# Neper Reference Manual

The documentation for Neper 3.5.0 A software package for polycrystal generation and meshing

1 October 2019



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## Conditions of Use

## Copying Conditions

Neper is "free software"; this means that everyone is free to use it and to redistribute it on a free basis. Neper is not in the public domain; it is copyrighted and there are restrictions on its distribution, but these restrictions are designed to permit everything that a good cooperating citizen would want to do. What is not allowed is to try to prevent others from further sharing any version of Neper that they might get from you.

Specifically, we want to make sure that you have the right to give away copies of Neper, that you receive source code or else can get it if you want it, that you can change Neper or use pieces of Neper in new free programs, and that you know you can do these things.

To make sure that everyone has such rights, we have to forbid you to deprive anyone else of these rights. For example, if you distribute copies of Neper, you must give the recipients all the rights that you have. You must make sure that they, too, receive or can get the source code. And you must tell them their rights.

Also, for our own protection, we must make certain that everyone finds out that there is no warranty for Neper. If Neper is modified by someone else and passed on, we want their recipients to know that what they have is not what we distributed, so that any problems introduced by others will not reflect on our reputation.

The precise conditions of the license for Neper are found in the General Public License that accompanies the source code (see Appendix E [GNU General Public License], page 91). Further information about this license is available from the GNU Project webpage http://www.gnu.org/copyleft/gpl-faq.html.

#### User Guidelines

If you use Neper for your own work, please, mention it explicitly in your reports (papers, books, talks, . . . ) and cite one of several of the following papers (depending of your use of Neper):

- R. Quey, P.R. Dawson, F. Barbe. Large-scale 3D random polycrystals for the finite element method: Generation, meshing and remeshing. Comput. Methods Appl. Mech. Engrg., vol. 200, pp. 1729–1745, 2011 (for Voronoi tessellation, regularization, meshing);
- R. Quey and L. Renversade, Optimal polyhedral description of 3D polycrystals: Method and application to statistical and synchrotron X-ray diffraction data, Comput. Methods Appl. Mech. Engrg., vol. 330, pp. 308-333, 2018 (for tessellation from experimental properties with option -morpho);
- R. Quey, A. Villani and C. Maurice, Nearly uniform sampling of crystal orientations, J. Appl. Crystallogr., vol. 51, pp. 1162-1173, 2018 (for uniform crystal orientation distribution with option -ori uniform).

## 1 Introduction

## 1.1 The Neper Project

## 1.1.1 Description

Neper is a software package for polycrystal generation and meshing. The polycrystals can be 2D or 3D. Neper is built around three modules:

- Module -T generates polycrystals as tessellations. The two main capabilities are: (i) the generation of tessellations from cell properties (e.g. a size distribution) and (ii) the generation of multiscale tessellations (i.e. including cell subdivisions). These capabilities can also be used together. Tessellations are Laguerre (or Voronoi) tessellations and are therefore composed of convex cells. Finally, the tessellations can be "regularized" by removing their smallest features (edges and faces), which then enables good-quality meshing with module -M. Periodicity conditions can be prescribed. Crystal orientations are provided for the grains. The output is a tessellation file written at a scalar (vectorial) or raster format. Scalar tessellations are intended to be passed to modules -M and -V while raster tessellations can be used by FFT solvers.
- Module -M meshes polycrystals described as tessellation files. Two meshing techniques are available: free (or unstructured) meshing, which generates triangular elements (in 2D) or tetrahedral elements (in 3D) that follow the grain shapes, and mapped meshing, which generates regular, square elements (in 2D) or regular, cubic elements (in 3D) that do not necessarily follow the grain shapes. Free meshing into good-quality elements is ensured by optimized meshing rules, and multimeshing—a complementary use of several meshing algorithms. Remeshing is also available and is similar to meshing except that it takes a mesh as input. Cohesive elements can be inserted at interfaces. The output is a mesh file that can be written under several formats.
- Module -V generates publication-quality images of tessellations and meshes. Colouring and transparency of the different entities can be set up in detail, and mesh nodes can be displaced. Mesh slicing is also available. The output is a PNG image file.

Neper aims to be an easy-to-use, efficient and robust tool. All the input data are prescribed non-interactively, using command lines and / or ASCII files. All treatments can therefore be automated.

#### 1.1.2 Resources and Support

Several, complementary resources describing Neper are available:

- The Neper reference manual, which is this document, describes all Neper's capabilities. Each module is dedicated a specific chapter, which describes the available commands and result files, and provides examples. The manual is available at the PDF and info formats.
- The Neper website, http://neper.info gives a general introduction to Neper (including examples with illustrations) and is where Neper can be downloaded from.
- The three Neper reference papers,
  - "R. Quey, P.R. Dawson and F. Barbe, Large-scale 3D random polycrystals for the finite element method: Generation, meshing and remeshing, Comput. Methods Appl. Mech. Engrg., vol. 200, pp. 1729-1745, 2011" describes the regularization / meshing methodologies. It can be downloaded from the Neper homepage or directly from this link: http://neper.info/docs/neper-reference-paper.pdf;

<sup>&</sup>lt;sup>1</sup> Provided that the info file is properly installed at your site, it can be accessed by the command: info neper.

• "R. Quey and L. Renversade, Optimal polyhedral description of 3D polycrystals: Method and application to statistical and synchrotron X-ray diffraction data, Comput. Methods Appl. Mech. Engrg., vol. 330, pp. 308-333, 2018" describes tessellation generation from experimental properties;

• "R. Quey, A. Villani and C. Maurice, Nearly uniform sampling of crystal orientations, J. Appl. Crystallogr., vol. 51, pp. 1162-1173, 2018." describes uniform sampling of crystal orientations.

The best way to report bugs is directly through the GitHub issue tracker, http://github.com/rquey/neper/issues. When reporting bugs, please help us helping you by providing a minimal working example. Neper also has two dedicated mailing lists (the GitHub issue tracker should be preferred, especially for bug reports): neper-announce (https://lists.sourceforge.net/lists/listinfo/neper-announce), the "read-only" list for release announcement and neper-users (https://lists.sourceforge.net/lists/listinfo/neper-users), the "read-write" list for users. As of October 2019, Neper also has an IRC channel, #neper, on the freenode network.

## 1.2 Installing Neper

Neper is written in (mostly ANSI) C and a little C++, and it can run on any Unix-like system. Neper is multithreaded (using openMP) and runs, by default, on all threads (as read in the OMP\_NUM\_THREADS environment variable). Neper must be compiled using CMake, as follows:

- Create a build directory, for instance as a subdirectory of Neper's src directory,
  - \$ mkdir build
- Run CMake from within the build directory, pointing to Neper's src directory,
  - \$ cd build
  - \$ cmake ..
- Build Neper,
  - \$ make

Use option '-j' for a multithreaded compilation.

• Install Neper on your system (as root),

```
$ make install
```

This procedure uses the default configuration options and should work out-of-the-box if the required dependencies are available in standard system locations. If needed, a finer configuration can be achieved, before building Neper, by running

\$ cmake-gui .. (for a graphical tool)

Several of Neper's dependencies can be managed at this stage. Some of them are optional and can be enabled or disabled through variables <code>HAVE\_LIBRARY</code>:

- The GNU Scientific Library (GSL, mandatory). It is likely to be available on your system or from your system package manager (binary and development packages); alternatively, the source code version can be downloaded from http://www.gnu.org/software/gsl.
- The NLopt library (optional, enabled by default). It is needed by module -T for tessellation generation from cell properties. It is likely to be available on your system or from your system package manager (binary and development packages); alternatively, the source code version can be downloaded from http://ab-initio.mit.edu/wiki/index.php/NLopt.
- The OpenMP library (optional, enabled by default). It is likely to be available on your system or from your system package manager.

- The libScotch library (version 5.1.12 or higher, optional, disabled by default). It is needed by module -M for mesh partitioning. The source code can be downloaded from www.labri.fr/perso/pelegrin/scotch.
- The pthread library (optional, enabled if libScotch enabled). It is needed if libScotch version 6.0.0 or higher is enabled. It is likely to be available on your system or from your system package manager.

Other dependencies are needed at run time only (they are not linked against Neper's binary):

- The Gmsh program (version 2.4.2 or higher, excluding version 2.5.1, mandatory for module -M). Both binary and source-code versions can be downloaded from http://www.geuz.org/gmsh (compiling from the source code significantly speeds up meshing). Gmsh must be available at the terminal as the command gmsh, or the path to its binary must be specified with option -gmsh (in module -M).
- The POV-Ray program (mandatory for module -V). It is likely to be available on your system or from your system package manager (binary package); alternatively, a binary, or the source code, can be downloaded from http://www.povray.org. POV-Ray must be available at the terminal as the command povray, or the path to its binary must be specified with option -povray (in module -V).

Neper has a few more dependencies, which are directly included in the source code (see directory src/contrib): nanoflann (https://github.com/jlblancoc/nanoflann) and muparser (http://beltoforion.de/article.php?a=muparser).

Finally, the Neper installation can be tested out by running

```
$ make test
or (equivalently)
$ ctest
```

## 1.3 Getting Started

The 'neper' binary must be run in a terminal, followed by a list of arguments,

```
$ neper list_of_arguments
```

Neper returns messages in the terminal and results in ASCII files.

The list of arguments describes the problem to solve. There are several general-purpose, self-explanatory arguments:

```
$ neper --help
$ neper --version
$ neper --license
```

This section provides information on how to call Neper's modules, properly format option arguments, and set up an initialization file.

#### 1.3.1 Modules

To call a module, run

```
$ neper module_name module_arguments
```

where the module name can be -T, -M or -V, and the module arguments can include both required input data and options. Input data (when not a file name) and options start by '-'. Options can be provided in arbitrary order, each of them being followed by a single argument (containing no space). American-english variants of options can be used. String completion is available for all options, so they may be abbreviated as long as the abbreviation is not ambiguous. For instance, in module -T, option -regularization can be abbreviated to -reg. Logical options can be enabled or disabled by providing argument values of '1' or '0', respectively. Integer or real

argument values can be written as such, or as mathematical or logical expressions (for details, see Section A.1 [Mathematical and Logical Expressions], page 59). For instance, in module -T, option -rcl 0.5 can also be written as -rcl 1/2 or -rcl "cos(pi/3)". Module -V shows some exceptions with respect to these rules: the argument cannot be listed in arbitrary order, string completion is not available, and option -loop takes several arguments.

## 1.3.2 Argument Separators

Some options may take several argument values. These values can be combined using *separators* (see Chapter 2 [Tessellation Module (-T)], page 9, Chapter 3 [Meshing Module (-M)], page 27, and Chapter 4 [Visualization Module (-V)], page 41, for details on each option). There are three possible separators:

- The ',' separator combines uncorrelated arguments, i.e. arguments of the same type, which can be processed independently from each other. Such arguments can be output file formats, for instance.
- The ':' separator is used to combine correlated arguments, i.e. arguments of different types, which cannot be processed independently from each other. Such arguments can be values of a variable in different directions, for instance.
- The '::' separator is used in module -T (and a little in module -M) for assigning argument values to the different scales of a multiscale tessellation. It is a "super-separator" that takes precedence over the ',' and ':' standard separators.

#### 1.3.3 Initialization File

When Neper is run, it starts by reading commands from an initialization file, \$HOME/.neperrc, if that file exists. Another initialization file can be specified with option --rcfile, before calling a module,

```
$ neper --rcfile my_file module_name module_arguments
```

To disable the reading of an initialization file, use option --rcfile none.

When a module of Neper is called, Neper looks for the occurrence of 'neper module\_name' in the initialization file and then reads all arguments until the next occurrence of 'neper' (which should denote the beginning of another module option field) or the end of the file. The arguments may be any legal arguments but are typically limited to frequently-used options. Moreover, any field of comments can be preceded by 'neper comments'.

Here is an example of initialization file:

If the initialization file is not found, or if 'neper module\_name' is not found inside it, Neper will consider only the command line arguments. Also, if an argument is initialized several times (for instance, both in the initialization file and at the command line), only the last specified value is used.

## 1.4 Reading this Manual

This manual is maintained as a Texinfo manual. Here are the writing conventions used in the document:

• A command that can be typed in a terminal is printed like this, or, in the case of a major command, like

```
$ this;
```

- A program (or command) option is printed like this;
- The name of a variable is printed like this;
- A meta-syntactic variable (i.e. something that stands for another piece of text) is printed like *this*;
- Literal examples are printed like 'this';
- File names are printed like this.

Module arguments are tagged by type and importance level:

- Prerequisites are tagged '[Prerequisite]'—they should be placed in the initialization file;
- Input data are tagged '[Input Data]';
- Standard options are tagged '[Option]';
- Secondary options, which should be used only for fine-tuning and if you really know what you are doing, are tagged '[Secondary option]';
- Post-processing options are tagged '[Post-processing]'.

Some abbreviations are used consistently for options and contribute to Neper's jargon:

algo algorithm
arch architecture
aspratio aspect ratio

cl characteristic length

col colour

conv convergence coo coordinate

crysym crystal symmetry csys coordinate system

dim dimension

dis distribution or distortion

dof degree of freedom
dup duplicate(d)
elset element set
elt element
expr expression
fact factor

faset element face set

geo geometry identifier id initial ini infinity inf inter interpolation iteration iter max maximum minimum min morphology morpho neighbour neigh nset node set optimization opti ori orientation partition part polyhedron poly POV-Ray file pov

qual quality

rad radius

rcl relative characteristic length

res resolution

rmax relative maximum

singsingularstatstatisticssurfsurface

tesr raster tessellation tess scalar tessellation

val value variable ver vertex

## 2 Tessellation Module (-T)

Module -T generates tessellations and multiscale tessellations of a bounded domain of space, in 2D or 3D. The domain must be convex, but once generated the tessellation can be cut by various shapes, e.g. to include a notch (experimental feature). Periodicity and semi-periodicity conditions can be prescribed. Module -T also enables to regularize the tessellations for better-quality meshing. The tessellations are provided in scalar (vectorial) or raster formats. Module -T also generates crystal orientations for the tessellation cells.

Tessellations can be generated from various types of morphological cell properties (option -morpho). Several predefined properties are available, such as those obtained by grain growth in metals (which are described by cell size and sphericity distributions). Custom properties can be specified using various metrics, including the size, the sphericity, the centroid or even the actual shape (using a raster tessellation), in terms of either distributions (when applicable) or individual cell values. Global morphological properties, such as a cell aspect ratio or a columnar axis, can also be specified. The generated tessellations are Laguerre (or Voronoi) tessellations whose seed attributes are set by optimization to obtain the desired cell properties. Of course, it is also possible to generate standard tessellations (e.g. Poisson-Voronoi or regular tessellations). Multiscale tessellations are characterized by the subdivision of the cells of a primary tessellation into secondary tessellations (and so on) and are obtained by combining into one, using the ":: 'separator, the option arguments that apply at the successive scales. The same value can be used for defining the tessellations at a given scale, or different values can be loaded using 'msfile(filename)', where filename is a multiscale cell file (see Section B.3 [Multiscale Cell File, page 78). So, all capabilities available for generating a standard (single-scale) tessellations are available for generating the tessellations at the different scales of a multiscale tessellation. Examples are provided in the following.

The domain of space in which the tessellation is created can be of any convex shape. In 3D, cuboidal, cylindrical and spherical shapes (and a few other, exotic shapes) are directly supported while other morphologies can be defined from a set of planes (option -domain). Non convex domain shapes can be obtained by cutting the tessellation by different geometrical primitives once generated (option -tranform cut, experimental).<sup>2</sup> Periodicity or semi-periodicity conditions can be applied to the tessellation (option -periodicity).

Crystal orientations can be randomly distributed (according to a uniform frequency distribution), either in the 3D space or along a specific orientation fibre, or uniformly distributed (option -ori). Uniform crystal orientation distributions ensure that all possible crystal orientations are equally represented (no orientation clustering). Crystal orientations can be provided according to different descriptors (option -oridescriptor).

Regularization can be applied to the tessellations and consists in removing their small edges and faces (option -regularization) which would otherwise be detrimental to good-quality meshing with module -M (see Chapter 3 [Meshing Module (-M)], page 27). It it not available for periodic tessellations yet.

Output files describe the tessellation either at the scalar format .tess or at the raster format .tesr (see Appendix B [File Formats], page 71). Both are input files of module -M (see Chapter 3 [Meshing Module (-M)], page 27) and module -V (see Chapter 4 [Visualization Module (-V)], page 41). Third-party software file formats are also available.

Here is what a typical run of module -T looks like,

<sup>&</sup>lt;sup>1</sup> As of version 3.5.0, 'msfile(filename)' should be preferred over 'file(filename)' to load a multiscale cell file.

 $<sup>^{2}</sup>$  Only non-convexities larger than the typical cell size are supported.

е

r

е

```
р
    : A software package for polycrystal generation and meshing.
Info
     : Version 3.5.0
     : Built with: gsl nlopt muparser
Info
     : <http://neper.info> <http://neper.info/community>
Info
     : Copyright (C) 2003-2019, and GNU GPL'd, by Romain Quey.
Info
Info
     : Loading initialization file '/home/rquey/.neperrc'...
      : -----
Info
Tnfo
      : MODULE -T loaded with arguments:
Info
     : [ini file]
     : [com line] -n 10 -id 1 -morpho gg -reg 1
     : ------
Info
Info
     : Reading input data...
     : Creating domain...
Info
      : Creating tessellation...
Tnfo
         - Running tessellation...
Info
          > Entering optimization...
Info
          > Setting seeds... 100%
Info
          > Initial solution: f
Info
                               =3.623581896
Info
          > Iteration
                      2864: fmin=0.077875850 f=0.077875946
Info
           > Reached 'reps' criterion.
    : Regularizing tessellation...
Info
        - loop 1/2: 100% del=2
Info
     : Writing tessellation...
Info
           [o] Writing file 'n10-id1.tess'...
Info
Tnfo
           [o] Wrote file 'n10-id1.tess'.
     : Elapsed time: 3.333 secs.
______
```

## 2.1 Arguments

## 2.1.1 Input Data

#### -n integer or char\_string

[Input data]

Specify the number of cells of the tessellation. The argument can be an integer, an expression based on the tessellation cell variables (see Section A.2 [Tessellation Keys], page 61), or 'from\_morpho' to set the value from the morphology (see -morpho).

Possible values: any. Default value: none.

#### -id integer

[Input data]

Specify the identifier of the tessellation. It defines the seed used by the random number generator to compute the (initial) seed positions.

Possible values: any. Default value: 1.

## -dim integer

[Option]

Specify the dimension of the tessellation. Possible values: 2 or 3. Default value: 3.

#### -domain char\_string

[Option]

Specify the domain morphology. In 3D. for a cuboidal shape, pro-'cube(size\_x,size\_y,size\_z)',  $_{
m for}$ cylindrical  $\mathbf{a}$ shape, 'cylinder(height, diameter)', and for a spherical shape, provide 'sphere(diameter)'. In 2D, for a rectangular shape, provide 'square(size\_x, size\_y)' and for a circular shape, provide 'circle(diameter)'. To specify the number of facets, facet\_nb, of a circle, cylinder or sphere domain, use 'circle(diameter, facet\_nb)', 'cylinder(height, diameter, facet\_nb)' or 'sphere(diameter, facet\_nb)'. Rodrigues space fundamental region, provide 'rodrigues(crysym)', where crysym is the crystal symmetry (see Section A.9 [Crystal Symmetries], page 67). For a standard stereographic triangle, provide 'stdtriangle(segment\_nb)', where segment\_nb is the number of segments on the [011]-[111] line. For an arbitrary convex 3D shape, provide 'planes (file\_name)', where file\_name is the name of a file containing the total number of planes then, for each plane, the 4 parameters of its equation (d, a, b and c, for an equation)of the form ax + by + cz = d). The plane normal, (a, b, c), must be an outgoing vector of the domain. For a tessellation cell, provide 'cell(file\_name, cell\_id)', where file\_name is the name of the tessellation file and cell\_id is the cell identifier. To transform the domain, append a transformation to the domain name using the ':' separator. Available transformations are: 'rotate(axis\_x,axis\_y,axis\_z,angle)' for a rotation of angle angle about axis (axis\_x, axis\_y, axis\_z), 'scale(x\_factor, y\_factor, z\_factor)' for scaling, 'translate(x\_delta,y\_delta,z\_delta)' for a translation and 'split(dir)' for splitting the domain in half along direction 'dir' ('x', 'y' or 'z'), which can be used to apply symmetries. For a 2D tessellation, the axis parameters can be omitted in 'rotate' (default (0,0,1)), and the z component can be omitted in 'scale' (default 1) and 'translate' (default 0). An example is 'sphere(1,100):translate(-0.5,-0.5,-0.5):scale(0.5,1,2)'. Possible values: see above list. Default value: cube(1,1,1) in 3D and square(1,1) in 2D.

## -periodicity char\_string

[Option]

Specify the periodicity conditions that apply to the domain (and therefore to the tessellation). Provide as argument '0' (or 'none') for no periodicity, '1' (or 'all') for full periodicity, or a list of periodicity directions (among 'x', 'y' and 'z') combined with ',' for semi-periodicity. Possible values: see above list. Default value: 0.

Is it also possible to load a tessellation or a raster tessellation from a file,

#### -loadtess file\_name

[Input data]

Load a tessellation from a file. Provide as argument the file name. Possible values: any. Default value: none.

#### -loadtesr file\_name

[Input data]

Load raster tessellation from file. Provide argument a as To load only a subregion of a raster tessellation, use the xmin, 'file\_name:crop(xmin,xmax,ymin,ymax,zmin,zmax)', where ymax, zmin and zmax are the minimum and maximum positions along x, y and z, respectively. For 2D raster tessellations, the z values can be omitted. To scale the number of voxels of a raster tessellation, use the syntax 'file\_name:rasterscale(factor)', where factor is the scaling factor, or 'file\_name:scale(factor\_x,factor\_y,factor\_z)', where factor\_x, factor\_y and factor\_z are the scaling factor along x, y and z, respectively. For 2D raster tessellations, the z value can be omitted.

Possible values: any. Default value: none.

Finally, it is possible to load a set of points. These points are used only for statistics, in option -statpoint; they are not seed points of the tessellation (see option -morphooptiini instead).

#### -loadpoint file\_name

[Input data]

Load points from a file. See Section B.4 [Position File], page 79, for the file format. Provide as argument the file name.

Possible values: any. Default value: none.

## 2.1.2 Morphology Options

These options can be used to set the cell morphology. If you want to set seeds attributes instead, use '-morphooptiini ... -morpho voronoi'.

#### -morpho char\_string

[Option]

Specify morphological properties of the cells. It can be done either by using a special morphology string (as defined below), or by specifying custom cell properties such as sizes, sphericities, centroids, or even exact shapes (using a raster tessellation). Global properties (sometimes referred to as morphological texture) can be added. Alternatively, a complete tessellation can also be loaded (as a tessellation file).

- (i) The special morphology strings are the following (mutually-exclusive):
- 'voronoi' for a standard Poisson-Voronoi tessellation;
- 'graingrowth' or 'gg' for grain-growth statistical properties, which correspond to a wider grain size distribution and higher grain sphericities than in a Voronoi tessellation (it actually is an alias for 'diameq:lognormal(1,0.35),1-sphericity:lognormal(0.145,0.03)', see below); the 'graingrowth(mean)' and 'gg(mean)' variants can be used to provide an absolute mean grain size, mean (in which case -n from\_morpho must be used, see below);
- 'centroidal' for a centroidal tessellation<sup>3</sup> (it actually is an alias for 'centroid:seed', see below);
- 'cube(N)' / 'square(N)' for a regular tessellation into cubic / square cells, where 'N' is the number of cells along a direction, or 'cube(N1,N2,N3)' / 'square(N1,N2)' for a regular tessellation into cubic / square cells, where 'N1', 'N2' and 'N3' are the number of cells along the different directions;
- $\bullet$  'tocta(N)' for a regular tessellation into truncated octahedra, where 'N' is the number of cells along a direction;
- 'lamellar(w=w,v=v,pos=pos)' for a lamellar morphology. Argument 'w=w' is mandatory, and arguments 'v=v' and 'pos=pos' are optional. Argument 'w=w' enables to specify the absolute lamella width w. For specifying several widths, combine them with ':'. Argument 'v=v' enables to specify the lamella plane normals v. For randomly-distributed normals taken from a uniform distribution, use 'random' (the default). For a direction of space, use '(dir\_x,dir\_y,dir\_z)', where (dir\_x,dir\_y,dir\_z) is the direction. For a direction of the parent crystal, use 'crysdir(crysdir\_x,crysdir\_y,crysdir\_z)', where (crysdir\_x,crysdir\_y,crysdir\_z) is the crystal direction. Argument 'pos=pos' enables to specify the position of the lamellaes, pos. It can be 'random' for a random position (the default) or 'start' for the first lamella starting (full-width) from the start point of the domain (along direction dir). In the case of a multiscale tessellation, multiscale cell files can be provided as values of 'w', 'v', and 'pos', see Section B.3 [Multiscale Cell File], page 78.
- (ii) Custom morphological properties can be defined by providing as argument the cell property and its value, combined with the ':' separator. The available properties are the following:
- 'size' for the size (volume in 3D and area in 2D) and 'diameq' for the equivalent diameter;
- 'sphericity' for the sphericity and '1-sphericity' for 1 the sphericity<sup>4</sup> 'centroid' for the centroid;
- 'centroidtol' for the centroid with a tolerance centroids with a tolerance higher than 1000 times the minimum tolerance are disregarded;
- 'centroidsize' for combined centroid and size, and 'centroiddiameq' for combined centroid and equivalent diameter;

<sup>3</sup> centroidal is not recommended as it does not correspond to a morphological property per se; size and/or sphericity properties should be used instead.

The reason behind the '1-sphericity' variable is that, for a grain growth microstructure, 1 – the sphericity follows a lognormal distribution; see R. Quey and L. Renversade, Optimal polyhedral description of 3D polycrystals: Method and application to statistical and synchrotron X-ray diffraction data, Comput. Methods Appl. Mech. Engrg., vol. 330, pp. 308-333, 2018.

• 'tesr' for cells of a raster tessellation.

Sizes, diameqs and sphericities can be defined by statistical distributions or on a per-cell basis, while centroids can be defined only on a per-cell basis. The list of available statistical distributions is provided in Section A.1 [Mathematical and Logical Expressions], page 59. If the number of cells is defined (see option -n), the size or diameq distribution is scaled to get the specified number of cells; otherwise, i.e. -n is set to 'from\_morpho', the number of cells is determined from the size or diameq distribution. An interval of possible values can also be provided using 'interval(min,max)'. A unique value can be assigned to all cells using 'value', where 'value' is the value. Cell-by-cell values can be provided using 'file(file\_name)', where 'file\_name' is the name of the file containing the cell values (see Section B.4 [Position File], page 79, for 'centroid'; add a tolerance to each position for 'centroidtol'). For 'centroid', provide 'seed' to get a centroidal tessellation. For 'tesr', 'file\_name' is the name of the raster tessellation file. If -n is set to 'from\_morpho', the number of cells is set to the number of cells of the raster tessellation.

(iii) The global cell properties are the following (mutually-exclusive):

- 'columnar(dir)' for a columnar morphology along coordinate axis 'dir', where 'dir' can be 'x', 'y' or 'z';
- 'bamboo(dir)' for a bamboo morphology along coordinate axis 'dir', where 'dir' can be 'x', 'y' or 'z';
- 'aspratio(r1,r2,r3)', where 'r1', 'r1' and 'r3' represents relative length along the coordinate axes. For a 2D tessellation, 'r3' can be omitted. When provided, other properties, such as the equivalent diameter or the sphericity, are considered to apply to the cells as if they had no aspect ratio.
- (iv) A tessellation can be loaded using 'file(file\_name)', where 'file\_name' is the name of the tessellation file.

To specify several properties, combine them with ',' (centroids and sizes/equivalent diameters should be seen as one property and specified with centroidsize/centroiddiameq). Possible values: any. Default value: voronoi.

#### -morphooptiini char\_string

[Option]

Specify the initial positions and/or weights of the seeds. The general form of the argument is 'coo:coo\_char\_string,weight:weight\_char\_string', but it is also possible to read the seeds of a tessellation file (provide its name as argument). Different values of 'coo\_char\_string' and 'weight\_char\_string' are available, depending on the value of option -morpho:

- 'weight\_char\_string' can be a real value, any mathematical expression based on variables 'radeq' and 'diameq' (see Section A.2 [Tessellation Keys], page 61) and their average values, 'avradeq' and 'avdiameq', respectively, or 'file(file\_name)' to load values from a file. The default depends on the value of option '-morpho': for 'voronoi', it is '0', for a cell-size statistical distribution, it is 'avradeq', and for cell-based size values (including -morpho tesr), it is 'radeq'.
- 'coo\_char\_string' can be 'random' for random positions, 'packing' for positions set by (rough) dense sphere packing using the weights as sphere radii, 'centroid' for cell centroids, 'LLLFP2011' for Lyckegaard et al.'s method<sup>5</sup>, or 'file(file\_name)' to load values from a file (see Section B.4 [Position File], page 79). The default depends on the value of option '-morpho': for 'voronoi', it is 'random', for a cell-size statistical distribution, it is 'none', and for cell-based coordinate values (including -morpho tesr), it is 'centroid'.

It is also possible to provide a tessellation file in 'file(file\_name)' (from which seed coordinates or weights are read).

Possible values: see above list. Default value: default.

A. Lyckegaard, E.M. Lauridsen, W. Ludwig, R.W. Fonda, and H.F. Poulsen. On the Use of Laguerre Tessellations for Representations of 3D Grain Structures. Advanced Engineering Materials, vol. 13, pp. 165–170, 2011.

#### -morphooptiobjective char\_string

[Secondary option]

Specify the objective function. The argument should be of the form 'prop1:objective\_function1,prop2:objective\_function2,...', where propx are properties as defined in option -morpho, and objective\_functionx are their objective functions. An objective function depends on the property and its definition.

- For properties defined by a statistical distribution (which can be 'size', 'diameq' or 'sphericity'), the available values are 'chi2' (Chi-square test), 'ks' (Kolmogorov-Smirnov test), 'kuiper' (Kuiper's test), 'cmv' (Cramér-Von Mises test), 'ad' (Anderson-Darling test), 'FL2' (L²-norm on F), 'FL2w' (weighted L²-norm on F)6, 'FL2wu' (weighted L²-norm on F corresponding to 'FL2w' for a unimodal distribution), and the default value is 'FL2w'.
- For 'centroid', a Minkowski distance between the seeds and centroids is used, and can be 'L1', 'L2' or 'Linf'.
- For 'tesr', the definition of the objective function includes several factors. First, preprocessing operations to the raster tessellation can be applied using 'transform(operations)', where 'operations' can include 'scale' to scale the tessellation to correct for a global cell elongation or 'rasterscale' to scale the raster itself to correct for a global voxel elongation (which may result from operation 'scale'); combine with ','. Second, control points can be defined using 'pts(args)' where 'args' can include 'region=region' where 'region' can be 'surf' for surface voxels or 'all' for all voxels, and 'res=res' where 'res' is the resolution, i.e. the average number of control points along a direction of a grain; combine with ','. Third, the expression of the objective function per se can be specified using 'val(expr)', where 'expr' can be 'bounddist' for minimizing the distance between the raster tessellation and tessellation cell boundaries, or 'intervol' for maximizing the volume intersection between the raster tessellation and tessellation (both provide similar results). To define the objective function, combine the above factors using '+'. The default value is 'pts(region=surf,res=5)+val(bounddist)'. It is finally possible to define how the different parts of the objective function are combined into the objective function (in the case where several properties are specified), using 'general:objective\_function', where 'objective\_function' can be 'L1', 'L2' or 'Linf'; the default is 'L2'.

Possible values: any. Default value: default.

## -morphooptidof char\_string

[Secondary option]

Specify the degrees of freedom. The available values are 'x', 'y' and 'z' for the 3 coordinates, and 'w' for the weights. Combine with ','.

Possible values: see above list. Default value: x,y,z,w.

#### -morphooptistop char\_string

[Secondary option]

Specify the stopping criteria of the optimization process. Note that you do not have to define all criteria; in most cases, only one or two are needed. A stopping expression must be of the form 'var=val', where 'var' is a variable and 'val' is its value. The available variables are: an absolute or relative error on the value of the objective function evaluated on a number of degrees of freedom basis, 'eps' or 'reps' (use 'nlopt\_eps' or 'nlopt\_reps' for the NLopt iteration-based values), an absolute or relative error on the components of the solution vector, 'xeps' or 'xreps', a value of the objective function, 'val', a maximum number of iterations, 'itermax', a maximum computation time, 'time', or a maximum number of iteration loops, 'loopmax' (see option '-morphooptialgomaxiter'). Combine them with ','. Optimization stops as soon as one stopping criterion is verified. Optimization can also be stopped anytime using the Ctrl+C command.

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<sup>&</sup>lt;sup>6</sup> R. Quey and L. Renversade, Optimal polyhedral description of 3D polycrystals: Method and application to statistical and synchrotron X-ray diffraction data, Comput. Methods Appl. Mech. Engrg., vol. 330, pp. 308-333, 2018.

Possible values: any. Default value: eps=1e-6 (val=1e-4,iter=10000 for -morpho centroidal).

#### -morphooptialgo char\_string

[Secondary option]

Specify the optimization algorithm. The available values are 'subplex' (Subplex), 'praxis' (Praxis), 'neldermead' (Nelder-Mead), 'cobyla' (Cobyla), 'bobyqa' (Bobyqa) and 'newuoa' (Newuoa) — only 'subplex' and 'praxis' are recommended; it is also possible to provide several algorithms combined with ',', in which case the additional algorithms may be used if previous ones fail. In the case of -morpho centroidal, another available value is 'lloyd' (Lloyd's algorithm); to specify the seed displacement factor (from the seed to the centroid), use 'lloyd(factor)' (the default value is 1.9). Another available value (use only if you know what you are doing) is 'random(seednb,dimnb,min,max,id)', for which, at each odd iteration, each of 'seednb' seeds sees 'dimnb' of its attributes (among those specified by option-morphooptidof) being randomly perturbed, the norm of the total perturbation vector ranging from 'min'-'max'; 'id' is the identifier of the distribution (similarly to option -id); variables can be any mathematical expression based on 'seednb' (the total number of seeds), 'dim' (the tessellation dimension), 'avdiameq' (the average equivalent cell diameter) and 'inistep' (the value of -morphooptiinistep); at each next (even) iteration, the attributes of the seeds are reverted to their original values.

Possible values: any. Default value: subplex, praxis (lloyd for -morpho centroidal).

## -morphooptialgoneigh char\_string

[Secondary option]

Specify the neighbour search algorithm. The available values are 'nanoflann' (nanoflann) and 'qsort' (direct computation with qsort). 'nanoflann' is much faster.

Possible values: any. Default value: nanoflann.

#### -morphooptigrid char\_string

[Secondary option]

Specify the grids used to discretize the distributions. Provide the values using the syntax 'var:grid', where var is the variable, among diameq, size and sphericity and grid is the grid. The grid must be of the form 'regular(min, max, bin\_nb)', where min and max are the minimum and maximum values of the grid interval, respectively, and bin\_nb is the number of bins.

Possible values: any. Default value: diameq:regular(-1,10,1100),size:regular(-1,10,1100),sphericity:regular(-0.1,1.1,1200).

#### -morphooptismooth char\_string

[Secondary option]

Specify the standard deviations of the Gaussian distributions which are assigned to each cell data to compute the distributions. Provide the values using the syntax 'var:val', where var is the variable, among diameq, size and sphericity and val is the value. It is also possible to specify how the convolution functions should be treated: provide 'analytical' for analytical functions or 'numerical' for numerical functions (the default, recommended). Combine with ','.

Possible values: any. Default value: diameq:0.05, size:0.05, sphericity:0.005, numerical.

#### -morphooptideltamax real

[Secondary option]

Specify the maximal value by which each variable is allowed to change during optimization. Possible values: any>=0. Default value: HUGE\_VAL.

#### -morphooptiinistep real

[Secondary option]

Specify the step used to perturb the seed positions and weights when optimization begins. The argument can be a function of avdiameq, the average equivalent cell diameter.

Possible values: any>0. Default value: avdiameg/10.

#### -morphooptilogtime char\_string

[Secondary option]

Log the time taken during the optimization process. The keys are provided in Section A.4 [Tessellation Optimization Keys], page 63. The log file has extension .logtime.

Possible values: any. Default value: none.

## -morphooptilogvar char\_string

[Secondary option]

Log the variables, i.e. the seed attributes, during the optimization process. The keys are provided in Section A.4 [Tessellation Optimization Keys], page 63. The log file has extension .logvar.

Possible values: any. Default value: none.

#### -morphooptilogval char\_string

[Secondary option]

Log the value of the objective function during the optimization process. The keys are provided in Section A.4 [Tessellation Optimization Keys], page 63. The log file has extension .logval. Possible values: any. Default value: none.

#### -morphooptilogdis char\_string

[Secondary option]

Log the distributions during the optimization process. The keys are provided in Section A.4 [Tessellation Optimization Keys], page 63. The log files have extension .logdis\*.

Possible values: any. Default value: none.

#### -morphooptilogtesr char\_string

[Secondary option]

Log the raster tessellation voxel data during the optimization process. The keys are provided in Section A.4 [Tessellation Optimization Keys], page 63. The log file has extension .logtesr. Possible values: any. Default value: none.

## 2.1.3 Crystal Orientation Options

#### -ori char\_string

[Option]

Specify the type of crystal orientation distribution. It can be:

- 'random' for randomly-distributed orientations in 3D space;
- 'uniform' for uniformly-distributed orientations in 3D space (the crystal symmetry must be specified using -oricrysym);
- 'fibre(dirs\_x, dirs\_y, dirs\_z, dirc\_x, dirc\_y, dirc\_z)' for randomly-distributed orientations about the fibre defined by crystal direction (dirc\_x, dirc\_y, dirc\_z) parallel to sample direction (dirs\_x, dirs\_y, dirs\_z);
- an ideal orientation, see Section A.8 [Rotations and Orientations], page 67;
- a discrete orientation defined using an orientation descriptor:
- 'g(g11,g12,g13,g21,g22,g23,g31,g32,g33,)' for a rotation matrix, 'e(e1,e2,e3)' for Euler angles in Bunge convention, 'ek(ek1,ek2,ek3)' for Euler angles in Kocks convention, 'er(er1,er2,er3)' for Euler angles in Roe convention, 'rtheta(r1,r2,r3,theta)' for an axis / angle (in degrees) pair, 'q(q1,q2,q3,q4)' for a quaternion, 'R(R1,R2,R3)' for a Rodrigues vector and 'm(h,k,l,u,v,w)' for Miller indices;
- 'equal' for orientations equal to the one of the parent cell;
- 'spread(thetam)' for orientations randomly distributed about the one of the parent cell, according to a 3-variate normal distribution, and so that the average misorientation angle with respect to the average orientation is equal to thetam;
- 'file(filename):des' for reading orientations from file filename and written using the descriptor des (see Section A.8 [Rotations and Orientations], page 67); if Euler angles (e), the descriptor can be omitted.

Possible values: see above list. Default value: random.

#### -oricrysym char\_string

[Option]

Specify the crystal symmetry (see Section A.9 [Crystal Symmetries], page 67). This is used by option -ori uniform and to reduce the domain of definition of the orientation descriptors. Possible values: see above. Default value: triclinic.

#### -orioptiini char\_string

[Secondary option]

Specify the initial crystal orientations. Provide 'random' for random orientations, or 'file(filename):des' for reading orientations from file filename and written using the descriptor des (see Section A.8 [Rotations and Orientations], page 67); if Euler angles (e), the descriptor can be omitted.

Possible values: any. Default value: random.

## -orioptifix char\_string

[Secondary option]

Fix some orientations during optimization. Provide 'none' for none, or 'file(filename)', where filename contains a logical value for each orientation: '0' if the orientation is not fixed and '1' if the orientation is fixed.

Possible values: any. Default value: none.

#### -orioptistop char\_string

[Secondary option]

Specify the stopping criterion of the optimization process, under the form of a logical expression based on the following variables: the relative error on the forces at orientations, 'reps', and the iteration number, 'iter'.

Possible values: any. Default value: reps<1e-3||iter>=1e3.

#### -orioptineigh char\_string

[Secondary option]

Use only the close neighbourhood of orientations to compute their forces (for '-ori uniform'). Specify the radius of the neighbourhood, which can be any mathematical expression based on dr (the average radius of an orientation). Nstar is the grand number of orientations (i.e., taking crystal symmetry into account).

Possible values: any. Default value: Nstar<10000?pi:20\*dr.

#### -orioptilogvar char\_string

[Secondary option]

Log the variables, i.e. the orientations, during the optimization process. The keys are provided in Section A.5 [Orientation Optimization Keys], page 65. The log file has extension .logorivar.

Possible values: any. Default value: none.

## 2.1.4 Transformation Options

#### -transform char\_string(...)

[Option]

Apply transformations to a tessellation (if scalar and raster tessellations are written in output, they are transformed independently; i.e., rasterization preceds transformation).

The following transformations apply to a scalar tessellation:

- 'scale( $x_{fact}$ ,  $y_{fact}$ ,  $z_{fact}$ )' scales a tessellation by  $x_{fact}$ ,  $y_{fact}$  and  $z_{fact}$  along directions x, y and z, respectively. For a 2D tessellation,  $z_{fact}$  can be omitted.
- 'rotate(axis\_x,axis\_y,axis\_z,angle)' for a rotation about the centre and by an axis/angle pair.
- 'translate( $dist_x$ ,  $dist_y$ ,  $dist_z$ )' for a translation by distances  $dist_x$ ,  $dist_y$  and  $dist_z$  along directions x, y and z, respectively.
- 'cut(primitive1, primitive2,...)' for cutting by a series of geometrical primitives (experimental). The primitives can be:
- (i) 'hspace(d,a,b,c)' for the half-space of equation  $ax + by + cz \ge d$ ;
- (ii) 'sphere(centre\_x,centre\_y,centre\_z,rad)' for a sphere of centre

(centre\_x, centre\_y, centre\_z) and radius rad;

(iii) 'cylinder(basis\_x,basis\_y,basis\_z,axis\_x,axis\_y,axis\_z,rad)' for a cylinder of basis point (basis\_x,basis\_y,basis\_z), axis (axis\_x,axis\_y,axis\_z) and radius rad;

(iv) 'ecylinder(basis\_x, basis\_y, basis\_z, axis\_x, axis\_y, axis\_z, esaxis1\_x, esaxis1\_y, esaxis1\_z, esaxis2\_x, esaxis2\_y, esaxis2\_z, srad1, srad2)' for an elliptic cylinder of basis point (basis\_x, basis\_y, basis\_z), axis (axis\_x, axis\_y, axis\_z), ellipse section first axis (esaxis1\_x, esaxis1\_y, esaxis1\_z), ellipse section second axis (esaxis2\_x, esaxis2\_y, esaxis2\_z), ellipse section first radius esrad1 and ellipse section second radius esrad2.

Append 'i' to a primitive name (to get 'cylinderi', etc.) for the complementary shape.

- 'planecut(d,a,b,c)' for cutting by the (oriented) plane of equation ax + by + cz = d.
- 'slice(d,a,b,c)' for slicing a 3D tessellation by the (oriented) plane of equation ax + by + cz = d (yielding to a 2D tessellation).
- 'mergecell(expr1, expr2,...)' for merging cells matching expression expr1, expr2, etc., where expressions are based on the variables defined in Section A.2 [Tessellation Keys], page 61. Cell merging operates incrementally through expressions.
- 'rmcell(expr1, expr2,...)' for removing cells matching expression expr1, expr2, etc., where expressions are based on the variables defined in Section A.2 [Tessellation Keys], page 61. Cell removing operates incrementally through expressions.
- 'resetcellid' for resetting cell ids (contiguous numbering from 1).

The following transformations apply to a raster tessellation:

- 'scale(x\_fact,y\_fact,z\_fact)' scales a tessellation by x\_fact, y\_fact and z\_fact along directions x, y and z, respectively. For a 2D tessellation, z\_fact can be omitted.
- 'rotate(axis\_x,axis\_y,axis\_z,angle)' for a rotation about the centre and by an axis/angle pair.
- 'translate(dist\_x, dist\_y, dist\_z)' for a translation by distances dist\_x, dist\_y and dist\_z along directions x, y and z, respectively.
- 'renumber' renumbers a tessellation to remove cells that are empty or have a zero id.
- 'oriaverage' sets the cell orientations (field '\*\*cell/\*ori') as the averages of the cell voxel orientations (field '\*\*oridata').
- 'crop: shape(parameters)' crops the raster tessellation by a shape, where 'shape(parameters)' can be 'cube(xmin, xmax, ymin, ymax, zmin, zmax)' or 'cylinder(centre\_x, centre\_y, diameter)' (the axis is z). The values can be any mathematical expression based on the variables defined in Section A.3 [Raster Tessellation Keys], page 63, (see general).
- 'autocrop' reduces the raster to its minimal size.
- 'rasterscale( $x_fact, y_fact, z_fact$ )' scales the number of voxels of the raster by factors  $x_fact$ ,  $y_fact$  and  $z_fact$  along directions x, y and z, respectively. For a 2D tessellation,  $z_fact$  can be omitted.
- 'rmsat' removes the cell "satellites", i.e. parts disconnected from the cell bulk.
- 'grow' grows the cells to fill the domain.
- 'tessinter(tess\_file)' computes the intersection with tessellation tess\_file.
- 'addbuffer(buffx, buffy, buffz)' adds a buffer of buffx void voxels on both sides in the x direction, a buffer of buffy void voxels on both sides in the y direction and a buffer of buffz void voxels on both sides in the z direction.
- '2d' transforms a 3D tessellation with 1 voxel along z into a 2D tessellation. Several transformations can be applied successively by combining them with ','. Possible values: any. Default value: none.

#### -sort char\_string

[Secondary option]

Sort the tessellation cells (typically to facilitate data post-processing). Provide as argument the mathematical expression used for sorting (see Section A.1 [Mathematical and Logical

Expressions, page 59).

Possible values: any. Default value: none.

## 2.1.5 Regularization Options

#### -regularization logical

[Option]

Regularize a tessellation, that is, removes the small edges and, indirectly, the small faces. In return, faces can become non-planar (in 3D). This is controlled by options -fmax, -sel and -mloop. Using regularization enables to get better-quality meshes using module -M (see Chapter 3 [Meshing Module (-M)], page 27).

Possible values: 0 or 1. Default value: 0.

-fmax real [Option]

Specify the maximum allowed face flatness fault (in degrees). The flatness fault is the maximum angle between the normals at two locations on a face.

Possible values: 0 to 180. Default value: 20.

#### -sel or -rsel real

[Secondary option]

Specify the absolute or relative small edge (maximum) length. rsel is defined relative to the average cell size (volume in 3D and area in 2D). The default -rsel 1 leads to a length of 0.25 for a unit volume cell in 3D and 0.125 for a unit area cell in 2D. The value also enables to avoid mesh refinement with the default meshing parameters (see Chapter 3 [Meshing Module (-M)], page 27). It is also possible to specify values on a per-cell basis. The first way is to use the syntax default\_sel,cell\_expr1:cell\_sel1,cell\_expr2:cell\_sel2..., where default\_sel is the default small edge length, cell\_expri is an expression defining the set of cells i and cell\_seli is the corresponding small edge length. 'cell\_expri' can be any expression based on variables provided in Section A.2 [Tessellation Keys], page 61. The expressions are processed one after the other. When processing expression cell\_expri, the matching cells are assigned cell\_seli as small edge length. Typically, option -rsel should be passed the same argument than option -rcl of module -M, see Chapter 3 [Meshing Module (-M)], page 27. The second way is to load values from an external file using the syntax 'file(file\_name)', where file\_name is the name of the file containing the length values.

Possible values: any. Default value: -rsel 1.

## -mloop integer

[Secondary option]

Specify the maximum number of regularization loops. During each loop, the small edges are considered in turn from the shortest to the largest. Regularization stops when the maximum number of loops is reached or no edges are deleted during a loop.

Possible values: any. Default value: 2.

#### 2.1.6 Output Options

-o file\_name [Option]

Specify the output file name.

Possible values: any. Default value: none.

#### -format char\_string

[Option]

Specify the format of the output file(s). For scalar tessellations, the available formats are the Neper 'tess', the Gmsh 'geo', the Ply 'ply', the STL 'stl' (for a separate file for each cell, append ':bycell)', the Wavefront 'obj', the 3dec '3dec' and the Surface Evolver 'fe'. For raster tessellations, the available formats are the Neper 'tesr' and the Kitware 'vtk'. Orientations for the cells can be obtained using 'ori' (see also options starting by '-ori'). Combine the values with ','.

Possible values: tess, geo, ply, stl(:bycell), obj, 3dec, fe, tesr, vtk, ori. Default value: tess.

#### -tesrformat char\_string

[Option]

Specify the format of the raster output file(s). The available formats are ASCII ('ascii'), 8-bit binary / unsigned char-type ('binary8'), 16-bit binary / short-type ('binary16' and 'binary16\_big') and 32-bit binary / int-type ('binary32' and 'binary32\_big'). Formats 'binary16' and 'binary32' mean little endianness while formats 'binary16\_big' and 'binary32\_big' mean big endianness.<sup>7</sup>

Possible values: ascii, binary8, binary16, binary16\_big, binary32, binary32\_big. Default value: binary16 or binary\_big (depending on the system).

#### -tesrsize integer

[Option]

Specify the number of points of a raster tessellation along a direction of the domain. In case of a domain of different lengths along the different directions, the argument stands for the geometrical average of the number of points along the different directions, so that the raster points are as cubic as possible. To specify different values along the x, y and z directions, combine the values with ':'.

Possible values: any. Default value: 20.

#### -oridescriptor char\_string

[Option]

Specify the orientation descriptor used in the .tess, .tesr and .ori files. It can be Euler angles in Bunge, Kocks or Roe convention (e, ek, er), rotation matrix (g), axis / angle of rotation (rtheta), angle of rotation (theta), Rodrigues vector (R) or quaternion (q).

Possible values: above-mentioned values. Default value: e.

#### -oriformat char\_string

[Option]

Specify the format of the .ori output file. The available formats are: the Neper-native plain (i.e. only the descriptors on successive lines), the Zset/Zébulon geof and the FEpX fepx. Possible values: above-mentioned values. Default value: plain.

#### 2.1.7 Post-Processing Options

The first options apply to the cells and seeds of a tessellation or a raster tessellation, independently of its dimension,

#### -statcell char\_string

[Post-processing]

Provide statistics on the tessellation cells. Give as argument the keys as described in Section A.2 [Tessellation Keys], page 61, for a tessellation and Section A.3 [Raster Tessellation Keys], page 63, for a raster tessellation (combine with ',').

Possible values: any. Default value: none.

Result file: extension .stcell.

#### -statseed char\_string

[Post-processing]

Provide statistics on the tessellation seeds. Give as argument the keys as described in Section A.2 [Tessellation Keys], page 61, for a tessellation and Section A.3 [Raster Tessellation Keys], page 63, for a raster tessellation (combine with ',').

Possible values: any. Default value: none.

Result file: extension .stseed.

For a tessellation, it is also possible to get statistics on an entity-basis,

## -statver char\_string

[Post-processing]

Provide statistics on the tessellation vertices. Give as argument the keys as described in Section A.2 [Tessellation Keys], page 61, (combine with ',').

Possible values: any. Default value: none.

Result file: extension .stver.

<sup>&</sup>lt;sup>7</sup> Endianness is both written in the tesr file and tested on the system when reading the tesr file, so that the user normally does not have to care about it (even when transferring files across systems).

#### -statedge char\_string

[Post-processing]

Provide statistics on the tessellation edges. Give as argument the keys as described in Section A.2 [Tessellation Keys], page 61, (combine with ',').

Possible values: any. Default value: none.

Result file: extension .stedge.

#### -statface char\_string

[Post-processing]

Provide statistics on the tessellation faces. Give as argument the keys as described in Section A.2 [Tessellation Keys], page 61, (combine with ',').

Possible values: any. Default value: none.

Result file: extension .stface.

## -statpoly char\_string

[Post-processing]

Provide statistics on the tessellation polyhedra. Give as argument the keys as described in Section A.2 [Tessellation Keys], page 61, (combine with ',').

Possible values: any. Default value: none.

Result file: extension .stpoly.

For a tessellation, it is also possible to get statistics on an voxel-basis, ww

## -statvox char\_string

[Post-processing]

Provide statistics on the tessellation voxels. Give as argument the keys as described in Section A.3 [Raster Tessellation Keys], page 63, (combine with ',').

Possible values: any. Default value: none.

Result file: extension .stpoly.

Finally, it is possible to get statistics for a particular set of points. The option applies to a tessellation.

## -statpoint char\_string

[Post-processing]

Provide statistics on points. The points must be loaded with option -loadpoint. Give as argument the keys as described in Section A.7 [Point Keys], page 66, (combine with ','). Possible values: any. Default value: none.

Result file: extension .stpoint.

# 2.1.8 Advanced Options

These advanced options set running conditions for the optimization libraries,

#### -morphooptialgomaxiter real

[Secondary option]

Specify the maximum number of iterations allowed to the optimization library for running without decreasing the objective function. The expression can be any mathematical expression based on variable 'varnb' (the total number of optimization variables).

Possible values: any. Default value: max(varnb, 1000).

## 2.1.9 Debugging Options

#### -checktess file\_name

[Input data]

Check a tessellation file. Provide as argument the file name. Use this option if the tessellation file fails to load using option -loadtess or in other modules.

Possible values: any. Default value: none.

## 2.2 Output Files

#### 2.2.1 Tessellation

• Neper tessellation file: .tess

It contains a scalar description of the tessellation. See Appendix B [File Formats], page 71, for the file syntax.

• Neper raster tessellation file: .tesr

It contains a raster description of the tessellation. See Appendix B [File Formats], page 71, for the file syntax.

• Gmsh geometry file: .geo

It contains a minimal description of the tessellation written under the Gmsh geometry file format .geo. This file can be opened with Gmsh for visualization.

• Ply file: .ply

It contains a description of the tessellation written under the standard "Polygon File Format" .ply.

• STL file: .stl

It contains a description of the tessellation written under the STL (STereoLithography) format .stl. If '-format stl:bycell' was used, a separate file is written for each cell, whose name ends in -id.stl, where 'id' is the cell identifier written with leading zeros.

• Wavefront geometry file: .obj

It contains a description of the tessellation written under the Wavefront geometry format .obj.

• 3dec file: .3dec

It contains a description of the tessellation written under the 3dec format .3dec.

• VTK file: .vtk

It contains a description of the raster tessellation written under the VTK format .vtk as supported by Amitex\_ffpt. Binary data are always written using BigEndians.

• Orientation file: .ori

It contains crystal orientations for the tessellation cells. The orientations are written on successive lines, using the descriptor specified by option -oridescriptor (see also Section A.8 [Rotations and Orientations], page 67) and the writing convention specified by option -oriformat.

#### 2.2.2 Statistics

Statistics files are provided for cells, seeds, vertices, edges, faces, polyhedra and points. They are formatted with one entity per line. Each line contains the data specified to the corresponding -stat option and described in Section A.2 [Tessellation Keys], page 61, and Section A.3 [Raster Tessellation Keys], page 63, (files .stcell and .stseed only).

- Tessellation cell statistics file, .stcell.
- Tessellation seed statistics file, .stseed.
- Tessellation vertex statistics file, .stver.
- Tessellation edge statistics file, .stedge.
- Tessellation face statistics file, .stface.
- Tessellation polyhedron statistics file, .stpoly.
- Point statistics file, .stpoint.

## 2.2.3 Tessellation Optimization Log Files

Log files are provided for the time, variables, statistical distributions and objective function value. The files contain the data specified to the corresponding -morphooptilog option and described on Section A.4 [Tessellation Optimization Keys], page 63.

- Time file, .logtime.
- Variables, i.e. seed attributes, file, .logvar.
- Statistical distribution files, .logdisid, where id is the identifier of the distribution.
- Objective function value file, .logval.
- Target raster tessellation file, -obj.tesr.

## 2.2.4 Orientation Optimization Log Files

A log file is provided for the orientation variables. The files contain the data specified to the -orioptilogvar option and described on Section A.5 [Orientation Optimization Keys], page 65.

• Variables, i.e. orientations, .logorivar.

## 2.3 Examples

Below are some examples of use of neper -T.

1. Generate a Voronoi tessellation containing 100 cells (with identifier = 1).

```
$ neper -T -n 100 -id 1
```

2. Use an elongated domain and generate a Voronoi tessellation containing 100 cells.

```
$ neper -T -n 100 -id 1 -domain "cube(3,1,0.33)"
```

3. Generate a Voronoi tessellation containing 100 cells and apply regularization.

```
$ neper -T -n 100 -id 1 -reg 1
```

4. Generate a 2D Voronoi tessellation containing 100 cells.

```
$ neper -T -n 100 -id 1 -dim 2
```

5. Generate a tessellation containing 100 cells with an x columnar axis.

```
$ neper -T -n 100 -id 1 -morpho "columnar(x)"
```

6. Generate a tessellation containing 100 cells with a bamboo structure along x.

```
$ neper -T -n 100 -id 1 -morpho "bamboo(x)"
```

7. Generate a tessellation containing 100 cells with experimental grain-growth morphological properties.

```
$ neper -T -n 100 -id 1 -morpho gg
```

8. Generate a tessellation containing 100 cells with experimental grain-growth morphological properties and an aspect ratio of 2:1:0.5.

```
$ neper -T -n 100 -id 1 -morpho "gg,aspratio(2,1,0.5)"
```

9. Generate a tessellation containing 100 cells with experimental grain-growth morphological properties, and get the equivalent diameters and sphericities of the cells.

```
$ neper -T -n 100 -id 1 -morpho gg -statcell diameq:rel,sphericity
```

10. Generate a tessellation of specified absolute grain size distribution (and determine the number of cells accordingly).

```
$ neper -T -n from_morpho -id 1 -morpho
"diameq:lognormal(0.1,0.03),1-sphericity:lognormal(0.145,0.03)"
```

11. Generate a tessellation in a non-convex domain (by cutting the tessellation once generated).

```
$ neper -T -n 100 -id 1 -morpho gg
   -transform "cut(cylinder(1.2,0.5,0.5,0,1,0,0.4))"
```

12. Generate a 2-scale Voronoi tessellation containing  $100 \times 10$  cells.

```
$ neper -T -n 100::10 -id 1::1
```

13. Generate a 2-scale tessellation containing 10 primary cells with grain-growth morphological properties, each one divided into lamellae of width 0.1.

```
$ neper -T -n 10::from_morpho -id 1::1 -morpho "gg::lamellar(w=0.1)"
```

14. Generate a 2-scale Voronoi tessellation containing 10 primary cells with grain-growth morphological properties, each one divided into lamellae of widths loaded from file lam\_width and plane normals loaded from file lam\_normal.

```
$ neper -T -n 10::from_morpho -id 1::1 -morpho "gg::lamellar(w=file(lam_width),v=file(lam_normal))"
```

```
lam_width:
 1 0.05
 2 0.10
 3 0.05
 4 0.10
 5 0.05
 6 0.10
 7 0.05
 8 0.10
 9 0.05
10 0.10
lam_normal:
 1 1.000000 0.000000 0.000000
 2 0.000000 1.000000 0.000000
 3 1.000000 0.000000 0.000000
 4 0.000000 1.000000 0.000000
 5 1.000000 0.000000 0.000000
 6 0.000000 1.000000 0.000000
 7 1.000000 0.000000 0.000000
 8 0.000000 1.000000 0.000000
 9 1.000000 0.000000 0.000000
10 0.000000 1.000000 0.000000
```

15. Generate a 2-scale Voronoi tessellation containing 3 primary cells divided into 1, 10 and 100 secondary cells, respectively.

```
$ neper -T -n "3::file(myfile)" -id 1::1
  myfile:
    1    1
    2    10
    3    100
```

16. Generate a 2-scale Voronoi tessellation containing  $2 \times 3$  cells with specific seed coordinates at both scales (files coo1 and coo2).

```
$ neper -T -n 2::3 -id 1::1 \
   -morphooptiini "coo:file(coo1), weight:0::coo:msfile(coo2), weight:0" \
   -morpho voronoi
   coo1:
    0.25    0.50    0.50
    0.75    0.50    0.50
   coo2:
    1    0.25    0.10    0.50
```

```
1 0.25 0.50 0.50
1 0.25 0.90 0.50
2 0.75 0.50 0.10
2 0.75 0.50 0.50
2 0.75 0.50 0.90
```

Note that coo1 is a simple position file (see Section B.4 [Position File], page 79) while coo2 is a multiscale cell file (see Section B.3 [Multiscale Cell File], page 78).

17. Generate a Voronoi tessellation containing 100 cells (with identifier = 1) with uniformly distributed crystal orientations and cubic crystal symmetry.

```
$ neper -T -n 100 -oricrysym cubic -ori uniform
```

18. Generate 100 uniformly distributed crystal orientations with cubic crystal symmetry (no tessellation).

```
$ neper -T -n 100 -oricrysym cubic -ori uniform -for ori
```

## 3 Meshing Module (-M)

Module -M is the module for meshing scalar and raster tessellations. Two meshing strategies are available. Free (or unstructured) meshing creates a conforming mesh into tetrahedral elements (triangular in 2D). Mapped (or structured) meshing generates a non-conforming mesh into regular hexahedral elements (quadrangular in 2D). Free meshing is carried out so that the elements have sizes as close as possible to the target value, and show high quality, that is, equilateral shapes. The input file is a tessellation file (.tess) or a raster tessellation file (.tesr), as provided by module -T. Standard tessellations, multiscale tessellations and periodic (or semi-periodic) tessellations are supported. Free meshing of raster tessellations works for 2D tessellations only. The output mesh can be written in various formats.

The target element size of the mesh can be specified through the element *characteristic length* ('cl'). It stands for the length of a 1D element, the length of the edge of a triangular or quadrangular element (2D) and the length of an edge of a tetrahedral or hexahedral element (3D). For convenience, a *relative characteristic length* (rcl) is also defined, whose value is relative to the average cell size and provides a medium number of elements. It is also possible to specify cl (or rcl) values on a per-cell basis, or to specify different values along the three coordinate axes.

For free meshing, mesh quality is ensured to the greatest extent possible using several advanced capabilities,

- Optimized meshing rules. The mesh properties are controlled by size parameters (options -cl, -rcl, etc.) and a size gradient parameter used for 1D meshing (option -pl).
- Multimeshing. Each tessellation face and volume is meshed separately of the others, with several meshing algorithms, until a target mesh quality is reached. This is controlled by options starting by -meshqual, and options -mesh2dalgo and -mesh3dalgo.

Note that, in general, tessellation regularization is also necessary to ensure good-quality meshing, see Chapter 2 [Tessellation Module (-T)], page 9.

Remeshing can also be applied to generate a new, good-quality mesh from a mesh containing poor-quality elements. The variables defined on the parent mesh can be transported on the child mesh (options starting by -transport).

For mapped meshing, mesh cleaning options enable to remove isolated elements or duplicate nodes, or to duplicate nodes subjected to singularity behaviour (options -clean, -dupnodemerge and -singnodedup).

Mesh partitioning enables to divide the mesh nodes and elements into several sets while minimizing the interfaces between them<sup>1</sup>, for parallel finite element calculations. Partitioning can return any number of partitions, or more efficiently, can be carried out according to a given parallel computer architecture (option -part).

In the output mesh, the individual entities of the tessellations (the vertices, edges, faces and polyhedra) can be described by element sets (option -dim). Node sets of the vertices, edges and faces of the boundary of the tessellation are also provided for prescribing the boundary conditions (option -nset). The surface element sets are also provided (option -faset). Element sets other than those corresponding to the tessellation cells can be defined (option -elset). The mesh order can be 1 or 2 (option -order). Statistical data can be obtained on the meshes (options starting by -stat).

<sup>&</sup>lt;sup>1</sup> Each partition being assigned to a processor in the finite element calculation, the minimization of the interfaces between the partitions is done in terms of the number of necessary communications between processors.

Here is what a typical run of module -M looks like,

#### \$ neper -M n10-id1.tess

```
N
                          е р е
                                        _____
                                    r
Info : A software package for polycrystal generation and meshing.
Info : Version 3.5.0
Info
     : Built with: gsl nlopt muparser
Info
     : <http://neper.info> <http://neper.info/community>
     : Copyright (C) 2003-2019, and GNU GPL'd, by Romain Quey.
     : Loading initialization file '/home/rquey/.neperrc'...
Info
     : ------
Tnfo
Info : MODULE -M loaded with arguments:
Info
     : [ini file] -gmsh /foo/bar/bin/gmsh
Info
     : [com line] n10-id1.tess
Info
     : -----
Info
     : Reading input data...
Info :
        - Reading arguments...
Info : Loading input data...
Info
        - Loading tessellation...
          [i] Parsing file 'n10-id1.tess'...
Info :
          [i] Parsed file 'n10-id1.tess'.
Info :
Info
    : Meshing...
Info : - Preparing... (cl = 0.2321) 100%
Info : - OD meshing... 100%
Info
        - 1D meshing... 100%
Info :
        - 2D meshing... 100% (0.72|0.87/83%|11%| 6%)
Info :
          > Checking 2D mesh for pinching out...
        - 3D meshing... 100% (0.89|0.91/100%| 0%| 0%)
Info
Info : Searching nsets...
Info
    : Writing mesh results...
Info
     : - Preparing mesh...
Info : - Mesh properties:
Info :
         > Node number:
                          287
         > Elt number:
Info
                         1006
         > Mesh volume:
                        1.000
Info :
Info : - Writing mesh...
Info
          [o] Writing file 'n10-id1.msh'...
     :
Info :
          [o] Wrote file 'n10-id1.msh'.
Info : Elapsed time: 8.537 secs.
______
```

## 3.1 Arguments

## 3.1.1 Prerequisites

#### -gmsh path\_name

[Prerequisite]

Specify the path of the Gmsh binary (for meshing into triangle and tetrahedral elements). Possible values: any. Default value: gmsh.

#### -tmp path\_name

[Prerequisite]

Specify the path of the temporary directory (used by Gmsh).

Possible values: any. Default value: ".".

## 3.1.2 Input Data

In normal use, the input data is a tessellation file, a raster tessellation file or a mesh file,

file\_name [Input data]

Specify the name of the input file. It can be a tessellation file (.tess), a raster tessellation file (.tesr) or a mesh file for remeshing (.msh). To load several of them (namely, both a tessellation file and a mesh file for remeshing), combine them with ','. To overwrite the coordinates of the nodes of a mesh, use the syntax 'file\_name:nodecoo\_file\_name', where file\_name is the name of the mesh file and nodecoo\_file\_name is the name of the file containing the coordinates of the nodes (see Section B.4 [Position File], page 79). To load only a subregion of a raster tessellation, use the syntax 'file\_name:crop(xmin,xmax,ymin,ymax,zmin,zmax)', where 'xmin', 'xmax', 'ymin', 'ymax', 'zmin' and 'zmax' are the minimum and maximum positions along x, y and z, respectively. For 2D raster tessellation, use the syntax 'file\_name:scale(factor)', where factor is the scaling factor, or 'file\_name:scale(factor\_x,factor\_y,factor\_z)', where factor\_x, factor\_y and factor\_z are the scaling factor along x, y and z, respectively. For 2D raster tessellations, the z factor can be omitted.

Possible values: any. Default value: none.

It is also possible to load a result mesh from a file (use option -o not to overwrite the file). If the file contains meshes of dimensions lower than the tessellation's dimension, these meshes are used and only higher-dimension meshes are generated.

#### -loadmesh file\_name

[Input data]

Load a mesh from a file (.msh format).

Possible values: any. Default value: none.

Finally, it is possible to load a set of points. These points are used only for statistics, in option-statpoint,

### -loadpoint file\_name

[Input data]

Load points from a file. See Section B.4 [Position File], page 79, for the file format. Provide as argument the file name.

Possible values: any. Default value: none.

## 3.1.3 Meshing Options

#### -elttype char\_string

[Option]

Specify the type of elements, among tetrahedral ('tet') and hexahedral ('hex'). (The 2D counterparts, 'tri' and 'quad', can also be used and are equivalent.)

Possible values: tet, hex. Default value: tet.

-cl or -rcl real [Option]

Specify the absolute or relative characteristic length of the elements. rcl is defined relative to the average cell size. The default, -rcl 1, leads to a mesh with about 100 elements per cell in average (64 in 2D). For free meshing, it is also possible to define the characteristic length on a per-cell basis, using any mathematical expression based on the variables defined in Section A.2 [Tessellation Keys], page 61, (or Section A.3 [Raster Tessellation Keys], page 63, for a 2D raster tessellation). A typical use is '-rcl (body>0)?val1:val2' to get interior cells meshed with rcl=val1 and boundary cells meshed with rcl=val2. The second way is to load values from an external file using the syntax 'file(file\_name)', where file\_name is the name of the file containing the characteristic length values.

Possible values: any. Default value: -rcl 1.

#### -dim char\_string

[Option]

Specify the meshing dimension. By default, it is equal to the input data dimension ('inputdim'). To get meshes of several dimensions in output, provide the values combined with ','. Provide 'all' for all and 'none' for none. Note that the meshes of all dimensions are always written into a .msh mesh file unless ':msh' is appended to the option argument. If a mesh dimension of 3 is required, but the input data is 2D, the 3D mesh is obtained by extrusion of the 2D mesh. With '-format geof', use '1,inputdim' to get the 1D mesh written as lisets (for visualization).

Possible values: 0 to 3, all, none, inputdim. Default value: inputdim.

-order integer [Option]

Specify the mesh order. 1 means 2-node linear elements, 3-node triangular elements, 4-node quadrangular elements, 4-node tetrahedral elements and 8-node hexahedral elements. 2 means 3-node linear elements, 6-node triangular elements, 8-node quadrangular elements, 10-node tetrahedral elements and 20-node hexahedral elements.

Possible values: 1 or 2. Default value: 1.

#### -clface or -rclface real

[Secondary Option]

Specify the absolute or relative characteristic length of the elements, on a per-face basis. Provide as argument any mathematical expression based on the variables defined in Section A.2 [Tessellation Keys], page 61, or 'default' (the value inherited from the parent polyhedra). A typical use is '-rcl (domface==id)?val:default' to get a finer mesh at domain surface id. The second way is to load values from an external file using the syntax 'file(file\_name)', where file\_name is the name of the file containing the characteristic length values. Possible values: any. Default value: none.

## -cledge or -rcledge real

[Secondary Option]

Specify the absolute or relative characteristic length of the elements, on a per-edge basis. Provide as argument any mathematical expression based on the variables defined in Section A.2 [Tessellation Keys], page 61, or 'default' (the value inherited from the parent faces). A typical use is '-rcl (domedge==id)?val:default' to get a finer mesh at domain edge id. The second way is to load values from an external file using the syntax 'file(file\_name)', where file\_name is the name of the file containing the characteristic length values. Possible values: any. Default value: none.

#### -clver or -rclver real

[Secondary Option]

Specify the absolute or relative characteristic length of the elements, on a per-vertex basis. Provide as argument any mathematical expression based on the variables defined in Section A.2 [Tessellation Keys], page 61, or 'default' (the value inherited from the parent edges). A typical use is '-rcl (domver==id)?val:default' to get a finer mesh at domain vertex id. The second way is to load values from an external file using the syntax 'file(file\_name)', where file\_name is the name of the file containing the characteristic

length values.

Possible values: any. Default value: none.

-pl real [Secondary option]

Specify the progression factor for the element characteristic lengths. This value is the maximum ratio between the lengths of two adjacent 1D elements.

Possible values: any >= 1. Default value: 2.

## -clratio char\_string

[Secondary option]

Specify the ratios between the *cl*-values along the different coordinate axes. Provide the values combined with ':'. For example, '2:1:1' leads to elements twice as long in the x direction as in the y and z directions.

Possible values: none. Default value: any.

#### -clmin real

[Not recommended option]

Specify the minimum characteristic length of the elements.

Possible values: any. Default value: none.

The following options define the multimeshing algorithm (for 2D and 3D free meshings). Multimeshing consists in using several meshing algorithms concurrently, for each face or polyhedron, until a minimum, target mesh quality is reached. The mesh quality factor, O, accounts for both the element sizes and aspect ratios. It is given by  $O = O_{dis}^{\alpha} \times O_{size}^{1-\alpha}$ , where  $O_{dis}$  and  $O_{size}$  range from 0 (poor quality) to 1 (high quality) and  $\alpha$  is a factor equal to 0.8. Therefore, O also ranges from 0 (poor quality) to 1 (high quality). See the Neper reference paper for more information. The minimum quality value can be modified using option -meshqualmin. The values of O and  $O_{dis}$  can be modified using options -meshqualexpr and -meshqualdisexpr. The value of the target mesh quality significantly influences meshing speed and output mesh quality. A value of 0 provides the fastest meshing while a value of 1 provides the best-quality meshing. The default value provides an effective balance. The meshing algorithms are taken from the Gmsh<sup>1</sup> and Netgen<sup>2</sup> libraries (options -mesh2dalgo and -mesh3dalgo).

### -meshqualmin real

[Option]

Specify the minimum, target value of mesh quality, O, as defined by option -meshqualexpr. Possible values: 0 to 1. Default value: 0.9.

#### -meshqualexpr char\_string

[Option]

Specify the expression of mesh quality, O, as a function of Odis and Osize.

Possible values: any. Default value: Odis^0.8\*Osize^0.2.

#### -meshqualdisexpr char\_string

[Secondary option]

Specify the expression of the mesh element distortion parameter, *Odis*, as a function of the element distortion parameter *dis* (see the Neper reference paper).

Possible values: any. Default value: dis^(exp((dis^0.1)/(dis^0.1-1))).

## -mesh2dalgo char\_string

[Secondary option]

Specify the 2D meshing algorithms (combine with ','). The available values are mead (MeshAdapt), dela (Delaunay) and fron (Frontal).

Possible values: mead, dela, fron. Default value: mead, dela, fron.

<sup>&</sup>lt;sup>1</sup> Ch. Geuzaine and J.-F. Remacle, Gmsh: a three-dimensional finite element mesh generator with built-in pre- and post-processing facilities, International Journal for Numerical Methods in Engineering, 79, 1309–1331, 2009.

<sup>&</sup>lt;sup>2</sup> J. Schoberl, Netgen, an advancing front 2d/3d-mesh generator based on abstract rules. Comput. Visual. Sci., 52, 1–41, 1997.

### -mesh3dalgo char\_string

[Secondary option]

Specify the 3D meshing algorithms (combine with ','). Each algorithm has format 'mesh: opti', where mesh and opti stand for the meshing and mesh optimization algorithms. The available values of mesh are currently limited to netg (Netgen). The available values of opti are 'gmsh' (Gmsh), 'netg' (Netgen) and 'gmne' (Gmsh + Netgen). Use 'none' for none. Possible values: netg:none, netg:gmsh, netg:netg, netg:gmne. Default value: netg:gmsh,netg:netg,netg:gmne.

## -interface char\_string

[Secondary option]

Specify the type of interface meshing. Provide 'continuous' for a continuous mesh at interfaces, with shared nodes between neighbour element sets (which are associated to the tessellation cells). Provide 'discontinuous' for a discontinuous mesh at interfaces, with distinct nodes for the neighbour element sets. Provide 'cohesive' for cohesive elements at interfaces, joining the neighbour element sets. In the case of a multiscale tessellation, it is possible to provide a different value for each scale using the '::' separator (if fewer values than tessellation scales are provided, the last provided value is used for all higher scales). See option -faset for the output format.

Possible values: see above. Default value: continuous.

#### -mesh2dpinchfix logical

[Secondary option]

Apply 2D-mesh pinches correction after 2D meshing. Disable only if you really know what you are doing.

Possible values: 0 or 1. Default value: 1.

## 3.1.4 Raster Tessellation Meshing Options

Raster tessellation meshing implies interface reconstruction, interface mesh smoothing then remeshing. The following options enable to control interface smoothing.

#### -tesrsmooth char\_string

[Secondary option]

Method for smoothing the interface meshes reconstructed from raster tessellations. Laplacian smoothing ('laplacian') is an iterative method that modifies the coordinates of a node using the coordinates of the neighbouring nodes. At iteration i, the position of a node,  $X_i$ , is calculated from its previous position,  $X_{i-1}$ , and the position of the barycentre of the neighbouring nodes (weighted barycentre, considering the inverse of the distance between the node and the neighbour),  $X_{i-1}^n$ , as follows:  $X_i = (1-A)X_{i-1} + AX_{i-1}^n$ .  $A \in [0, 1]$  is an adjustable parameter (see option -tesrsmoothfact). The number of iterations is set by option -tesrsmoothitermax. There is no stop criterion, so itermax will always be reached. Possible values: laplacian or none. Default value: laplacian.

### -tesrsmoothfact real

[Secondary option]

Specify the factor used for the interface mesh smoothing (A in option -tesrsmooth).

Possible values: 0 to 1. Default value: 0.5.

#### -tesrsmoothitermax integer

[Secondary option]

Specify the number of iterations used for interface mesh smoothing. Possible values: any >= 0. Default value: 5.

# 3.1.5 Mesh Cleaning Options

The following options are specific to mapped meshing of raster tessellations containing voids.

## -clean integer

[Secondary option]

Clean the mesh so that it consists of a set of connected elements. Provide as argument the level of cleaning. A value of 1 indicates that two elements should be considered connected to each other if they share at least a vertex. A value of 2 indicates that two elements should

be considered connected to each other if they share at least a face. Using this option, the elements (or bunches of elements) that are not connected to the main skeleton are removed. Possible values: 0 to 2. Default value: 0.

## -singnodedup logical

[Secondary option]

Duplicate nodes which are the subject of singularity. Such a node belongs to several elements which share only a node or an edge, which provides a singularity behaviour. In Mechanics, it corresponds to imposing a common displacement, while the point can carry no stress. In Thermics, it corresponds to imposing a given temperature at a particular location shared by two bodies, but not enabling heat flux to operate at that location. When this option is enabled, such a node is duplicated, so that each body has its own node. Option <code>-dupnodemerge</code> enables to merge back duplicate nodes.

Possible values: 0 or 1. Default value: 0.

#### -dupnodemerge real

[Secondary option]

Merge duplicate nodes. Provide as argument the distance between nodes below which two nodes are merged. Note that Neper does not generate meshes with duplicate nodes, except using options -singnodedup or -interface.

Possible values: 0. Default value: any>0.

## 3.1.6 Transformation Options

## -transform char\_string(...)

[Option]

Apply transformations to a mesh. The following transformations can be applied:

- 'scale( $x_{fact}$ ,  $y_{fact}$ ,  $z_{fact}$ )' scales a mesh by  $x_{fact}$ ,  $y_{fact}$  and  $z_{fact}$  along directions x, y and z, respectively. For a 2D mesh,  $z_{fact}$  can be omitted.
- 'translate( $dist_x$ ,  $dist_y$ ,  $dist_z$ )' translates a mesh by distances  $dist_x$ ,  $dist_y$  and  $dist_z$  along directions x, y and z, respectively.
- 'smooth(fact,itermax,type)' smooths the interfaces of a mesh by Laplacian smoothing (use only if you know what you are doing). Laplacian smoothing is an iterative method that modifies the coordinates of a node using the coordinates of the neighbouring nodes. At iteration i, the position of a node,  $X_i$ , is calculated from its previous position,  $X_{i-1}$ , and the position of the barycentre of the neighbouring nodes (weighted barycentre, considering the inverse of the distance between the node and the neighbour),  $X_{i-1}^n$ , as follows:  $X_i = (1 fact) X_{i-1} + fact X_{i-1}^n$ ;  $0 \le fact \le 1$ . itermax iterations are applied. type defines the nodes used for smoothing and can be 'all' for all nodes or 'interior' for interior nodes. Possible values: see above. Default value: none.

#### 3.1.7 Mesh Partitioning Options

Mesh partitioning is achieved using the libScotch library<sup>3</sup>. The principle of mesh partitioning is to create partitions of same size while minimizing the interfaces between them. This affects the same load to all computation units and minimizes communications between them, therefore minimizes the total computation time. There are two available strategies for mesh partitioning. The first one creates partitions and arranges them independently of each other, while the second one consists in optimizing the size and arrangement of the partitions based on a given computer cluster architecture to minimize computation time further. For those clusters that contain processors made of several cores, the communication time between cores of a processor is much lower than the communication time between cores of different processors. To minimize the global communication time, partitions which are processed by cores of the same processor can be grouped together. Partitioning is applied to the higher-dimension mesh. On top of defining

<sup>&</sup>lt;sup>3</sup> F. Pellegrini, Scotch and libScotch 5.1 User's Guide, INRIA Bordeaux Sud-Ouest, ENSEIRB & LaBRI, UMR CNRS 5800, 2008.

the partitions, it renumbers the nodes and elements by increasing partition identifier and writes partitions as element and node sets (vtk, inp and geof formats). This can be managed using option -part.

## -part integer or char\_string

[Option]

Specify the number of partitions or a computer cluster architecture. Using the first option, the number of partition can be any. At the opposite, for a computer cluster architecture, the total number of partitions must be a power of 2. An architecture can be specified in two ways. First, for clusters that contain processors made of several cores, the number of processors and the number of cores per processor can be combined using the ':' separator. A ratio of 10 is considered between the computation time between cores located on different processors and the one between cores of the same processor. Second, the name of a file describing the cluster architecture at the Scotch format can be provided.

Possible values: any. Default value: none.

## -partbalancing real

[Secondary option]

Specify the rate of element partition balancing. The partitioning algorithm applies to the nodes; the element partitions are determined afterwards and can be somewhat unbalanced. This option enables to enforce balancing, but getting a full balancing is highly CPU-demanding.

Possible values: 0 to 1. Default value: 0.5.

### -partmethod char\_string

[Secondary option]

Specify the partitioning method. Provide the partitioning expression in Scotch's jargon, or 'none' for none.

Possible values: any. Default value: see\_the\_source.

## 3.1.8 Field Transport Options

## -transport char\_string:char\_string:file\_name,...

[Option]

Transport data from a parent mesh to a child mesh. The parent mesh is the input mesh and the child mesh is the result mesh (created by remeshing or loaded with -loadmesh). A transport entry must have format 'entity\_type:data\_type:file\_name', where 'entity\_type' must be 'node' or 'elt', 'data\_type' is the type of data, under format 'integerX' or 'realX', where X is the dimension, and file\_name is the name of the file containing the parent data. For several data transports, combine the transport entries with ','. Nodal data are transported by interpolation using the shape functions (2D only). Elemental data are transported as specified by -transporteltmethod.

Possible values: any. Default value: none.

## -transportfepx char\_string:char\_string...

[Option]

Transport FEpX data from a parent mesh to a child mesh. The parent mesh is the input mesh and the child mesh is the result mesh (created by remeshing or loaded with <code>-loadmesh</code>). A transport entry must have format 'orientation\_file:tau\_file', where 'orientation\_file' is the orientation file (a list of Euler angles in Kocks convention) and 'tau\_file' is the critical resolved shear strength file (a list of scalars). These elemental data are transported as specified by <code>-transporteltmethod</code>. Moreover, the <code>.kocks</code> and <code>.opt</code> FEpX files are generated from these data and can be used to run a new simulation.

Possible values: any. Default value: none.

#### -transporteltmethod char\_string:char\_string... [Secondary option]

Specify the method to transport elemental data from the parent mesh to the child mesh. For each element of the child mesh, its centre, c, is considered. Use 'distance' to choose, for each element of the child mesh (of centre c), the element of the parent mesh whose centre is

the closest to c, or 'location' to choose the element c belongs to.

Possible values: see above. Default value: distance.

## 3.1.9 Output Options

-o file\_name [Option]

Specify the output file name.

Possible values: any. Default value: none.

## -format char\_string

[Option]

Specify the format of the output file(s). Mesh formats are: the Gmsh 'msh', the VTK 'vtk', the Abaqus 'inp', the Zset/Zébulon 'geof' and the FEpX 'fepx' (for the FEpX legacy format, provide 'fepx:legacy'). For 'msh', append ':format' to specify the format, which can be 'ascii' or 'binary' (default 'ascii'). The tessellation file format 'tess' is also available. Combine arguments with ','.

Possible values: see above. Default value: msh.

### -nset char\_string

[Option]

Specify the node sets to provide, among: faces, edges, vertices for all domain faces, edges and vertices, and facebodies and edgebodies for all face and edge bodies. Provide all for all and none for none. To get the node sets corresponding to individual entities, provide their labels. For a cuboidal domain, they are [x-z][0,1] for the domain faces, [x-z][0,1][x-z][0,1] for the edges, and [x-z][0,1][x-z][0,1][x-z][0,1] for the vertices. For a cylindrical domain, they are z[0,1] for the z faces, and z[0,1] for the faces on the circular part of the domain. For other domains, they are z[0,1] for the faces. For cylindrical and other types of domains, the edge and vertex labels are obtained from the face labels as for cuboidal domains. For a 2D mesh (generated from a 2D tessellation), the labels are z[0,1] for the edges and z[0,1] for the vertices. Append body to a label to get only the body nodes of the set. Combine labels with ','.

Possible values: see above. Default value: faces in 3D and edges in 2D.

## -faset char\_string

[Option]

Specify the element surface meshes (edge meshes in 2D) to provide. Use 'faces' for all domain faces. To get the meshes of individual faces, provide their labels (see option -nset). For internal mesh faces (edges in 2D) as created by '-interface discontinuous', provide 'internal'. Combine them with ','. Provide none for none.

Possible values: see above. Default value: none.

#### -elset char\_string

[Secondary option]

Specify the element sets to provide. The argument can be: default for the default element sets (those corresponding to the input tessellation cells), or an expression of the form 'elset\_label:elset\_definition', where elset\_label is a custom elset label and elset\_definition is an expression defining the elements belonging to the elset, defined from the variables provided in Section A.6 [Mesh Keys], page 66. Combine arguments with ','.

Possible values: see above. Default value: default.

#### -oriformat char\_string

[Option]

Specify the format of the .per output file. The available formats are: the Neper-native plain and the Zset/Zébulon geof.

Possible values: see above. Default value: plain.

## 3.1.10 Post-Processing Options

The following options provide statistics on the nodes ('nodes'), 0D elements ('elt0d') and element sets ('elset0d'), 1D elements ('elt1d') and element sets ('elset1d'), 2D elements

('elt2d') and element sets ('elset2d') and 3D elements ('elt3d') and element sets ('elset3d'). Also note that the 'elt' and 'elset' labels can be used in place of 'eltnd' and 'elsetnd', where n is the higher mesh dimension. This enables to use the same command whatever the higher mesh dimension is.

## -statnode char\_string

[Post-processing]

Provide statistics on the nodes. Provide as argument the keys as described in Section A.6 [Mesh Keys], page 66, (combine with ',').

Possible values: any. Default value: none.

Result file: extension .stnode.

## -statelt0d char\_string

[Post-processing]

Provide statistics on the 0D elements. Provide as argument the keys as described in Section A.6 [Mesh Keys], page 66, (combine with ',').

Possible values: any. Default value: none.

Result file: extension .stelt0d.

#### -statelt1d char\_string

[Post-processing]

Provide statistics on the 1D elements. Provide as argument the keys as described in Section A.6 [Mesh Keys], page 66, (combine with ',').

Possible values: any. Default value: none.

Result file: extension .stelt1d.

#### -statelt2d char\_string

[Post-processing]

Provide statistics on the 2D elements. Provide as argument the keys as described in Section A.6 [Mesh Keys], page 66, (combine with ',').

Possible values: any. Default value: none.

Result file: extension .stelt2d.

#### -statelt3d char\_string

[Post-processing]

Provide statistics on the 3D elements. Provide as argument the keys as described in Section A.6 [Mesh Keys], page 66, (combine with ',').

Possible values: any. Default value: none.

Result file: extension .stelt3d.

#### -statelset0d char\_string

[Post-processing]

Provide statistics on the 0D element sets. Provide as argument the keys as described in Section A.6 [Mesh Keys], page 66, (combine with ',').

Possible values: any. Default value: none.

Result file: extension .stelset0d.

#### -statelset1d char\_string

[Post-processing]

Provide statistics on the 1D element sets. Provide as argument the keys as described in Section A.6 [Mesh Keys], page 66, (combine with ',').

Possible values: any. Default value: none.

Result file: extension .stelset1d.

## -statelset2d char\_string

[Post-processing]

Provide statistics on the 2D element sets. Provide as argument the keys as described in Section A.6 [Mesh Keys], page 66, (combine with ',').

Possible values: any. Default value: none.

Result file: extension .stelset2d.

### -statelset3d char\_string

[Post-processing]

Provide statistics on the 3D element sets. Provide as argument the keys as described in Section A.6 [Mesh Keys], page 66, (combine with ',').

Possible values: any. Default value: none.

Result file: extension .stelset3d.

## -statpoint char\_string

[Post-processing]

Provide statistics on points. The points must be loaded with option -loadpoint. Provide as argument the keys as described in Section A.7 [Point Keys], page 66, (combine with ',').

Possible values: any. Default value: none.

Result file: extension .stpoint.

## 3.1.11 Advanced Options

These advanced options set running conditions for the meshing libraries (triangle and tetrahedral meshing),

### -mesh3dclreps real

[Secondary option]

Specify the relative tolerance on the average element characteristic length of each polyhedron (compared to cl). The value can also be defined on a per-cell basis, using any mathematical expression based on the variables defined in Section A.2 [Tessellation Keys], page 61, or by loading values from an external file, using the syntax 'file(file\_name)', where file\_name is the name of the file containing the values. As Neper proceeds iteratively to adjust the average element characteristic length, this is a highly CPU-sensitive capability, and low values will increase computation time significantly.

Possible values: any. Default value: 0.02.

#### -mesh2dmaxtime real

[Secondary option]

Specify the maximum processing time allowed to the meshing library for meshing a tessellation face (in seconds).

Possible values: any. Default value: 1000.

#### -mesh2drmaxtime real

[Secondary option]

Specify a factor used to determine the maximum processing time allowed to the meshing library for meshing a tessellation face. This option is similar to -mesh2dmaxtime, but the actual maximum time is the product of the maximum processing time of the previous meshings by the value provided in argument.

Possible values: any. Default value: 100.

## -mesh2diter integer

[Secondary option]

Specify the maximum number of 2D meshing attempts for a particular face (in case of failure). Possible values: any. Default value: 3.

#### -mesh3dmaxtime real

[Secondary option]

Specify the maximum processing time allowed to the meshing library for meshing a tessellation polyhedron (in seconds).

Possible values: any. Default value: 1000.

#### -mesh3drmaxtime real

[Secondary option]

Specify a factor used to determine the maximum processing time allowed to the meshing library for meshing a tessellation polyhedron. This option is similar to <code>-mesh3dmaxtime</code>, but the actual maximum time is the product of the maximum processing time of the previous meshings by the value provided in argument.

Possible values: any. Default value: 100.

#### -mesh3diter integer

[Secondary option]

Specify the maximum number of 3D meshing attempts for a particular polyhedron (in case of failure).

Possible values: any. Default value: 3.

## 3.2 Output Files

#### 3.2.1 Mesh

The mesh can be written in the following formats,

Gmsh format: file .mshVTK format: file .vtkAbaqus format: file .inp

• Zset/Zébulon format: file .geof

• FEpX format: files .mesh, .grain and .bcs (.parms, .mesh, .surf, .opt, .bcs and .kocks in legacy mode)

## 3.2.2 Periodicity

• File .per.

It contains the mesh periodicity conditions, written following the convention specified by option -performat. For format 'plain', for each slave node, the file provides (one slave node per line): the node id, the master node id and the shift vector of the slave. For format 'geof', the file provides the displacement relationships between master and slaves nodes.

### 3.2.3 Interfaces

• File .intl. For each 2D interface, the file provide (one 2D interface per line): the labels of the two element sets of the interface.

#### 3.2.4 Statistics

Statistics files are provided for nodes, elements, element sets and points. They are formatted with one entity per line. Each line contains the data specified to the corresponding -stat option and described in Section A.6 [Mesh Keys], page 66.

- Node statistics file, .stnode.
- (Higher-dimension) element statistics file, .stelt.
- (Higher-dimension) element set statistics file, .stelset.
- 0D element statistics file, .stelt0d.
- 1D element statistics file, .stelt1d.
- 2D element statistics file, .stelt2d.
- 3D element statistics file, .stelt3d.
- 0D element set statistics file, .stelset0d.
- 1D element set statistics file, .stelset1d.
- 2D element set statistics file, .stelset2d.
- 3D element set statistics file, .stelset3d.
- Point statistics file, .stpoint.

## 3.3 Examples

Below are some examples of use of neper -M,

1. Mesh tessellation n100-id1.tess.

```
$ neper -M n100-id1.tess
```

2. Mesh 2D raster tessellation n100-id1.tesr.

```
$ neper -M n100-id1.tesr
```

3. Mesh tessellation n100-id1.tess with a mesh size of rcl = 0.5 and in 2nd-order elements.

```
$ neper -M n100-id1.tess -rcl 0.5 -order 2
```

4. Mesh tessellation n100-id1.tess with small elements for the interior cells and bigger elements for the boundary cells.

```
$ neper -M n100-id1.tess -rcl "0.2,body==0:0.5"
```

5. Remesh mesh n150\_def.msh (comprising poor-quality elements) into a clean, new mesh. Transport the scalar data of file n150\_def.data from the deformed mesh to the new mesh.

```
$ neper -M n150.tess,n150_def.msh -transport elt:real1:n150_def.data
-rcl 0.5 -o n150_new
```

6. Mesh tessellation n100-id1.tess and divide the mesh into 8 partitions.

```
$ neper -M n100-id1.tess -part 8
```

7. Mesh tessellation n100-id1.tess into regular hexahedral elements (non-conformal mesh).

```
$ neper -M n100-id1.tess -elt hex
```

8. Mesh tessellation n100-id1.tess and get, for each element, its radius ratio and its volume.

```
$ neper -M n100-id1.tess -statelt rr,vol
```

# 4 Visualization Module (-V)

Module -V is the Neper visualization module, with which the tessellations and meshes can be printed as publication-quality images. It is also possible to visualize data on them using colours and transparency, or displacements of the nodes and to plot data on slices of the mesh. Points of specific size and colour can also be shown. The output is a PNG image file. The POV-Ray ray-tracing library is used for generating the images.

Contrary to other modules, module -V processes the command arguments one after the other. Typically, using module -V consists in loading a tessellation or a mesh, then data fields to render them. The data can apply to the tessellation entities: polyhedra, faces, edges and vertices, to the mesh entities: 3D, 2D, 1D and 0D elements and nodes, and to points (options starting by -data). The entities that are to be visible, for example particular tessellation cells, element sets or elements, can also be specified (options starting by -show). The way they are plotted: camera position and angle, projection type, image size, etc., can be set up too (options starting by -camera or -image). Finally, the coordinate system can be added.

Here is what a typical run of module -V looks like,

```
$ neper -V n10-id1.tess,n10-id1.msh -dataelsetcol id -print img
```

```
е
                                          r
                                              _____
                                р
      : A software package for polycrystal generation and meshing.
Info
      : Version 3.5.0
Info
      : Built with: gsl nlopt muparser
Info
      : <http://neper.info> <http://neper.info/community>
Info
      : Copyright (C) 2003-2019, and GNU GPL'd, by Romain Quey.
Info
      : Loading initialization file '/home/rquey/.neperrc'...
Info
Info
      : MODULE -V loaded with arguments:
Info
Info
      : [ini file]
      : [com line] n10-id1.tess,n10-id1.msh -dataelsetcol id -print img
Info
      : ------
Tnfo
Info
      : Loading tessellation...
Info
            [i] Parsing file 'n10-id1.tess'...
            [i] Parsed file 'n10-id1.tess'.
Info
Info
      : Loading mesh...
            [i] Parsing file 'n10-id1.msh'...
Info
            [i] Parsed file 'n10-id1.msh'.
Info
      : Reconstructing mesh...
Info
Info
      : Reading data (elset3d, col)...
      : Printing image...
Info
Info
            [o] Writing file 'img.pov'...
Info
          - Printing mesh...
            > Reducing data...
Tnfo
              . Number of 3D elt faces reduced by 90% (to 410).
Info
Info
              . Number of 3D elt edges reduced by 50% (to 615).
                                    reduced by 100% (to 0).
              . Number of OD elts
Info
Tnfo
            [o] Wrote file 'img.pov'.
          - Generating png file (1080x1080 pixels)...
Info
            [o] Writing file 'img.png'...
Info
            [o] Wrote file 'img.png'.
Info
Info
      : Printing scale...
```

Info : Elapsed time: 1.620 secs.

## 4.1 Arguments

## 4.1.1 Prerequisites

-povray path\_name

[Prerequisite]

Specify the path of the POV-Ray binary (for generating PNG images).

Possible values: any. Default value: povray.

## 4.1.2 Input Data

file\_name [Input data]

Specify the name of the input file. It can be a tessellation file (.tess), a raster tessellation file (.tess), a mesh file (.msh) or a point file (see Section B.4 [Position File], page 79). To load several of them, combine them with ','.

Possible values: any. Default value: none.

## 4.1.3 Tessellation Data Loading and Rendering

The following options enable to define the properties (colour and size) of the tessellation cells or entities (polyhedra, faces, edges and vertices). This can be done either directly, by specifying the property values (e.g. the RGB channel values for colour) or indirectly, e.g. using scalar values that are converted in colour using a given *colour scheme*. In this case, a scale image is generated in addition to the tessellation image. The scale properties can be set up (minimum, maximum and tick values).

The following options apply to the cells of a tessellation or a raster tessellation, independently of its dimension,

## -datacellcol char\_string

[Option]

Set the colours of the tessellation cells. The argument can be one of the following: (i) 'id' for colouring based on the identifier, using a colour palette (see Section A.10 [Colours], page 68), (ii) 'ori' for colouring based on the crystal orientations, (iii) the name of a colour that will be used for all cells (see Section A.10 [Colours], page 68), (iv) the name of a file containing a list of colours (provided as RGB channel values), or (v) a string indicating how the colours can be obtained. The string has the format 'var:file\_name', where var can be 'id' for identifiers, 'ori' for crystal orientations or 'scal' for scalar values, and 'file\_name' is the name of the file containing the data. The colour schemes used to derive the colours from the data can be specified with option -datacellcolscheme.

Possible values: any. Default value: white.

#### -datacellcolscheme char\_string

[Option]

Set the colour scheme used to get colours from the data of the tessellation cells loaded with option -datacellcol. The type of colour scheme depends on the type of data.

- For crystal orientations (cubic symmetry is assumed), the colour scheme can be: 'R' for Rodrigues vector colouring (default is inside the fundamental region, can be bounded using 'R(max)', where max is the maximum extent), 'r' for rotation axis colouring, 'theta' for rotation angle colouring (can be bounded using 'theta(max)', where max is the maximum angle (in radian)) and 'rtheta' for rotation axis / angle colouring (can be bounded using 'rtheta(max)', where max is the maximum angle (in radian)).
- For scalars, the colour scheme can be any list of colours.

Possible values: see above list. Default value: "R" for crystal orientations and "blue, cyan, yellow, red" for scalars.

-datacelltrs real [Option]

Set the transparency of the tessellation cells. Provide as argument a value that applies to all cells or 'file(file\_name)' to load values from a file.

Possible values: 0 to 1. Default value: 0.

## -datacellscale char\_string

[Option]

Set the scale relative to the '-datacellcol scal' data. Provide as argument the start and end values, combined with ':'. To specify the intermediate values, provide as argument the start value, the intermediate values and then the end value, combined with ':'. The labels of the scale follow the format used for the start value.

Possible values: any. Default value: data minimum:data maximum.

## -datacellscaletitle char\_string

[Option]

Set the title of the scale relative to the '-datacellcol scal' data.

Possible values: any. Default value: none.

For tessellations, it is also possible to set data on a per-entity basis,

### -datapolycol char\_string

[Option]

Set the colours of the tessellation polyhedra. The argument can be one of the following: (i) 'id' for colouring based on the identifier, using a colour palette (see Section A.10 [Colours], page 68), (ii) 'scaleid(scale)' for colouring based on the identifier of the scale tessellation the polyhedron belongs to, using a colour palette (see Section A.10 [Colours], page 68), (iii) the name of a colour that will be used for all polyhedra (see Section A.10 [Colours], page 68), (iv) the name of a file containing a list of colours (provided as RGB channel values), or (v) a string indicating how the colours can be obtained. The string has the format 'var:file\_name', where var can be 'ori' for crystal orientations or 'scal' for scalar values, and 'file\_name' is the name of the file containing the data. The colour schemes used to derive the colours from the data can be specified with option -datapolycolscheme.

Possible values: any. Default value: white.

## -datapolycolscheme char\_string

[Option]

Set the colour scheme used to get colours from the data of the tessellation faces loaded with option -datafacecol. See option -datacellcolscheme for the argument format.

Possible values: see option -datacellcolscheme. Default value: see option -datacellcolscheme.

## -datapolytrs real

[Option]

Set the transparency of the tessellation polyhedra. Provide as argument a value that applies to all polyhedra or 'file(file\_name)' to load values from a file.

Possible values: 0 to 1. Default value: 0.

### -datapolyscale char\_string

[Option]

Set the scale relative to the '-datapolycol scal' data. Provide as argument the start and end values, combined with ':'. To specify the intermediate values, provide as argument the start value, the intermediate values and then the end value, combined with ':'. The labels of the scale follow the format used for the start value.

Possible values: any. Default value: data minimum:data maximum.

#### -datapolyscaletitle char\_string

[Option]

Set the title of the scale relative to the '-datapolycol scal' data.

Possible values: any. Default value: none.

#### -datafacecol char\_string

[Option]

Set the colours of the tessellation faces. See option -datapolycol for the argument format. Possible values: any. Default value: white.

### -datapolycolscheme char\_string

[Option]

Set the colour scheme used to get colours from the data of the tessellation faces loaded with option -datafacecol. See option -datacellcolscheme for the argument format.

Possible values: see option -datacellcolscheme. Default value: see option -datacellcolscheme.

### -datafacecolscheme char\_string

[Option]

Set the colour scheme used to get colours from the data of the tessellation faces loaded with option -datafacecol. See option -datacellcolscheme for the argument format.

Possible values: see option -datacellcolscheme. Default value: see option -datacellcolscheme.

-datafacetrs real

[Option]

Set the transparency of the tessellation faces. Provide as argument a value that applies to all faces or 'file(file\_name)' to load values from a file.

Possible values: 0 to 1. Default value: 0.

### -datafacescale char\_string

[Option]

Set the scale relative to the '-datafacecol scal' data. Provide as argument the start and end values, combined with ':'. To specify the intermediate values, provide as argument the start value, the intermediate values and then the end value, combined with ':'. The labels of the scale follow the format used for the start value.

Possible values: any. Default value: data minimum:data maximum.

#### -datafacescaletitle char\_string

[Option]

Set the title of the scale relative to the '-datafacecol scal' data.

Possible values: any. Default value: none.

### -dataedgerad char\_string

[Option]

Set the radii of the tessellation edges. The argument can be one of the following: a real value that will be used for all entities or the name of a file containing a list of radii.

Possible values: any. Default value: tessellation dependent.

#### -dataedgecol char\_string

[Option]

Set the colours of the tessellation edges. See option -datapolycol for the argument format. Possible values: any. Default value: black.

#### -dataedgecolscheme char\_string

[Option]

Set the colour scheme used to get colours from the data of the tessellation edges loaded with option -dataedgecol. See option -datacellcolscheme for the argument format.

Possible values: see option -datacellcolscheme. Default value: see option -datacellcolscheme.

### -dataedgetrs real

[Option]

Set the transparency of the tessellation edges. Provide as argument a value that applies to all edges or 'file(file\_name)' to load values from a file.

Possible values: 0 to 1. Default value: 0.

#### -dataedgescale char\_string

[Option]

Set the scale relative to the '-dataedgecol scal' data. Provide as argument the start and end values, combined with ':'. To specify the intermediate values, provide as argument the start value, the intermediate values and then the end value, combined with ':'. The labels of the scale follow the format used for the start value.

Possible values: any. Default value: data minimum:data maximum.

### -dataedgescaletitle char\_string

[Option]

Set the title of the scale relative to the '-dataedgecol scal' data.

Possible values: any. Default value: none.

## -dataverrad char\_string

[Option]

Set the radii of the tessellation vertices. See option -dataedgerad for the argument format. Possible values: any. Default value: tessellation dependent.

#### -datavercol char\_string

[Option]

Set the colours of the tessellation vertices. See option -datapolycol for the argument format. Possible values: any. Default value: black.

## -datavercolscheme char\_string

[Option]

Set the colour scheme used to get colours from the data of the tessellation vertices loaded with option -datavercol. See option -datacellcolscheme for the argument format.

Possible values: see option -datacellcolscheme. Default value: see option -datacellcolscheme.

-datavertrs real [Option]

Set the transparency of the tessellation vertices. Provide as argument a value that applies to all vertices or 'file(file\_name)' to load values from a file.

Possible values: 0 to 1. Default value: 0.

## -dataverscale char\_string

[Option]

Set the scale relative to the '-datavercol scal' data. Provide as argument the start and end values, combined with ':'. To specify the intermediate values, provide as argument the start value, the intermediate values and then the end value, combined with ':'. The labels of the scale follow the format used for the start value.

Possible values: any. Default value: data minimum:data maximum.

## -dataverscaletitle char\_string

[Option]

Set the title of the scale relative to the '-datavercol scal' data.

Possible values: any. Default value: none.

## -dataseedrad char\_string

[Option]

Set the radii of the tessellation seeds. See option -dataedgerad for the argument format. Possible values: any. Default value: tessellation dependent.

### -dataseedcol char\_string

[Option]

Set the colours of the tessellation seeds. See option -datapolycol for the argument format. Possible values: any. Default value: grey.

### -dataseedcolscheme char\_string

[Option]

Set the colour scheme used to get colours from the data of the tessellation seeds loaded with option -dataseedcol. See option -datacellcolscheme for the argument format.

Possible values: see option -datacellcolscheme. Default value: see option -datacellcolscheme.

#### -dataseedscale char\_string

[Option]

Set the scale relative to the '-dataseedcol scal' data. Provide as argument the start and end values, combined with ':'. To specify the intermediate values, provide as argument the start value, the intermediate values and then the end value, combined with ':'. The labels of the scale follow the format used for the start value.

Possible values: any. Default value: data minimum:data maximum.

## -dataseedscaletitle char\_string

[Option]

Set the title of the scale relative to the '-dataseedcol scal' data.

Possible values: any. Default value: none.

Below are options specific to raster tessellations, For a raster tessellation, it is also possible to set data on a per-voxel basis,

### -datavoxcol char\_string

[Option]

Set the colours of the voxels. The argument can be one of the following: (i) 'id' for colouring based on the identifier, using a colour palette (see Section A.10 [Colours], page 68), (ii) 'ori' for colouring based on the crystal orientations, (iii) 'disori' for colouring based on the disorientations with respect to the corresponding mean cell orientation, (iv) the name of a colour that will be used for all cells (see Section A.10 [Colours], page 68), (v) the name of a file containing a list of colours (provided as RGB channel values), or (vi) a string indicating how the colours can be obtained. The string has the format 'var:file\_name', where var can be 'id' for identifiers, 'ori' for crystal orientations or 'scal' for scalar values, and 'file\_name' is the name of the file containing the data. The colour schemes used to derive the colours from the data can be specified with option -datavoxcolscheme.

Possible values: any. Default value: white.

### -datavoxcolscheme char\_string

[Option]

Set the colour scheme used to get colours from the data of the voxels loaded with option -datavoxcol. See option -datacellcolscheme for the argument format.

Possible values: see option -datacellcolscheme. Default value: see option -datacellcolscheme.

### -datavoxscale char\_string

[Option]

Set the scale relative to the '-datavoxcol scal' data. Provide as argument the start and end values, combined with ':'. To specify the intermediate values, provide as argument the start value, the intermediate values and then the end value, combined with ':'. The labels of the scale follow the format used for the start value.

Possible values: any. Default value: data minimum:data maximum.

#### -datavoxscaletitle char\_string

[Option]

Set the title of the scale relative to the '-datavoxcol scal' data.

Possible values: any. Default value: none.

#### -datavoxedgerad real

[Option]

Set the radius of the edges of the raster points.

Possible values: any. Default value: proportional to the raster point size.

#### -datavoxedgecol char\_string

[Option]

Set the colour of the edges of the raster points. Provide as argument the name of a colour that will be used for all points (see Section A.10 [Colours], page 68).

Possible values: any. Default value: black.

## 4.1.4 Mesh Data Loading and Rendering

The following options enable to define the properties (colour, size, etc.) of the mesh entities (3D, 2D, 1D and 0D elements, and nodes). This can be done either directly, by specifying the property values (e.g. the RGB channel values for colour) or indirectly, e.g. using scalar values that are rendered in colour using a given *colour scheme*. In this case, a scale image is generated in addition to the mesh image. The scale properties can be set up (start and end values, tick values).

The options are listed below for 3D elements ('elt3d') and element sets ('elset3d'), 2D elements ('elt2d') and element sets ('elset2d'), 1D elements ('elt1d') and element sets ('elset1d'), 0D elements ('elt0d') and element sets ('elset0d') and nodes ('nodes'). Also note that the 'elt' and 'elset' labels can be used in place of 'eltnd' and 'elsetnd', where n is the highest mesh dimension. This enables to use the same command whatever the highest mesh dimension is.

The following options enable to load data relative to the 3D mesh elements. Note that the options can be applied to element sets by changing 'elt' to 'elset'.

## -dataelt3dcol char\_string

[Option]

Set the colours of the 3D elements. The argument can be one of the following: (i) 'id' for the default colour palette (see Section A.10 [Colours], page 68), (ii) the name of a colour that will be used for all elements (see Section A.10 [Colours], page 68), (iii) the name of a file containing a list of colours (provided as RGB channel values), (iv) a string indicating how the colours can be obtained, or (v) 'from\_nodes' to derive the colours of the elements from the colours of the nodes (the node colours must be loaded using option -datanodecol). In case (iv), the string has the format 'var:file\_name', where var can be 'ori' for crystal orientations or 'scal' for scalar values, and 'file\_name' is the name of the file containing the data. The colour schemes used to derive the colours from the data can be specified with option -dataelt3dcolscheme.

Possible values: any. Default value: white.

### -dataelt3dcolscheme char\_string

[Option]

Set the colour scheme used to get colours from the data of the 3D elements loaded with option -dataelt3dcol. The type of colour scheme depends on the type of data. For crystal orientations, the colour scheme can be: 'R' for Rodrigues vector colouring; for scalar data, the colour scheme can be any list of colours.

Possible values: "R" for crystal orientations and any list of colours for scalars. Default value: "R" for crystal orientations and "blue, cyan, yellow, red" for scalars.

#### -dataelt3dscale char\_string

Option

Set the scale relative to the '-dataelt3dcol scal' data. Provide as argument the start and end values, combined with ':'. To specify the intermediate values, provide as argument the start value, the intermediate values and then the end value, combined with ':'. The labels of the scale follow the format used for the start value.

Possible values: any. Default value: data minimum:data maximum.

### -dataelt3dscaletitle char\_string

[Option]

Set the title of the scale relative to the '-dataelt3dcol scal' data.

Possible values: any. Default value: none.

#### -dataelt3dedgerad real

[Option]

Set the radius of the edges of the 3D elements.

Possible values: any. Default value: mesh dependent.

## -dataelt3dedgecol char\_string

[Option]

Set the colour of the edges of the 3D elements. Provide as argument the name of a colour that will be used for all elements (see Section A.10 [Colours], page 68).

Possible values: any. Default value: black.

The following options enable to load data relative to the 2D elements. Note that the options can be applied to element sets by changing 'elt' to 'elset'.

### -dataelt2dcol char\_string

[Option]

Set the colours of the 2D elements. See option -dataelt3dcol for the argument format. Possible values: any. Default value: white.

## -dataelt2dcolscheme char\_string

[Option]

Set the colour scheme used to get colours from the data of the 2D elements loaded with option -dataelt2dcol. See option -dataelt3dcolscheme for the argument format.

Possible values: see option -dataelt3dcolscheme. Default value: see option -dataelt3dcolscheme.

## -dataelt2dscale char\_string

[Option]

Set the scale relative to the '-dataelt2dcol scal' data. Provide as argument the start and end values, combined with ':'. To specify the intermediate values, provide as argument the start value, the intermediate values and then the end value, combined with ':'. The labels of the scale follow the format used for the start value.

Possible values: any. Default value: data minimum:data maximum.

### -dataelt2dscaletitle char\_string

[Option]

Set the title of the scale relative to the '-dataelt2dcol scal' data.

Possible values: any. Default value: none.

## -dataelt2dedgerad real

[Option]

Set the radius of the edges of the 2D elements.

Possible values: any. Default value: mesh dependent.

### -dataelt2dedgecol char\_string

[Option]

Set the colours of the edges of the 3D elements. See option -dataelt3dedgecol for the argument format.

Possible values: any. Default value: black.

The following options enable to load data relative to the 1D elements. Note that the options can be applied to element sets by changing 'elt' to 'elset'.

## -dataelt1dcol char\_string

[Option]

Set the colours of the 1D elements. See option -dataelt3dcol for the argument format. Possible values: any. Default value: black.

### -dataelt1dcolscheme char\_string

[Option]

Set the colour scheme used to get colours from the data of the 1D elements loaded with option -dataelt1dcol. See option -dataelt3dcolscheme for the argument format.

Possible values: see option -dataelt3dcolscheme. Default value: see option -dataelt3dcolscheme.

#### -dataelt1dscale char\_string

[Option]

Set the scale relative to the '-dataelt1dcol scal' data. Provide as argument the start and end values, combined with ':'. To specify the intermediate values, provide as argument the start value, the intermediate values and then the end value, combined with ':'. The labels of the scale follow the format used for the start value.

Possible values: any. Default value: data minimum:data maximum.

#### -dataelt1dscaletitle char\_string

[Option]

Set the title of the scale relative to the '-dataelt1dcol scal' data.

Possible values: any. Default value: none.

## -dataelt1drad char\_string

[Option]

Set the radius of the 1D elements.

Possible values: any. Default value: mesh dependent.

The following options enable to load data relative to the 0D mesh elements. Note that the options can be applied to element sets by changing 'elt' to 'elset'.

## -dataeltOdcol char\_string

[Option]

Set the colours of the 0D elements. See option -dataelt3dcol for the argument format. Possible values: any. Default value: black.

#### -dataeltOdcolscheme char\_string

[Option]

Set the colour scheme used to get colours from the data of the 0D elements loaded with option -dataelt0dcol. See option -dataelt3dcolscheme for the argument format.

Possible values: see option -dataelt3dcolscheme. Default value: see option -dataelt3dcolscheme.

## -dataeltOdscale char\_string

[Option]

Set the scale relative to the '-dataelt0dcol scal' data. Provide as argument the start and end values, combined with ':'. To specify the intermediate values, provide as argument the start value, the intermediate values and then the end value, combined with ':'. The labels of the scale follow the format used for the start value.

Possible values: any. Default value: data minimum:data maximum.

## -dataelt0dscaletitle char\_string

[Option]

Set the title of the scale relative to the '-dataelt0dcol scal' data.

Possible values: any. Default value: none.

### -dataelt0drad char\_string

[Option]

Set the radius of the 0D elements.

Possible values: any. Default value: mesh dependent.

The following options enable to load data relative to the nodes.

## -datanodecoo char\_string

[Option]

Set the coordinates of the nodes. The argument can be the name of a file containing a list of coordinates, or a string indicating how the coordinates can be obtained. The string has the format 'var:file\_name', where var can be 'disp' for displacements, and file\_name is the name of the file containing the data.

Possible values: any. Default value: none.

#### -datanodecoofact real

[Option]

Set the value of the scaling factor to apply to the displacements of the nodes.

Possible values: any. Default value: 1.

## -datanoderad file\_name

[Option]

Set the radius of the nodes.

Possible values: any. Default value: mesh dependent.

#### -datanodecol file\_name

[Option]

Set the colours of the nodes. See option -dataelt3dcol for the argument format.

Possible values: any. Default value: black.

### -datanodecolscheme char\_string

[Option]

Set the colour scheme used to get colours from the data of the nodes loaded with option -datanodecol. See option -dataelt3dcolscheme for the argument format.

Possible values: see option -dataelt3dcolscheme. Default value: see option -dataelt3dcolscheme.

## -datanodescale char\_string

[Option]

Set the scale relative to the '-datanodecol scal' data. Provide as argument the start and end values, combined with ':'. To specify the intermediate values, provide as argument the start value, the intermediate values and then the end value, combined with ':'. The labels of the scale follow the format used for the start value.

Possible values: any. Default value: data minimum:data maximum.

## -datanodescaletitle char\_string

[Option]

Set the title of the scale relative to the '-datanodecol scal' data.

Possible values: any. Default value: none.

## 4.1.5 Point Data Loading and Rendering

The following options enable to define the properties (colour, shape, size, etc.) of points loaded as input. This can be done either directly, by specifying the property values (e.g. the RGB channel values for colour) or indirectly, e.g. using scalar values that are rendered in colour using a given *colour scheme*. In this case, a scale image is generated in addition to the image. The scale properties can be set up (start and end values, tick values).

### -datapointcoo char\_string

[Option]

Set the coordinates of the points. The argument can be the name of a file containing a list of coordinates, or a string indicating how the coordinates can be obtained. The string has the format 'var:file\_name', where var can be 'disp' for displacements, and file\_name is the name of the file containing the data.

Possible values: any. Default value: none.

#### -datapointcoofact real

[Option]

Set the value of the scaling factor to apply to the displacements of the points.

Possible values: any. Default value: 1.

#### -datapointrad char\_string

[Option]

Set the radius (and shape) of the points. The argument can be a value that applies to all points, a file containing a list of radii, or a string indicating how the radii can be obtained. The string has the format 'var:file\_name', where var stands for the morphology of the points and file\_name is the name of the file containing the morphology parameters. For cube shape, var must be 'cube' and the file must contain, for each point, the radius (half of the edge length) and then the coordinates of the three axes (which also is the rotation matrix that brings the reference axes into coincidence with the cube axes). For cylinder shape, var must be 'cyl' and the file must contain, for each point, the radius, the length, and then the coordinates of the axis. For arrow shape, var must be 'arr' and the file must contain, for each point, the radius, the length, and then the coordinates of the axis. For disc (2D) shape, var must be 'disc' and the file must contain, for each point, the radius, then the coordinates of the axis. For ellipsoidal shape, var must be 'ell' and the file must contain, for each point, the three radii then the coordinates of the three axes. For torus shape, var must be 'tor' and the file must contain, for each point, the major radius (centre to centre line), the minor radius, and then the coordinates of the normal axis. The last capability is very specific: if the points are plotted in Rodrigues space, appending ':rodrigues' to the option argument enables to account for space distortion.

Possible values: any. Default value: point set dependent.

## -datapointcol char\_string

[Option]

Set the colours of the points. The argument can be one of the following: (i) 'id' for the default colour palette (see Section A.10 [Colours], page 68), (ii) the name of a colour that will be used for all points (see Section A.10 [Colours], page 68), (iii) the name of a file containing a list of colours (provided as RGB channel values) or (iv) a string indicating how the colours can be obtained,. In case (iv), the string has the format 'var:file\_name', where var can be 'id' for identifiers, 'ori' for crystal orientations or 'scal' for scalar values, and 'file\_name' is the name of the file containing the data. The colour schemes used to derive the colours from the data can be specified with option -datapointcolscheme.

Possible values: any. Default value: grey.

## -datapointcolscheme char\_string

[Option]

Set the colour scheme used to get colours from the data of the points loaded with option <code>-datapoint</code>. The type of colour scheme depends on the type of data. For crystal orientations, the colour scheme can be: 'R' for Rodrigues vector colouring; for scalar data, the colour scheme can be any list of colours.

Possible values: "R" for crystal orientations and any list of colours for scalars.

Default value: "R" for crystal orientations and "blue, cyan, yellow, red" for scalars.

### -datapointtrs real

[Option]

Set the transparency of the points. Provide as argument a value that applies to all points or 'file(file\_name)' to load values from a file.

Possible values: 0 to 1. Default value: 0.

### -datapointscale char\_string

[Option]

Set the scale relative to the '-datapointcol scal' data. Provide as argument the start and end values, combined with ':'. To specify the intermediate values, provide as argument the start value, the intermediate values, and then the end value, combined with ':'. The labels of the scale follow the format used for the start value.

Possible values: any. Default value: data minimum:data maximum.

## -datapointscaletitle char\_string

[Option]

Set the title of the scale relative to the '-datapointcol scal' data.

Possible values: any. Default value: none.

## 4.1.6 Coordinate System Rendering

## -datacsyscoo char\_string

[Option]

Set the coordinates of the origin of the coordinate system. Combine the coordinates with ':'. Possible values: any. Default value: 0:0:0.

#### -datacsyslength real

[Option]

Set the length of the coordinate system axes.

Possible values: any. Default value: 0.2.

## -datacsysrad real

[Option]

Set the radius of the coordinate system axes.

Possible values: any. Default value: 0.01.

#### -datacsyslabel char\_string

[Option]

Set the labels of the coordinate system axes. Combine the labels with ':'.

Possible values: any. Default value: X1:X2:X3.

### -datacsyscol char\_string

[Option]

Set the colour of the coordinate system. Provide as argument any colour as detailed in Section A.10 [Colours], page 68.

Possible values: any. Default value: 32|32|32.

## 4.1.7 Slice Settings

### -slicemesh char\_string

[Option]

plot one (or several) slice(s) of the mesh. Provide as argument the equation(s) of the plane(s), under the form 'a\*x+b\*y+c\*z=d' or any equivalent mathematical expression. Combine with ','.

Possible values: any. Default value: none.

## 4.1.8 Show Settings

The following options apply to the full tessellations or mesh.

## -showtess logical

[Option]

Show or hide the tessellation.

Possible values: 0 or 1. Default value: 1 if tess loaded and no mesh.

## -showtesr logical

[Option]

Show or hide the raster tessellation.

Possible values: 0 or 1. Default value: 1 if tesr loaded and no mesh.

#### -showmesh logical

[Option]

Show or hide the mesh.

Possible values: 0 or 1. Default value: 1 if mesh loaded and no slice.

## -showmeshslice logical

[Option]

Show or hide the mesh slice(s).

Possible values: 0 or 1. Default value: 1 if existing slice(s).

## -showpoint logical or char\_string

[Option]

Show or hide the points. To show only specific points, provide 'file(file\_name)' to load point numbers from a file.

Possible values: any. Default value: none.

The following option applies to the cells of a tessellation or a raster tessellation, independently of its dimension,

#### -showcell char\_string

[Option]

Specify the cells to show. The argument can be: 'all' for all, 'none' for none, 'file(file\_name)' to load polyhedron identifiers from a file, or any expression based on the keys listed in Section A.2 [Tessellation Keys], page 61, or Section A.3 [Raster Tessellation Keys], page 63.

Possible values: any. Default value: all.

For a tessellation, it is also possible to set visibility on a per-entity basis,

#### -showpoly char\_string

[Option]

Specify the polyhedra to show. The argument can be: 'all' for all, 'none' for none, 'file(file\_name)' to load polyhedron identifiers from a file, or any expression based on the keys listed in Section A.2 [Tessellation Keys], page 61.

Possible values: any. Default value: all.

#### -showface char\_string

[Option]

Specify the faces to show. The argument can be: 'all' for all, 'none' for none, 'file(file\_name)' to load face identifiers from a file, or any expression based on the keys listed in Section A.2 [Tessellation Keys], page 61. The following specific keys are also available: 'cell\_shown' and 'poly\_shown'.

Possible values: any. Default value: none.

### -showedge char\_string

[Option]

Specify the edges to show. The argument can be: 'all' for all, 'none' for none, 'file(file\_name)' to load edge numbers from a file, or any expression based on the keys listed in Section A.2 [Tessellation Keys], page 61. The following specific keys are also available: 'cell\_shown', 'poly\_shown' and 'face\_shown'.

Possible values: any. Default value: cell\_shown.

### -showver char\_string

[Option]

Specify the vertices to show. The argument can be: 'all' for all, 'none' for none, 'file(file\_name)' to load vertex numbers from a file, or any expression based on the keys listed in Section A.2 [Tessellation Keys], page 61. The following specific keys are also available: 'cell\_shown', 'poly\_shown', 'face\_shown' and 'edge\_shown'.

Possible values: any. Default value: none.

#### -showseed char\_string

[Option]

Specify the seeds to show. The argument can be: 'all' for all, 'none' for none, 'file(file\_name)' to load seed numbers from a file, or any expression based on the keys listed in Section A.2 [Tessellation Keys], page 61. The following specific key is also available: 'cell\_shown'.

Possible values: any. Default value: none.

### -showfaceinter logical

[Secondary option]

Show the interpolations of the tessellation faces (if any). The interpolation edges are printed in grey with a radius equal to the radius of the face edges.

Possible values: 0 or 1. Default value: 0.

For a raster tessellation, it is possible to set visibility of the individual voxels,

## -showvox char\_string

[Option]

Specify the voxels to show. The argument can be: 'all' for all, 'none' for none, 'file(file\_name)' to load voxel identifiers from a file, or any expression based on the keys listed in Section A.2 [Tessellation Keys], page 61.

Possible values: any. Default value: all.

The following options apply to the entities of the mesh. The options apply to 3D elements ('elt3d') and element sets ('elset3d'), 2D elements ('elt2d') and element sets ('elset2d'), 1D elements ('elt1d') and element sets ('elset1d'), 0D elements ('elt0d') and element sets ('elset0d'), and nodes ('nodes'). Also note that the 'elt' and 'elset' labels can be used in place of 'eltnd' and 'elsetnd', where n is the highest mesh dimension. This enables to use the same command whatever the highest mesh dimension is.

In the following option descriptions, note that any options can be applied to element *sets* by changing 'elt' to 'elset'.

#### -showelt3d char\_string

[Option]

Specify the 3D elements to show. The argument can be: 'all' for all, 'none' for none, 'file(file\_name)' to load element identifiers from a file, or any expression based on the keys listed in Section A.6 [Mesh Keys], page 66.

Possible values: any. Default value: all if highest mesh dim. is 3 and none otherwise.

## -showelt2d char\_string

[Option]

Specify the 2D elements to show. The argument can be: 'all' for all, 'none' for none, 'file(file\_name)' to load element identifiers from a file, or any expression based on the keys listed in Section A.6 [Mesh Keys], page 66. The following specific key is also available: 'elt3d\_shown'.

Possible values: any. Default value: all if highest mesh dim. is 2 and none otherwise.

#### -showelt1d char\_string

[Option]

Specify the 1D elements to show. The argument can be: 'all' for all, 'none' for none, 'file(file\_name)' to load element numbers from a file, or any expression based on the keys listed in Section A.6 [Mesh Keys], page 66. The following specific keys are also available: 'elt2d\_shown' and 'elt3d\_shown'.

Possible values: any. Default value: all if highest mesh dim. is 1 and none otherwise.

#### -showelt0d char\_string

Option

Specify the 0D elements to show. The argument can be: 'all' for all 'none' for none, 'file(file\_name)' to load element numbers from a file, or any expression based on the keys listed in Section A.6 [Mesh Keys], page 66. The following specific keys are also available: 'elt1d\_shown', 'elt2d\_shown' and 'elt3d\_shown'.

Possible values: any. Default value: all if highest mesh dim. is 0 and none otherwise.

### -shownode char\_string

Option

Specify the nodes to show. The argument can be: 'all' for all, 'none' for none, 'file(file\_name)' to load node numbers from a file, or any expression based on the keys listed in Section A.6 [Mesh Keys], page 66. The following specific keys are also available: 'elt0d\_shown', 'elt1d\_shown', 'elt2d\_shown' and 'elt3d\_shown'.

Possible values: any. Default value: none.

## -showcsys logical

[Option]

Show the coordinate system.

Possible values: 0 or 1. Default value: 0.

### -showshadow logical

[Option]

Show the shadows. If you want colours not affected by shadowing, switch this option off. Possible values: 0 or 1. Default value: 1 in 3D and 0 in 2D.

### 4.1.9 Camera Settings

## -cameracoo char\_string:char\_string:char\_string

[Option]

Specify the camera coordinates. By default, the camera is shifted by length times a vector v from the centre of the bounding box of the tessellation or mesh. The variable length is the average length of the bounding box (1 for a unit cube), and the coordinates of vector v are denoted as vx, vy and vz (= 3.462, -5.770 and 4.327, respectively, in 3D, and 0, 0 and 8, respectively, in 2D). The coordinates of the tessellation or mesh centre are denoted as x, y and z (if both a tessellation and a mesh have been loaded, the mesh is considered). Provide as argument the expression for the 3 coordinates, combined with ':'.

Possible values: any. Default value: x+length\*vx:y+length\*vy:z+length\*vz.

## -cameralookat $char\_string:char\_string:char\_string$

[Option]

Specify the location the camera looks at. By default, the camera looks at the tessellation or mesh centre. The coordinates of the tessellation or mesh centre are denoted as x, y and z (if both a tessellation and a mesh have been loaded, the mesh is considered). Provide as argument the expression for the 3 coordinates, combined with ':'.

Possible values: any. Default value: x:y:z.

### -cameraangle real

[Option]

Specify the opening angle of the camera along the horizontal direction (in degrees). The opening angle along the vertical direction is determined from the opening along the horizontal direction and the image size ratio.

Possible values: any. Default value: 25.

#### -camerasky real:real:real

[Option]

Specify the sky vector of the camera (vertical direction). Provide as argument the coordinates combined with ':'.

Possible values: any. Default value: 0:0:1.

## -cameraprojection char\_string

[Option]

Specify the type of projection of the camera.

Possible values: perspective or orthographic. Default value: perspective for 3D and orthographic for 2D.

## 4.1.10 Output Image Settings

#### -imagesize int:int

[Option]

Specify the size of the image (in pixels). Provide as argument the width and height, combined with ':'.

Possible values: any. Default value: 1200:900.

### -imagebackground char\_string

[Option]

Specify the colour of the background. Provide as argument any colour as detailed in Section A.10 [Colours], page 68.

Possible values: any. Default value: white.

## -imageantialias logical

[Option]

Use antialiasing to produce a smoother image. Switch antialiasing off for faster image generation or smaller image file.

Possible values: 0 or 1. Default value: 1.

#### -imageformat char\_string

[Option]

Specify the output image format. It can be the PNG format (png) or the POV-Ray format (pov). Use 'pov:objects' to get a POV-Ray file containing only the objects<sup>1</sup>. Combine with ','.

Possible values: see above list. Default value: png.

### 4.1.11 Scripting

## -loop char\_string real real real ... -endloop

[Option]

Create a loop of commands. Provide as argument the name of the loop variable, its initial value, the loop increment value, the final value, and then the commands to execute. An example of use of the -loop / -endloop capability is provided in the Examples Section. Possible values: any. Default value: none.

## 4.1.12 Advanced Options

#### -includepov char\_string:char\_string:...

[Option]

Use this option to include additional objects to the image, under the form of a POV-Ray file. Provide as first argument the name of the POV-Ray file and as next arguments successive transformations to apply to the objects of the POV-Ray file. The

 $<sup>^{1}</sup>$  Not compatible with 'png'; the resulting file can be loaded with -includepov.

transformations can be 'translate(vx, vy, vz)' for a translation of vector (vx, vy, vz), 'scale(sx, sy, sz)' for scaling by factors sx, sy and sz in the three directions of space, and 'rotate(thetax, thetay, thetaz)' for a rotation of angles thetax, thetay and thetaz about axes x, y and  $z^2$ .

Possible values: any. Default value: none.

## 4.2 Output Files

The output files are

- PNG file, .png: a bitmapped image (the alpha channel is off).
- POV-Ray file, .pov: a POV-Ray script file.

A PNG image can be obtained from a POV-Ray file by invoquing POV-Ray as follows (see the POV-Ray documentation for details and further commands), povray file.pov +Wimage\_width +Himage\_height -D +A0.2.

## 4.3 Examples

Below are some examples of use of neper -V.

1. Print out tessellation n10-id1.tess with cells coloured from their identifiers and an image size of  $900 \times 450$  pixels.

```
$ neper -V n10-id1.tess -datacellcol id -imagesize 900:450 -print img
```

2. Print out tessellation n10-id1.tess with cells coloured from crystal orientations and semi-transparency.

```
$ neper -V n10-id1.tess -datacellcol ori -datacelltrs 0.5 -print img
```

3. Print out mesh n10-id1.msh with elements coloured from scalar values written in file v and a scale ranging from 0 to 100.

4. Print out mesh n10-id1.msh with elements coloured from nodal scalar values written in file v and a scale ranging from 0 to 100.

5. Print out the 10 first cells of a 100-cell tessellation, coloured from their identifiers and semi-transparency, and with edges shown in red and vertices shown as green spheres of radius 0.01.

<sup>&</sup>lt;sup>2</sup> The rotation is read in POV-Ray style; i.e., according to the POV-Ray documentation: Note that the order of the rotations does matter. Rotations occur about the x-axis first, then the y-axis, then the z-axis. If you are not sure if this is what you want then you should only rotate on one axis at a time using multiple rotation statements to get a correct rotation. Rotation is always performed relative to the axis. Thus if an object is some distance from the axis of rotation it will not only rotate but it will orbit about the axis as though it was swinging around on an invisible string. POV-Ray uses a left-handed rotation system. Using the famous "Computer Graphics Aerobics" exercise, you hold up your left hand and point your thumb in the positive direction of the axis of rotation. Your fingers will curl in the positive direction of rotation. Similarly if you point your thumb in the negative direction of the axis your fingers will curl in the negative direction of rotation.

6. Print out the interior element sets of mesh n100-id1.msh and show the 1D elements.

7. Print out 3 slices of mesh n100-id1.msh.

8. Print out slices of mesh n100-id1.msh, at z coordinates ranging from 0.1 to 0.9 by step of 0.1, each slice being printed in a separate file.

# Appendix A Expressions and Keys

# A.1 Mathematical and Logical Expressions

Neper can handle mathematical expressions. It makes use of the muparser library. The expression must contain no space, tabulation or new-line characters, and match the following syntax<sup>1</sup>.

#### A.1.1 Functions

The following table gives an overview of the functions supported by the default implementation. It lists the function names, the number of arguments and a brief description.

Name	Description
sin	sine function
cos	cosine function
tan	tangens function
asin	arcus sine function
acos	arcus cosine function
atan	arcus tangens function
sinh	hyperbolic sine function
cosh	hyperbolic cosine
tanh	hyperbolic tangens function
asinh	hyperbolic arcus sine function
acosh	hyperbolic arcus tangens function
atanh	hyperbolic arcur tangens function
log2	logarithm to the base 2
log10	logarithm to the base 10
log	logarithm to the base 10
ln	logarithm to base $e(2.71828)$
exp	e raised to the power of x
sqrt	square root of a value
sign	sign function: -1 if $x < 0$ ; 1 if $x > 0$
rint	round to nearest integer
abs	absolute value
min	min of all arguments
max	max of all arguments
sum	sum of all arguments
avg	mean value of all arguments

## A.1.2 Binary Operators

The following table lists the default binary operators supported by the parser.

Operator	Description	Priority
&&	logical and	1
11	logical or	2
<=	less or equal	4
>=	greater or equal	4
! =	not equal	4
==	equal	4

Taken from the muparser documentation, see http://beltoforion.de/article.php?a=muparser for more information.

>	greater than	4
<	less than	4
+	addition	5
_	subtraction	5
*	multiplication	6
/	division	6
^	raise x to the power of y	7

## A.1.3 Ternary Operators

The parser has built in support for the if-then-else operator. It uses lazy evaluation in order to make sure only the necessary branch of the expression is evaluated.

Operator	Description
?:	if-then-else operator, following the $C/C++$ syntax:
	<pre>(test)?value_if_true:value_if_false.</pre>

### A.1.4 Statistical Distributions

The following table lists the statistical distributions. Arguments enclosed in square brackets ('[' and ']') are optional. Custom endpoints (not indicated) can also be added as arguments, as described in the following.

Operator	Description	Information
normal(mean, sigma)	normal	
lognormal(mean, sigma)	lognormal	
dirac(mean)	Dirac	
beta(x,y)	beta function	x > 0, y > 0
lorentzian(mean, sigma)	Lorentzian	
studentst(mean, sigma)	Student's t	
weibull(k, sigma)	Weibull	k > 0 represents the shape
<pre>breitwigner(mean, sigma[, gamma])</pre>	Breit-Wigner	$gamma \ge 0$ , default 1
<pre>expnormal(mean, sigma[, gamma])</pre>	exp-normal	gamma > 0 default $sigma$
<pre>moffat(mean, sigma[, gamma])</pre>	Moffat	gamma > 0, default 1
<pre>pearson7(mean,sigma[,gamma])</pre>	Pearson type VII	default $gamma = 1.5$
<pre>pseudovoigt(mean, sigma[, gamma])</pre>	Pseudo-Voigt	$gamma \in [0, 1]$ , default 0.5
<pre>skewnormal(mean, sigma[, gamma])</pre>	skewed normal	default $gamma = sigma$

'mean' represents the mean (or centre), and 'sigma' (> 0) represents the standard deviation (or scale). 'gamma' depends on the distribution function (see the above table). For all distributions, custom endpoints can be added as last arguments, 'from, to', where 'from' is the lower end point and 'to' is the upper endpoint. If the parameter keywords are used, the parameters can be given in any order; e.g., 'moffat(gamma=1,from=0,to=1,sigma=0.1,mean=0.5)'. Otherwise, the parameters are read based on their positions; e.g., 'lognormal(0.25,0.01)' yields mean = 0.25 and sigma = 0.01. It is also possible (but not recommended) to specify some variables by keyword and let others be read by position. Endpoints are considered inclusive by default, but exclusive endpoints can be specified using 'fromexclusive=from' and 'toexclusive=to' ('frominclusive=from' and 'toinclusive=to' can be used for inclusive endpoints). String completion is available for the keywords. Finally, a sum of distributions of increasing averages can be provided; e.g., '0.3\*lognormal(0.5,0.1)+0.7\*normal(1,0.1)'.

## A.2 Tessellation Keys

Available keys for tessellation seeds, vertices, edges, faces and polyhedra are provided below. Also note that the descriptors apply to *cells* if they are tagged to apply to *polyhedra* and the tessellation is 3D and *faces* and the tessellation is 2D.

To turn a key value into a value relative to the mean over all entities (e.g. the relative cell size), append the key expression with the ':rel' modifier. To turn a key value into a value which holds for a unit cell size, append the key expression with the ':uc' modifier. To use as a reference only the body or true entities (see below), append 'b' or 't' to the modifiers, respectively.

Key	Descriptor	Apply to
id	identifier	seed, ver, edge, face, poly
X	x coordinate	seed, ver, edge, face, poly
У	y coordinate	seed, ver, edge, face, poly
Z	z coordinate	seed, ver, edge, face, poly
xmin	minimum x coordinate	edge, face, poly
ymin	minimum y coordinate	edge, face, poly
zmin	minimum z coordinate	edge, face, poly
xmax	maximum x coordinate	edge, face, poly
ymax	maximum y coordinate	edge, face, poly
zmax	maximum z coordinate	edge, face, poly
W	weight (width for a lamella tessellation)	seed, cell
true	true level	ver, edge, face, poly
body	body level	ver, edge, face, poly
state	state	ver, edge, face, poly
domtype	type of domain (0 if on a domain vertex, 1	ver, edge, face
	if on a domain edge and 2 if on a domain	
	face)	
domface	domain face (-1 if undefined)	face
domedge	domain edge (-1 if undefined)	edge
domver	domain vertex (-1 if undefined)	ver
scale	scale	$face^2$
length	length	edge
area	area	face, poly
vol	volume	poly
size	size (area/volume in 2D/3D)	cell
diameq	equivalent diameter <sup>3</sup>	face, poly
radeq	equivalent radius <sup>4</sup>	face, poly
circularity	circularity (2D counterpart of sphericity)	face
sphericity	sphericity <sup>5</sup>	poly
convexity	convexity <sup>6</sup>	face <sup>7</sup> , poly
dihangleav	average dihedral angle	face, poly

<sup>&</sup>lt;sup>2</sup> Applies only to a 3D tessellation and relevant for multiscale tessellations. The scale of a face is the scale at which the face was created, and it ranges from 0 (for domain faces) to the number of scales of the tessellation (for the last created faces).

<sup>&</sup>lt;sup>3</sup> Equivalent diameter = diameter of the circle of equivalent area/volume in 2D/3D.

<sup>&</sup>lt;sup>4</sup> Equivalent radius = radius of the circle of equivalent area/volume in 2D/3D.

<sup>&</sup>lt;sup>5</sup> Sphericity of a polyhedron = ratio of the surface area of the sphere of equivalent volume to the surface area of the polyhedron.

<sup>&</sup>lt;sup>6</sup> Convexity of a polyhedron (face) = ratio of the volume (area) of the polyhedron (face) to the volume (area) of the convex hull of the polyhedron (face).

Applies only to a 2D tessellation.

foco poly

minimum dihadral angla

dihanglemin	minimum dihedral angle	face, poly
dihanglemax	maximum dihedral angle	face, poly
dihangles	dihedral angles	face, poly
ff	flatness fault (in degrees)	face
theta	disorientation angle (in degrees)	edge (in 2D), face (in 3D)
cyl	whether or not is used to describe the cir-	edge
	cular part of a cylinder domain	
vernb	number of vertices	edge, face, poly
vers	vertices	edge, face, poly
edgenb	number of edges	ver, face, poly
edges	edges	ver, face, poly
facenb	number of faces	ver, edge, poly
faces	faces	ver, edge, poly
polynb	number of polyhedra	ver, edge, face
polys	polyhedra	ver, edge, face
nfacenb	number of neighbouring faces	face
nfaces	neighbouring faces	face
npolynb	number of neighbouring polyhedra	poly
npolys	neighbouring polyhedra	poly
nseednb	number of neighbouring seeds	poly
nseeds	neighbouring seeds <sup>8</sup>	poly
vercoos	vertex coordinates	face, poly
faceareas	face surface areas	poly
faceeqs	face equations <sup>9</sup>	poly
scaleid(scale)	identifier of the corresponding cell at scale	cell
	scale	
lamid	lamella width $id^{10}$	face, poly
modeid	$mode id^{11}$	face, poly
е	Euler angles (Bunge convention)	seed, face (in 2D), poly
**		

Variables consisting of several values ('vers', etc.) are not available for sorting (option -sort). For a cell, the body and true variables are defined as follows,

- body is an integer equal to 0 if the cell is at the domain boundary, i.e. if it shares at least one face with it (edge in 2D), and is equal to 1 or higher otherwise. This is determined as follows: if a cell is surrounded by cells with body values equal to or higher than n, its body value is equal to n + 1. Therefore, body tends to increase with the distance to the domain boundary and can be used to define cells that may suffer from boundary effects.
- true is an integer equal to 0 it the cell shape is biased by the domain boundary, and is equal to 1 or higher otherwise. A value higher than 0 is achieved if and only if any seed that would have been located outside the domain (where it could not be) would not have affected the shape of the cell. This condition is fulfilled if the distance between the seed of the cell and any of its vertices is lower than the minimum distance between a vertex of the cell and the domain boundary. true is extended to values higher than 1 in the same way as body: if a cell is surrounded by cells with true values equal to or higher than n, its true value is equal to n + 1. As body, true tends to increase with the distance to the domain

 $<sup>^{8}\,</sup>$  If a polyhedron has no neighbour on a face, a negative value is returned.

<sup>&</sup>lt;sup>9</sup> A face equation is specified by the parameters d, a, b and c, with the equation being: ax + by + cz = d. The vector (a, b, c) is pointing outwards of the polyhedron.

<sup>&</sup>lt;sup>10</sup> In the case of a lamellar tessellation with several lamella widths, *lamid* stands for the actual lamellar width of the cell (starting from 1).

In the case of a multimodal tessellation (e.g. in terms of cell size), modeid stands for the actual mode (starting from 1).

boundary, and  $true \leq body$ . true is especially useful for statistics on the cells (morphology, mesh, etc.), for which only cells with  $true \geq 1$  should be considered.

For entities of lower dimension than cells (vertices, edges and faces), body and true are equal to the maximum body or true values of the cells they belong to.

## A.3 Raster Tessellation Keys

Available keys for raster tessellation seeds and cells are provided below. Mathematical and logical expressions based on these keys can also be used. To turn a key value into a value relative to the mean over all entities (e.g. the relative cell size), append the key expression with the ':rel' modifier. To turn a key value into a value which holds for a unit cell size, append the key expression with the ':uc' modifier.

Key	Descriptor	Apply to
id	identifier	seed, cell, voxel
x	x coordinate	seed, cell, voxel
у	y coordinate	seed, cell, voxel
z	z coordinate	seed, cell, voxel
xyz	x, y and z coordinates	seed, cell, voxel
VX	x coordinate (in voxel)	voxel
vy	y coordinate (in voxel)	voxel
VZ	z coordinate (in voxel)	voxel
vxyz	x, y and z coordinates (in voxel)	voxel
е	Euler angles (Bunge convention)	cell, voxel
cell	cell	voxel
W	Laguerre weight	seed
size	size (area/volume in 2D/3D)	cell
diameq	equivalent diameter <sup>12</sup>	cell
radeq	equivalent radius <sup>13</sup>	cell
convexity	$convexity^{14}$	cell
voxsizex	Voxel size in direction x	general
voxsizey	Voxel size in direction y	general
voxsizez	Voxel size in direction z	general
domsizex	Domain size in direction x	general
domsizey	Domain size in direction y	general
domsizez	Domain size in direction z	general

# A.4 Tessellation Optimization Keys

## A.4.1 Time Keys

The available keys for option -morphooptilogtime are provided below. Use 'iter(factor)', where 'factor' is an integer reduction factor, to log values only at specific iteration numbers.

Key	Descriptor
iter	iteration number
varupdateqty	number of updated variables
seedupdateqty	number of updated seeds

 $<sup>^{12}\,</sup>$  Equivalent diameter = diameter of the circle of equivalent area/volume in 2D/3D.

 $<sup>^{13}</sup>$  Equivalent radius = radius of the circle of equivalent area/volume in 2D/3D.

<sup>&</sup>lt;sup>14</sup> Convexity of a cell = ratio of the volume of the cell to the volume of the convex hull of the cell.

seedupdatelist	list of updated seeds
cellupdateqty	number of updated cells
cellupdatelist	list of updated cells
var	time for variable update
seed	time for seed update
cell_init	time for cell update initialization
cell_kdtree	time for cell update kdtree computation
cell_shift	time for cell update shift computation
cell_neigh	time for cell update neigh. computation
cell_cell	time for cell update cell computation
cell_other	time for cell update others
cell_total	total time for cell update
val	time for (objective function) value update
val_init	time for (objective function) value update / initialization
val_penalty	time for (objective function) value update / penalty computation
val_val	time for (objective function) value update / value computation
val_val_	time for (objective function) value update / value computation / cell values
cellval	
val_val_comp	time for (objective function) value update / value computation /
	computation
val_comp	time for (objective function) value update / computation
total	total time
cumtotal	cumulative total time

## A.4.2 Variable Keys

The available keys for option -morphooptilogvar are provided below. Use 'iter(factor)', where 'factor' is an integer reduction factor, to log values only at specific iteration numbers.

Key	Descriptor	Apply to
iter	iteration number	n/a
id	identifier	seed
x	x coordinate	seed
У	y coordinate	$\operatorname{seed}$
z	z coordinate	seed
W	weight	$\operatorname{seed}$

# A.4.3 Objective Function Value Keys

The available keys for option -morphooptilogval are provided below. Use 'iter(factor)', where 'factor' is an integer reduction factor, to log values only at specific iteration numbers.

Key	Descriptor	Apply to
iter	iteration number	n/a
val	value	n/a
valmin	minimal value	n/a
val0	value, without smoothing	n/a
valmin0	minimal value, without smoothing	n/a
val(i)	ith subvalue	n/a
valO(i)	ith subvalue, without smoothing	n/a
eps	error on the objective function (see option	n/a
	-morphooptistop)	

reps	relative error on the objective function (see	n/a
	option -morphooptistop)	
loop	optimization loop	n/a
plateaulength	current plateau length $^{15}$	n/a

## A.4.4 Statistical Distribution Keys

The available keys for option -morphooptilogdis are provided below. PDF stands for probability density function and CDF stands for cumulative probability density function. Use 'iter(factor)', where 'factor' is a reduction factor, to log values only at specific iteration numbers.

Key	Descriptor	Apply to
iter	iteration number	n/a
x	x coordinate	n/a
tarpdf	target PDF	n/a
tarcdf	target CDF	n/a
curpdf	current PDF	n/a
curcdf	current CDF	n/a
tarpdf0	target PDF, not smoothed	n/a
tarcdf0	target CDF, not smoothed	n/a
curcdf0	current CDF, not smoothed	n/a

## A.4.5 Raster Tessellation Voxel Keys

The available keys for option -morphooptilogtesr are provided below. Values are written for each voxel used to compute the objective function. Use 'iter(factor)', where 'factor' is a reduction factor, to log values only at specific iteration numbers.

Key	Descriptor	Apply to
iter	iteration number	n/a
id	cell identifier	n/a
x	x coordinate	n/a
У	y coordinate	n/a
z	z coordinate	n/a
dist	distance to the cell	n/a

## A.5 Orientation Optimization Keys

## A.5.1 Variable Keys

The available keys for option -orioptilogvar are provided below. For all orientation descriptors but 'q', the returned orientation are located in the fundamental region.

Key	Descriptor	Apply to
iter	iteration number	n/a
id	identifier	seed
g	rotation matrix	seed
rtheta	rotation axis / angle pair	seed
R	Rodrigues vector	seed
q	quaternion	seed

 $<sup>^{15}</sup>$  Number of iterations during which the objective function did not decrease.

е	Euler angles (Bunge convention)	seed
ek	Euler angles (Kocks convention)	seed
er	Euler angles (Roe convention)	seed

# A.6 Mesh Keys

Available keys for mesh node, elements and element sets (of all dimensions) and points are provided below.

Key	Descriptor	Apply to
id	identifier	node, $nD$ elt, $nD$ elset
x	x coordinate	node, $nD$ elt, $nD$ elset
У	y coordinate	node, $nD$ elt, $nD$ elset
z	z coordinate	node, $nD$ elt, $nD$ elset
dim	dimension (= lowest parent elt dimension)	node
elset0d	0D elset	0D elt
elset1d	1D elset	1D elt
elset2d	2D elset	2D elt
elset3d	3D elset	3D elt
part	partition	nD elt, node
cyl	whether or not is used to describe the cir- cular part of a cylinder domain	1D elt, 1D elset
vol	volume	3D elt, 3D elset
area	area	2D elt
length	length	1D elt, 3D elt, 1D elset
elsetvol	elset volume	3D elt
elsetarea	elset area	2D elt
elsetlength	elset length	1D elt
rr	radius ratio	3D elt
rrav, rrmin,	average, min and max radius ratios	3D elset
rrmax		aD 1
Osize	Osize	3D elset
eltnb	number of elements	nD elset
true	true level	nD elt, nD elset
body	body level	nD elt, nD elset
domtype	type of domain (0 if on a domain vertex, 1	2D elset, 1D elset, 0D elset,
	if on a domain edge and 2 if on a domain face)	2D elt, 1D elt, 0D elt
2dmeshp	coordinates of the closest point of the 2D mesh	node, 3D elt
2dmeshd	distance to '2dmeshp'	node, 3D elt
2dmeshv	vector to '2dmeshp'	node, 3D elt
2dmeshn	outgoing normal vector of the 2D mesh at '2dmeshp'	node, 3D elt
е	Euler angles (Bunge convention)	2D elt, 3D elt, 2D elset, 3D elset
nD stands for an a		
nD stands for an arbitrary dimension (from 0D to 3D). Variables starting by '2dmesh' are only		

available for statistics (options starting by -stat of module -M); for elements, they apply to the

# A.7 Point Keys

centroids.

Available keys for points are provided below.

Key	Descriptor	Apply to	Require
id	identifier	point	
X	x coordinate	$\operatorname{point}$	
у	y coordinate	$\operatorname{point}$	
Z	z coordinate	$\operatorname{point}$	
cell	cell	$\operatorname{point}$	tessellation
elt	containing element	$\operatorname{point}$	mesh
elset	containing elset	$\operatorname{point}$	mesh
2dmeshp	coordinates of the closest point of the 2D	$\operatorname{point}$	3D mesh
	mesh		
2dmeshd	distance to '2dmeshp'	point	3D mesh
2dmeshv	vector to '2dmeshp'	point	3D mesh
2dmeshn	outgoing normal vector of the 2D mesh at	point	3D mesh
	'2dmeshp'		

# A.8 Rotations and Orientations

Rotations and orientations can be described using the following descriptors (see Orilib, http://orilib.sourceforge.net, for more information).

Key	Descriptor	Number of variables
g	rotation matrix	9
rtheta	rotation axis / angle pair	4
R	Rodrigues vector	3
q	quaternion	4
е	Euler angles (Bunge convention)	3
ek	Euler angles (Kocks convention)	3
er	Euler angles (Roe convention)	3

Keys are available for ideal orientations:

Cube	(001)[100]
Goss	(011)[100]
U	$(101)[\bar{1}01]$
45NDCube	$(001)[1\bar{1}0]$
S1	$(123)[63\bar{4}]$
S2	$(\bar{1}23)[6\bar{3}4]$
S3	$(1\bar{2}3)[6\bar{3}\bar{4}]$
S4	$(\bar{1}\bar{2}3)[634]$
Brass1	$(110)[1\bar{1}2]$
Brass2	$(\bar{1}10)[11\bar{2}]$
Copper1	$(112)[11\bar{1}]$
Copper2	$(\bar{1}12)[1\bar{1}1]$

# A.9 Crystal Symmetries

Crystal symmetries can be described using the following descriptors.

Key	Descriptor	Number of operators
triclinic	triclinic (Laue group $\overline{1}$ )	24
cubic	cubic	24

hexagonal	hexagonal	1
-1	Laue group $\overline{1}$	1
2/m	Laue group $2/m$	2
mmm	Laue group mmm	4
4/m	Laue group $4/m$	4
4/mmm	Laue group $4/mmm$	8
-3	Laue group $\overline{3}$	3
-3m	Laue group $\overline{3}m$	6
6/m	Laue group $6/m$	6
6/mmm	Laue group $6/mmm$	12
m-3	Laue group $m\overline{3}$	12
m-3m	Laue group $m\overline{3}m$	24

Keys are available for ideal orientations:

Cube Goss U 45NDCube S1 S2 S3 S4 Brass1 Brass2	$ \begin{array}{c} (001)[100] \\ (011)[100] \\ (101)[\bar{1}01] \\ (001)[1\bar{1}0] \\ (123)[63\bar{4}] \\ (\bar{1}23)[6\bar{3}4] \\ (1\bar{2}3)[6\bar{3}\bar{4}] \\ (\bar{1}\bar{2}3)[6\bar{3}4] \\ (\bar{1}\bar{2}3)[6\bar{3}4] \\ (\bar{1}\bar{1}0)[1\bar{1}2] \\ (\bar{1}10)[1\bar{1}2] \\ (\bar{1}10)[11\bar{2}] \end{array} $
210001	, , ,

# A.10 Colours

The available colours are provided below, with their corresponding RGB channel values. Any other colour can be defined from the RGB channel values, under format  $`R\_value|G\_value|B\_value"$ .

( 0,  0,  0)	black	(255, 0, 0)	red
(0, 255, 0)	green	(0, 0, 255)	blue
(255, 255, 0)	yellow	(255, 0, 255)	magenta
(0, 255, 255)	cyan	(255, 255, 255)	white
(128, 0, 0)	maroon	(0, 0, 128)	navy
(127, 255, 0)	chartreuse	(0, 255, 127)	springgreen
(128, 128, 0)	olive	(128, 0, 128)	purple
(0, 128, 128)	teal	(128, 128, 128)	grey
(0, 191, 255)	deepskyblue	(124, 252, 0)	lawngreen
(64, 64, 64)	darkgrey	(255, 69, 0)	orangered
(192, 192, 192)	silver	(255, 250, 250)	snow
(139, 0, 0)	darkred	(0, 0, 139)	darkblue
(255, 140, 0)	darkorange	(240, 255, 255)	azure
(248, 248, 255)	ghostwhite	(255, 255, 240)	ivory
(0, 0, 205)	mediumblue	(255, 182, 193)	lightpink
(245, 255, 250)	mintcream	(75, 0, 130)	indigo
(240, 128, 128)	lightcoral	(255, 192, 203)	pink
(255, 127, 80)	coral	(250, 128, 114)	salmon
(255, 250, 240)	floralwhite	(127, 255, 212)	aquamarine

(255, 250, 205)	lemonchiffon	(255, 215, 0)	gold
(0, 100, 0)	darkgreen	(255, 165, 0)	orange
(240, 248, 255)	aliceblue	(224, 255, 255)	lightcyan
(255, 255, 224)	lightyellow	(139, 0, 139)	darkmagenta
(0, 139, 139)	darkcyan	(205, 133, 63)	peru
(70, 130, 180)	steelblue	(255, 240, 245)	lavenderblush
(255, 245, 238)	seashell	(0, 250, 154)	mediumspringgreen
(72, 61, 139)	darkslateblue	(184, 134, 11)	darkgoldenrod
(255, 160, 122)	lightsalmon	(255, 228, 196)	bisque
(135, 206, 250)	lightskyblue	(250, 250, 210)	lightgoldenrodyellow
(240, 255, 240)	honeydew	(255, 248, 220)	cornsilk
(255, 218, 185)	peachpuff	(245, 245, 245)	whitesmoke
(255, 99, 71)	tomato	(112, 128, 144)	slategrey
(255, 105, 180)	hotpink	(253, 245, 230)	oldlace
(255, 235, 205)	blanchedalmond	(189, 183, 107)	darkkhaki
(255, 228, 181)	moccasin	(0, 206, 209)	darkturquoise
(60, 179, 113)	mediumseagreen	(199, 21, 133)	mediumvioletred
(238, 130, 238)	violet	(173, 255, 47)	greenyellow
(255, 239, 213)	papayawhip	(143, 188, 143)	darkseagreen
(188, 143, 143)	rosybrown	(255, 20, 147)	deeppink
(139, 69, 19)	saddlebrown	(148, 0, 211)	darkviolet
(30, 144, 255)	dodgerblue	(119, 136, 153)	lightslategrey
(222, 184, 135)	burlywood	(255, 222, 173)	navajowhite
(250, 240, 230)	linen	(123, 104, 238)	mediumslateblue
(64, 224, 208)	turquoise	(135, 206, 235)	skyblue
(72, 209, 204)	mediumturquoise	(245, 245, 220)	beige
(255, 228, 225)	mistyrose	(210, 180, 140)	tan
(250, 235, 215)	antiquewhite	(216, 191, 216)	thistle
(50, 205, 50)	limegreen	(233, 150, 122)	darksalmon
(176, 196, 222)	lightsteelblue	(65, 105, 225)	royalblue
(152, 251, 152)	palegreen	(220, 20, 60)	crimson
(245, 222, 179)	wheat	(186, 85, 211)	mediumorchid
(230, 230, 250)	lavender	(240, 230, 140)	khaki
(144, 238, 144)	lightgreen	(175, 238, 238)	paleturquoise
(47, 79, 79)	darkslategrey	(153, 50, 204)	darkorchid
(46, 139, 87)	seagreen	(154, 205, 50)	yellowgreen
(138, 43, 226)	blueviolet	(219, 112, 147)	palevioletred
(107, 142, 35)	olivedrab	(147, 112, 219)	mediumpurple
(244, 164, 96)	sandybrown	(85, 107, 47)	darkolivegreen
(102, 205, 170)	mediumaquamarine	(106, 90, 205)	slateblue
(238, 232, 170)	palegoldenrod	(34, 139, 34)	forestgreen
(25, 25, 112)	midnightblue	(32, 178, 170)	lightseagreen
(211, 211, 211)	lightgrey	(218, 112, 214)	orchid
(100, 149, 237)	cornflowerblue	(160, 82, 45)	sienna
(178, 34, 34)	firebrick	(176, 224, 230)	powderblue
(205, 92, 92)	indianred	(105, 105, 105)	dimgrey
(173, 216, 230)	lightblue	(210, 105, 30)	chocolate
(165, 216, 236) $(165, 42, 42)$	brown	(218, 165, 32)	goldenrod
(220, 220, 220)	gainsboro	(221, 160, 221)	plum
(95, 158, 160)	cadetblue	(,,)	r
( 00, 100, 100)			

The default colour palette (used for options -datacellcol, -dataelt3dcol, etc.) defined from the above colour list, by excluding colours of brightness below 0.2 and above 0.8. The brightness is defined as the average of the channel values divided by 255. The resulting list of colours is: red, green, blue, yellow, magenta, cyan, chartreuse, springgreen, olive, purple, teal, grey, deepskyblue, lawngreen, darkgrey, orangered, silver, darkorange, mediumblue, indigo, lightcoral, coral, salmon, aquamarine, gold, orange, darkmagenta, darkcyan, peru, steelblue, mediumspringgreen, darkslateblue, darkgoldenrod, lightsalmon, lightskyblue, tomato, slategrey, hotpink, darkkhaki, darkturquoise, mediumseagreen, mediumvioletred, violet, greenyellow, darkseagreen, rosybrown, deeppink, saddlebrown, darkviolet, dodgerblue, lightslategrey, burlywood, mediumslateblue, turquoise, skyblue, mediumturquoise, tan, limegreen, darksalmon, lightsteelblue, royalblue, palegreen, crimson, mediumorchid, khaki, lightgreen, darkslategrey, darkorchid, seagreen, yellowgreen, blueviolet, palevioletred, olivedrab, mediumpurple, sandybrown, darkolivegreen, mediumaquamarine, slateblue, forestgreen, midnightblue, lightseagreen, orchid, cornflowerblue, sienna, firebrick, indianred, dimgrey, chocolate, brown, goldenrod, plum and cadetblue.

# Appendix B File Formats

# B.1 Tessellation File (.tess)

Here are details on the .tess file format version 2.0. Developers should note that read and write functions are available as 'neut\_tess\_fscanf' and 'neut\_tess\_fprintf', defined in directories neut/neut\_tess/neut\_tess\_fscanf and neut/neut\_tess\_fprintf.

```
***tess
 **format
   format
 **general
   dim type
 **cell
   number_of_cells
   cell1_id cell2_id ...]
 [*seed
   seed_id seed_x seed_y seed_z seed_weight
 [*ori
   descriptor
   cellid_param1 cellid_param2 ...
   ...]
 [*lamid
   cell1_lamid cell2_lamid ...]
 [*modeid
   cell1_modeid cell2_modeid ... ]
 [*crysym
   crysym]
 **vertex
   total_number_of_vertices
   ver_id ver_x ver_y ver_z ver_state
 **edge
   total_number_of_edges
   edge_id ver_1 ver_2 edge_state
   . . .
 **face
   total_number_of_faces
   face_id number_of_vertices ver_1
                                      ver_2
           number_of_edges
                              edge_1* edge_2* ...
           face_eq_d face_eq_a face_eq_b face_eq_c
           face_state face_point face_point_x face_point_y face_point_z
 **polyhedron
   total_number_of_polyhedra
   poly_id number_of_faces face_1* face_2* ...
 **domain
  *general
```

```
dom_type
  *vertex
   total_number_of_dom_vertices
   dom_ver_id dom_ver_x dom_ver_y dom_ver_z dom_ver_label
               number_of_dom_tess_vertices ver_1
  *edge
   total_number_of_dom_edges
   dom_edge_id number_of_dom_vertices [dom_ver_1 dom_ver_2]
               dom_edge_label
               number_of_dom_tess_edges edge_1 edge_2 ...
  *face
   total_number_of_dom_faces
   dom_face_id number_of_dom_vertices dom_ver_1 dom_ver_2 ...
               number_of_dom_edges
                                      dom_edge_1 dom_edge_2 ...
               dom_face_type
               number_of_params dom_face_param1 dom_face_param2 ...
               dom_face_label
               number_of_dom_tess_faces dom_tess_face_1 dom_tess_face_2 ...
   . . .
 **periodic
  *general
  per_x per_y per_z
  per_dist_x per_dist_y per_dist_z
  *seed
   slave_seed_qty
  slave_seed_id master_seed_id per_shift_x per_shift_y per_shift_z
  *vertex
  slave_ver_qty
  slave_ver_id master_ver_id per_shift_x per_shift_y per_shift_z
   . . .
  *edge
   slave_edge_qty
   slave_edge_id master_edge_id per_shift_x per_shift_y per_shift_z slave_edge_
ori
  *face
   slave_face_qty
   slave_face_id master_face_id per_shift_x per_shift_y per_shift_z slave_face_
ori
 **scale
  *general
  number_of_scales
  *cellid
   cell1_id cell1_scale1 cell1_scale2 ... cell1_scalenumber_of_scales
***end
```

where (with identifiers being integer numbers),

- \*\*\*tess denotes the beginning of a tessellation file.
- \*\*format denotes the beginning of the format field.
- format is the file format, currently '2.0' (character string).
- \*\*general denotes the beginning of the general information field.
- dim is the dimension of the tessellation (1, 2 or 3).
- type is the type of tessellation (always 'standard').
- \*\*cell denotes the beginning of the cell field.
- number\_of\_cells is the number of cells.
- \*id denotes the beginning of an optional identifier field. It the field is not present, the cells are considered to be numbered contiguously from 1.
- cell1\_id, cell2\_id, ... are the actual identifiers of the cells.
- \*lamid denotes the beginning of an optional lamella identifier field.
- cell1\_lamid, cell2\_lamid, ... are the lamella identifiers of the cells.
- \*modeid denotes the beginning of an optional mode identifier field.
- cell1\_modeid, cell2\_modeid, ... are the mode identifiers of the cells.
- crysym is the crystal symmetry (triclinic, cubic or hexagonal).
- \*seed denotes the beginning of a seed field.
- seed\_id is the identifier of a seed and ranges from 1 to number\_of\_cells.
- seed\_x, seed\_y and seed\_z are the three coordinates of a seed (real numbers).
- seed\_weight is the weight of a seed (real number).
- \*ori denotes the beginning of an optional crystal orientation field.
- descriptor is the descriptor used to parametrize the crystal orientations. See Section A.8 [Rotations and Orientations], page 67, for the list of available descriptors.
- cellid\_param1, cellid\_param2, ... are the values of the orientation descriptor of cell id.
- \*\*vertex denotes the beginning of the vertex field.
- total\_number\_of\_vertices is the total number of vertices.
- ver\_id is the identifier of a vertex and ranges from 1 to total\_number\_of\_vertices.
- ver\_x, ver\_y and ver\_z are the three coordinates of a vertex (real numbers).
- ver\_state is an integer indicating the state of a vertex. For a standard tessellation (no regularization), it equals 0. For a regularized tessellation, it equals 0 if the vertex has not been modified by regularization and is higher than 0 otherwise.
- \*\*edge denotes the beginning of the edge field.
- total\_number\_of\_edges is the total number of edges.
- edge\_id is the identifier of an edge and ranges from 1 to total\_number\_of\_edges.
- ver\_1, ver\_2, ... are identifiers of vertices.
- edge\_state is an integer indicating the state of an edge (always 0).
- \*\*face denotes the beginning of the face field. It is present for a tessellation of dimension 2 or 3.
- total\_number\_of\_faces is the total number of faces.
- face\_id is the identifier of a face and ranges from 1 to total\_number\_of\_faces.
- number\_of\_vertices is the number of vertices of a face.
- number\_of\_edges is the number of edges of a face.

• edge\_1\*, edge\_2\*, ... are identifiers of the edges of a face, signed according to their orientation in the face.

- face\_eq\_a, face\_eq\_b, face\_eq\_c and face\_eq\_d are the parameters of the equation of a face: face\_eq\_a  $x + face_eq_b y + face_eq_c z = face_eq_d$ . The parameters are scaled so that face\_eq\_a<sup>2</sup> + face\_eq\_b<sup>2</sup> + face\_eq\_c<sup>2</sup> = 1.
- face\_state is an integer indicating the state of a face. For a standard tessellation (no regularization), it equals 0. For a regularized tessellation, it equals 0 if it has not been modified by regularization and 1 otherwise.
- face\_point is an integer indicating the point used for the interpolation of a face. For a standard tessellation (no regularization), it equals 0. For a regularized tessellation: if the point is the face barycentre, it equals 0; if the point is one of the face vertices, it equals to the position of the vertex in the list of vertices of the face. It equals -1 if the point is undefined.
- face\_point\_x, face\_point\_y and face\_point\_z are the coordinates of the point used for the interpolation of a face (equal 0 if undefined).
- \*\*polyhedron denotes the beginning of the polyhedron field. It is present for a tessellation of dimension 3.
- total\_number\_of\_polyhedra is the total number of polyhedra.
- poly\_id is the identifier of a polyhedron and ranges from 1 to total\_number\_of\_polyhedra.
- number\_of\_faces is the number of faces of a polyhedron.
- face\_1\*, face\_2\*, ... are identifiers of the faces of a polyhedron, signed according to their orientations in the polyhedron (positive if the normal of the face is pointing outwards and negative if it is pointing inwards).
- \*\*domain denotes the beginning of the domain field.
- \*general denotes the beginning of the domain general information field.
- dom\_type is the type of the domain (one of cube, cylinder, square, circle, poly and planes).
- \*vertex denotes the beginning of the domain vertex field.
- total\_number\_of\_dom\_vertices is the total number of domain vertices.
- dom\_ver\_id is the identifier of a domain vertex and ranges between 1 to total\_number\_ of\_dom\_vertices.
- dom\_ver\_x, dom\_ver\_y and dom\_ver\_z are the three coordinates of a domain vertex (real numbers).
- dom\_ver\_label is the label of a domain vertex.
- number\_of\_dom\_tess\_vertices is the number of tessellation vertices of a domain vertex (must be 1).
- \*edge denotes the beginning of the domain edge field (for a tessellation of dimension 2 or 3).
- total\_number\_of\_dom\_edges is the total number of domain edges.
- dom\_edge\_id is the identifier of a domain edge and ranges between 1 to total\_number\_ of\_dom\_edges.
- number\_of\_dom\_vertices is the number of domain vertices of a domain edge or a domain face.
- dom\_ver\_1, dom\_ver\_2, ... are identifiers of the domain vertices of a domain edge or face.
- dom\_edge\_label is the label of a domain edge.

- number\_of\_dom\_tess\_edges is the number of tessellation edges of a domain edge.
- \*face denotes the beginning of the domain face field (for a tessellation of dimension 3).
- total\_number\_of\_dom\_faces is the total number of domain faces.
- dom\_face\_id is the identifier of a domain face and ranges from 1 to total\_number\_of\_ dom\_faces.
- number\_of\_dom\_edges is the number of domain edges of a domain face.
- dom\_edge\_1, dom\_edge\_2, ... are identifiers of the domain edges of a domain face.
- dom\_face\_type is the type of a face, among 'plane', 'cylinder' or 'sphere'.
- number\_of\_params is the number of parameters of a domain face.
- dom\_face\_param1, dom\_face\_param2, ... are the parameters of a domain face. For a planar face, they are the parameters of the equation of the face, listed in the order face\_eq\_d, face\_eq\_a, face\_eq\_b and face\_eq\_c. For a cylindrical face, they are the coordinates of the base point, the axis and the radius. For a spherical face, they are the coordinates of the centre and the radius.
- dom\_face\_label is the label of a domain face. If dom\_type is 'cube', it is one of 'x0', 'x1', 'y0', 'y1', 'z0' or 'z1'. If dom\_type is 'cylinder', it is one of 'z0', 'z1', 'f1', 'f2', ... Otherwise, it is one of 'f1', 'f2', ...
- number\_of\_dom\_tess\_faces is the number of tessellation faces of a domain face.
- dom\_tess\_face\_1, dom\_tess\_face\_2, ... are the identifiers of the tessellation faces of a domain face.
- \*\*\*end denotes the end of a tessellation file.
- \*\*periodicity denotes the beginning of the periodicity field.
- \*general denotes the beginning of the periodicity general information field.
- per\_x, per\_y and per\_z are booleans indicating x, y, and z periodicity.
- per\_dist\_x, per\_dist\_y and per\_dist\_z are the periodicity distances along x, y, and z.
- \*seed denotes the beginning of the periodicity seed field.
- slave\_seed\_qty is the number of slave seeds.
- slave\_seed\_id is the identifier of a slave seed.
- master\_seed\_id is the identifier of the master of a slave seed.
- per\_shift\_x, per\_shift\_y and per\_shift\_z are the shifts of a slave seed (or vertex, etc.) relative to its master, along x, y and z. The values can be -1, 0 or 1.
- \*vertex denotes the beginning of the periodicity vertex field.
- slave\_vertex\_qty is the number of slave vertices.
- slave\_vertex\_id is the identifier of a slave vertex.
- master\_vertex\_id is the identifier of the master of a slave vertex.
- \*edge denotes the beginning of the periodicity edge field.
- slave\_edge\_qty is the number of slave edges.
- slave\_edge\_id is the identifier of a slave edge.
- master\_edge\_id is the identifier of the master of a slave edge.
- slave\_edge\_ori is the orientation of the slave edge with respect to the master edge: 1 if identical, -1 if opposite.
- \*face denotes the beginning of the periodicity face field (for a tessellation of dimension 3).
- slave\_face\_qty is the number of slave faces.
- slave\_face\_id is the identifier of a slave face.

- master\_face\_id is the identifier of the master of a slave face.
- slave\_face\_ori is the orientation of the slave face with respect to the master face: 1 if identical, -1 if opposite.
- number\_of\_scales is the number of scales.
- cell1\_scale1, cell1\_scale2, . . . are the identifiers of the cells of the scale-1, scale-2, . . . tessellations which the cell belongs to.

# B.2 Raster Tessellation File (.tesr)

Here are details on the .tesr file format version 2.0. Developers should note that read and write functions are available as 'neut\_tesr\_fscanf' and 'neut\_tesr\_fprintf', defined in directories neut/neut\_tesr/neut\_tesr\_fscanf and neut/neut\_tesr/neut\_tesr\_fprintf. Compared to a tessellation file (.tess), a raster tessellation file can include cell morphological properties such as their centroids or volumes. This is motivated by the fact that, for a raster tessellation, these properties are both in small number and relatively expensive to compute, and so are stored once known. Square brackets ([]) denote optional fields.

```
***tesr
 **format
   format data_format
 **general
   dimension
   size_x size_y [size_z]
   voxsize_x voxsize_y [voxsize_z]
 [*origin
   origin_x origin_y [origin_z]]
 [*hasvoid has_void]
[**cell
   number_of_cells
 [*id
   cell1_id cell2_id ...]
   seed_id seed_x seed_y [seed_z] seed_weight
   ...]
 [*ori
   descriptor
   cell1_param1 cell1_param2 ...
   cell2_param1 cell2_param2 ...
   ...]
 [*coo
   cell1_x cell1_y [cell1_z]
   cel12_x cel12_y [cel12_z]
   ...]
 [*vol
   cell1_vol
   cell2_vol
   . . . ]
 [*convexity
   cell1_convexity
   cell2_convexity
   ...]
```

```
[*crysym
    crysym
]
    **data
    vox1_cell vox2_cell ...
or
    *file data_file_name
[**oridata
    descriptor
    vox1_param1 vox1_param2 ...
    vox2_param1 vox2_param2 ...
or
    descriptor
    *file oridata_file_name
]
***end
```

#### where,

- \*\*\*tesr denotes the beginning of a raster tessellation file.
- \*\*format denotes the beginning of the format field.
- format is the file format, currently '2.0' (character string).
- data\_format is the format of the data in field \*\*data. It can be either ascii, binary8 (8-bit binary), binary16 (16-bit binary, LittleEndian), binary16\_big (16-bit binary, BigEndian), binary32 (32-bit binary, LittleEndian) or binary32\_big (32-bit binary, BigEndian).
- \*\*general denotes the beginning of the general information field.
- dimension is the dimension of the raster tessellation.
- size\_x, size\_y and size\_z are the raster sizes along the coordinate axes. The number of sizes must match dimension.
- voxsize\_x, voxsize\_y and voxsize\_z are the voxel (pixel, in 2D) sizes along the coordinate axes. The number of sizes must match dimension.
- \*origin denotes the beginning of an optional origin field.
- origin\_x, origin\_y and origin\_z are the (absolute) coordinates of the origin of the raster tessellation along the coordinate axes. The number of coordinates must match dimension.
- \*hasvoid denotes the beginning of an optional has-void field.
- has\_void is a boolean indicating whether the tessellation contains void voxels (which have a cell id of 0).
- \*\*cell denotes the beginning of an optional cell field.
- number\_of\_cells is the number of cells.
- \*id denotes the beginning of an optional identifier field. If the field is present, the cell identifiers listed under \*\*data are supposed to be numbered contiguously from 1 (or 0 in case of void), and their actual identifiers are considered to be the ones provided in the list. The actual identifiers are used in output files.
- cell1\_id, cell2\_id, ... are the actual identifiers of the cells.
- \*seed denotes the beginning of a seed field.
- seed\_id is the identifier of a seed and ranges from 1 to number\_of\_cells.
- seed\_x, seed\_y and seed\_z are the three coordinates of a seed (real numbers).

- seed\_weight is the weight of a seed (real number).
- \*ori denotes the beginning of an optional crystal orientation field.
- descriptor is the descriptor used to parametrize the crystal orientations. See Section A.8 [Rotations and Orientations], page 67, for the list of available descriptors.
- cellid\_param1, cellid\_param2, ... are the values of the orientation descriptor of cell id.
- \*coo denotes the beginning of an optional centroid field.
- cellid\_x, cellid\_y and cellid\_z are the coordinates of the centroids of cell id.
- \*vol denotes the beginning of an optional volume field.
- cellid\_vol is the volume of cell id.
- \*convexity denotes the beginning of an optional convexity field.
- cellid\_convexity is the convexity of cell id.
- \*crysym denotes the beginning of an optional crystal symmetry field.
- crysym is the crystal symmetry (triclinic, cubic or hexagonal).
- \*\*data denotes the beginning of the data field. Data can be provided in the .tesr file or in a separate file, using \*file, see below.
- $voxid\_cell$  is the cell voxel id belongs to. Voxels must be listed in column-major order (x varying first, y varying second and z varying last). The cell identifiers should start from 1. Use 0 for voids.
- \*file denotes the beginning of a file field.
- data\_file\_name is the name of a file that contains the data. It must be located in the same directory as the parent tesr file, or its path relative to the parent tesr file must be provided. Typically, it is a .raw file.
- \*\*oridata denotes the beginning of the orientation data field. Data can be provided in the .tesr file or in a separate file, using \*file, see below.
- voxid\_param1, voxid\_param2, . . . are the values of the orientation descriptor of voxel id. Orientations must be listed in column-major order (x varying first, y varying second and z varying last). Arbitrary orientations can be used for void voxels (voxid\_cell = 0). These data must be written under format data\_format, in terms of ASCII or binary. In the case of binary format, double-precision numbers are considered.
- oridata\_file\_name is the name of a file that contains the orientation data. It must be located in the same directory as the parent tesr file, or its path relative to the parent tesr file must be provided. Typically, it is a .raw file.

#### B.3 Multiscale Cell File

A multiscale cell file provides cell-by-cell values for a multiscale tessellation and can be loaded using 'msfile(filename)'<sup>1</sup>. The file contains, for each cell, its multiscale identifier, mid, and the value(s). A cell multiscale identifier (mid) is a character string identifying a cell at a specific scale. For a given cell, C, mid combines the identifiers of the cells that C belongs to, at successive scales, to its own id, separated by '::'. For a 1-scale tessellation, mid equals id. For a 2-scale tessellation composed of  $2 \times 3$  cells, the mids are equal to 1::1, 1::2, 1::3, 2::1, 2::2 and 2::3. The domain (which can be considered as a cell at scale 0), mid is nil. An example of a multiscale cell file that could be used to define the amounts of cells of a 3-scale tessellation is:

<sup>1 2</sup> 2 4

<sup>&</sup>lt;sup>1</sup> As of version 3.5.0, 'msfile(filename)' should be preferred over 'file(filename)'

1::1 3 1::2 4 2::1 5 2::2 6 2::3 7 2::4 8

The file could be used in -T as: -n msfile(filename)::msfile(filename)::msfile(filename). The first instance of 'msfile(filename)' reads the number of scale-1 cells in line 1, the second instance of 'msfile(filename)' reads the number of scale-2 cells in lines 2-3, and the third instance of 'msfile(filename)' reads the number of scale-3 cells in lines 4-7.

#### **B.4** Position File

A position file lists the coordinates of a given number of points. The file must contain 1 coordinate per point in 1D, 2 coordinates per point in 2D and 3 coordinates per point in 3D. While the dimension can be known from the context in which the file is read, it can also be specified by appending ':dim' to the name of the position file, where dim is the dimension. A coordinate can be an integer or real number. A real number can have an arbitrary number of digits, but the decimal mark must be '.'. The coordinates can be separated from each other by spaces, tabulators or newlines (any number as well as arbitrary combinations of them are supported). However, a good practice is to format the file with one line per point. An example of a position file containing 5 points in 3D is:

```
2.1235 9.4544 5.2145
5.9564 3.6884 9.2145
2.2547 3.2658 8.2514
8.2515 9.4157 2.9454
0.5874 4.2848 2.4874
```

# Appendix C Developer's Guide

This chapter provides information useful to anyone who plans to contribute to Neper or wishes to better understand how it works. The code structure is detailed and information are given on how to efficiently contribute to it. If you are missing information, complain!

#### C.1 Code Structure

The Neper root directory content is as follows (the slash character '/' denotes directories),

- COPYING: license terms;
- README: information about other files and directories in the directory;
- VERSIONS: information on the versions of Neper;
- src/: source code directory;
- doc/: documentation directory.

Details on the 'src/' and 'doc/' directories are provided in the following.

#### C.1.1 Source Code

Neper's source code is located in directory src/ and consists of roughly 120,000 lines shared between 250 directories and 1000 text files. The 'src/' directory contains the following files and directories,

#### • neper\_.h and neper.c

These are the main source code header file and source code file of Neper. 'neper.c' contains Neper's 'main' function. It reads the arguments passed at the command line and runs the corresponding functions, which can be one of the program module.

#### • neper\_t/, neper\_m/ and neper\_v/

These are directories that contain the source code of each of the program modules. The modules aim to be independent from each other; that is, a function of one module will never calls a function of another module (with a few exceptions).

#### • neut/

'neut' stands for *Neper utilities*. The directory contains utility functions specific to Neper and used by several modules.

#### • contrib/

This directory contains utility functions not specific to Neper. The first one is 'ut', which is a collection of general-purpose, low-level C functions (memory allocation, etc.). The second one is 'orilib', which is a collection of routines for orientation manipulation (see http://orilib.sourceforge.net). Another one is nanoflann, a library for nearest neighbour searching (see https://github.com/jlblancoc/nanoflann), and the last one is muparser, a library for interprating mathematical and logical expressions (see http://beltoforion.de/article.php?a=muparser). Although these libraries are also distributed alone (and might be already installed on your system), they are included into Neper instead of being considered as dependencies (contrary to the GSL, . . . ) to make installation easier.

## • CMakeLists.txt, neper\_config.h.in and cmake/

These files and directories are specific to the building system, CMake. CMakeLists.txt is the CMake source file, which tells CMake where to find the program source files, how to manage dependencies, where to install Neper, etc. neper\_config.h.in is a small configuration file that is useful to CMake for managing dependencies and program version numbers. cmake/ contains.cmake files which help CMake locating the dependencies on the system (library and header files).

A module directory, neper\_X/, where 'X' stands for the module letter (one of 't', 'm' or 'v'), is structured as follows,

#### • neper\_X.h, neper\_X.h and neper\_X.c

These are the source code header files and source code file of the module. neper\_X.c contains the module function, 'neper\_X'. neper\_X\_h is the source code header file, which is #include'ed in neper\_X.c and contains a bunch of #includes to all necessary library header files. neper\_X.h contains the prototype of the module function and is #include'ed in neper\_h. Hence, files \_.h are local header files while files .h are header files #include'ed into a upper-level source code header file. This is true everywhere in the source code. Moreover, any function specific to module X is prefixed 'neX\_'.

## • neX\_input/ and structIn\_X.h

The 'neX\_input/' directory contains functions for reading the value of the arguments passed to module X from the command line. The information are recorded into an 'IN\_X' C structure, which is declared in file 'structIn\_X.h'.

• neX\_foo/, neX\_bar/, etc.

Each of these directories is associated to a specific task of the module and contains a function of the same name ('neX\_foo', etc.) which is called from function 'neper\_X'. Each directory contains a directory tree structure.

#### • CMakeLists.txt

This file tells CMake where to find the source files and how to manage dependencies in the module. It is used by the upper-level CMakeLists.txt file (there is no lower-level CMakeLists.txt file).

The neut directory is roughly structured as follows,

#### • CMakeLists.txt

This file tells CMake where to find the source files and how to manage dependencies in the module. It is used by the upper-level CMakeLists.txt file (there is no lower-level CMakeLists.txt file).

neut.h, neut\_t.h, neut\_m.h and neut\_v.h

These files are source code header files that #include header files of neut (which contain function prototypes) and are #included in the modules. neut.h #includes all header files while the three others #include header files only necessary to the corresponding module (this speeds up compilation at development stage).

neut\_structs/

This directory contains header files which defines all C structures used in the program.

• neut\_foo/, neut\_bar/, etc.

Each of these directories contain functions specific to a particular C structure. For example, neut\_tess contains functions relative to the 'TESS' structure, which describes a tessellation.

#### C.1.2 Documentation

Neper's documentation is located in directory doc/. It is written in Texinfo, the GNU software documentation system. The documentation consists of a collection of .texi files (text files). The documentation may be compiled in PDF, info or html format by running make pdf, make info or make html, respectively. In official releases, both the PDF and info documentation files are built and included in the archive.

# C.2 Contributing to Neper

The Neper development repository is hosted on GitHub: https://github.com/rquey/neper. Code contributions to be included in Neper's official (public) version should be submitted as pull requests on this repository.

## C.2.1 Coding Conventions

Neper is written following the GNU Coding Standards (http://www.gnu.org/prep/standards), with the exception that braces are not indented (because there is so often 3+loop levels in Neper). Please follow this convention. Here are a few tips and other remarks,

• For Vim, put the following commands in file \$HOME/.vimrc:

```
:set sw=2
:set cindent
:syntax enable
:set textwidth=72
```

- You can run indent -bli0 source\_files for automatic formatting.
- Break up the code into meaningful chunks using blank lines. Always use a single blank line to separate parts of the code.
- Neper admits no compilation warnings. Please fix up all of them.
- Please help us maintaining good documentation by documenting any capability you may add

# C.2.2 Adding a New Option

In modules -T and -M, adding a new option can be done by following these steps:

- Add a variable to the 'IN\_X' structure to record the value of the option (file structIn\_X.h).
- If necessary, allocate / free the variable in the neX\_in\_set\_zero and neX\_in\_free functions (file neX\_input1.c) Assign it a default value in net\_input\_options\_default (file neX\_input3.c).
- Add the option to the option list in net\_input\_options\_set (file neX\_input3.c), taking as an example another option of the same type (integer, etc.).
- Where appropriate in the source code, add a new function for the new option (if necessary
  in a new file or directory). The function should be executed depending on the value of the
  option.
- If adding one or several files or directories, add the source file(s) to the source file list in the CMakeLists.txt file of the corresponding module.
- Make sure the whole thing compiles and runs properly for your purpose.
- Make sure your own changes did not break anything in the rest of the code by running full testing, using make test (or ctest). You may also want to add a test specific to the new option.

In module -V, options are processed differently. Instead of being recorded in a C structure, they are read one after the other and associated functions are executed along the way. To add a new option, take an existing option as an example.

# C.2.3 Compilation Options

For development, several compilation options can be changed from their default values. This must be done at configuration stage, using commands 'ccmake ..' or 'cmake-gui ..'. The compilation options are

#### • DEVEL\_DEBUGGING\_FLAG

Setting the option to ON turns on the debugging compilation flag '-g', which is required for debugging with gdb and valgrind, and turns on the compilation flag '-Werror', which makes all compilation warnings into errors.

#### • DEVEL\_DEBUGGING\_TEST

Setting the option to ON runs internal tests during Neper execution at places where the code is otherwise considered robust.

#### • DEVEL\_OPTIMIZATION

Setting this option to OFF disables code optimization, which is useful for debugging with gdb and valgrind.

• DEVEL\_PROFILING

Setting this option to ON turns on the code profiling compilation flag '-pg', which is required for profiling with gprof. This is a highy CPU-sensitive option, which should be used only when profiling is actually carried out.

#### C.2.4 Testing

The code can be tested using CTest. The usual way is as follows:

\$ ctest

It is also possible to run only some of the tests.

• Option -R selects the tests whose name contains a character string:

```
$ ctest -R string
```

As test names start by the letter of the module they refer to, followed by character '\_', it becomes handy to run tests on a specific module, for example:

```
$ ctest -R T_
```

• Option -E selects the tests that do not contain a character string:

```
$ ctest -E string
```

• Option -I selects the tests from their numbers, for example:

```
$ ctest -I 3,5
```

# Appendix D Versions

New in 3.5.0 (01 Oct 2019):

- module -T: added -transform slice and oriaverage, added new statistical distributions to -morpho: beta, lorentzian, studentst, weibull, breitwigner, expnormal, moffat, pearson7, pseudovoigt and skewnormal, added endpoints to statistical distributions, added variable 1-sphericity to -morpho, added tessellation keys, added -orioptilogvar, improved argument reading (multiscale tessellation), improved tesr format, improved -transform renumber, improved -ori fibre, improved -statcell convexity, replaced -transform plane with -transform hspace, fixed -loadtesr file.tesr:..., fixed -statvox e, fixed -for ori, fixed -domain, fixed -morpho centroidal, fixed tesr reading, fixed vtk output, enrich tesr file, made minor fixes.
- module -M: added -transform scale, translate and smooth, added -transporteltmethod, added -transportfepx, added mesh keys, added -performat, added kocks file to -for fepx:legacy, fixed -interface cohesive for Abaqus, fixed -elt hex, merged -scale into -transform, speed up -transport, made minor fixes.
- module -V: added -showvox, added -datavoxcol disori, added colour schemes R(), r, theta and rtheta, added -imageformat pov:objects, improved -includepov, fixed visualization of periodic meshes, made small fixes.
- documentation: made minor fixes and improvements.
- general: fixed compilation when GSL and NLopt locally installed, website now at http://neper.info.

## New in 3.4.0 (15 Apr 2019):

- module -T: added tessellation cutting (to get non-convex domains) using -transform cut, added cell merging and removal using -transform mergecell and rmcell, added -transform resetcellid, added -ori spread, improved -morpho lamellar, improved -morpho diameq, added -format stl:bycell, added tessellation keys, fixed -morpho aspratio and rasterization of periodic tessellations, fixed -domain circle:split, made small fixes and improvements.
- module -M: made -interface mutliscale, renamed -mesh3dclconv into
  -mesh3dclreps, improved -cl, -rcl and -mesh3dclreps argument expressions,
  speed up -transport, fixed 2D remeshing, speed up -statelt and -statelset,
  added -[r]clface, -[r]cledge and -[r]clver.
- module -V: improved visualization of non-convex cells, fixed visualization of hex meshes, minor other fixes.

#### New in 3.3.0 (25 Jul 2018):

- New paper: "R. Quey, A. Villani, and C. Maurice. Nearly uniform sampling of crystal orientations. J. Appl. Crystallogr., vol. 51, doi:10.1107/S1600576718009019, 2018."
- module -T: added -ori uniform for uniform orientation distribution, added sister options -orioptiini, -orioptifix, -orioptistop and -orioptineigh, added -morpho tocta, columnar, bamboo and aspratio, fixed -morpho multimodal, improved -morphooptiini, added -transform translate, fixed tesr output for periodic tessellations, fixed tess to tesr conversion, added several tessellation keys, merged option -scale into -transform, made minor improvements.
- module -M: fixed meshing of periodic tessellation with openMP, allowed

- Gmsh development versions.
- module -V: improved camera parameters, fixed -slicemesh for hex meshes.

#### New in 3.2.0 (23 May 2018):

- general: Neper is now fully multithreaded.
- module -T: improved -morpho, added -morpho variable:value, added -morpho centroidtol, improved -morphooptiobjective, improved -transform crop, fixed -n from\_morpho, added -transform addbuffer, renamed -datarpt\* into -datavox\*, added -transform renumber, added -domain stdtriangle, added \*\*oridata to the tesr file, added -statvox, speed up tesr generation, added -morphooptilogtime val\_ keys, minor fixes.
- module -M: improved inp format.
- module -V: improved msh reading, added -datapointrad arr, added -datavox options.
- documentation: small fixes.

#### New in 3.1.1 (20 Feb 2018):

- New paper: "R. Quey and L. Renversade, Optimal polyhedral description of 3D polycrystals: Method and application to statistical and synchrotron X-ray diffraction data, Comput. Methods Appl. Mech. Engrg., vol. 330, pp. 308-333, 2018."
- module -T: fixed -scale, added -domain rodrigues.
- module -M: fixed mesh of regularized tessellation through 2D-mesh pinches correction, fixed -stat when a tesr is meshed, improved -loadmesh, added -mesh2dpinchfix, added test on Gmsh's version.
- module -V : fixed -datapolyscale.
- general: fixed use without nlopt or openmp.

#### New in 3.1.0 (05 Sep 2017):

- module -T: made all options applicable to multiscale tessellations,
  improved -morpho for all types of data, improved -morpho\*
  options, added -n from\_morpho to set the number of cells from all
  -morpho inputs, added -format stl, added -transform crop and 2d, added
  -morphooptilogtesr, added tessellation key 'scale', included openMP
  parallelization for -morpho tesr.
- module -M: allowed -interface cohesive -periodic in 2D, improved -dim for -format geof, improved -format geof, minor fixes.
- module -V: added -datapointrad tor and disc.
- documentation: small fixes.
- general: support OpenMP.

#### New in 3.0.2 (16 Feb 2017):

- module -T: added -transform scale and transform rotate for scalar tessellations (.tess), fixed -morpho with -periodic, fixed -morpho with non-unitary domains, fixed -statedge/-statface theta with -oricrysym hexagonal, improved -ori, added -morpho lamellar(v=crysdir), added \*\*\*tess/\*\*cell/\*crysym section to .tess file, fixed -morphooptialgo random, small fixes.
- module -M: fixed -interface cohesive in 2D and 3D (for Abaqus), enable -interface discontinuous and cohesive for periodic tessellations, added -format msh:binary, fixed faset internal for 3D, added

- -transport node:..., changed point keys "elt3d" and "elset3d" into "elt" and "elset" (now apply to 3D or 2D), small fixes.
- documentation: minor fixes.

#### New in 3.0.1 (01 Dec 2016):

- module -T: fixed up options -periodic and -morphooptialgoneigh qsort, added tessellation key 'modeid' (for cells), added -morpho cube(N1,N2,N3) and -morpho square(N1,N2), enabled -loadtess -scale, added -oricrysym hexagonal, added tessellation keys 'nfacelist' and 'theta', cleaned code, fixed documentation of .tess file, added tests on conflicing options.
- module -M: added option -scale, fixed hexahedral meshing of periodic tessellations, added physical groups to .msh, fixed 2D meshes in Abaqus (.inp) file, fixed up option -faset internal.
- module -V: fixed options -dataseed\*.
- general: removed libmatheval dependency, fixed testing.

#### New in 3.0.0 (12 Sep 2016):

- module -T: added 3 major capabilities: (i) tessellation generation from morphological cell properties (options starting by -morpho), (ii) multiscale tessellation generation (using the :: separator), and (iii) periodic and semi-periodic tessellation generation (option -periodic); made some other improvements and some clean up all over the place.
- module -M: added ability to mesh the new tessellations, including periodic tessellations; added interface meshing using cohesive elements (option -interface); made small other improvements.
- module -V: made small improvements.
- module -D: replaced by "make test" using CTest.
- new development website: https://github.com/rquey/neper.

#### New in 2.0.5 (06 Feb 2016):

- module -T: fixed up -domain planes in 3D, added -domain sphere, added
  'rotate', 'translate' and 'scale' arguments to -domain, added normal
  specification in -morpho lamella, minor other improvements.
- module -M: fixed up vtk output.
- module -V: added -datacellcol id:filename, fixed up options -data\*col
  id.
- module -D: minor improvements.

#### New in 2.0.4 (22 Jun 2015):

- module -T: fixed up regularization in 2D, extended -morpho planes to 2D, added semi-periodicity for raster tessellations, minor fixes.
- module -M: fixed up 2D mesh output in Abaqus format, minor fixes.
- module -V: fixed up -datacellcolscheme, improved -cameracoo to account for the tessellation/mesh dimensions.

#### New in 2.0.3 (27 Nov 2014):

- module -M: fixed up bug on Mac OS X, fixed up Ctrl-C, fixed up and speed up option -statpoint 2dmesh\*.
- module -T: improved options for 2-scale tessellations, added option
  '-clip'.

#### New in 2.0.2 (29 Sep 2014):

- module -T: fixed up regularization of cylinder tessellations, fixed up option '-domain planes', added tessellation cell domain, fixed up 3dec and ply support, added Wavefront obj format, added / fixed up tessellation keys.

- module -M: added vtk mesh format, fixed up fepx and geof mesh formats, added extrusion of a 2D mesh to get a 3D mesh (option -dim), fixed up topology reconstruction.
- module -V: added points plotting as cubes, spheres, cylinders or ellipsoids (options -showpoint and -datapoint\*).

#### New in 2.0.1 (12 Mar 2014):

- Fixed up compilation on some systems, added support for libscotch version 6.0, small fixes and cleanups.
- module -T: enabled square and cube tessellations in .tess format, fixed up cell sorting, made option -id mandatory, improved regularization of 2D tessellations, added bunch of tessellation keys, small fixes.
- module -M: added 'domtype' mesh key.
- module -V: fixed up simultaneous tess and mesh printing, fixed up colouring based on id, improved camera positioning for 2D and 1D inputs, added coordinate system, improved option -slicemesh, added options -data\*scaletitle, improved -data\*scale options.

#### New in 2.0.0 (10 Jan 2014):

- General: Full restructuring and added many new features. Neper now has 3 main modules: tessellation module (-T), meshing module (-M) and visualization module (-V); details are provided below. Added developer's guide and module (-D). Documentation has been much improved.
- module -T: added several tessellation algorithms (hardcore Voronoi and Laguerre Voronoi); added orientation generation (was previously in -0); significantly sped up tessellation; included and significantly sped up regularization (was previously in -FM); added 2-scale polycrystal generation; added 2D and 1D supports; improved statistics; enabled both scalar (tess) and raster (tesr) outputs; cleaned up tess file.
- module -M: module for free and mapped meshings (merging of -FM and -MM). Removed regularization (now in -T); added per-cell mesh size definition; sped up multimeshing; improved statistics.
- module -V: full restructuring; added support for 2D and 1D tessellations and meshes; the way all entities are shown (cells, polyhedra, faces, edges, vertices, germs, 3D/2D/1D/0D element sets and elements, nodes) can be set in great detail; added transparency.

#### New in 1.10.3 (26 Nov 2012):

- module -T: added 3dec geometry format, added option -checktess, minor improvements, added individual file extension support in -stattess, changed option -neigh 1 to -statp i,f,npl,fal,feql.
- module -FM: added 3dec geometry format; changed "top" and "bot" nset names for cylindrical domains to "z0" and "z1"; minor bug fixes;

- improved fev format support; added individual file extension support in options -stattess and -statmesh.
- module -0: minor bug fixes.
- module -MM: sped up meshing; fixed -domain, -scale and -nset options, add .nper file for periodicity conditions; fixed msh output for meshes with different element dimensions; minor other bug fixes.
- module -VS: sped up meshing reconstruction and PNG file generation, added option '-camerasky', added option '-showeltedge', sped up mesh reconstruction, minor fixes
- documentation: minor fixes.
- General: minor fixes.

#### New in 1.10.2 (09 Aug 2012):

- module -T: fixed -centroid option.
- module -FM: fixed list of available meshing algorithms. Added tests.
- module -MM: fixed nset syntax in inp (Abaqus) files.
- module -VS: added capability to plot mapped meshes.
- General: various minor improvements, code cleaning.

#### New in 1.10.1 (08 June 2012):

- Bug fix to get Neper working after invoquing 'make install'.

#### New in 1.10.0 (04 June 2012):

- General: New (hopefully simpler) installation procedure based on Cmake. Added support for domains of any convex polyhedral shape.
- module -VS: major code rewriting and option changes. New capabilities for defining the colours and sizes of the tessellation / mesh (including gradients). Added options to show only specific parts of the tessellation / mesh and to view slices of a mesh. Other small enhancements.
- module -T : added option '-domain' to specify the shape of the domain (cuboidal, cylindrical or of any convex shape), small bug fixes, added centroid Voronoi tessellation generation (option -centroid), merged option -centrecoo into option -morpho, added polyhedron centroid coordinates in file .stt3, changed option -load to -loadtess, added output format '.ply' (thanks Ehsan!).
- module -FM: mesh partitionning needs libscotch version 5.1.12 or later, small bug fixes, changed default value of -faset to "" (i.e. no faset in output), fixed bug for Abaqus output, added polyhedron centroid coordinates in file .stt3, added output format '.ply' (geometry only).
- module -MM: new options -dsize and -scale, new option -loadmesh, new option -outdim, changed arguments of -ttype, changed default value of -faset to "" (i.e. no faset in output), fixed bug for Abaqus output, small bug fixes.

#### New in 1.9.2 (Sep 2011):

- module -T: added option -morpho for specifying the type of grain structure (equiaxed, columnar or bamboo), merged option -regular with -morpho, added post-processing -neighbour option for information on the polyhedron neighbours, added geo (Gmsh geometry) output format (mostly for visualization), fixed bugs.

- module -MM: proper processing of the input tess files, added msh
   (Gmsh) and inp (Abaqus) output formats, added options -morpho and
   -centrecoo (as in module -T), small bug fixes, code cleaning.
- module -FM: added geo (Gmsh geometry) output format (mostly for visualization), small bug fixes.
- documentation: small corrections.

#### New in 1.9.1 (May 2011):

- module -FM: fixed bug occurring when -mesh3dalgo is not set by the user. Small other bug fixes.
- module -MM: small bug fixes.

#### New in 1.9.0 (Apr 2011):

This is a major release. Neper now has its own paper:

"R.Quey, P.R. Dawson and F. Barbe. Large-scale 3D random polycrystal for the finite element method: Generation, meshing and remeshing. Computer Methods in Applied Mechanics and Engineering, Vol. 200, pp. 1729--1745, 2011."

Please cite it in your works if you use Neper.

- General: added option --rcfile to disregard / change the initialization file; big distribution and source clean up; bug fixes.
- module -T: added capability to generate regular morphologies (truncated octahedra), tess file format bumped to 1.9; big clean up.
- module -FM: included multimeshing, remeshing and mesh partitioning capabilities; big clean up. Neper now uses the \*standard\* Gmsh distribution for 2D and 3D meshings (versions >=2.4.2). Strongly reduced memory usage.
- module -0: added capability to handle different orientation descriptors.
- module -VS: new visualization module to generate publication-quality images (PNG format) of the tessellations, meshes and more...

#### New in 1.8.1 (Aug 2009):

- upgraded website at http://neper.sourceforge.net
- module -T: new file format \*\*\*tess1.8, new option -restart to load an existing tessellation (not through std input any more), new option -printformat, bug fixes.
- module -MM: bug fixes.
- module -FM: new output format mae, new option -restart to restart from an existing geometry or mesh (options -mesh and -conv removed); new options -printformat and -maeextension; better mesh numbering (+ new options -elementfirstid and -nodefirstid), new way to choose the node sets to output (-nset 4), fixed option -estat, renamed -bwcy-clmin to -clmin, cleaned bunch of options, bug fixes.
- module -0: added option -euleranglesconvention (Bunge, Roe & Kocks); new output formats mae and geof (option -format).
- manual: some corrections.

#### New in 1.8.0 (Jul 2009):

- First GPL-distributed version of Neper.

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Version 3, 29 June 2007

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