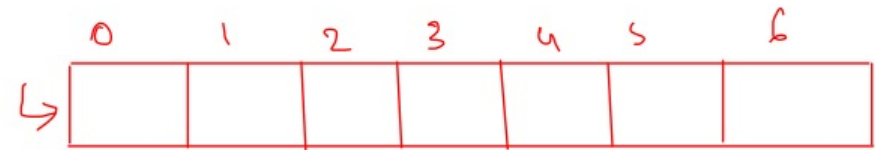
right



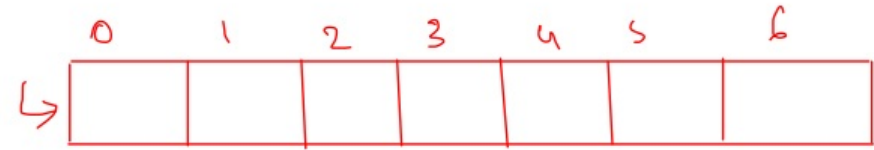
```

int maximumArea(int arr[],int n)
{
    stack<Integer> st = new Stack<Integer>
    int right[n] //nse index on right
    st.push(arr.length-1);
    right[arr.length-1]=arr.length;
    for(i=n-1;i>=0;i--)
    {
        while(st.size>0 && arr[i]<arr[st.peek()])
        {
            st.pop()
        }
        if(st.size()==0)
            right[i]=arr.length()
        else
            right[i]=st.peek()
        st.push(i)
    }
}

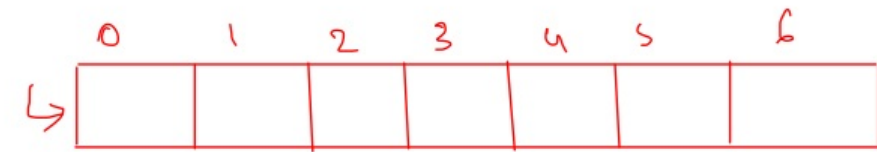
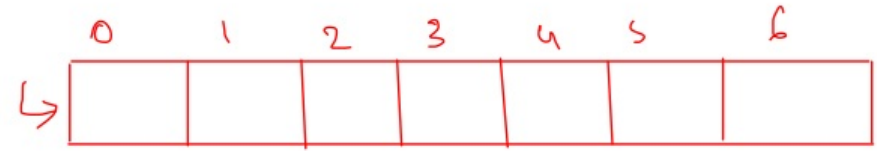
```



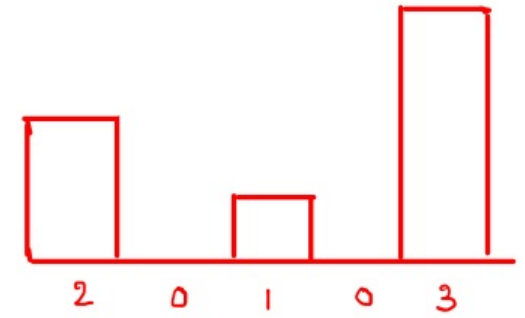
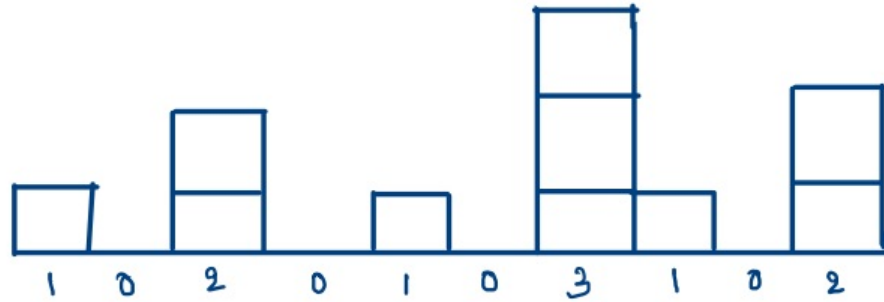
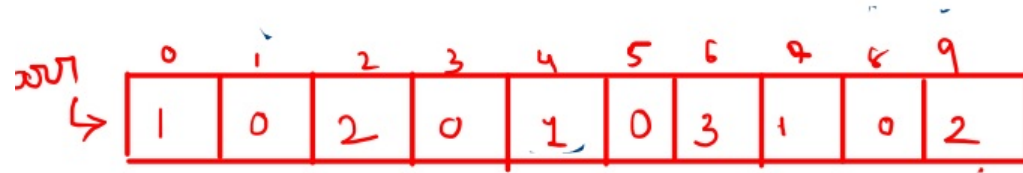
```
int left[n] // nse index on left
st=new Stack<>()
st.push(0)
left[0]=-1
for(i=1;i<arr.length;i++)
{
    while(st.size()>0 && arr[i]<arr[st.peek()])
    {
        st.pop()
    }
    if(st.size()==0)
    {
        left[i]=-1
    }
    else
    {
        left[i]=st.peek()
    }
    st.push(i)
}
```



```
maxArea=0
for(i=0;i<arr.length;i++)
{
    width=right[i]-left[i]-1;
    area=arr[i]*width
    if(area>maxArea)
    {
        maxArea=area
    }
}
return maxArea;
}
```



## Trapping Rain water problem



```

function maxWater(arr[], n)
{
    res = 0;

    for(i = 1; i < n - 1; i++)
    {
        left = arr[i];
        for(j = 0; j < i; j++)
        {
            left = Math.max(left, arr[j]);
        }

        right = arr[i];
        for(j = i + 1; j < n; j++)
        {
            right = Math.max(right, arr[j]);
        }

        res += Math.min(left, right) - arr[i];
    }
    return res;
}

```

arr

0	1	2	3	4	5	6	7	8	9
1	0	2	0	1	0	3	1	0	2





```
function findWater(arr[],n)
{
    let left[n], right[n]

    water = 0;

    left[0] = arr[0];
    for (i = 1; i < n; i++)
    {
        left[i] = Math.max(left[i - 1], arr[i]);
    }

    right[n - 1] = arr[n - 1];

    for (i = n - 2; i >= 0; i--)
    {
        right[i] = Math.max(right[i + 1], arr[i]);
    }

    for (i = 0; i < n; i++)
        water += Math.min(left[i], right[i]) - arr[i];

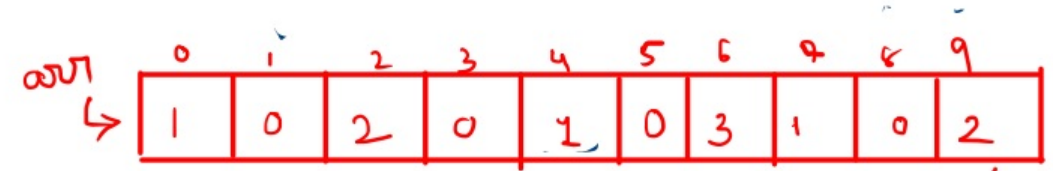
    return water;
}
```

```

function findWater(arr[], n)
{
    result = 0, left_max = 0, right_max = 0, lo = 0, hi = n - 1;

    while (lo <= hi)
    {
        if (arr[lo] < arr[hi])
        {
            if (arr[lo] > left_max)
                left_max = arr[lo];
            else
                result += left_max - arr[lo];
            lo++;
        }
        else
        {
            if (arr[hi] > right_max)
                right_max = arr[hi];
            else
                result += right_max - arr[hi];
            hi--;
        }
    }
    return result;
}

```



→  $n \times n$  → searching

①

2

2

3

3

1

4

1

1

5

6

$O(n)$

$O(1)$

~~$O(1)$~~

$O(1)$

Java  
HashMap()

key

value

digit

1

1

2

~~1~~ 2

3

1