Principles of Database Systems (CS307)

Lecture 11: Indexing

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- Most contents are from slides made by Stéphane Faroult and the authors of Database System Concepts (7th Edition).
- Their original slides have been modified to adapt to the schedule of CS307 at SUSTech.

Intro

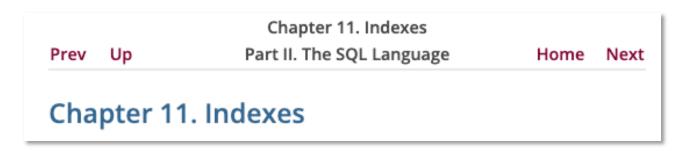
Motivation

- Think about an example in a library:
 - How can we find a book?
 - Books are on the shelves in a sequential order
 - We had drawers where you could look for books by <u>author</u>, <u>title</u> or sometimes <u>subject</u> that were telling you what were the "coordinates" of a book.



Terminology

- Plural of index: indices, or indexes?
 - Both are correct in English
 - indices (Latin): Often used in scientific and mathematical context representing the places of an element in an array, vector, matrix, etc.
 - indexes (American English): Used in publishing for the books
 - What about database?
 - A good way: Follow the naming convention of the project or the DBMS



- Remember searching algorithms in Data Structure?
 - Linear search
 - Scan all records from top to bottom
 - Binary search
 - Divide and conquer
 - Assumption: Records are sorted by the <u>search key</u>

```
1,12 stulyev,ru,1971,161
2,Al-mummia test,eg,1969,102
3, "Ali Zaoua, prince de la rue", ma, 2000, 90
4, Apariencias, ar, 2000, 94
5, Ardh Satya, in, 1983, 130
6, Armaan, in, 2003, 159
7, Armaan, pk, 1966,
8, Babettes gæstebud, dk, 1987, 102
9, Banshun, jp, 1949, 108
10, Bidaya wa Nihaya, eg, 1960,
11, Variety, us, 2008, 106
12, "Bon Cop, Bad Cop", ca, 2006,
13, Brilliantovaja ruka, ru, 1969, 100
14,C'est arrivé près de chez vous,be,1992,95
15, Carlota Joaquina - Princesa do Brasil, br, 1995,
16, Cicak-man, my, 2006, 107
```

- Remember searching algorithms in Data Structure?
 - Linear search
 - Scan all records from top to bottom
 - Binary search
 - Divide and conquer
 - Assumption: Records are sorted by the search key
 - E.g., Find movies with IDs larger, than 100 and smaller than 200

```
1,12 stulyev,ru,1971,161
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```

In the current storage structure, the records are sorted by movieid

 So, it will be easy to find a specific movieid with binary search

- Remember searching algorithms in Data Structure?
 - Linear search
 - Scan all records from top to bottom
 - Binary search
 - Divide and conquer
 - Assumption: Records are sorted by the <u>search key</u>
 - However, how can we find data based on the non-sorted columns?
 - E.g., find all Chinese movies

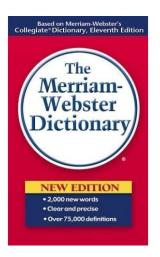
```
1,12 stulyev,ru,1971,161
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```

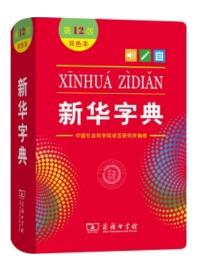
country

Find the rows where country = 'cn'

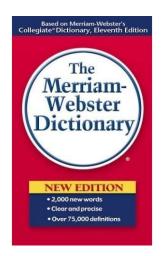
 The country codes are not sorted in the current storage structure, so the binary search algorithm cannot be used

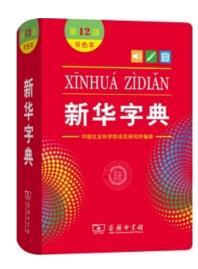
- This happens in real life too
 - English dictionary
 - The words are sorted in an alphabetical order
 - Chinese dictionary
 - The characters are usually sorted in the alphabetical order of Pinyin





- This happens in real life too
 - English dictionary
 - The words are sorted in an alphabetical order
 - Chinese dictionary
 - The characters are usually sorted in the alphabetical order of Pinyin
 - However, we have other ways of looking up a character
 - Radicals (偏旁部首)
 - Number of strokes (数笔画)
 - Four-corner method (四角号码)





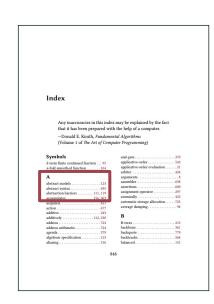
Practical Use

Index in Databases

- Concept
 - An **index** is a data structure which <u>improves the efficiency of retrieving data</u> with <u>specific values</u> from a database
 - Usually, indexes locate a row by a series of location indicators
 - E.g., (filename, block number, offset)

Index in Databases

- Concept
 - An index is a data structure which improves the efficiency of retrieving data with specific values from a database
 - Usually, indexes locate a row by a series of location indicators
 - E.g., (filename, block number, offset)
 - It is like indexes in books
 - Location indicator: (page, row)



Index in Databases

Actually, we have been benefited from indexes off-the-shelf

```
✓ indexes 2

j<sub>U</sub> movies_pkey (movieid) UNIQUE

j<sub>U</sub> movies_title_country_year_released_key (title, country, year_released) UNIQUE
```

• In PostgreSQL, indexes are built <u>automatically</u> on columns with <u>primary key</u> or unique constraints

Experiment on Using Indexes

Duplicate a table with no index

```
create table movies_no_index as select * from movies;
```



```
-- auto-generated definition
create table movies_no_index
(

movieid integer,
title varchar(100),
country char(2),
year_released integer,
runtime integer,
user_name varchar(20)
);
```

Experiment on Using Indexes

- Check the performance on retrieving data
 - Significant difference between queries on the two tables

```
-- Query 1
explain analyze
select *
from movies
where movieid > 100 and movieid < 300;

-- Query 2
explain analyze
select *
from movies_no_index
where movieid > 100 and movieid < 300;
```

```
Query 1 (on movies)
```

```
Imm QUERY PLAN

1 Bitmap Heap Scan on movies (cost=10.32..136.35 rows=199 width=40) (actual time=0.162..0.440 rows=199 loops=1)

2 Recheck Cond: ((movieid > 100) AND (movieid < 300))

3 Heap Blocks: exact=6

4 -> Bitmap Index Scan on movies_pkey (cost=0.00..10.28 rows=199 width=0) (actual time=0.136..0.136 rows=199 loops=1)

5 Index Cond: ((movieid > 100) AND (movieid < 300))

6 Planning Time: 0.413 ms

7 Execution Time: 0.507 ms</pre>
```

```
Query 2
(on movies_no_index)
```

```
■ QUERY PLAN

1 Seq Scan on movies_no_index (cost=0.00..217.06 rows=199 width=40) (actual time=0.039..5.075 rows=199 loops=1)

2 Filter: ((movieid > 100) AND (movieid < 300))

3 Rows Removed by Filter: 9005

4 Planning Time: 0.444 ms

5 Execution Time: 5.156 ms
```

Experiment on Using Indexes

• If there is no index on a column (or several columns), we can create one manually

```
-- SQL Syntax for creating indexes create index index_name on table_name (column_name [, ...]);
```

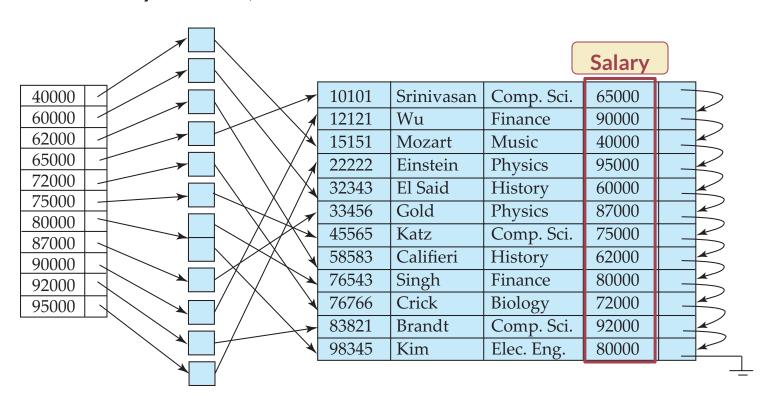
Theoretical Aspects

- 1) In terms of storage structure, is the index completely separated with the data records?
 - No ⇒ Integrated index
 - PK index in a MySQL InnoDB database
 - PK index in a SQL Server database
 - Yes ⇒ External index
 - Indexes in a PostgreSQL database
 - Indexes in a MySQL MyISAM database

- 2) Does the index specify the order in which records are stored in the data file?
 - Yes ⇒ Clustered index (a.k.a. primary index)
 - No ⇒ Non-clustered index (a.k.a. secondary index)

A secondary index on the column "salary"

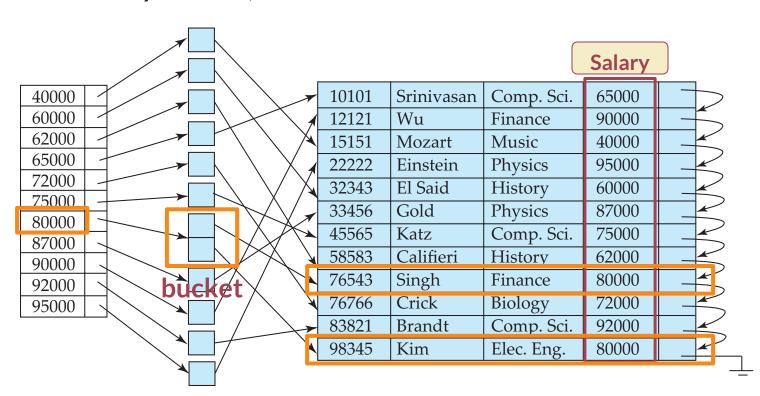
- Index record points to a bucket that contains pointers to all the actual records with that particular search-key value
- Secondary indices have to be dense



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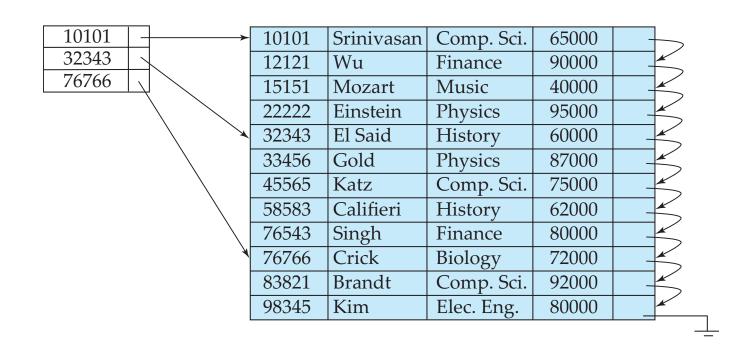
A secondary index on the column "salary"

- Index record points to a bucket that contains pointers to all the actual records with that particular search-key value
- Secondary indices have to be dense



- 3) Does every search key in the data file correspond to an index entry?
 - Yes ⇒ Dense Index
 - No ⇒ Sparse Index

10101	→	10101	Srinivasan	Comp. Sci.	65000	
12121		12121	Wu	Finance	90000	
15151		15151	Mozart	Music	40000	
22222		22222	Einstein	Physics	95000	
32343	—	32343	El Said	History	60000	
33456		33456	Gold	Physics	87000	
45565	-	45565	Katz	Comp. Sci.	75000	
58583		58583	Califieri	History	62000	
76543		76543	Singh	Finance	80000	
76766		76766	Crick	Biology	72000	
83821		83821	Brandt	Comp. Sci.	92000	
98345		98345	Kim	Elec. Eng.	80000	



Dense Index

Sparse Index

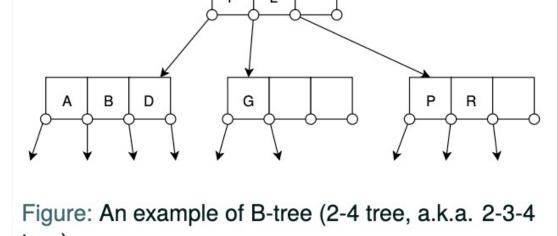
- 4) Does the search key contain more than one attribute?
 - Yes ⇒ Multi-key index (Multi-column index)
 - No ⇒ Single-key index (Single-column index)
 - We mainly focus on single-key index for now

Index Implementation

- Data Structures for Indexes
 - B-tree, B+-tree
 - Very famous data structures for building indexes
 - Hash table

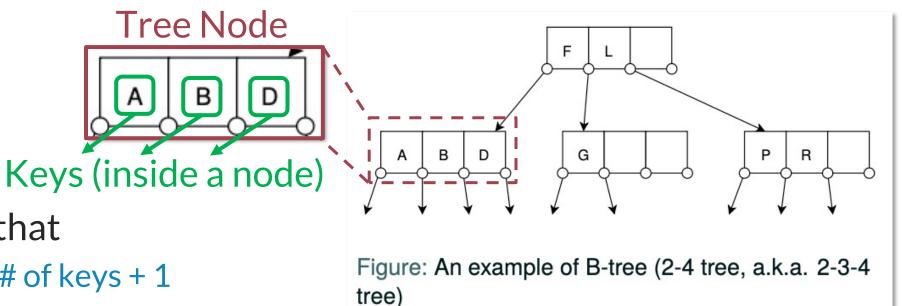
- A B-tree of order *m* satisfies that
 - For every node, # of children = # of keys + 1
 - (Ordered) For a node containing n keys ($K_1 < K_2 < K_3 < \dots < K_n$) with n+1 children (pointed by $P_0, P_1, P_2, \dots, P_n$), any key $k_{sub i}$ in the sub-tree pointed by P_i satisfies that $K_i < k_{sub i} < K_{i+1}$
 - (Multiway) For an internal node, [m/2] ≤ # of children ≤ m
 - ... except that <u>a root node</u> may have less than [m/2] children
 - (Always balanced) All leaves appear on the same level

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tree)

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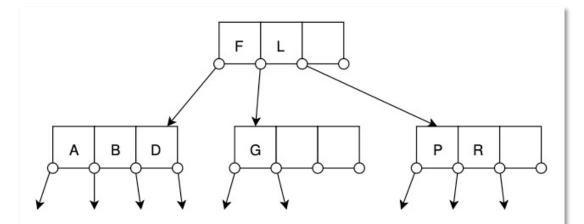


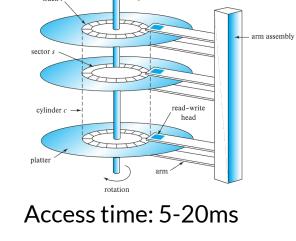
Figure: An example of B-tree (2-4 tree, a.k.a. 2-3-4 tree)

- (Ordered) For a node containing n keys ($K_1 < K_2 < K_3 < \dots < K_n$) with n+1 children (pointed by $P_0, P_1, P_2, \dots, P_n$), any key $k_{sub i}$ in the sub-tree pointed by P_i satisfies that $K_i < k_{sub i} < K_{i+1}$
- (Multiway) For an internal node, [m/2] ≤ # of children ≤ m
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- [m/2] is the called the minimum branching factor (a.k.a. minimum degree) of the tree
- A B-tree of order m is usually called a "[m/2]-m tree", like 2-3 tree, 2-4 tree, 3-5 tree, 3-6 tree,...
 - In practice, the order m is much larger (~100)

- Height of a *B*-tree: $h \le 1 + \log_{\lceil m/2 \rceil} \left(\frac{n+1}{2} \right)$
 - If we take an 50-100 tree with 1M records:
 - $h \le 1 + \log_{100/2}(1000000/2) = 4.354$ (i.e., 4 levels)

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 - If we take an 50-100 tree with 1M records:
 - $h \le 1 + \log_{100/2}(1000000/2) = 4.354$ (i.e., 4 levels)
 - Why do we use B-trees?
 - We can set the size of a B-tree node as the disk page size
 - i.e., m can be chosen with consideration on the page size
 - The height of the tree -> Number of disk I/Os
 - The number of disk I/Os can be relatively small





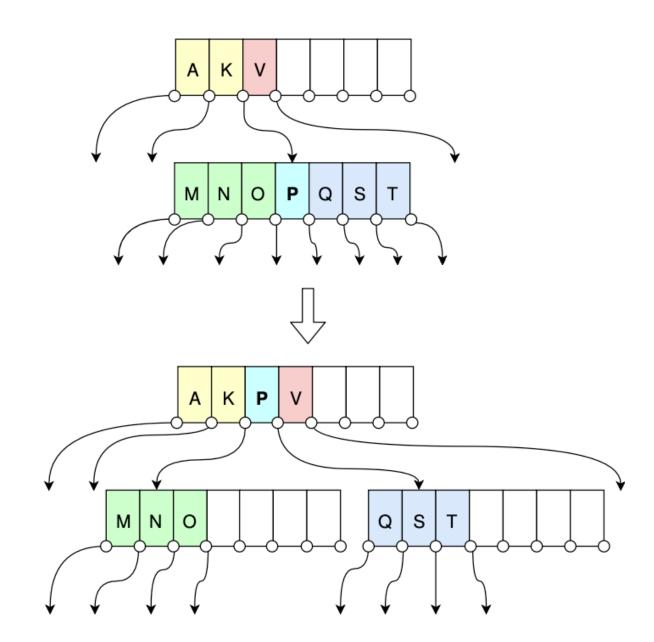


Access time: 50-70ns



- Tree operations:
 - Search, Insert, Delete
 - Update (Delete + Insert)
- What is special in B-tree
 - Split and merge nodes

- Split a node in a B-tree
 - Example: when m=7
 - ... and we want to insert the record with key="P"

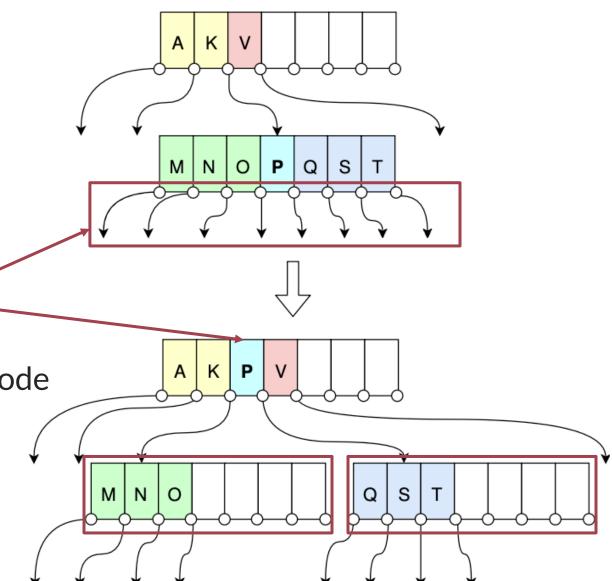


- Split a node in a B-tree
 - Example: when m=7
 - ... and we want to insert the record with key="P"

The number of children is larger than m (m=7)

• This node will be split into two nodes

• The pivot key will be elevated into the parent node



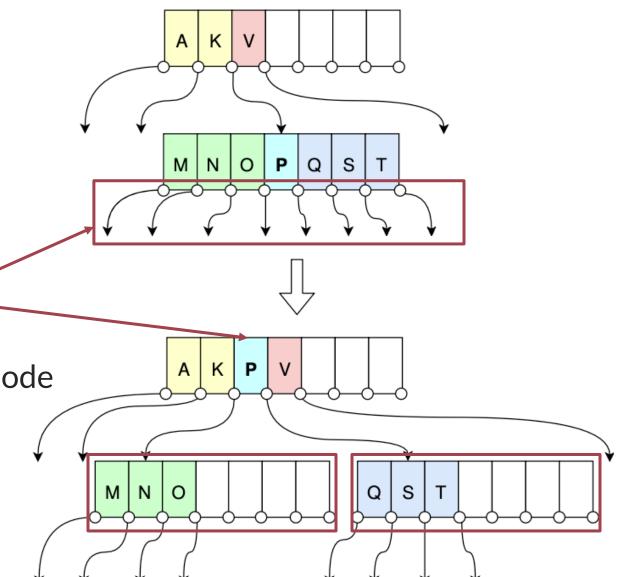
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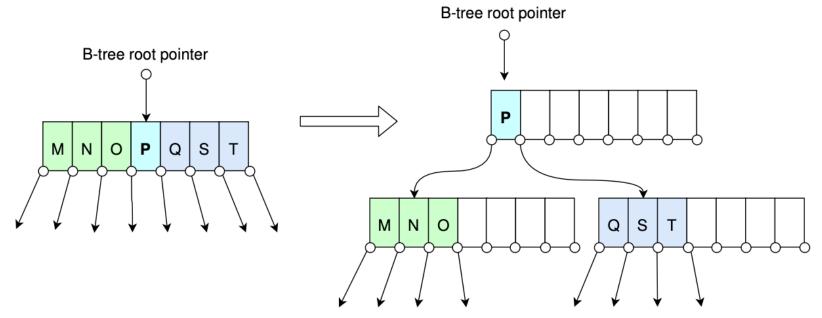
• This node will be split into two nodes

• The pivot key will be elevated into the parent node

 What if the parent (or even the root) node is also full?



- Split a node in a B-tree
 - Example: when m=7
 - ... and we want to insert the record with key="P"
- Split the root node of the B-tree



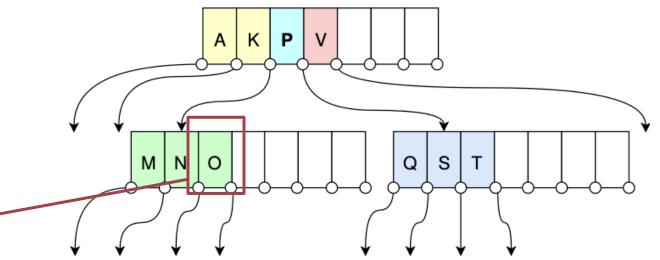
Note that the height of the B-tree is increased by 1 in this case

• This is the only way that a B-tree increases its height

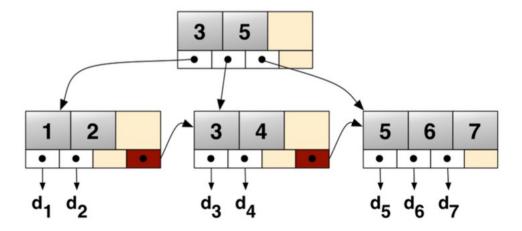
- A Problem in B-tree: Table traversal when only the B-tree is provided
 - In B-tree, data are stored on all nodes
 - What if we want to traverse all records in the table?
 - select * from letters

For example, we have accessed the node for letter "O"

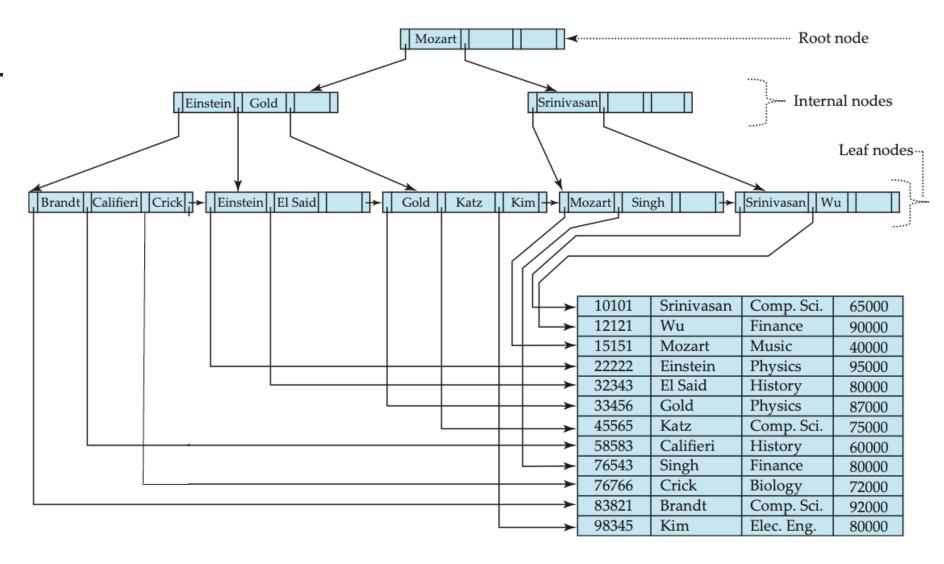
- How can we find the next row?
 - We must go back to the parent node to access "P" (extra time cost)



- Features of a B+-tree (compared with B-trees)
 - Data stored only in leaves
 - Leaves are <u>linked sequentially</u>



- A complete example of a B+tree
 - Data stored only in leaves
 - No need to <u>squeeze data</u> <u>into non-leaf nodes</u>
 - Leaves are <u>linked sequentially</u>
 - Faster table traversal from top to bottom
 - Better support for range queries



Index It or Not: Where Indexing May Help

- Check whether the PK / Unique index helps first
- Index those columns frequently appeared as search criteria

```
exists
c, <=, >, >=, between
in
exists
like (prefix matching)
```

- Be cautious when the indexed columns need frequent writing operations
 - Overhead to update indexes in insert, update, and delete opereations
- Functions

```
SELECT attr1, attr2
FROM table
WHERE function(column) = search_key

-- Create an index on the return values of the function
-- instead of the original values
create index idx_name ON table1(function(col1));
```

Index It or Not: Where Indexing May Help

- Be cautious when using indexes on a small table
 - Full scan ≠ Bad scheme
 - Index retrieval ≠ Good scheme

Hashing

- A bucket is a unit of storage containing one or more entries
 - A bucket is typically <u>a disk block</u>
 - We obtain the bucket of an entry from its search-key value using a hash function
 - Hash function h is a function from the set of all search-key values K to the set of all bucket addresses B
 - Hash function is used to locate entries for access, insertion as well as deletion.
- Entries with different search-key values may be mapped to the same bucket
 - ... thus, the entire bucket must be searched sequentially to locate an entry.

Hashing Index & Hashing File Organization

• In a hash index, buckets store entries with pointers to records

bucket1

15151: block 1, offset 0

bucket2

32343: block 3, offset 0 58583: block 3, offset 24

• In a hash file-organization, buckets store records

bucket	: 0		
bucket	: 1		
15151	Mozart	Music	40000
bucket	: 2		
32343	El Said	History	80000
58583	Califieri	History	60000
bucket	3		
22222		Physics	95000
33456	Gold	Physics	87000
98345	Kim	Elec. Eng.	80000

bucket 4

bucket 5

bucket 6

bucket 7

45565 Katz

83821 Brandt

12121 Wu

76543 Singh

76766 Crick

Finance

Finance

Biology

Comp. Sci. 75000

Comp. Sci. 92000

10101 Srinivasan Comp. Sci. 65000