

# Novel Remapping Method for HR-EBSD based on Computer Vision Algorithm

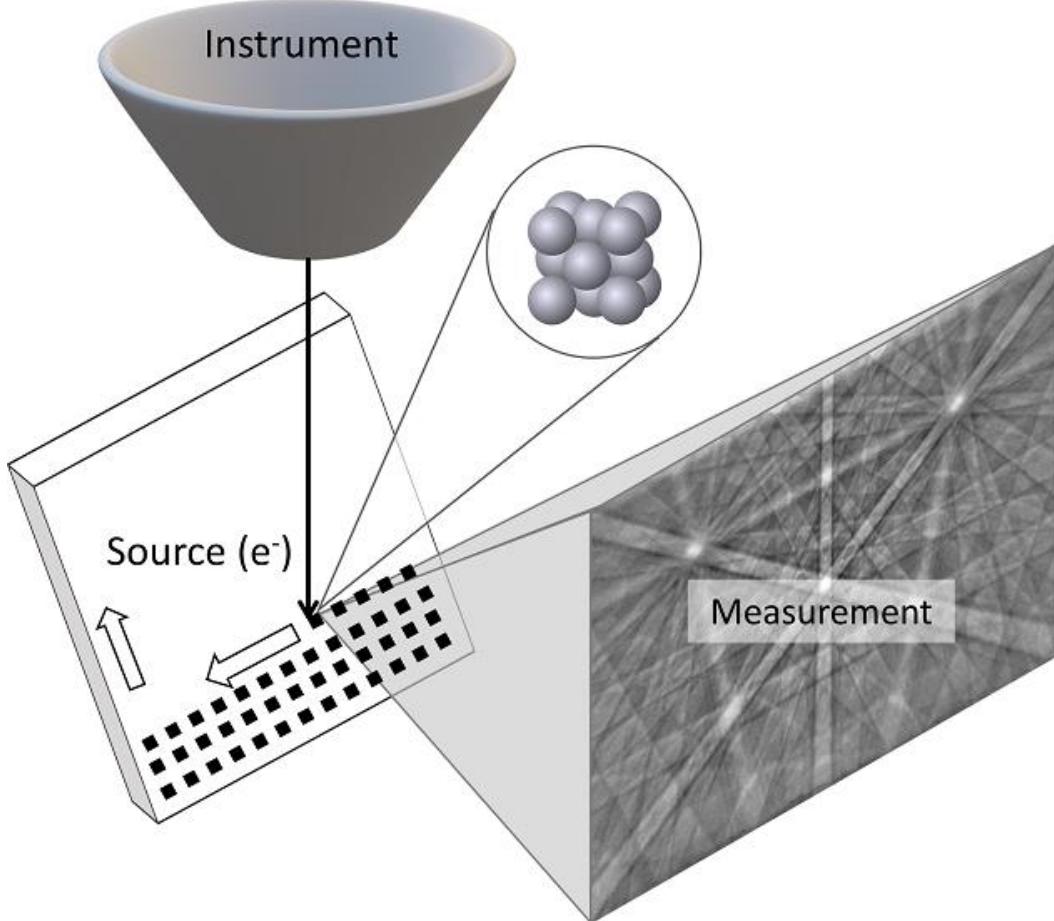
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USA*

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# Materials Characterization

## Electron Backscatter Diffraction

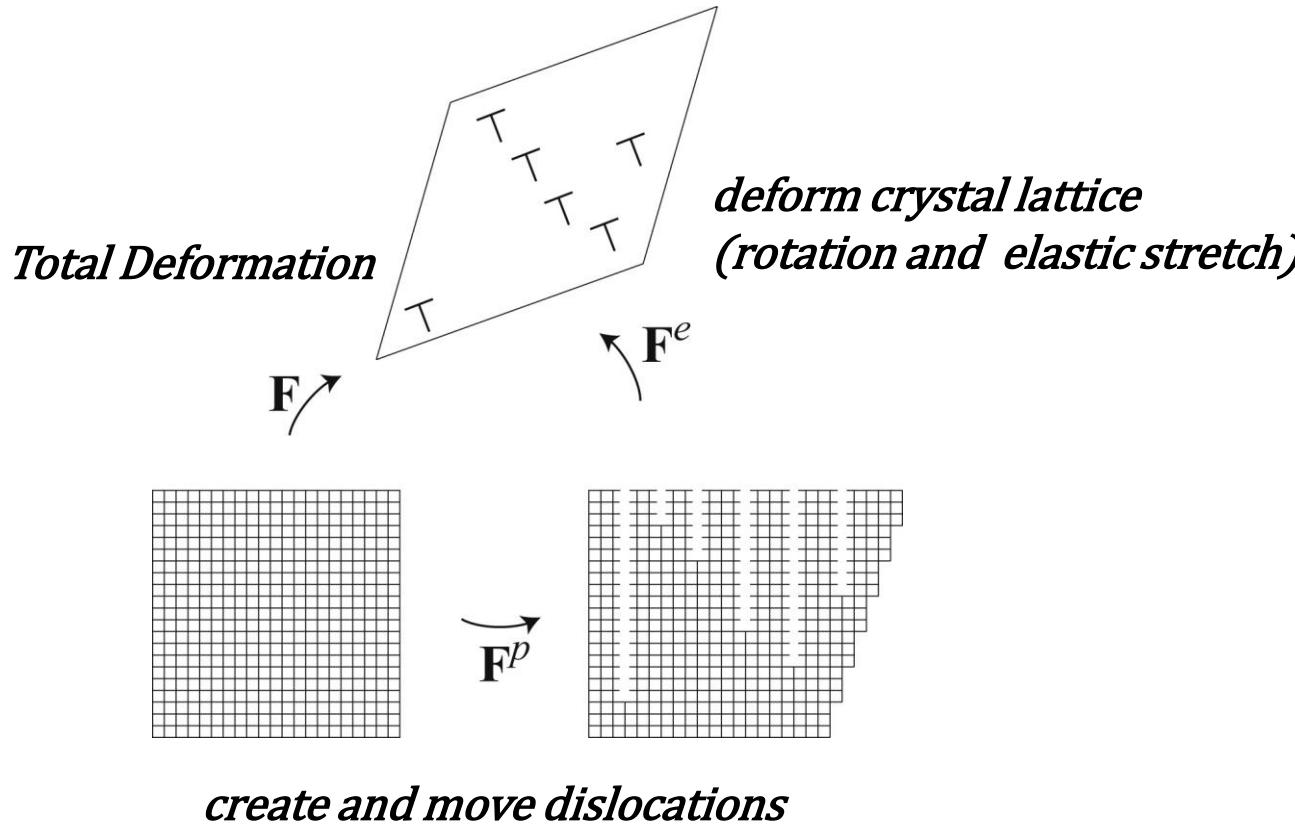


Texture

Microstructure

Deformation

# Crystal Deformation



Deformation gradient tensor:

$$\mathbf{F} = \mathbf{F}^e \mathbf{F}^p$$

Elastic stretch: shift of the zone axis and changes in the interplanar angles

$$\boldsymbol{\varepsilon} = \frac{1}{2} (\mathbf{F}^e + \mathbf{F}^{eT}) - \mathbf{I}$$

Lattice rotation: whole pattern rotation

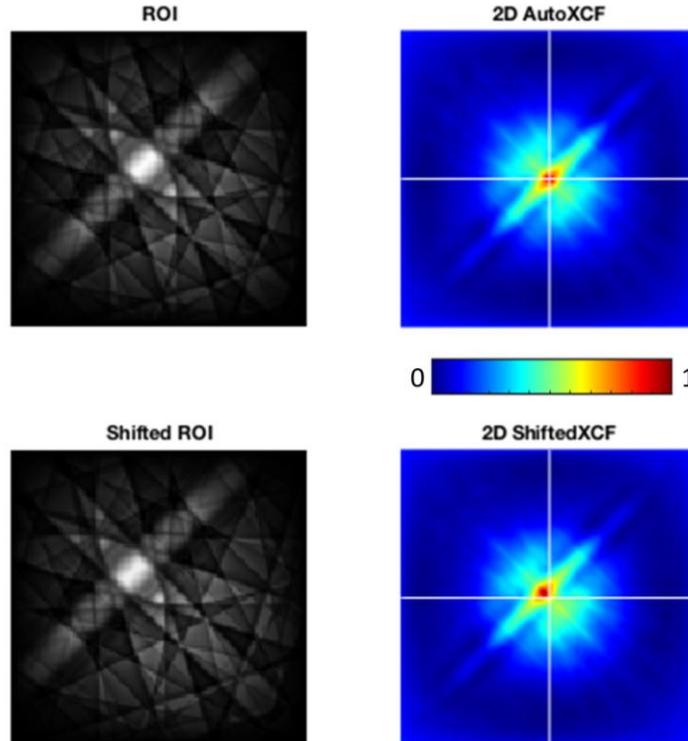
$$\boldsymbol{\omega} = \frac{1}{2} (\mathbf{F}^e - \mathbf{F}^{eT})$$

K.C. Le *et al.*, 2015;

Kröner, 1958;

B.C. Larson *et al.*, 2007

## Cross-Correlation



$$f_{test} * f_{ref} = \mathfrak{I}^{-1}[\mathfrak{I}(f_{test}) \cdot \text{conj}(\mathfrak{I}(f_{ref}))]$$

10/31/2020

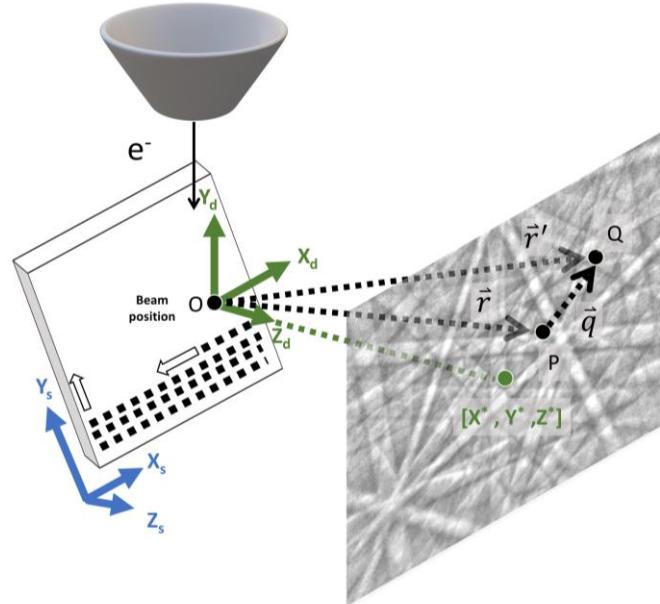
Wilkinson et al, 2006

## Higher level of sensitivity:

- Rotation:  $1 \times 10^{-4}$  rad or  $0.006^\circ$
- Elastic strain:  $1 \times 10^{-4}$
- GND lower noise floor:
  - Hough:  $\Delta\rho \approx 10^{14}$  lines/m<sup>2</sup>
  - HR-EBSD:  $\Delta\rho \approx 10^{12}$  lines/m<sup>2</sup>

Shift of the XCF peak from the origin represents the shift of the test ROI from reference ROI.

# HR-EBSD (Cross-Correlation)



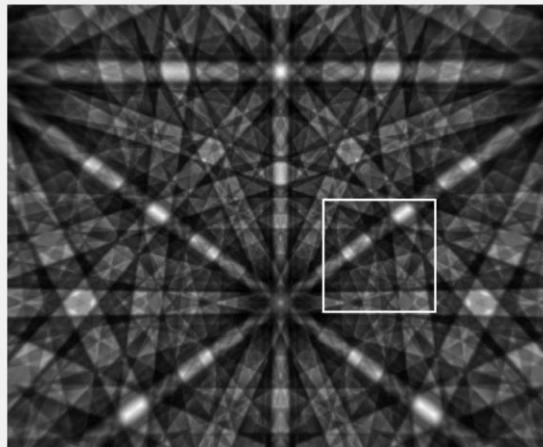
**Non-linear minimization method to obtain deformation gradient tensor ( $F^e$ ):**

$$\min f(F^e) = \sum_{\{ROI\}} \frac{1}{2} \left| \frac{Z^*}{(F^e \cdot \vec{r}) \cdot \vec{k}} F^e \cdot \vec{r} - (\vec{r} + \vec{q}) \right|^2$$

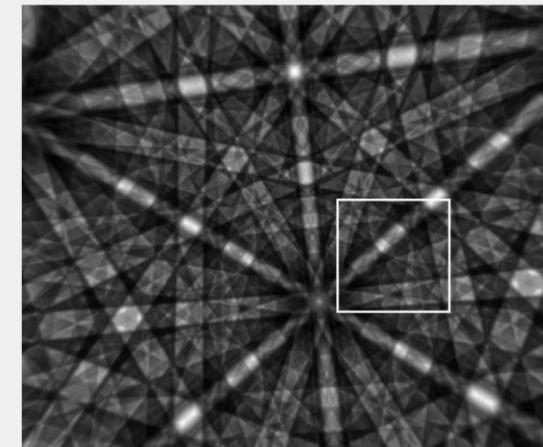
$\vec{r}$ : center of ROI  
 $Z^*$ : detector distance  
 $\vec{q}$  : measured shift

$F^e$  between two images can be calculated from shifts measured between many regions of interest (ROIs).

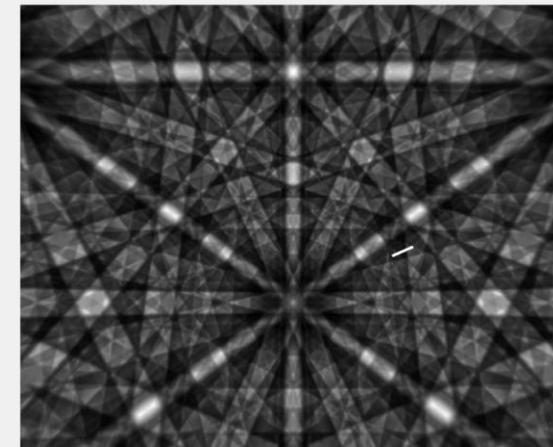
Reference Pattern



Test Pattern

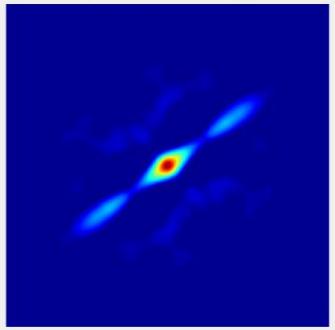
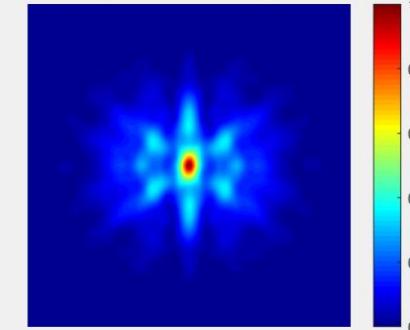
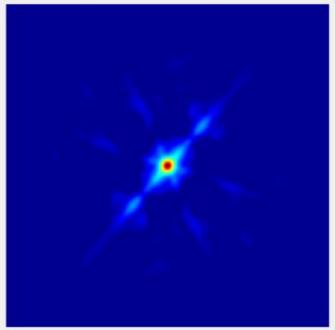
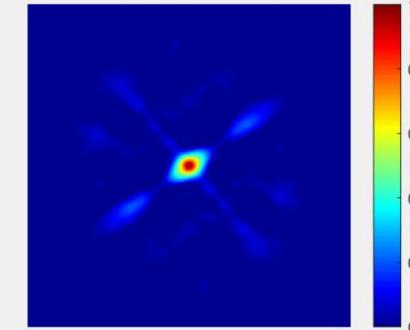


Total Shift



# Cross-Correlation: Limitation

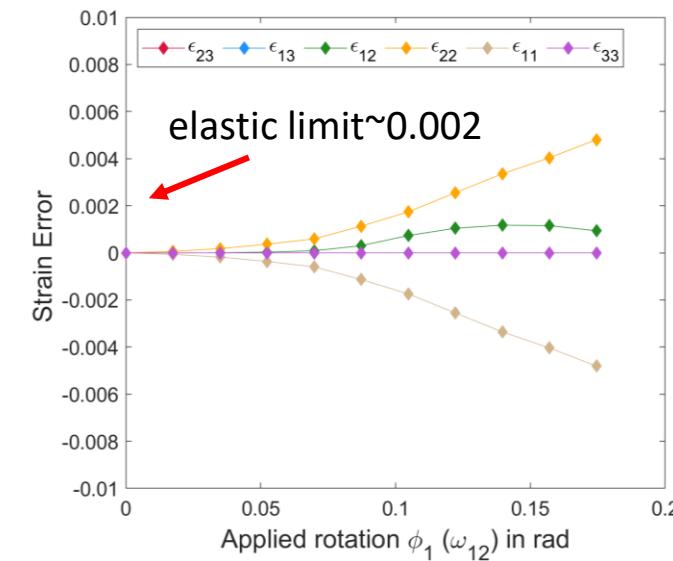
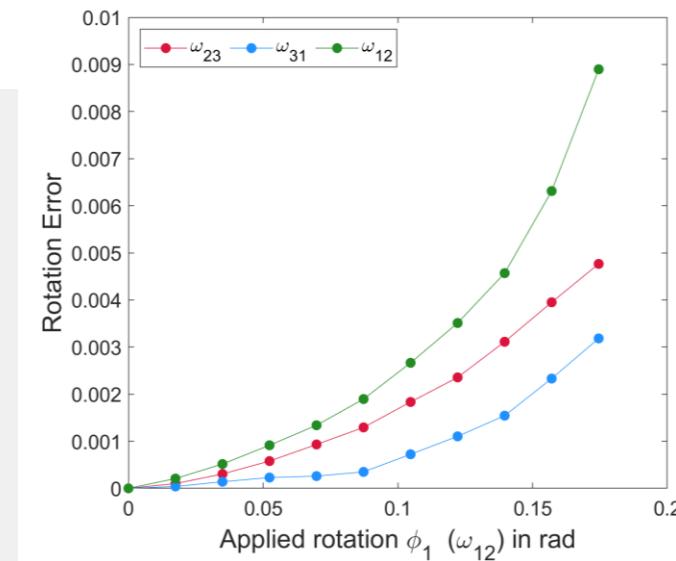
## Cross-Correlation Between Patterns of Large Relative Rotations

XCF of ROI<sub>1</sub> at applied  $\omega_{12}$ : 0.00 (rad)XCF of ROI<sub>25</sub> at applied  $\omega_{12}$ : 0.00 (rad)XCF of ROI<sub>65</sub> at applied  $\omega_{12}$ : 0.00(rad)XCF of ROI<sub>95</sub> at applied  $\omega_{12}$ : 0.00 (rad)

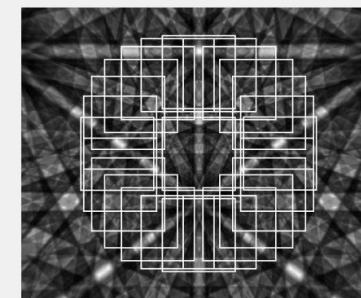
XCF peak changes at higher rotations

- Multiple peaks
- Peak shape distortion

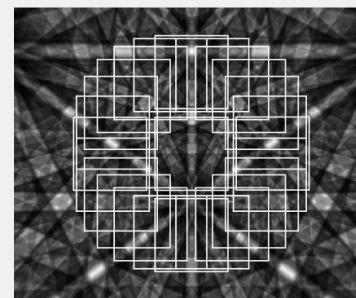
## Rotation and Strain Error



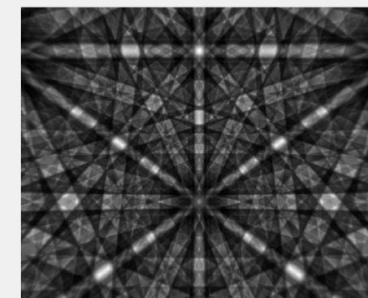
## Reference Pattern



## Test Pattern



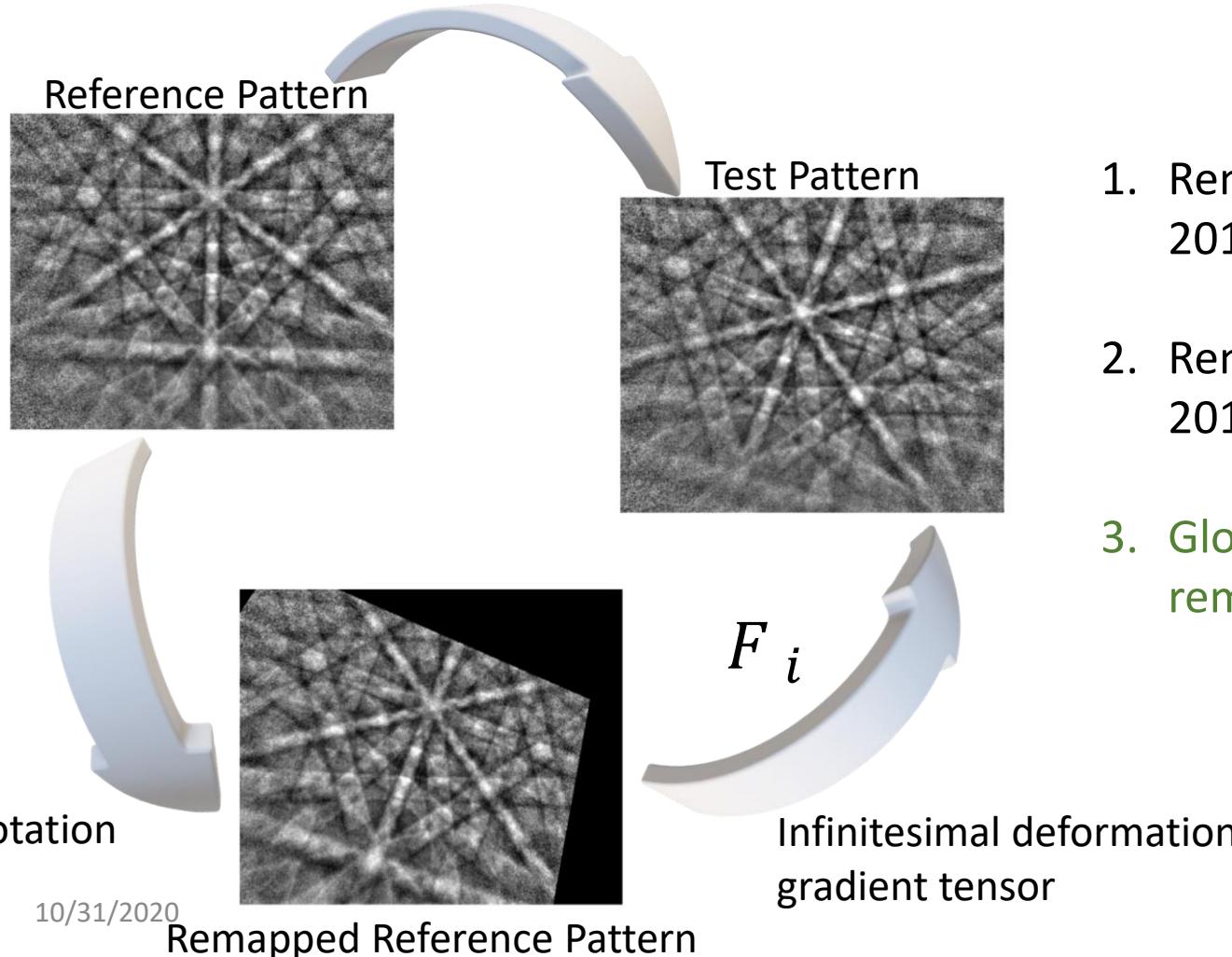
## Total Shift



# Pattern Remapping Technique

Total deformation gradient tensor

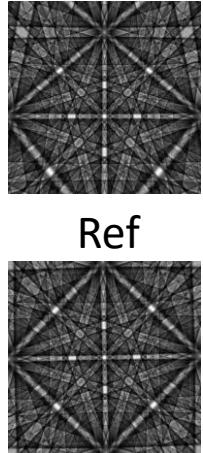
$$F_f = F_i \cdot R_f$$



1. Remapping using orientation matrix (Maurice *et al*, 2012)
2. Remapping using cross-correlation (Britton *et al*, 2012)
3. Global matching using computer vision for remapping (Zhu *et al*, 2019)

Britton *et al*, Ultramicroscopy 2012  
Maurice *et al*, Ultramicroscopy 2012  
Zhu *et al*, Ultramicroscopy 2020

Test

Fixed Image  
(deformed)Moving Image  
(undeformed)Histogram  
Matching Filter  
&  
Anisotropic  
Diffusion Filter

Moving Image Pyramid

 $P_{n=N}$  $P_{n=0}$ Demons  
Registration  
Iteration

Fixed Image Pyramid

 $P_{n=N}$  $P_{n=0}$ Move to Next  
Pyramid Level if  $P \neq P_{n=N}$ 

$$\min(R_f) = \sum_{\{ROI\}} \frac{1}{2} \left| \frac{Z^*}{(R_f \cdot \vec{r}) \cdot \vec{k}} R_f \cdot \vec{r} - (\vec{r} + \vec{q}) \right|^2$$

Non-linear  
MinimizationMeasured  
 $\vec{q}$ 

YES

Last  
Pyramid  
Level?

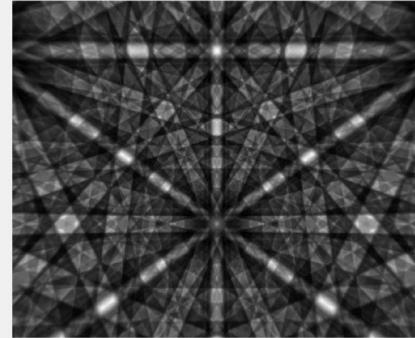
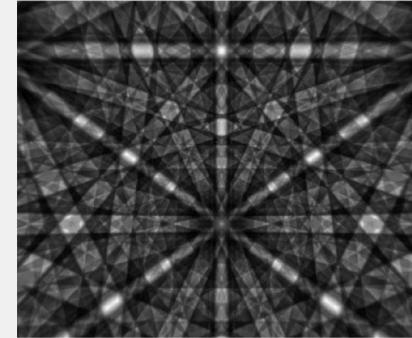
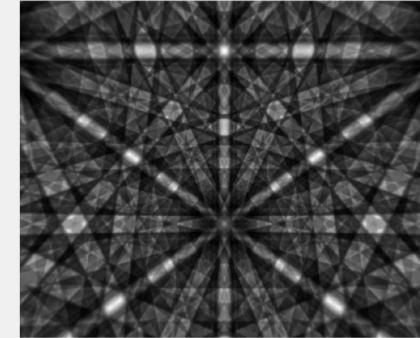
YES

Last  
Iteration?

NO

NO

# Determine the Remapping Rotation Matrix

**Reference Pattern****Test Pattern****Registered Reference Pattern**

$$\min f(R_f) = \sum_{\{ROI\}} \frac{1}{2} \left| \frac{Z^*}{(R_f \cdot \vec{r}) \cdot \vec{k}} R_f \cdot \vec{r} - (\vec{r} + \vec{q}) \right|^2$$

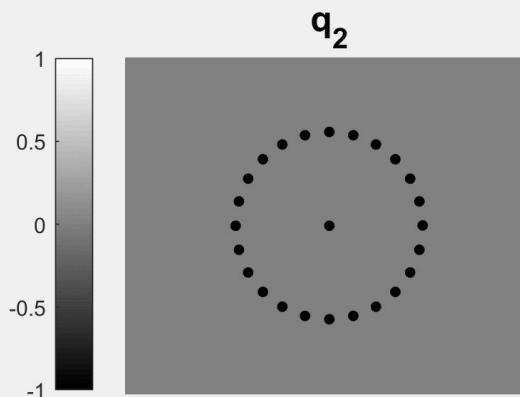
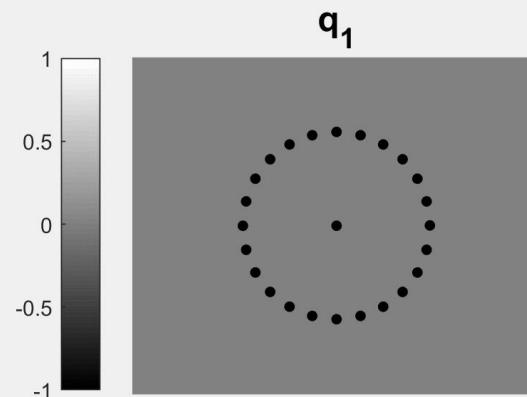
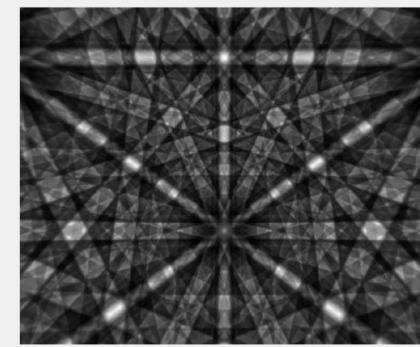
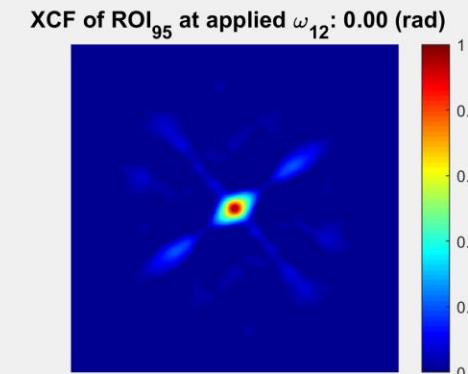
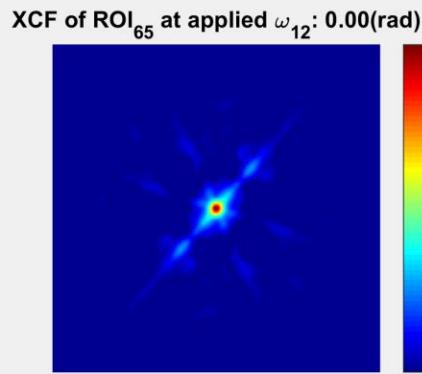
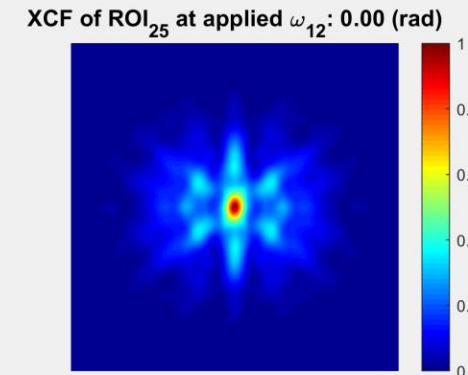
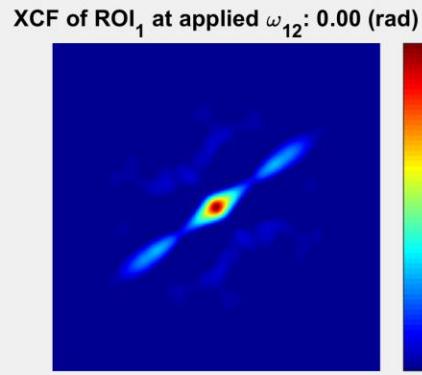
**Total Shift**

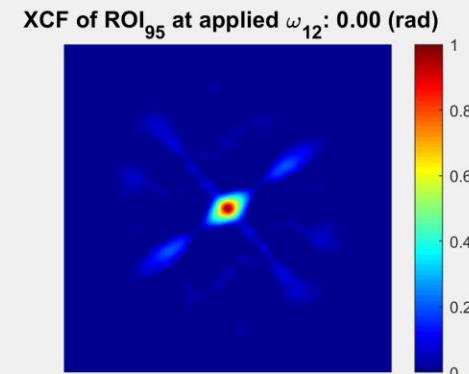
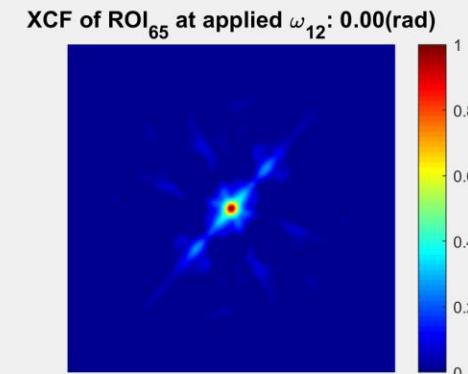
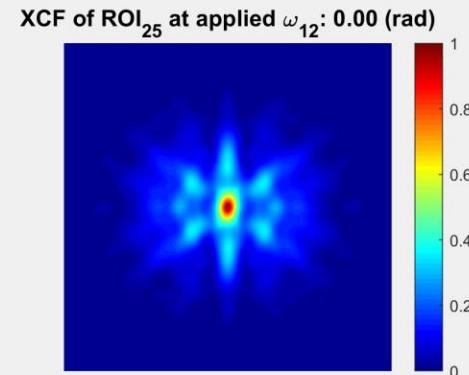
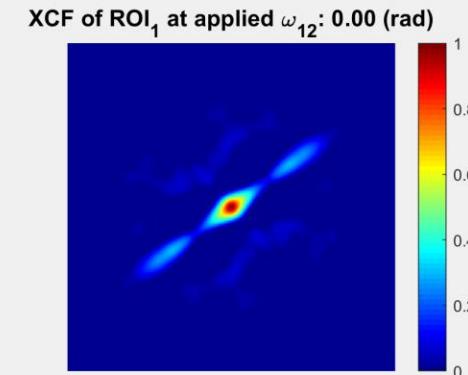
Image Registration Shift Field:  $\vec{q} = [q_1, q_2]$

# Cross-Correlation (after Remapping)

Cross-Correlation (No remapping)



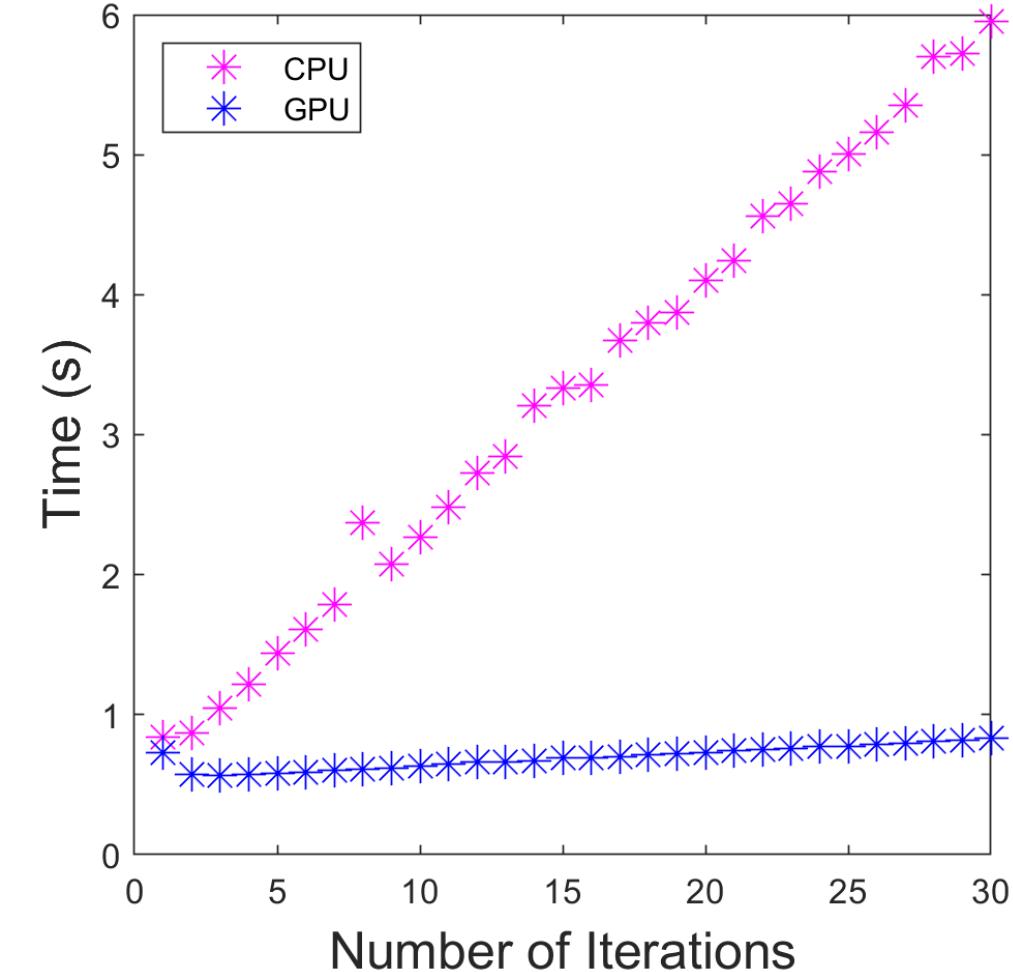
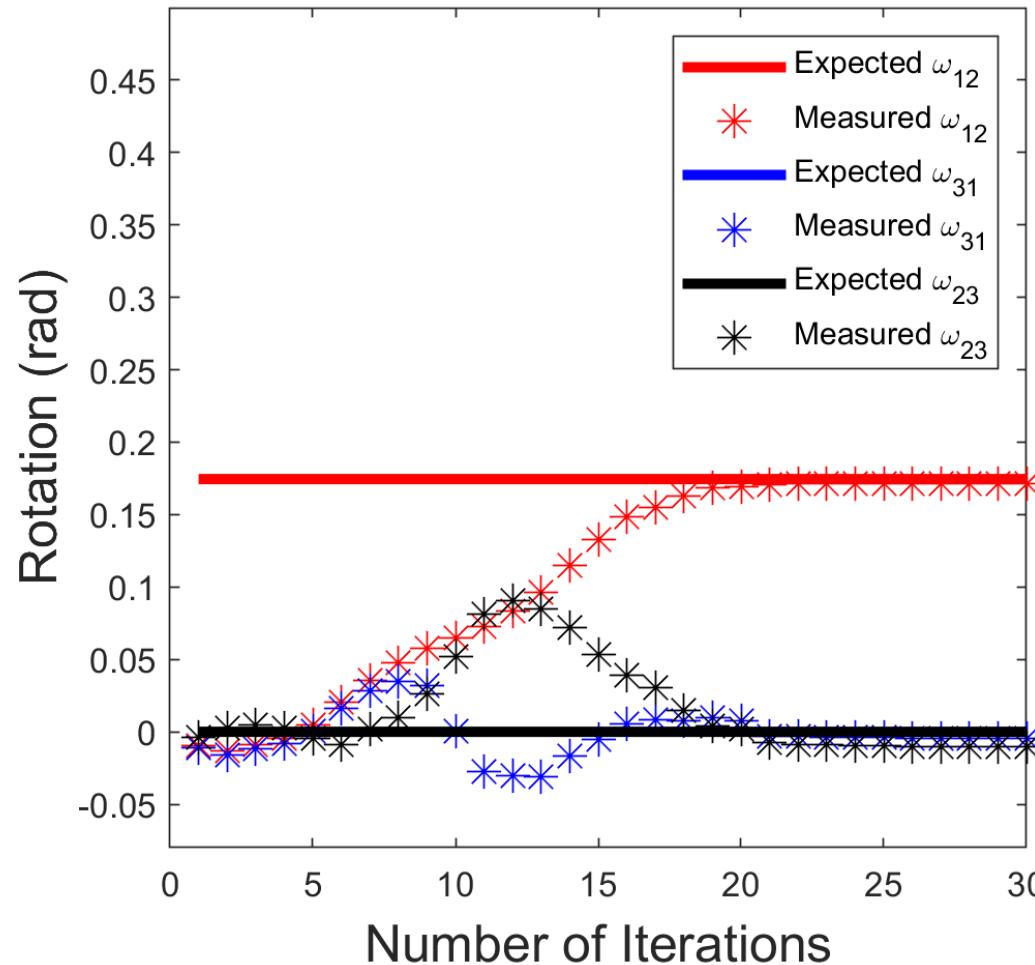
Cross-Correlation (After remapping)



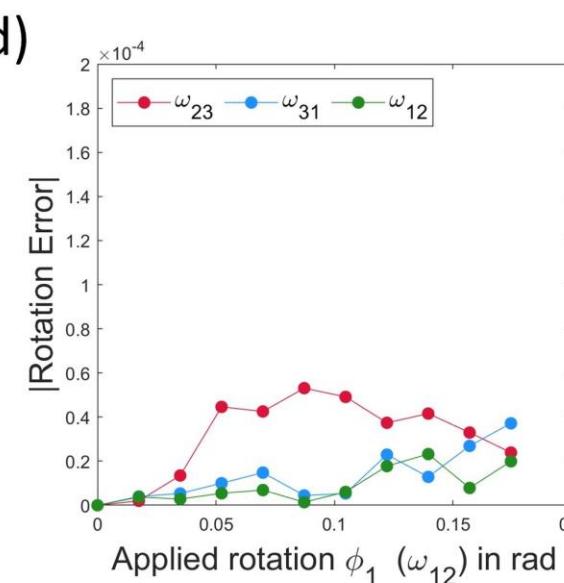
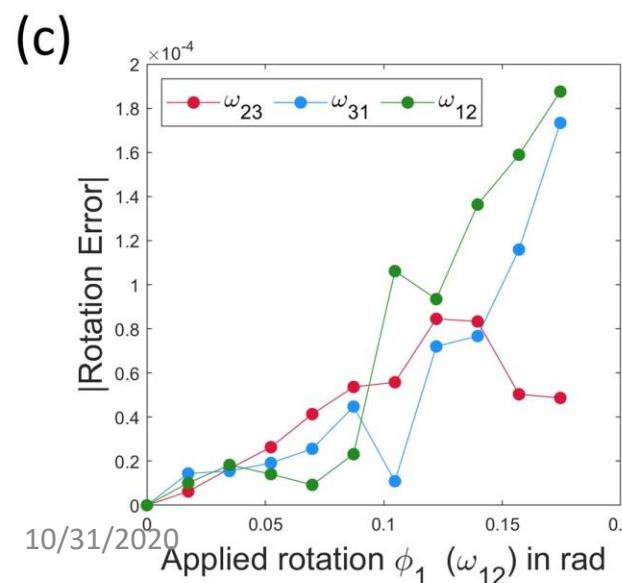
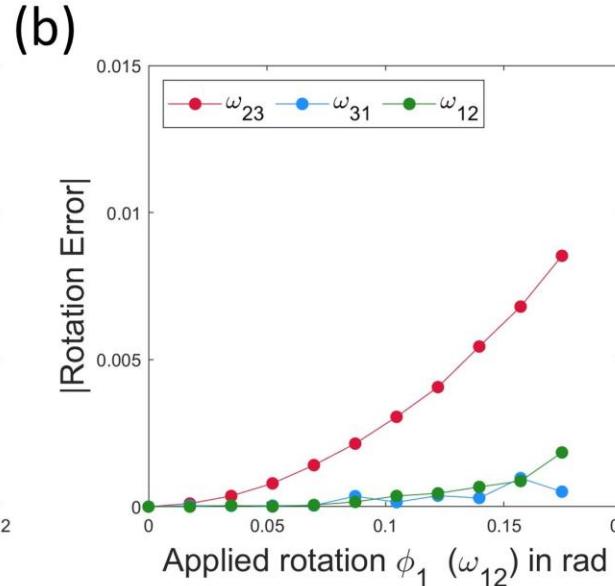
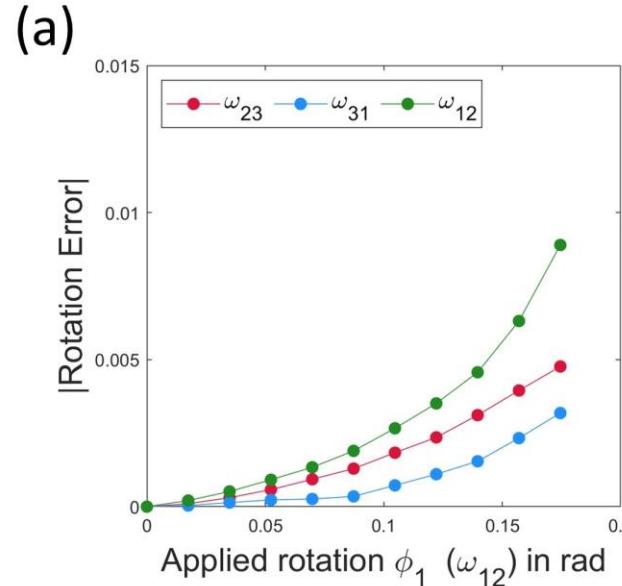
$$F_f = F_i \cdot R_f$$

- No peak distortion for the cross-correlation after remapping
- Single high intensity peak only

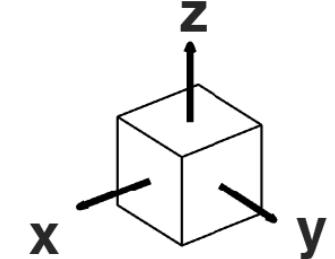
# GPU Acceleration for Image Registration



## Angular Resolution of Different Methods



Reference pattern: [0,0,0]  
Test pattern: [i,0,0]  $i=0^\circ \sim 10^\circ$



(a) cross-correlation

(b) image registration

(c) 1<sup>st</sup> pass cross-correlation for remapping + 2<sup>nd</sup> pass cross-correlation for infinitesimal deformation

(d) 1<sup>st</sup> pass image registration for remapping + 2<sup>nd</sup> pass cross-correlation for infinitesimal deformation

- image registration (b) can not be used alone for accuracy.
- Method (d) outperforms (a) and (b).
- (d) slightly improves angular resolution compared to (c).

# Phantom strain and stress

Cross-Correlation

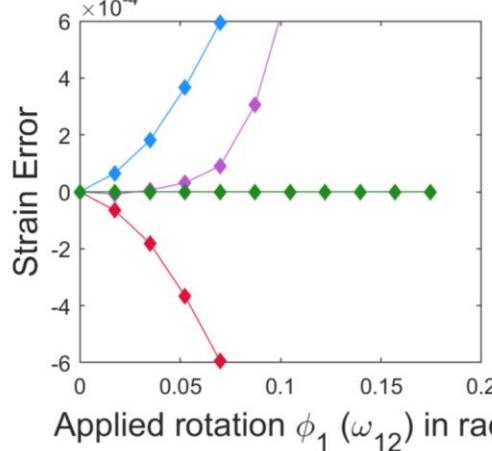
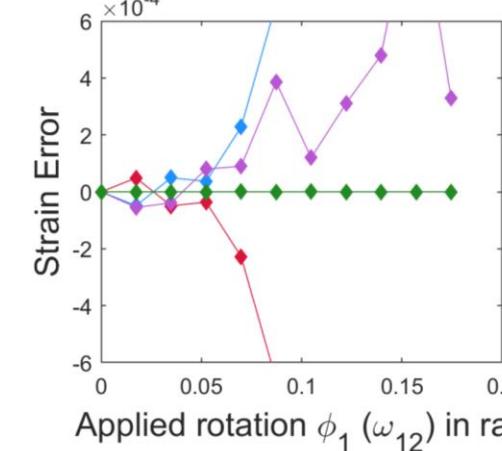


Image Registration



Cross-Correlation Remap

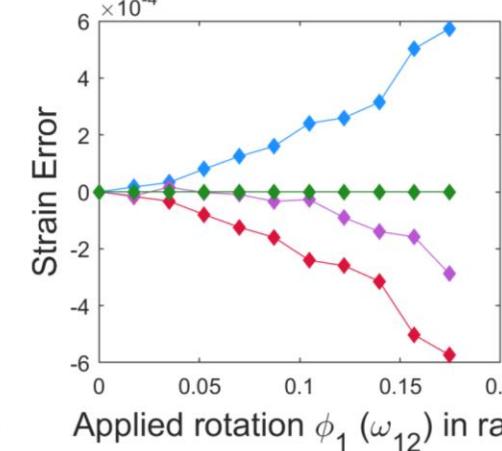
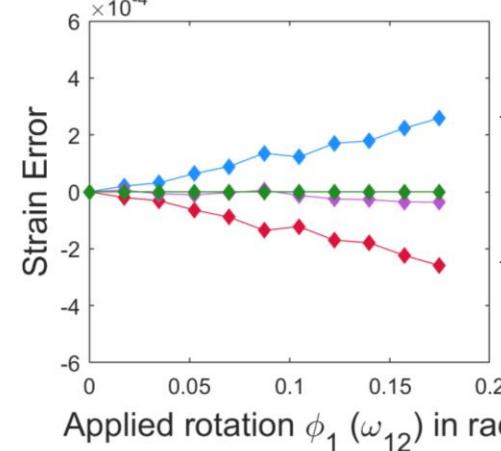


Image Registration Remap



Phantom strain  
 $<2 \times 10^{-4}$

Cross-Correlation

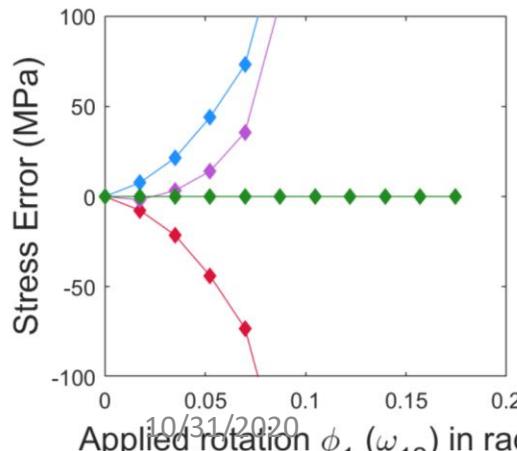
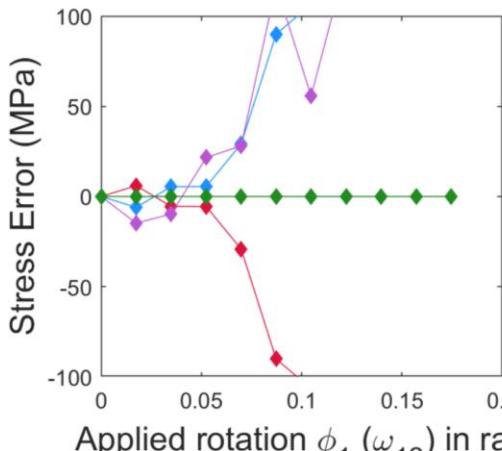


Image Registration



Cross-Correlation Remap

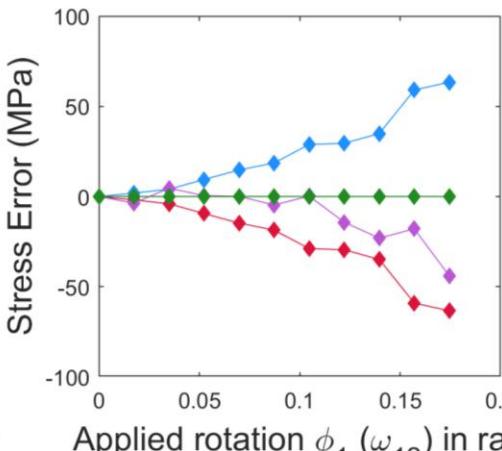
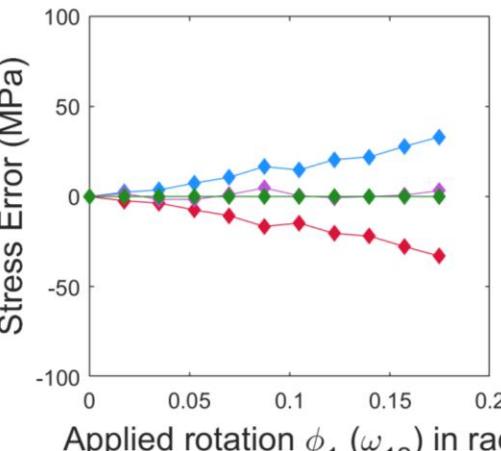


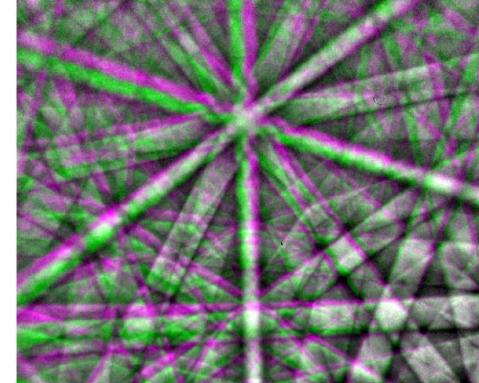
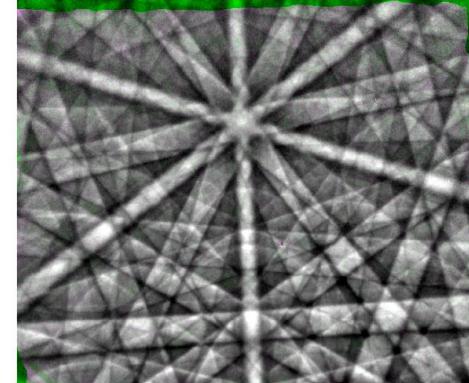
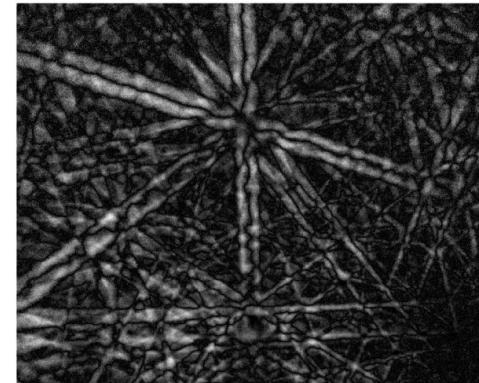
Image Registration Remap



Phantom stress  
 $<30$  MPa

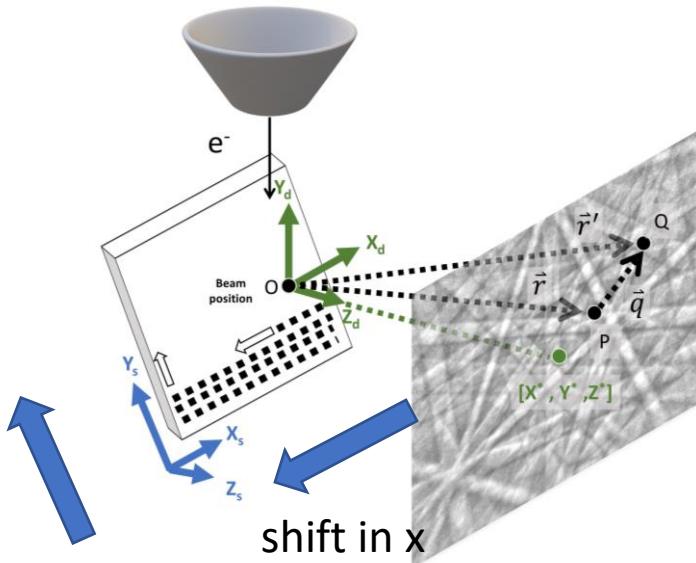
Zhu et al, 2020

# Registration with Experimental Pattern

**Unregistered****Registered****Unregistered Residual****Registered Residual**

# Zoom and Shift Correction

Zoom  
&  
shift in y

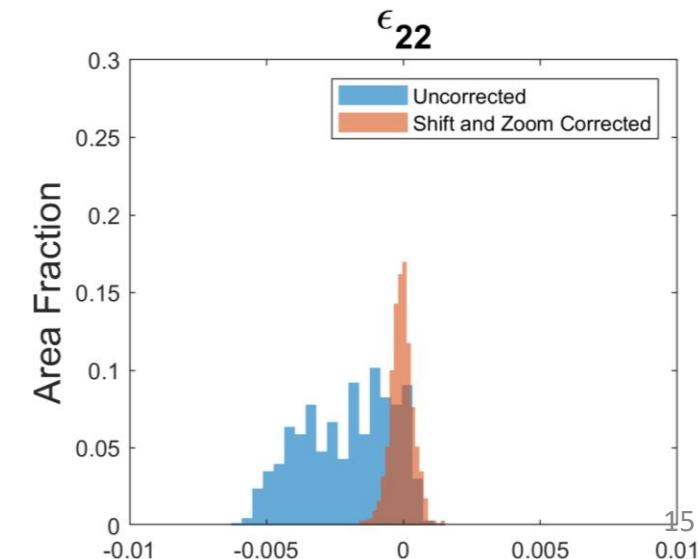
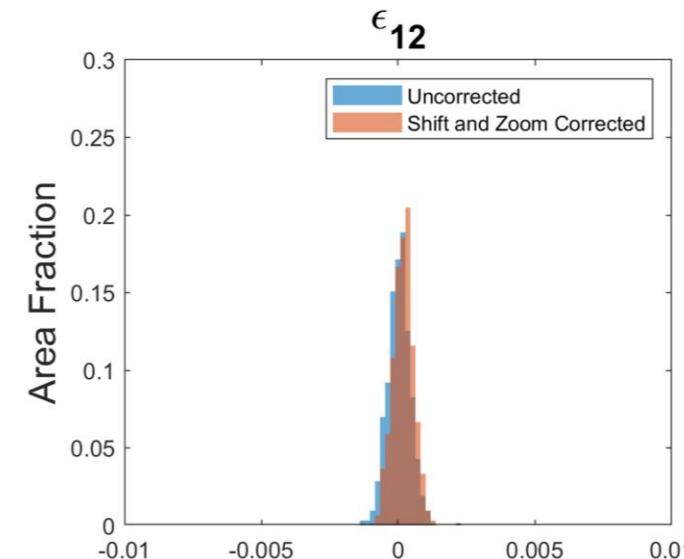
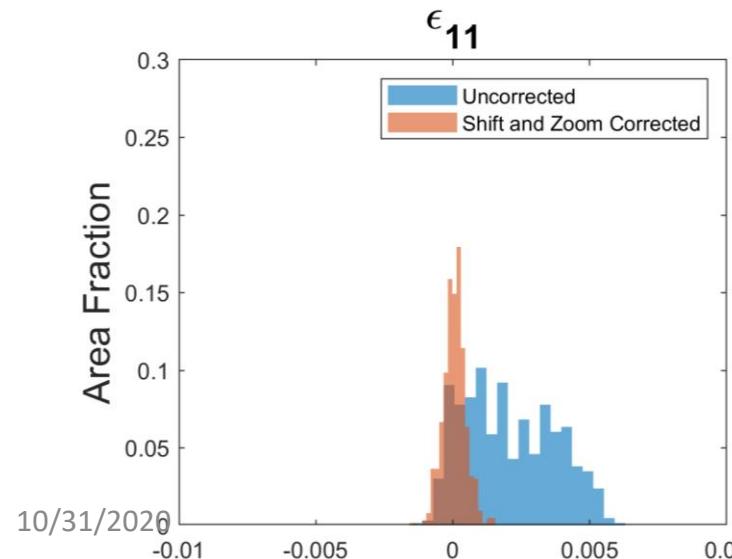


Zoom or Shrinkage Correction: ratio between detector distance (DD) between the reference and test patterns.

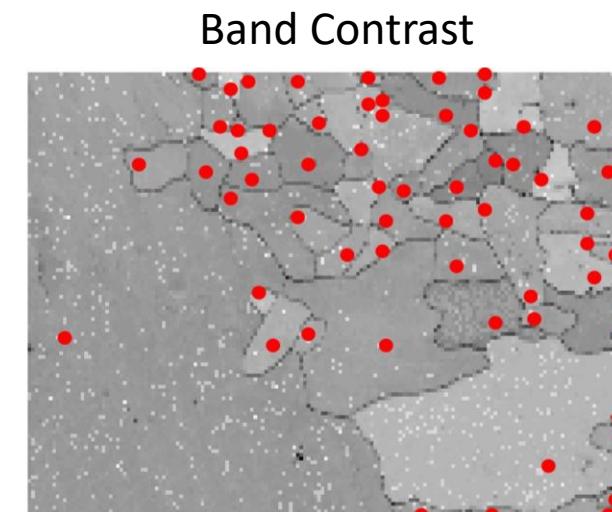
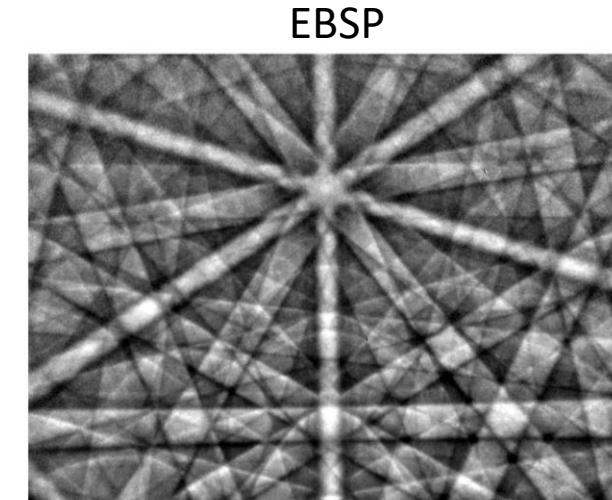
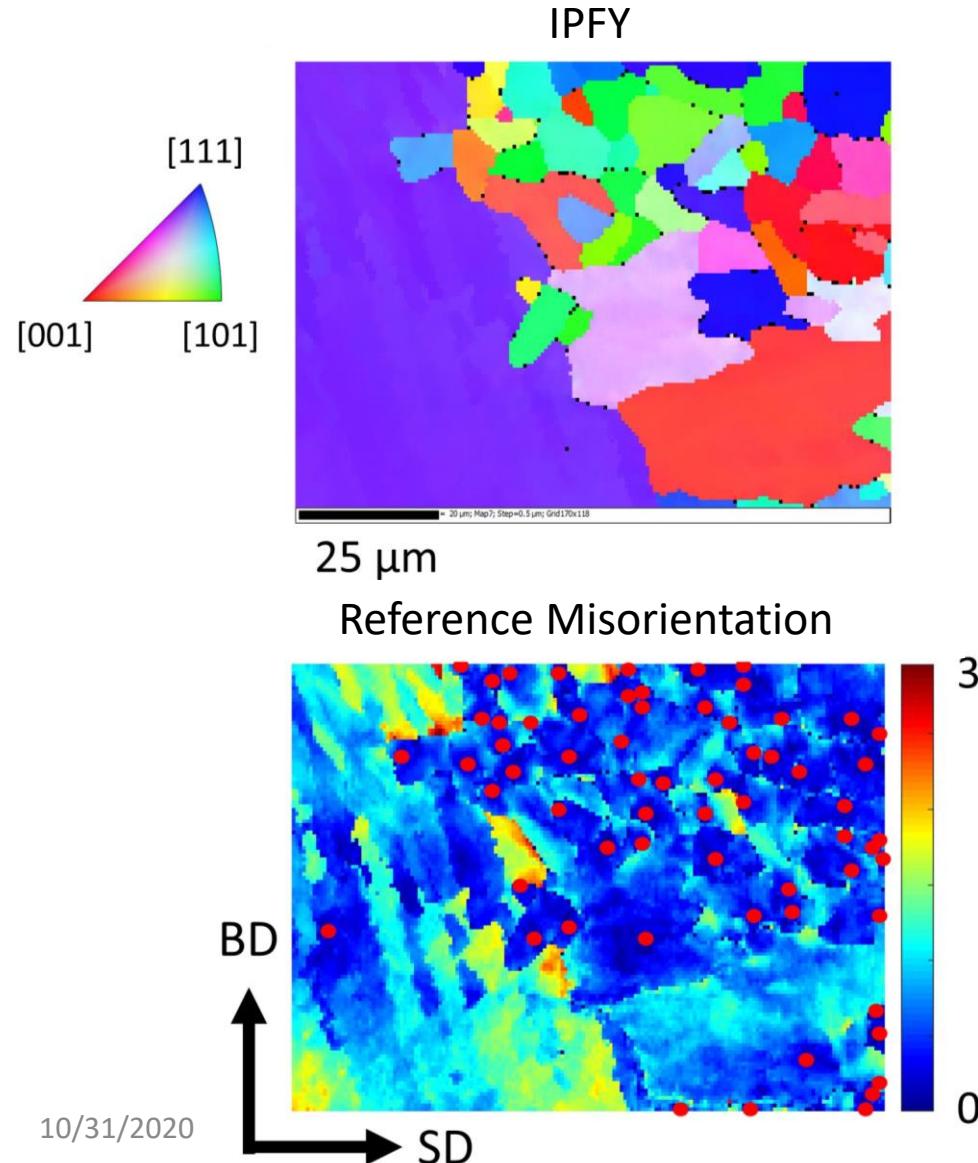
Shift Correction: difference in beam position on the sample.

Britton *et al*, Ultramicroscopy 2011

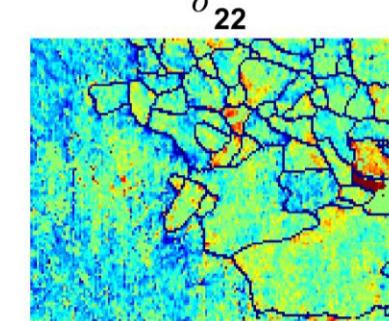
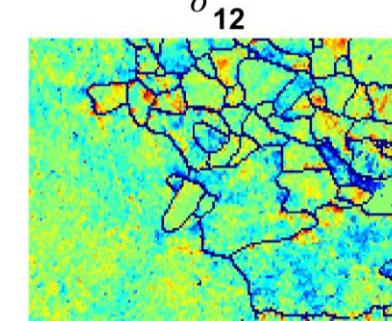
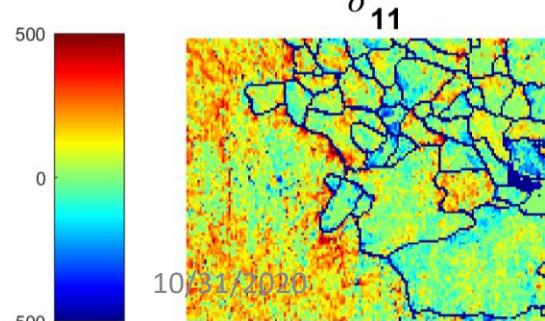
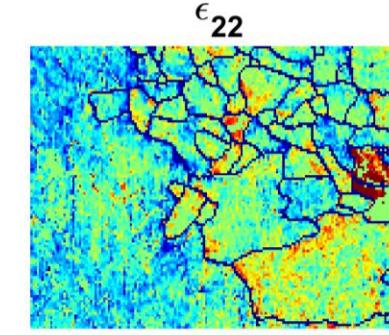
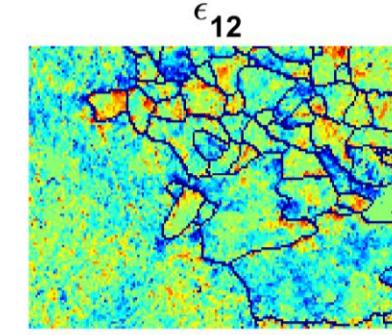
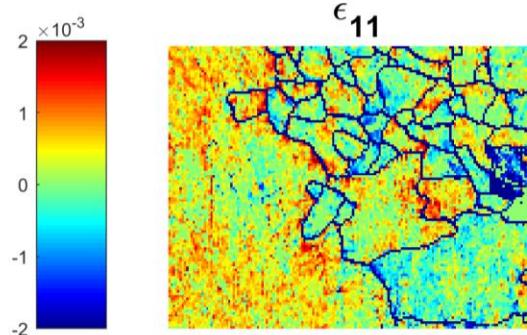
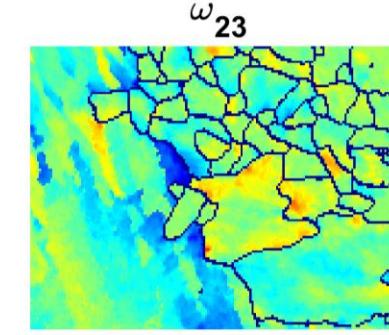
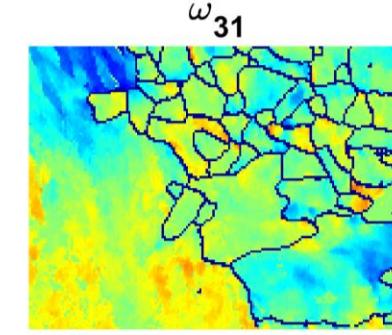
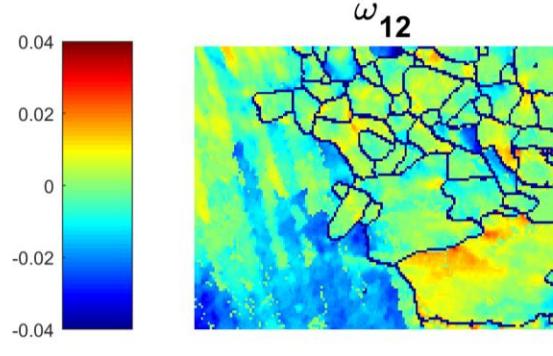
Test Sample: Single crystal Silicon (200  $\mu\text{m}$  by 200  $\mu\text{m}$ )



## Additively Manufactured Inconel 625



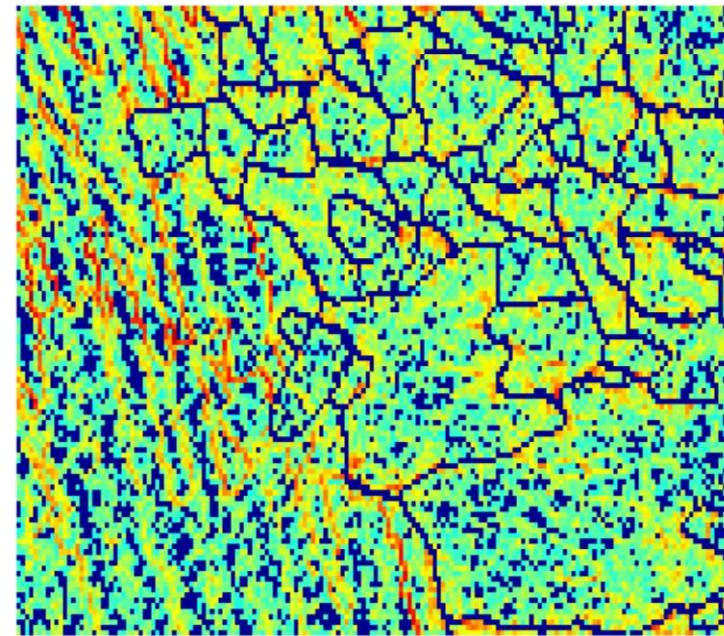
# Lattice Rotation, Strain, Stress



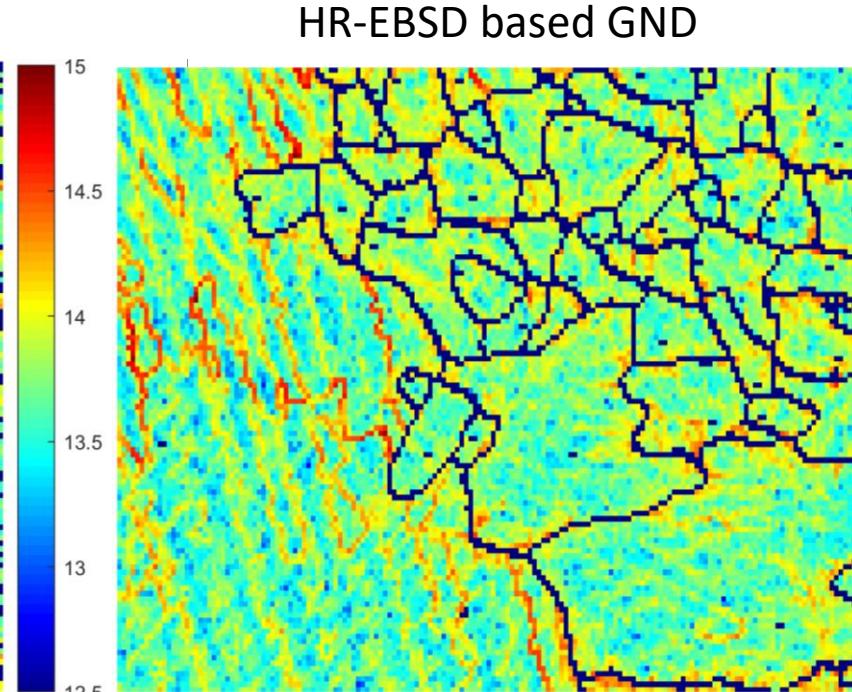
- Columnar growth in the large grain (sub-grain structure)
- Large compressive or tensile residual stresses in the columnar grain.
- Stress concentration near triple junctions and high angle grain boundaries (strain compatibility).

# Hough vs HR-EBSD based GND Density

Hough based GND

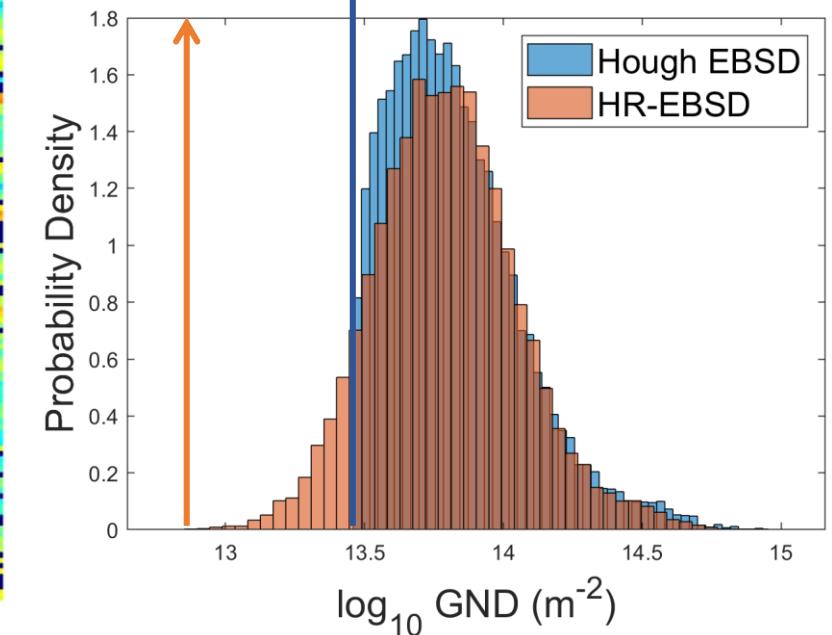


HR-EBSD based GND



Hough EBSD  
Noise floor

HR-EBSD  
Noise floor



- High density dislocation structures are very similar between the two
- Low density dislocation structures are more clearly revealed in HR-EBSD based GND map

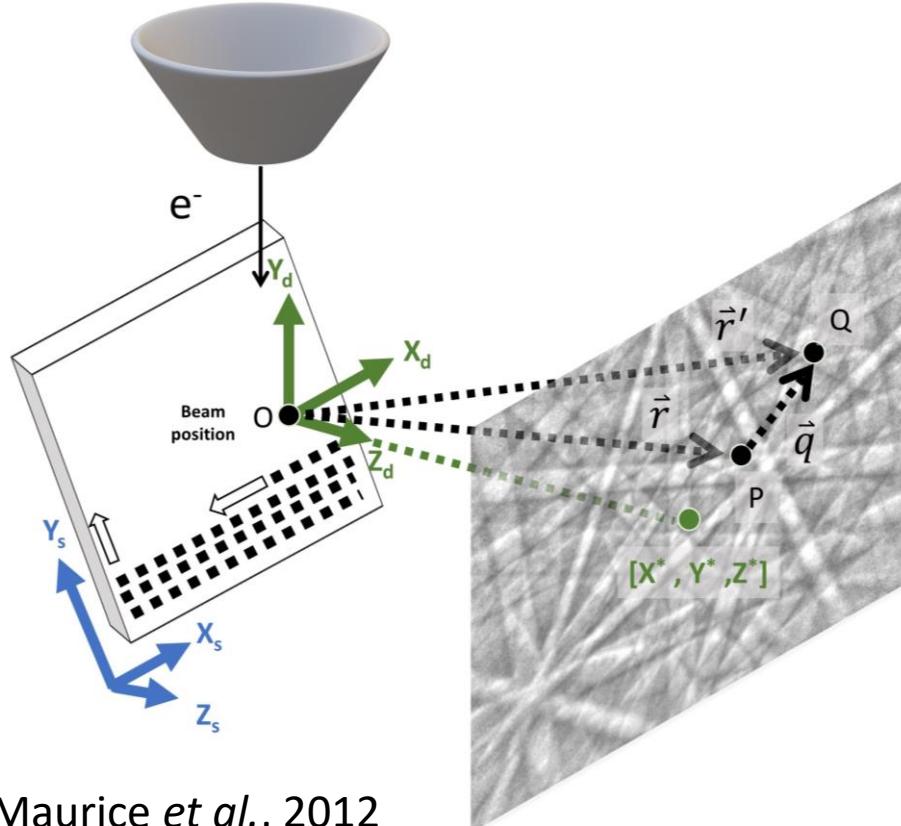
# Summary

- Multiresolution image registration is a fast and accurate remapping for HR-EBSD.
- Phantom strain  $< 2 \times 10^{-4}$  and phantom stress  $< 30$  MPa.
- Lower GND noise floor ( $\Delta\rho \approx 2 \times 10^{12}$  lines/m<sup>2</sup>)
- Additively manufactured Inconel 625 shows significant residual stress build-up in the columnar grain region/ stress concentration near grain boundaries and triple junctions (strain compatibility).

Zhu, C., Kaufmann, K. and Vecchio, K., 2020. Novel Remapping Approach for HR-EBSD based on Demons Registration, Ultramicroscopy

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# HR-EBSD (Essentials)



Maurice *et al.*, 2012

Deformation gradient tensor  $F$  between two images can be calculated from shifts measured between many regions of interest (ROIs).

Non-linear minimization method to obtain deformation gradient tensor:

$$\text{minf}(F) = \sum_{\{\text{ROI}\}} \frac{1}{2} \left| \frac{Z^*}{(F \cdot \vec{r}) \cdot \vec{k}} F \cdot \vec{r} - (\vec{r} + \vec{q}) \right|^2 \quad (\text{Levenberg–Marquardt})$$

$$*F_{\text{sample}} = R_{\theta_{\text{tilt}}} F {R_{\theta_{\text{tilt}}}}^T \quad (\text{Coordinate Transformation})$$

$$F_{\text{sample}} = P D Q^T \quad (\text{SVD})$$

$$R_{\text{sample}} = P Q^T \quad (\text{Rotation Matrix})$$

$\omega$  can then be obtained through parametrizing  $R_{\text{sample}}$  using Rodrigues vector i.e. axis-angle pair  $(m_k, \theta)$

$$\omega_{ij} = -\varepsilon_{ijk} m_k \theta = -\varepsilon_{ijk} \theta_k \quad (\text{Lattice Rotation Tensor})$$

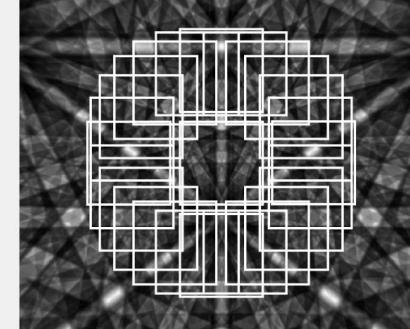
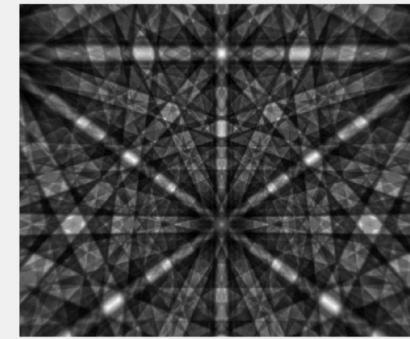
$$\varepsilon_{\text{sample}} \approx \frac{1}{2} (F_{\text{sample}} + {F_{\text{sample}}}^T) - I \quad (\text{Residual Strain Tensor})$$

$$\sigma_{\text{sample}} = C : \varepsilon_{\text{sample}} \quad (t = \sigma_{\text{sample}} Z_s = [0,0,0]) \quad (\text{Residual Stress Tensor})$$

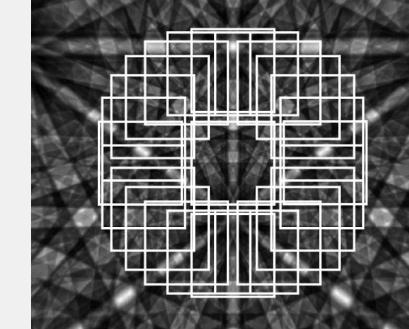
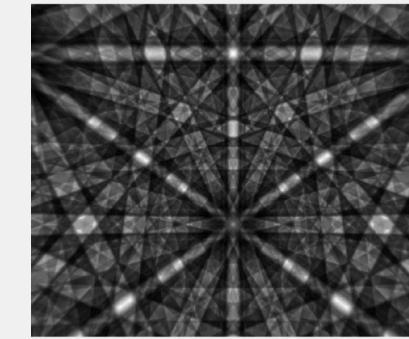
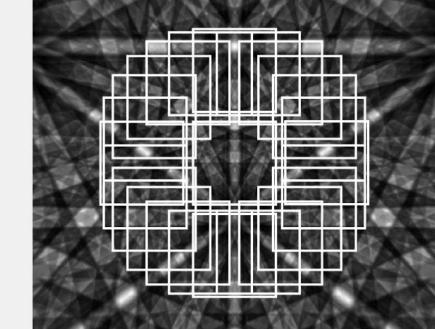
## Higher level of sensitivity:

- Rotation: whole diffraction pattern moving ( $1 \times 10^{-4}$  rad)
- Elastic stretch: change interplanar angles and lattice spacing ( $1 \times 10^{-4}$ )
- GND lower limit:
  - $\Delta\theta = 0.5^\circ$  (Hough based)  $\rightarrow \Delta\rho \approx 2 \times 10^{14}$  lines/m<sup>2</sup>
  - $\Delta\theta = 10^{-4}$  rads (XCF based)  $\rightarrow \Delta\rho \approx 2 \times 10^{12}$  lines/m<sup>2</sup>

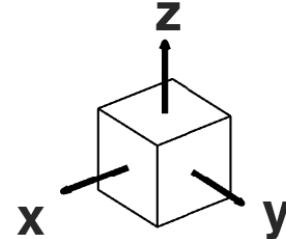
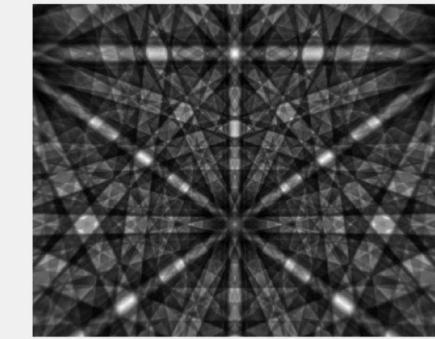
## Obtaining the total shift vectors

**Reference Pattern** $q_f$ **Finite Shift**

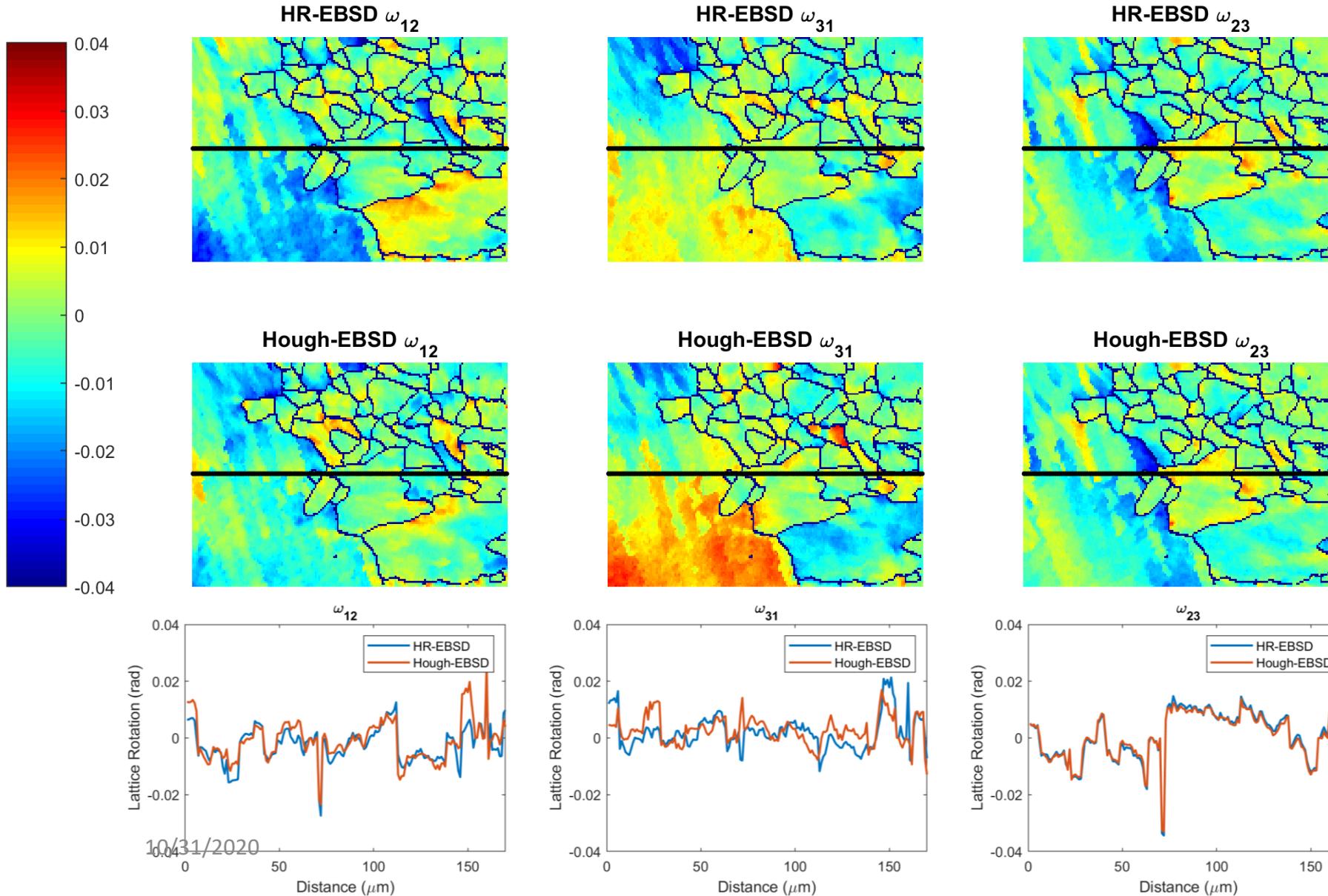
$$F_f = F_i \cdot R_f$$

**Remapped Reference Pattern** $q_i$ **Infinitesimal Shift****Test Pattern**

$$q = q_f + q_i$$

**Total Shift**

# Hough vs HR-EBSD based Lattice Rotation



Hough-EBSD lattice rotation tensor

$$\omega_{23} \approx \frac{1}{2}(g_{23} - g_{32})$$

$$\omega_{31} \approx \frac{1}{2}(g_{31} - g_{13})$$

$$\omega_{12} \approx \frac{1}{2}(g_{12} - g_{21})$$

- Nominally similar values and trend, especially  $\omega_{23}$
- Hough based lattice rotation tensor can be used as a quick check

# Hough Indexing

