

## 1. Overview of Classes

**Class:**

edge

**Description:**

this is an edge with vertices and weight.

**Member variables:**

Double weight;

int,x,y; x,y is the index of the vertices

**Member functions:**

~edge();default destructor

edge();initialize an edge with weight 0, index -1

edge(double w,int u, int v); initialize an edge with necessary info

functions for accessing private variables: int get\_x(), int get\_y()

**Class:**

node

**Description:**

this is an vertice with its index and next node. It is the basic unit of a linkedlist.

**Member variables:**

int vertex;

node \*next;

**Member functions:**

node();default constructor

~node();default destructor

node(int vertex); initialize a node with an index

functions for accessing private variables: int get\_index(); node \*get\_next();

**Class:**

nodelist

**Description:**

This is a linked list, representing a set of elements

**Member variables:**

node \*head;

node \*tail;

**Member functions:**

nodelist();default constructor

~nodelist();default destructor

nodelist(node\*a);initialize a linked list with a node as its head and tail

functions for accessing private variables: node \*get\_head(); node \*get\_tail();

**Class:**

set

**Description:**

This is a universe set with several set represented as nodelist

**Member variables:**

vector<nodelist> theSet;

**Member functions:**

set();default constructor

~set();default destrucor

void makeset (int num); make a universe set with the number of vertices

node \*findset (int num); pass the index to the function and return its head to check if two vertices are in the same set.

void merge(int a, int b); merge two vertices into the same set by setting them with same head and tail.

**Class:**

graph

**Description:**

This is the graph storing edge info and giving responds to the input command

**Member variables:**

vector<vector<edge>> matrix; adjacency matrix

int size; the number of vertices

class illegal\_commal{};handling failure

int edge\_count; the total number of edges

**Member functions:**

graph(); constructor

~graph(); destructor

void set\_size(int m); set the size of the table

void print\_eount(); print the number of edges

void insert(int u, int v, double w); connect index u and index v

void del(int u, int v);delete the edge between index u and index v

void degree(int u); return the degree of index u  
void clear(); remove all the edges  
void mst(); create an mst and print the total weight

2. Class diagrams

edge	node
double weight; int x,y;	int vertex; node *next;
edge(); edge(double w,int u, int v); int get_x();//accessing private variables int get_y(); double get_weight(); ~edge()=default;	node()=default; ~node()=default; node(int vertex); int get_vertex();//accessing private variables node *get_next(); void set_next(node *a); bool operator==(const node &a); bool operator!=(const node &a);

nodelist	set
node *head; node *tail;	vector<nodelist> theSet;
nodelist()=default; nodelist(node *a); ~nodelist()=default;//accessing private variables node *get_head(); node *get_tail(); void set_head(node *a); void set_tail(node *a);	set()=default; ~set()=default; void makeset(int num); //consistent with lecture notes node *findset(int num); void merge(int a, int b);
graph	
vector<vector<edge>> matrix; int size; class illegal_argument{}; int edge_count;	
void set_size(int m); //function name consistent with commands int get_size(); void print_ecount(); graph(); ~graph(); void insert(int u,int v,double w); void del(int u,int v);//delete void degree(int u); void clear(); void mst();	

3. Constructors/Destructor

**Class edge:** edge() initialize an edge with weight 0, index -1  
edge(double w,int u, int v) initialize an edge with necessary info  
**Class node:** node(int vertex); initialize a node with an index.  
== != operators are overloaded for the ease of comparison of nodes.  
**Class set:** the destructor is modified to manually delete all the elements in the disjoint set to ensure there is no memory leak.  
Other constructors and destructors are kept as default.

4. Test Cases

There are 2 cases I tested in addition to the example tests.  
Test1: the size is 1, it should be successful but insert, delete should be failure.  
Test2: insert a connected tree, calculate the mst. Delete some edges make it not connected. Add new edges with new weights and calculate the mst again.  
Test3: update the weight of edge.

5. Performance

**Analysis of applying Kruskal’s algorithm:**

the algorithm is applied in the member function named `mst()` under class `graph`. The number of edges is  $E$ , the number of vertices is  $N$ . Sorting the edges takes  $O(E \lg E)$  by `std::sort()`. `Makeset()` takes  $O(n)$ . The for loop takes  $O(E) * (\text{Findset}() \text{ and } \text{merge}())$ . `Findset()` which returns the head of a node takes  $O(1)$ . In my implementation of disjoint-set, each node's head is updated at most  $\lg N$  times, the total time spent in `merge()` during the for loop is  $O(N \lg N)$ . The total time for applying Kruskal's algorithm is  $O(N \lg N + E + E \lg E)$ . Since  $|E| \geq |N| - 1$ , we can restate it as  $O(E \lg N)$ . However, the edges are initially stored in a 2d vector (adjacency matrix). Declaring an empty vector of edge takes  $O(1)$ . Pushing all the existed edges to the vector takes  $O(N^2)$ . The total time complexity of the function `mst()` is  $O(N^2)$ .