ASPC 6213 Analytical Method in Engineering III

Homework 6 Question 3 - f

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In [1]: import numpy
    from matplotlib import pyplot
    %matplotlib inline
    pyplot.rcParams['font.family'] = 'serif'
    pyplot.rcParams['font.size'] = 16

In [2]: # parameters
    L = 1.0
    D = 1.0
    pi = numpy.pi

    dx = 0.001 # step length
    nx = int(L/dx) + 1 # steps number
    x0 = numpy.linspace(0.0, L, num=nx)

    T = [0.001, 0.01, 0.1, 10.0] # different time value
```

```
In [3]: x = x0.copy()
f_history = [x0.copy()]
for t in T:
    f1 = x / L - (x / L)**2
    temp = 0.0
    for n in range(1, 2001):
        temp = temp + ((-1)**n - 1) / (n**3) * numpy.sin(n*pi*x/L) * numpy.exp
(-D*((n*pi/L)**2)*t)
    f2 = 4 / (pi**3) * temp
    f = f1 + f2
    f_history.append(f)
```

```
In [4]: # plot
    pyplot.figure(figsize=(12.0, 5.0))
    pyplot.title('HW 6 Question 6-f')
    pyplot.ylabel('x')
    pyplot.ylabel(r'$\frac{T(x,t)-T^{0}}{QL^2/2k}$')
    pyplot.grid()
    pyplot.plot(x, f_history[1], label='t=0.001 s', linestyle='-', linewidth=2)
    pyplot.plot(x, f_history[2], label='t=0.01 s', linestyle='--', linewidth=2)
    pyplot.plot(x, f_history[3], label='t=0.1 s', linestyle=':', linewidth=2)
    pyplot.plot(x, f_history[4], label='t=10.0 s', linestyle='--', linewidth=2)
    pyplot.legend();
```

