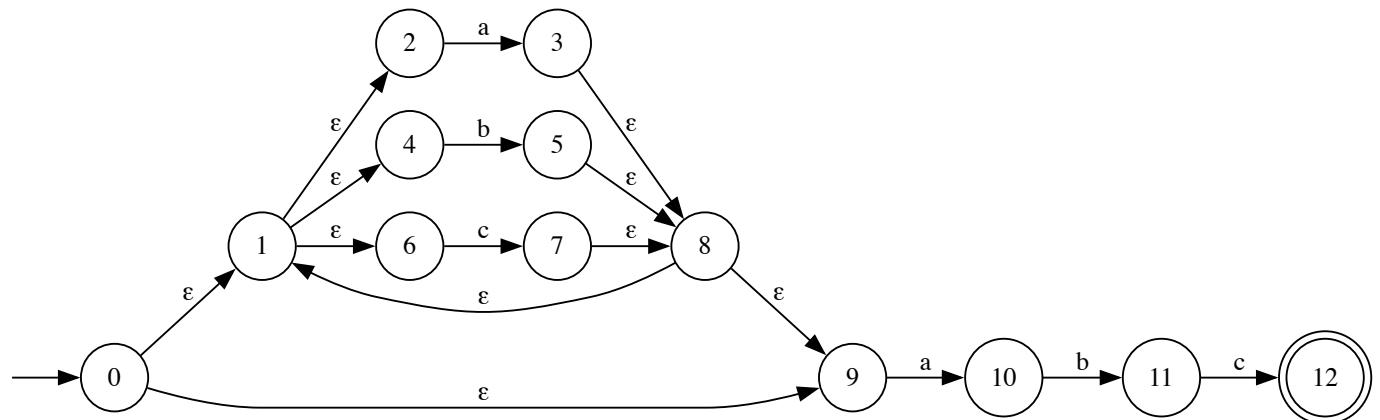


CS323 Written Assignment 2 Sample Answer

Exercise 1

NFA:



The NFA can accept the string $abcabc$, the sequence is 0, 1, 2, 3, 8, 1, 4, 5, 8, 1, 6, 7, 8, 9, 10, 11, 12.

$$A = \epsilon\text{-closure}(\{0\}) = \{0, 1, 2, 4, 6, 9\}$$

$$B = \epsilon\text{-closure}(\text{move}[A, a]) = \epsilon\text{-closure}(\{3, 10\}) = \{1, 2, 3, 4, 6, 8, 9, 10\}$$

$$C = \epsilon\text{-closure}(\text{move}[A, b]) = \epsilon\text{-closure}(\{5\}) = \{1, 2, 4, 5, 6, 8, 9\}$$

$$D = \epsilon\text{-closure}(\text{move}[A, c]) = \epsilon\text{-closure}(\{7\}) = \{1, 2, 4, 6, 7, 8, 9\}$$

$$E = \epsilon\text{-closure}(\text{move}[B, b]) = \epsilon\text{-closure}(\{5, 11\}) = \{1, 2, 4, 5, 6, 8, 9, 11\}$$

$$F = \epsilon\text{-closure}(\text{move}[E, c]) = \epsilon\text{-closure}(\{7, 12\}) = \{1, 2, 4, 6, 7, 8, 9, 12\}$$

$$\text{DTran}[A, a] = B$$

$$\text{DTran}[A, b] = C$$

$$\text{DTran}[A, c] = D$$

$$\text{DTran}[B, a] = B$$

$$\text{DTran}[B, b] = E$$

$$\text{DTran}[B, c] = D$$

$$\text{DTran}[C, a] = B$$

$$\text{DTran}[C, b] = C$$

$$\text{DTran}[C, c] = D$$

$$\text{DTran}[D, a] = B$$

$$\text{DTran}[D, b] = C$$

$D\text{Tran}[D, c] = D$

$D\text{Tran}[E, a] = B$

$D\text{Tran}[E, b] = C$

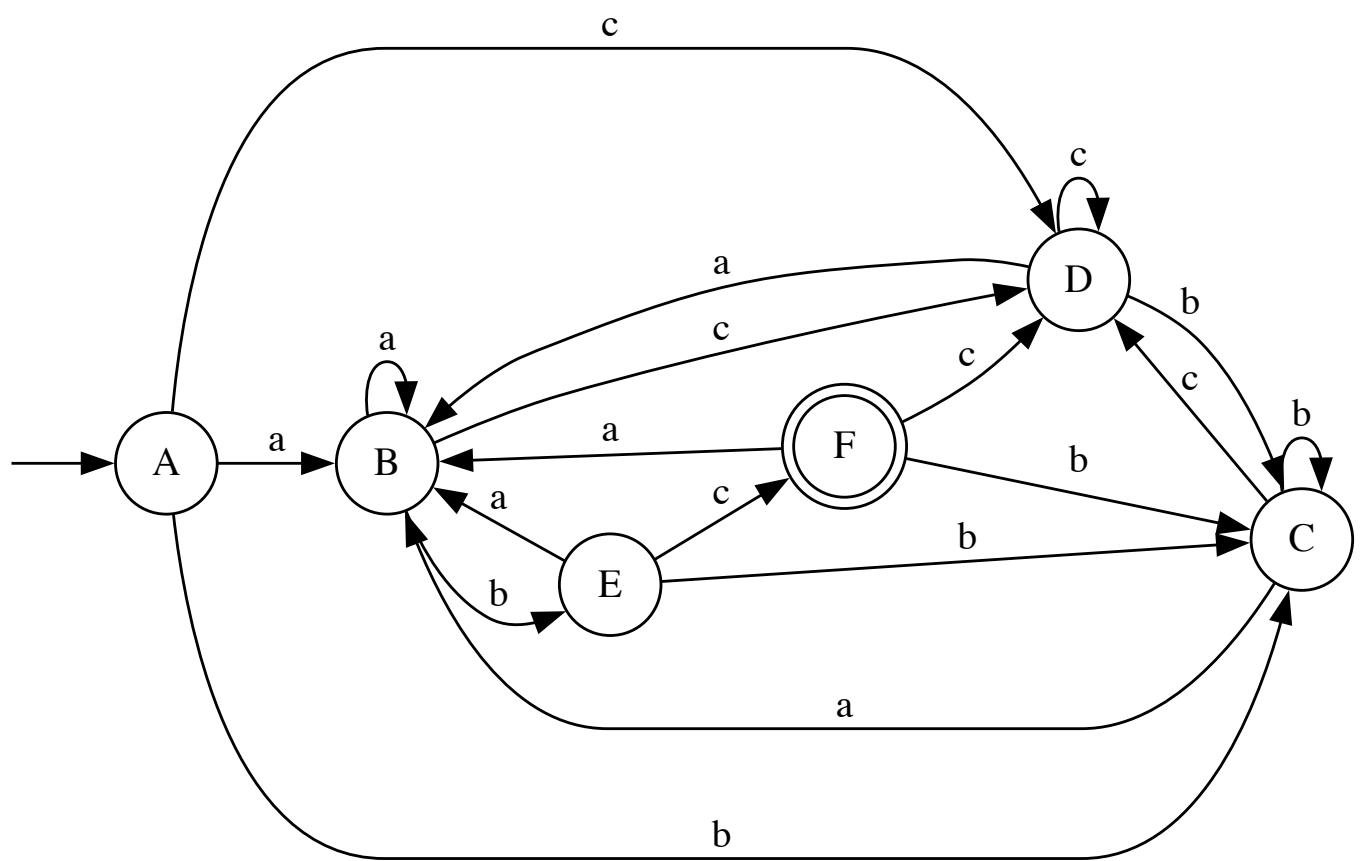
$D\text{Tran}[E, c] = F$

$D\text{Tran}[F, a] = B$

$D\text{Tran}[F, b] = C$

$D\text{Tran}[F, c] = D$

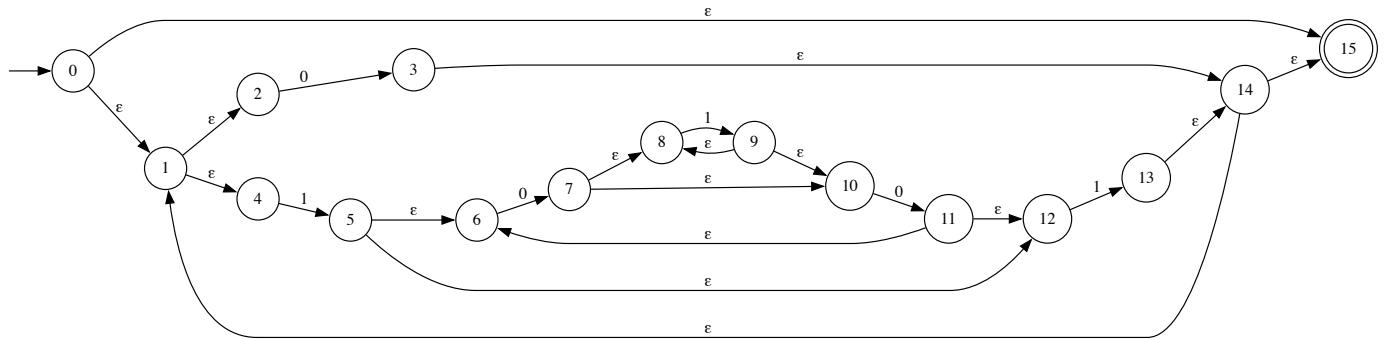
DFA:



The DFA can accept the string $abcabc$, the sequence is A, B, E, F, B, E, F .

Exercise 2

NFA:



The NFA can accept the string 10101.

$$A = \epsilon\text{-closure}(\{0\}) = \{0, 1, 2, 4, 15\}$$

$$B = \epsilon\text{-closure}(\text{move}[A, 0]) = \epsilon\text{-closure}(\{3\}) = \{1, 2, 3, 4, 14, 15\}$$

$$C = \epsilon\text{-closure}(\text{move}[A, 1]) = \epsilon\text{-closure}(\{5\}) = \{5, 6, 12\}$$

$$D = \epsilon\text{-closure}(\text{move}[C, 0]) = \epsilon\text{-closure}(\{7\}) = \{7, 8, 10\}$$

$$E = \epsilon\text{-closure}(\text{move}[C, 1]) = \epsilon\text{-closure}(\{13\}) = \{1, 2, 4, 13, 14, 15\}$$

$$F = \epsilon\text{-closure}(\text{move}[D, 0]) = \epsilon\text{-closure}(\{11\}) = \{6, 11, 12\}$$

$$G = \epsilon\text{-closure}(\text{move}[D, 1]) = \epsilon\text{-closure}(\{9\}) = \{8, 9, 10\}$$

$$\text{DTran}[A, 0] = B$$

$$\text{DTran}[A, 1] = C$$

$$\text{DTran}[B, 0] = B$$

$$\text{DTran}[B, 1] = C$$

$$\text{DTran}[C, 0] = D$$

$$\text{DTran}[C, 1] = E$$

$$\text{DTran}[D, 0] = F$$

$$\text{DTran}[D, 1] = G$$

$$\text{DTran}[E, 0] = B$$

$$\text{DTran}[E, 1] = C$$

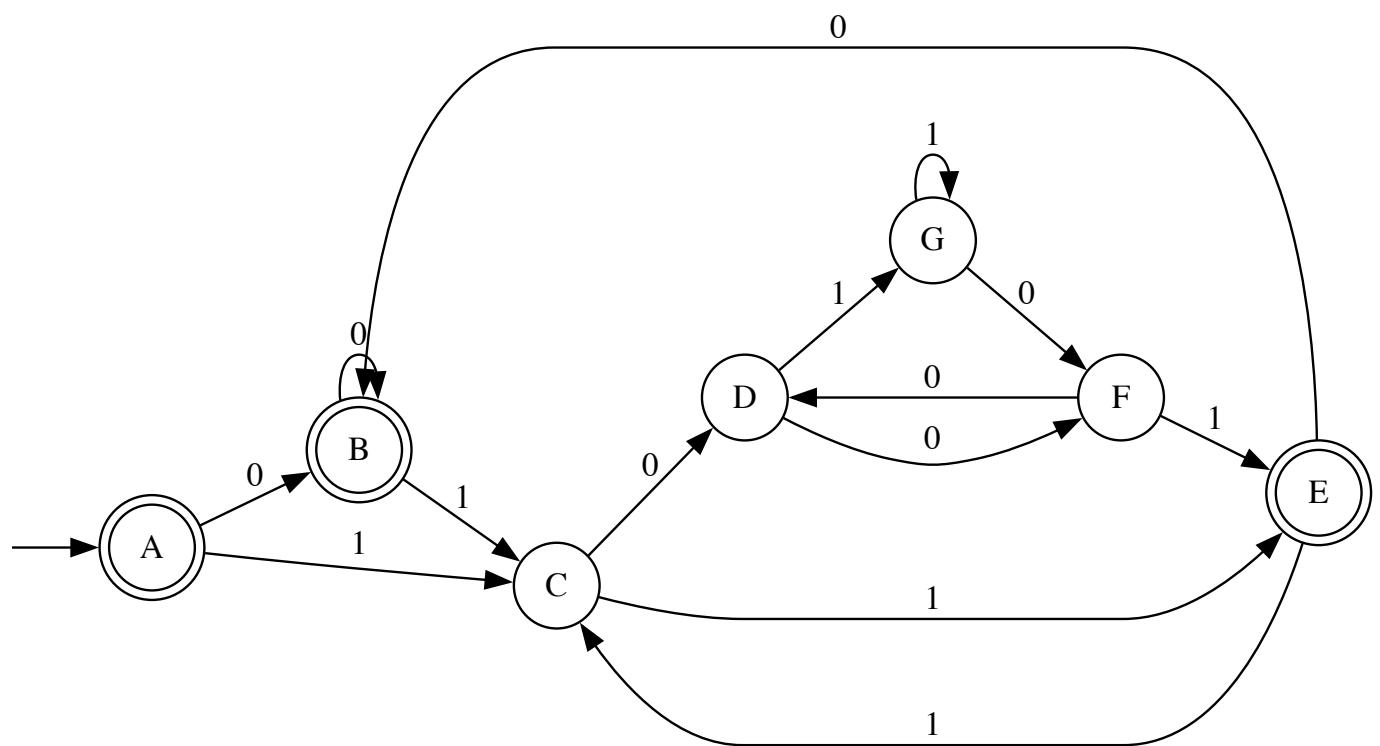
$$\text{DTran}[F, 0] = D$$

$$\text{DTran}[F, 1] = E$$

$$\text{DTran}[G, 0] = F$$

$$\text{DTran}[G, 1] = G$$

DFA:



The DFA will reject the string 10.