HYBGRAG: Hybrid Retrieval-Augmented Generation on Textual and Relational Knowledge Bases

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Abstract

Given a semi-structured knowledge base (SKB), where text documents are interconnected by relations, how can we effectively retrieve relevant information to answer user questions? Retrieval-Augmented Generation (RAG) retrieves documents to assist large language models (LLMs) in question answering; while Graph RAG (GRAG) uses structured knowledge bases as its knowledge source. However, many questions require both textual and relational information from SKB — referred to as "hybrid" questions — which complicates the retrieval process and underscores the need for a hybrid retrieval method that leverages both information. In this paper, through our empirical analysis, we identify key insights that show why existing methods may struggle with hybrid question answering (HQA) over SKB. Based on these insights, we propose HYBGRAG for HQA, consisting of a retriever bank and a critic module, with the following advantages: (1) Agentic, it automatically refines the output by incorporating feedback from the critic module, (2) Adaptive, it solves hybrid questions requiring both textual and relational information with the retriever bank, (3) Interpretable, it justifies decision making with intuitive refinement path, and (4) Effective, it surpasses all baselines on HQA benchmarks. In experiments on the STARK benchmark, HYBGRAG achieves significant performance gains, with an average relative improvement in Hit@1 of 51%.

1 Introduction

Retrieval-Augmented Generation (RAG) (Lewis et al., 2020; Guu et al., 2020) enables large language models (LLMs) to access the information from an unstructured document database. This allows LLMs to address unknown facts and solve Open-Domain Question Answering (ODQA) with additional textual information. Graph RAG

(GRAG) has extended this concept by retrieving information from structured knowledge bases, where documents are interconnected by relationships. Existing GRAG methods focus on two directions: extracting relational information from knowledge graphs (KGs) and leverages LLMs for Knowledge Base Question Answering (KBQA) (Yasunaga et al., 2021; Sun et al., 2024; Jin et al., 2024; Mavromatis and Karypis, 2024), and building relationships between documents in the database to improve ODQA performance (Li et al., 2024a; Dong et al., 2024; Edge et al., 2024).

Recently, an emerging problem concentrates on "hybrid" question answering (HQA), where a question requires both relational and textual information to be answered correctly, given a semi-structured knowledge base (SKB) (Wu et al., 2024b). SKB consists of a structured knowledge base, i.e., knowledge graph (KG), and unstructured text documents, where the text documents are associated with entities of KG. In Fig. 1 top, an example of hybrid questions is given, which involves both the textual aspect (paper topic) and the relational aspect (paper author), and SKBs are the cylinders.

Nevertheless, through our empirical analysis, we uncover two critical insights showing that existing methods that perform RAG or GRAG cannot effectively tackle HQA, which requires a synergy between the two retrieval methods. First, they focus solely on retrieving either textual or relational information. As shown in Fig. 1(a) and (b), this limitation reduces their applicability when the synergy between the two modalities is required. Second, in hybrid questions, the aspects required to retrieve different types of information may not be easily distinguishable. In Fig. 1(c), question routing (Li et al., 2024b) is performed to identify the aspects of the question. However, in an unsuccessful routing, confusion between the textual aspect "nanofluid heat transfer papers" and the relational aspect "by John Smith", leads to incorrect retrieval.

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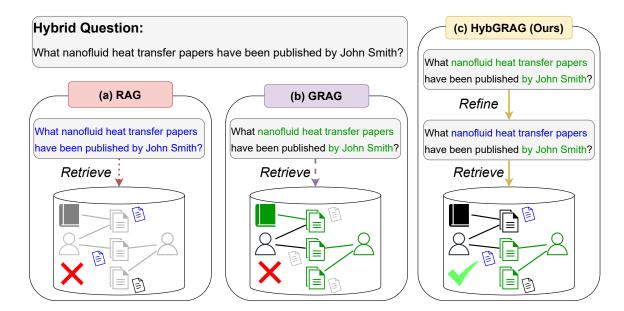


Figure 1: **HYBGRAG** solves hybrid questions in SKB, which are semi-structured, involving textual and relational aspects. (a) RAG overlooks the interconnections between documents and does not meet the requirements specified by the relational aspect. (b) GRAG relies solely on the relational aspect and misidentifies the textual aspect as part of the relational one. (c) HYBGRAG refines the question routing through self-reflection and successfully retrieves the target document in SKB, addressing both textual and relational aspects.

Table 1: <u>HYBGRAG matches all properties</u>, while baselines miss more than one property.

			qc.		
		RAG	n-Graj	•	RAG
		egular	nink-o	AVATAR	BGRA
	Property	Re	Th	ΑV	H
1. Agentic				~	~
	2.1. Questions in ODQA	~		~	~
2. Adaptive	2.2. Questions in KBQA		~		~
	2.3. Questions in HQA				~
3. Interpreta	ble	?	~	~	~

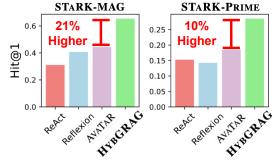


Figure 2: <u>HYBGRAG wins</u> in STARK, outperforming baselines by up to 21% in Hit@1.

To solve HQA in SKB, we propose HYBGRAG. HYBGRAG handles hybrid questions with a retriever bank, which leverages both textual and relational information simultaneously. To improve the accuracy of the retrieval, HYBGRAG performs self-reflection (Renze and Guven, 2024), which iteratively improves its question routing based on feedback from a carefully designed critic module. Similarly to chain-of-thought (CoT) (Wei et al., 2022), which is widely regarded as interpretable, HYB-GRAG's refinement path provides intuitive explanations for the performance improvement. Last but not least, the framework of HYBGRAG is designed to be flexible, and can easily be adapted to different problems. We summarize the contributions of HYBGRAG as follows:

- 1. *Agentic*: it automatically refines the question routing with self-reflection;
- 2. *Adaptive*: it solves textual, relational and hybrid questions with a unified framework;
- 3. *Interpretable*: it justifies the decision making with intuitive refinement path; and
- 4. *Effective*: it outperforms all baselines on realworld HQA benchmarks.

In Table 1, HYBGRAG is the only work that satisfies all the properties and solves HQA. In Fig. 2, evaluating in a HQA benchmark STARK, HYBGRAG outperforms the second-best baseline with relative improvements in Hit@1 47% in STARK-MAG, and 55% in STARK-PRIME, respectively.

2 Proposed Insights: Challenges in HQA

What are the new challenges in HQA over SKB that cannot be solved by the existing RAG and GRAG methods? In this section, we first define the problem, and then conduct experiments to uncover two critical insights in HQA, laying the foundation for designing our method for HQA.

2.1 Problem Definition

A semi-structured knowledge base (SKB) consists of a KG $G = (\mathcal{E}, \mathcal{R})$, where \mathcal{E} and \mathcal{R} are sets of entities and relations, respectively, and a set of text documents \mathcal{D} . Entity and relation types are denoted as \mathcal{T}_E and \mathcal{T}_R , respectively. Each hybrid question q in SKB involves semi-structured information, namely, textual and relational information. We define hybrid question answering (HQA) as follows:

- Given a SKB consisting of $G = (\mathcal{E}, \mathcal{R})$ and \mathcal{D} , and a hybrid question q.
- Retrieve a set of documents $\mathcal{X} \subseteq \mathcal{E}$, where each document satisfies the requirements specified by the relational and textual aspects of q.

2.2 C1: Hybrid-Sourcing Question

To investigate whether it is necessary to leverage both textual and relational information to answer hybrid questions, we conduct an experiment to show that text documents and KG contain useful but non-overlapping information. As a retriever that uses only textual information, vector similarity search (VSS) (Karpukhin et al., 2020) performs retrieval and ranking by comparing the question and documents in the embedding space ("ada-002"); as a retriever that uses only relational information, Personalized PageRank (PPR) (Andersen et al., 2006) performs random walks starting from the topic entities identified by an LLM (Claude 3 Sonnet) and ranks neighboring entities based on their connectivity in KG of SKB.

In Table 2, the text and the graph retrievers have competitive performance. Interestingly, if an optimal routing always picks the retriever that gives the correct result, the performance is significantly higher, indicating little overlap between the strengths of the text and graph retrievers. This highlights the importance of a solution to leverage both textual and relational information simultaneously by synergizing these two retrievers. In Fig. 1(c), we show a hybrid question that requires both textual and relational information to be answered. Based on this observation, we uncover the first challenge:

Table 2: Textual and relational information are both useful to answer hybrid question in STARK-MAG.

Method	Hit@1	Hit@5
Text Retriever: VSS Graph Retriever: PPR	0.2908 0.2533	0.4961 0.5523
Optimal Routing	0.4522	0.7463

Table 3: LLMs frequently extracts a subgraph from KG in SKB without target entities in STARK-MAG.

# of Iterations	Feedback Type	Hit Rate
1	N/A	0.6769
2	Simple	0.7914
2	Corrective	0.9231

Challenge 1 (Hybrid-Sourcing Question). *In HQA*, there are questions that require both textual and relational information to be answered.

2.3 C2: Refinement-Required Question

The success of KBQA often relies on the assumption that the target entities are within an extracted subgraph from KG (Lan et al., 2022). Similarly, answering a question in HQA requires extracting a subgraph from KG in SKB. As hybrid questions involve both textual and relational aspects, they can be challenging for an LLM to comprehend. To study this, we test if an LLM can extract a subgraph from KG that contains the target entities (hit). More specifically, an LLM (Claude 3 Sonnet) is prompted to identify the relational aspect in the question, i.e. topic entities and useful relations used to extract the subgraph. An oracle is used to instruct LLM to perform an extra iteration with feedback if the target entities are not included in the subgraph.

In Table 3, if the result is incorrect, simply prompting LLM to redo the extraction gives a much better hit ratio. Moreover, if the LLM receives feedback that points out the erroneous part of the extraction (e.g., extracted topic entity is wrong), it significantly improves the result. This is because in hybrid questions that contain both textual and relational aspects, LLM can falsely identify the textual aspect as the relational one. In Fig. 1 (c), there is an error in retrieving the correct reference from LLM, as it confuses the textual aspect as an entity of type "field of study" on the first attempt. Based on this observation, we uncover the second challenge:

Challenge 2 (Refinement-Required Question). In HQA, LLM struggles to distinguish between the textual and relational aspects of the question on the first attempt, necessitating further refinements.

3 Proposed Method: HYBGRAG

To solve HQA, we propose HYBGRAG, consisting of the *retriever bank* and the *critic module*, to address Challenge 1 and Challenge 2, respectively.

3.1 Retriever Bank (for C1)

To solve Challenge 1, we propose the retriever bank, composed of multiple retrieval modules and a router. Given a question q, the router determines the selection and usage of the retrieval module, a process known as question routing. The selected retrieval module then retrieves the top-K references \mathcal{X} , as elaborated in the next paragraph.

Retrieval Modules We design two retrieval modules, namely text and hybrid retrieval modules, to retrieve information from text documents and SKB, respectively. Each retrieval module includes a retriever and a ranker, which offers the flexibility to cover a wide range of questions.

The text retrieval module retrieves documents using similarity search for a given question q, such as dense retrieval, which is designed to directly find answers within text documents. We use VSS between question q and documents \mathcal{D} in the embedding space as both the retriever and the ranker. This is typically used when nothing can be extracted from the hybrid retrieval module.

The hybrid retrieval module takes the identified topic entities $\hat{\mathcal{E}}$ and useful relations $\hat{\mathcal{R}}$ as input. It uses a graph retriever to extract entities in the egograph of $\hat{\mathcal{E}}$, connected by $\hat{\mathcal{R}}$. For example, in Fig. 1, $\{\hat{\mathcal{E}}=\{\text{John Smith}\},\hat{\mathcal{R}}=\{\text{author writes paper}\}\}$ and the graph retriever extracts the entities/papers connected by the path "John Smith -> author writes paper -> $\{\text{papers}\}$ ". If more than one ego-graph is extracted, their intersection is used as the final result. Finally, to solve hybrid questions, we propose ranking the documents associated with the extracted entities using a VSS ranker between question q and documents \mathcal{D} . This ensures the synergy between the relational and textual information.

Router Given a question q, the LLM router performs question routing to determine the selection and usage of the retrieval module. More specifically, the router first identifies the relational aspect, i.e., topic entities $\hat{\mathcal{E}}$ and useful relations $\hat{\mathcal{R}}$ based on the types of entities \mathcal{T}_E and the types of relation \mathcal{T}_R using few shot examples (Brown, 2020). The router then makes the selection s_t , determining whether to use a text or a hybrid retrieval module. Identifying

 $\hat{\mathcal{E}}$ and $\hat{\mathcal{R}}$ before determining s_t improves the quality of s_t . For example, if there is no entity extracted $\hat{\mathcal{E}} = \emptyset$, a text retrieval module is a better option.

3.2 Critic Module (for C2)

Given a hybrid question q, the router is asked to perform question routing, including identifying topic entities $\hat{\mathcal{E}}$ and useful relations $\hat{\mathcal{R}}$. However, as mentioned in Challenge 2, they may be incorrectly identified in the first iteration.

To solve this, we propose the critic module, which provides feedback to help the router perform better question routing. Instead of using a single LLM to complete this complicated task, we divide the critic into two parts, an LLM validator C_{val} to validate the correctness of the retrieval \mathcal{X} , and an LLM commentor C_{com} to provide feedback f_t if the retrieval is incorrect. This divide-and-conquer step, similar to previous works (Gao et al., 2022; Asai et al., 2024), is crucial to our critic module, offering two key advantages: (1) By breaking a difficult task into two easier ones, we can now leverage pre-trained LLMs to solve them while maintaining good performance. This resolves the issue when the labels are not available for fine-tuning an LLM critic. (2) Since the tasks of C_{val} and C_{com} are independent, they can each have their own exclusive contexts, preventing the inclusion of irrelevant information and avoiding the "lost in the middle" phenomenon (Shi et al., 2023; Liu et al., 2024).

Validator The LLM validator C_{val} aims to validate if the top references retrieved \mathcal{X} meet the requirements specified by the question q, which is a binary classification task. To improve accuracy, we provide an additional validation context for the validator. We use the reasoning paths between topic entities and entities in the extracted ego-graph as the validation context, which are used to verify whether the output satisfies certain requirements in the question. The reasoning paths are verbalized as "{topic entity} \rightarrow {useful relation} \rightarrow ... \rightarrow {useful relation} \rightarrow {neighboring entity}". For example, if a hybrid question asks for a paper (i.e. a document) from a specific author, then the context including the reasoning paths "{author} \rightarrow {writes} \rightarrow {paper}" is essential for verification.

Commentor The LLM commentor C_{com} aims to provide feedback f to help the router refine question routing. To effectively guide the router, we construct *corrective* feedback that it can easily understand. In more detail, it points out the error(s) in

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Table 4: Corrective	reedback or	the critic modu	ie in Hyb	BGRAG for STARK.

Error Source	Error Type	Feedback
	Incorrect Entity/Relation	Entity/relation {name} is incorrect. Please remove or substitute this entity/relation.
	Missing Entity	There is only one entity but there may be more. Please extract one more entity and relation.
	No Entity	There is no entity extracted. Please extract at least one entity and one relation.
Identification	No Intersection	There is no intersection between the entities. Please remove or substitute one entity and relation.
	Incorrect Intersection	There is an intersection between the entities, but the answer is not within it. Please remove or substitute one entity and relation.
Selection	Incorrect Retrieval Module	The retrieved document is incorrect. The current retrieval module may not be helpful to narrow down the search space.

each action, such as incorrect identification of topic entities, as shown in Table 4. Unlike natural language feedback, which may cause uncertainty or inconsistency depending on the LLM used, our corrective feedback provides clear guidance on how to refine the question routing. Furthermore, it leverages in-context learning (ICL) to provide sophisticated feedback. We collect a small number of successful experiences (≈ 30) in the training set as examples, with each experience $\{s_t, \hat{\mathcal{E}}_t, \hat{\mathcal{R}}_t, f_{t+1}\}$ comprising a pair of router action and feedback, which is verified by ground truth. During inference, the commentor gives high-quality feedback based on multiple pre-collected examples.

3.3 Overall Algorithm

The algorithm of HYBGRAG is in Algo. 1. Given a question q, in iteration t, the router determines s_t , $\hat{\mathcal{E}}_t$ and $\hat{\mathcal{R}}_t$ to retrieve the references \mathcal{X}_t from both G and \mathcal{D} in SKB, or only \mathcal{D} , with the selected retrieval module. The validator C_{val} in the critic module then decides whether to accept \mathcal{X}_t as the final answer or reject it. If \mathcal{X}_t is rejected, the commentor C_{com} generates feedback f_{t+1} for the router to assist in refining its action in iteration t+1.

4 Experiments

We conduct experiments to answer the following research questions (RQ):

- RQ1. **Effectiveness:** How well does HYBGRAG perform in real-world GRAG benchmarks?
- RQ2. **Ablation Study:** Are all the design choices in HYBGRAG necessary?
- RQ3. **Interpretability:** How does HYBGRAG refine its question routing based on feedback?

GRAG Benchmarks We conduct experiments on two GRAG benchmarks: STARK¹ (Wu et al., 2024b), which serves as the primary evaluation

Algorithm 1: HYBGRAG

Input: Question q, a SKB with G and \mathcal{D} , Entity Types \mathcal{T}_E , Relation Types \mathcal{T}_R , and Maximum Iterations T

```
1 f_1 = "";
 2 for t = 1, ..., T do
          /* Retriever Bank
           s_t, \hat{\mathcal{E}}_t, \hat{\mathcal{R}}_t = Router(q, \mathcal{T}_E, \mathcal{T}_R, f_t);
 4
          if s_t is hybrid retrieval module then
 5
            \mathcal{X}_t = HybridRM(q, G, \mathcal{D}, \hat{\mathcal{E}}_t, \hat{\mathcal{R}}_t);
 6
 7
            \mathcal{X}_t = TextRM(q, \mathcal{D});
 8
           /* Validator
 9
                                                                     */
10
          if C_{val}(q, \mathcal{X}_t) = True then
            Return \mathcal{X}_t;
11
          else
12
13
                 /* Commentor
                                                                     */
                f_{t+1} = C_{com}(q, s_t, \hat{\mathcal{E}}_t, \hat{\mathcal{R}}_t);
15 Return \mathcal{X}_t;
```

benchmark and focuses on retrieval, and CRAG (Yang et al., 2024), a complementary benchmark to evaluate end-to-end RAG performance. Detailed benchmark descriptions are provided in Appx. A.

4.1 Retrieval Evaluation on STARK

We use the default evaluation metrics provided by STARK, which are Hit@1, Hit@5, Recall@20 and mean reciprocal rank (MRR), to evaluate the performance of the retrieval task. We compare HYBGRAG with various baselines, including recent GRAG methods (QAGNN (Yasunaga et al., 2021) and Think-on-Graph (Sun et al., 2024)); traditional RAG approaches; and self-reflective LLMs (ReAct (Yao et al., 2023), Reflexion (Shinn et al., 2023), and AVATAR (Wu et al., 2024a)). The details of the implementation are in Appx. C.

¹Due to legal issue, only STARK-MAG and STARK-PRIME are used in this article.

Table 5: Retrieval Evaluation on STARK: HYBGRAG wins	s. '*' denotes that only 10% of the testing questions
are evaluated due to the high latency and cost of the methods.	denotes our proposed method.

M-41- J		STAF	RK-MAG			STAR	K-PRIME	
Method	Hit@1	Hit@5	Recall@20	MRR	Hit@1	Hit@5	Recall@20	MRR
QAGNN	0.1288	0.3901	0.4697	0.2912	0.0885	0.2123	0.2963	0.1473
Think-on-Graph*	0.1316	0.1617	0.1130	0.1418	0.0607	0.1571	0.1307	0.1017
Dense Retriever	0.1051	0.3523	0.4211	0.2134	0.0446	0.2185	0.3013	0.1238
VSS (Text Retrieval Module)	0.2908	0.4961	0.4836	0.3862	0.1263	0.3149	0.3600	0.2141
Multi-VSS	0.2592	0.5043	0.5080	0.3694	0.1510	0.3356	0.3805	0.2349
VSS w/ LLM Reranker*	0.3654	0.5317	0.4836	0.4415	0.1779	0.3690	0.3557	0.2627
ReAct	0.3107	0.4949	0.4703	0.3925	0.1528	0.3195	0.3363	0.2276
Reflexion	0.4071	0.5444	0.4955	0.4706	0.1428	0.3499	0.3852	0.2482
AvaTaR	0.4436	0.5966	0.5063	<u>0.5115</u>	0.1844	0.3673	0.3931	0.2673
Hybrid Retrieval Module (Ours)	0.5028	0.5820	0.5031	0.5373	0.2492	0.3274	0.3366	0.2842
HyBGRAG (Ours)	0.6540	0.7531	0.6570	0.6980	0.2856	0.4138	0.4358	0.3449
Relative Improvement	47.4%	26.2%	29.3%	36.5%	54.9%	12.7%	10.9%	29.0%

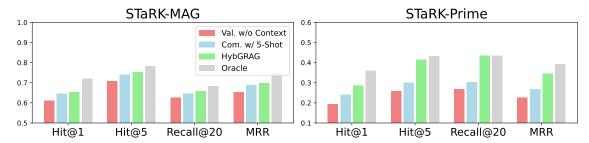


Figure 3: **Design choices in HYBGRAG are necessary** in STARK. We compare HYBGRAG with two variants: a validator without validation context, and a commentor with only 5-shot. Oracle uses ground truth during inference.

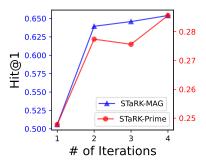


Figure 4: **HYBGRAG** improves its question routing thanks to the critic module.

4.1.1 Effectiveness (RQ1)

In Table 5, HYBGRAG outperforms all baselines significantly in both datasets in STARK. Most baselines are designed to handle ODQA and KBQA, and the results have shown that they cannot handle HQA effectively (Challenge 1). Our hybrid retrieval module is the second-best performing method, highlighting the importance of designing a synergized retrieval module that uses both textual and relational information simultaneously. In addition, HYBGRAG performs significantly better

Table 6: **HYBGRAG maintains strong performance** with a less powerful LLM model in STARK-MAG.

Base Model	Hit@1	Hit@5	Recall@20	MRR	Speedup
Claude 3 Haiku Claude 3 Sonnet	0.6019	0.7084	0.6067		1.96×
Claude 3 Sonnet	0.6540	0.7531	0.6570	0.6980	1.00×

than the hybrid retrieval module, indicating that the extracted entity and relation are frequently incorrect in the first iteration (Challenge 2). By tackling Challenge 1 and 2 with our retriever bank and critic module respectively, HYBGRAG has a significant improvement in performance.

4.1.2 Ablation Study (RQ2)

Critic Module We compare HYBGRAG variants with a validator without validation context, a commentor with only five shots, and those with oracles. The oracle has access to the ground truth, which gives the optimal judgement on the correctness of the output and the error type of question routing, if there is any. In Fig. 3, we show that HYBGRAG performs the best with all our design choices, approaching the performance of an oracle.

(a) Error Type: Incorrect Entity/Relation Q: Any 2012 publications from Netaji Subhash Engineering College on optical TALU implementations in electronic circuits? Selection: Hybrid retrieval module Entity: Netaji Subhash Engineering College (institution), optical TALU implementations in electronic circuits (field of study) Relation: author affiliated with institution, author writes paper, paper has topic field of study Feedback 1: The retrieved document is incorrect. Entity "optical TALU implementations in electronic circuits" and relation "paper has topic field of study" are incorrect. Please remove or substitute one entity and relation. Action 2: Selection: Hybrid retrieval module Entity: Netaji Subhash Engineering College (institution) Relational: author affiliated with institution, author writes paper

Feedback 2: Accept.

(b) Error Type: Missing Entity Q: Are there any 2016 publications by co-authors of "A Low Abundance of 135Cs in the Early Solar System from Barium Isotopic Signatures" which discuss the comparison of Earth's chemical composition with that of chondrites? Action 1: Selection: Hybrid retrieval module Entity: A Low Abundance of 135Cs in the Early Solar System from Barium Isotopic Signatures (paper) Relation: author writes paper Feedback 1: The retrieved document is incorrect. There is only one entity but there may be more. Please extract one more entity Action 2:

Selection: Hybrid retrieval module

Entity: A Low Abundance of 135Cs in the Early Solar System from Barium

Isotopic Signatures (paper), chondrites (field of study) Relational: author writes paper, paper has topic field of study

Feedback 2: Accept.

Figure 5: HYBGRAG is interpretable. In examples from STARK-MAG, HYBGRAG successfully refines its entity and relation extraction based on corrective feedback from the critic module.

Table 7: End-to-End RAG Evaluation on CRAG: HYBGRAG wins. All baselines (except CoT LLM) share our retriever bank, but use different critics to provide feedback. denotes our proposed method.

Method	Llama 3.1 70B				Claude 3 Sonnet			
Method	Accuracy ↑	Halluc.↓	Missing	$Score_a \uparrow$	Accuracy ↑	Halluc.↓	Missing	$Score_a \uparrow$
CoT LLM	0.4607	0.5026	0.0367	-0.0419	0.3910	0.4052	0.2038	-0.0142
Text-Only RAG	0.4105	0.3685	0.2210	0.0420	0.5034	0.3955	0.1011	0.1079
Graph-Only RAG	0.4861	0.4442	0.0697	0.0419	0.5303	0.2974	0.1723	0.2329
Text & Graph RAG	0.4120	0.3790	0.2090	0.0330	0.5820	0.3416	0.0764	0.2404
ReAct	0.1745	0.2360	0.5895	-0.0615	0.4352	0.4075	0.1573	0.0277
Corrective RAG	0.4509	0.4652	0.0839	-0.0143	0.4674	0.3333	0.1993	0.1341
HYBGRAG (Ours)	0.5206	0.3588	0.1206	0.1618	0.6322	0.2959	0.0719	0.3363

Self-Reflection In Figure 4, we demonstrate that with more self-reflection iterations, the performance of HYBGRAG improves further. Performance improves significantly when increasing the number of iterations from 1 to 2, where no selfreflection is performed in iteration 1. It is also shown that a few iterations are sufficient, as the improvement diminishes over iterations.

Model Size Although we do not have access to Claude 3 Opus, we conduct experiments with Claude 3 Haiku, a more cost-efficient but less powerful alternative to Claude 3 Sonnet². In Table 6, HYBGRAG maintains strong performance even with Claude 3 Haiku. The results also follow the scaling law of LLMs (Kaplan et al., 2020).

4.1.3 Interpretability (RQ3)

Fig. 5 illustrates examples of the interaction between the router in the retriever bank and the critic module in STARK-MAG. In the first iteration of Fig. 5(a), the router misidentifies a "optical TALU

implementations in electronic circuits" as a topic entity representing the field of study (relational aspect). Since the ego-graph extracted based on this entity has no intersection with the ego-graph extracted based on "Netaji Subhash Engineering College", the critic module recognizes that the former entity has a higher chance of being a textual aspect. Thus, it gives the feedback to the router, and the router addresses it accordingly. This refinement path of HYBGRAG is similar to CoT, making it interpretable and easy for the user to understand. Examples in STARK-Prime are given in Appx. B.1.

4.2 End-to-End RAG Evaluation on CRAG

To adapt to CRAG, modifications are made in HY-BGRAG, and the details are in Appx. C. We use default evaluation metrics, where an LLM evaluator is used to determine if the predicted answers are accurate, incorrect (hallucination), or missing, and apply a three-way scoring Score_a with 1, -1, and 0for these respective categories. We compare HYB-GRAG with CoT LLM, text-only RAG, graph-only RAG, and RAG that concatenates text and graph

²https://www.anthropic.com/news/claude-3-family

Table 8: Number of API calls and tokens for STARK.

HYBGRAG Component	API Call # per Iteration	Token # for for Prompts	Token # for Examples in MAG	Token # for Examples in Prime	
Router	2	159	2709	3018	
Validator	1	39	1383	2107	
Commentor	1	52	1215	1583	

Table 9: Number of API calls and tokens for CRAG.

HYBGRAG Component	API Call # / Iteration	Token # for Prompts	Token # for Examples
Router	4	266	5752
Validator	1	56	0
Commentor	1	78	598
Generator	2	168	553

references. To demonstrate the advantages of our critic module, we include two self-reflective LLMs (ReAct, Corrective RAG) that share the same retriever bank but use different critics.

In Table 7, HYBGRAG outperforms all baselines in CRAG. RAGs with a single retrieval module cannot handle both types of questions. RAG with a concatenated reference also distracts by irrelevant content in the long reference. Although the same retriever bank is provided, self-reflective baselines still find it difficult to refine their action. Since ReAct relies on the LLM's ability to think and provide natural language feedback, it often lacks clear guidance for improving its actions. Without a finetuned retrieval evaluator, Corrective RAG cannot effectively identify the usefulness of a reference. This demonstrates the advantages of our critic module with corrective feedback. Furthermore, HYB-GRAG is robust to the choice of LLM base models. The ablation study is provided in Appx. B.2.

4.3 Model Cost Analysis

We report the number of API calls and token consumption (excluding references) for each step in an iteration of HYBGRAG in Table 8 and 9 for STARK and CRAG, respectively. While most of the token consumption arises from the examples used for ICL, the prompts themselves require very few tokens. Moreover, since HYBGRAG uses the chat LLM as the router, the examples for ICL only need to be given once. Compared to the state-of-the-art baseline AVATAR in STARK, which requires at least 500 API calls during training, our hybrid retrieval module achieves a relative improvement 24% in Hit@1 with only 2 API calls, while HYBGRAG achieves 51% with at most 14 API calls, both without training.

5 Related Works

Graph RAG (GRAG) Various settings have been explored for GRAG (Peng et al., 2024), and can be roughly divided into three directions. The first focuses on KBQA, taking advantage of the LLM capability (Yasunaga et al., 2021; Sun et al., 2024; Jin et al., 2024; Mavromatis and Karypis, 2024). The second focuses on ODQA, building relationships between documents to improve retrieval (Li et al., 2024a; Dong et al., 2024; Edge et al., 2024). The last assumes that a subgraph is given when answering a question (He et al., 2024; Hu et al., 2024). In contrast, this paper focuses on solving HQA in SKB, and previous GRAG methods are not easily generalized to HQA.

Self-Reflective LLMs For complex tasks, LLMs are unlikely to generate the correct output on their first attempt. Self-reflection addresses this issue by optimizing the output through a feedback-driven reflection process. A critic is commonly used to give feedback, implemented with various approaches: pre-trained LLMs (Yao et al., 2023; Shinn et al., 2023; Madaan et al., 2023), external tools (Gou et al., 2024), or fine-tuned LLMs (Paul et al., 2024; Asai et al., 2024; Yan et al., 2024). AVATAR (Wu et al., 2024a) is the most recent work on optimizing the prompt iteratively through contrastive reasoning. In our problem, while external tools and labels for fine-tuning are not available, using pre-trained LLMs as critics requires careful designs. For example, ReAct (Yao et al., 2023) relies on the LLM's ability to think and provide natural language feedback, which is often too implicit to support effective self-reflection in HQA.

6 Conclusions

To solve hybrid question answering (HQA), we propose HYBGRAG, which is based on insights from our empirical analysis. In summary, HYBGRAG has following advantages:

- 1. *Agentic*: it refines question routing with self-reflection by our critic module;
- 2. *Adaptive*: it solves textual, relational and hybrid questions by our retriever bank;
- 3. *Interpretable*: it justifies the decision making with intuitive refinement path; and
- 4. *Effective*: it significantly outperforms all the baselines on HQA benchmarks.

Applied on STARK, HYBGRAG achieves an average relative improvement 51% in Hit@1.

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A Appendix: Benchmarks

A.1 STARK

We use two datasets from the STARK benchmark, STARK-MAG and STARK-PRIME. Each dataset contains a knowledge graph (KG) and unstructured documents associated with some types of entities. The task is to retrieve a set of documents from the database that satisfy the requirements specified in the question. Noting that the majority of questions are hybrid questions, and there are very few textual questions. We use the testing set from STARK for evaluation, which contains 2665 and 2801 questions for STARK-MAG and STARK-PRIME, respectively. The KG of STARK-MAG is an academic KG, and the one of STARK-PRIME is a precision medicine KG. Their types of entity and relations are provided in the benchmark.

A.2 CRAG

In the CRAG benchmark, there are KGs from 5 different domains that can be utilized to retrieve useful reference. For each question, a database that includes 50 retrieved web pages and all 5 KGs is given, but the answer is not guaranteed to be on the web pages, KGs, or both. The task is to generate the answer to the question, with or without the help of the retrieved reference. There are textual and relational questions, covering various question types, such as simple, simple with condition, comparison, and multi-hop. We use the testing set from CRAG for evaluation. There are 1335 textual and relation questions, covering various question types, such as simple, comparison, and multi-hop.

B Appendix: Experiments

B.1 Interpretability (RQ3) in STARK-Prime

Fig. 6 shows two examples that HYBGRAG refines its question routing in STARK-Prime. In the example of Fig. 6(a), HYBGRAG selects to use the text retrieval module in the first iteration, and the retrieved document is rejected by the validator. HYBGRAG then takes the feedback from the commentor and turns to using the hybrid retrieval module, and refines the extraction of topic entities and useful relations in the next two iterations.

B.2 Ablation Study on Critic Module

We compare HYBGRAG variants with validators without validator context, commentors with few or zero shots, and those with oracles. The oracle has

access to the ground truth, which gives the optimal judgement on the correctness of the output and the error type of the action, if there is any. In Table 10 and 11, we show that HYBGRAG performs the best with all our design choices, approaching the performance of an oracle.

C Appendix: Reproducibility

C.1 Experimental Details

All the experiments are conducted on an AWS EC2 P4 instance with NVIDIA A100 GPUs. Most LLMs are implemented with Amazon Bedrock³, and Llama 3.1 is implemented with Ollama⁴.

C.1.1 HyBGRAG Implementation

STARK The examples in the prompts are collected from the training set provided by STARK. We use the default entity and relation types provided by STARK. The radius of the extracted egograph is no more than two. Four self-reflection iterations have been done. When extracting the entity name from the question, multiple entities in the knowledge base may have exactly the same name. In these cases, we select the entity that has the answer in its one-hop neighborhood for disambiguation, since it is not the focus of our paper. Moreover, these cases rarely happen, where only 3.83% and 0.07% of questions have this issue in STARK-MAG and STARK-PRIME, respectively.

CRAG In the text retrieval module, the web search based on the question is used as the retriever, which is done by CRAG ahead of time. The VSS ranker ranks the web pages based on their similarity to the question in the embedding space. In this module, we provide an additional choice for the router. If the output generated based on the current batch of retrieved web pages is rejected by the validator, the router can choose to move on to the next batch in the ranking list. In CRAG, since there is no hybrid question, the hybrid retrieval module is replaced by the graph retrieval module to be prepared for relational questions. In the graph retrieval module, the retriever extracts the ego-graph connected by the useful relations for each topic entity. As there is no document associated with entity, the retriever retrieves the reasoning paths from topic entities to entities in the extracted egographs. Reasoning paths are verbalized as "{topic

https://aws.amazon.com/bedrock/

⁴https://github.com/ollama/ollama

(a) Error Type: Incorrect Module & Missing Entity (b) Error Type: Incorrect Entity/Relation Q: Which autosomal dominant diseases are linked to the development Q: Please find me genes or proteins linked to pediatric liver cancer, of supernumerary breast tissue? interacting with PAXIP1, highly expressed in lung adenocarcinoma, with a nuclear signal and similarity to GAGE/PAGE proteins. Action 1: Selection: Text retrieval module Action 1: Selection: Hybrid retrieval module Feedback 1: The retrieved document is incorrect. Entity: PAXIP1 (gene/protein), pediatric liver cancer (disease), lung The current retrieval module may not be helpful to narrow down the adenocarcinoma (disease) search space. Relational: ppi, associated with, expression present Feedback 1: The retrieved document is incorrect. Action 2: Entities "pediatric liver cancer" and "lung adenocarcinoma" are incorrect. Selection: Hybrid retrieval module Please remove or substitute these entities. Entity: autosomal dominant diseases (disease) Relations "associated with" and "expression present" are incorrect. Relational: phenotype present Please remove or substitute these relations Feedback 2: The retrieved document is incorrect. There is only one entity but there may be more. Please extract one more entity and relation. Selection: Hybrid retrieval module Entity: PAXIP1 (gene/protein) Relational: ppi Selection: Hybrid retrieval module Entity: autosomal dominant diseases (disease), supernumerary breast Feedback 2: Accept. tissue (effect/phenotype) Relational: phenotype present, associated with Feedback 3: Accept.

Figure 6: **HYBGRAG** is interpretable. In examples from STARK-PRIME, HYBGRAG successfully refines its entity and relation extraction based on corrective feedback from the critic module.

Table 10: <u>The design choices in HYBGRAG are necessary in STARK.</u> denotes the settings of HYBGRAG, and denotes the baseline that use ground truth during inference.

Validator	Commentor	STARK-MAG				STARK-PRIME				
validator Co	Commentor	Hit@1	Hit@5	Recall@20	MRR	Hit@1	Hit@5	Recall@20	MRR	
w/o Context	ICL	0.6105	0.7073	0.6245	0.6541	0.1946	0.2592	0.2685	0.2251	
w/ Context	5-Shot	0.6465	0.7407	0.6458	0.6884	0.2406	0.3006	0.3038	0.2676	
w/ Context	ICL	0.6540	0.7531	0.6570	0.6980	0.2856	0.4138	0.4358	0.3449	
Oracle	Oracle	0.7193	0.7824	0.6840	0.7479	0.3606	0.4320	0.4358	0.3932	

entity} \rightarrow {useful relation} \rightarrow ... \rightarrow {useful relation} \rightarrow {neighboring entity}", and ranked by VSS.

The retrieved reference is used as the validation context to check if it is reliable to answer the question. The validator takes the output of the generator and the validation context as the input. As the prompts for the generator and the validator are specialized for different tasks, this allows the validator to offer meaningful validation. Although the ground truth of the retrieval is not available in CRAG, we construct corrective feedback based on the router's action and the evaluation, as shown in Table 12. If the graph retrieval module is used and the evaluation is incorrect, then either the retrieval input (extracted entity and relation or the domain) is incorrect, or selecting graph retrieval module is incorrect; if the text retrieval module is used and the evaluation is incorrect, then the information in the current batch of documents is considered as not useful to answer the question.

The examples in the prompts are collected from

the validation set provided by CRAG. Since the entity and relation types are not given by CRAG, and the KGs are only accessible with the provided API, we collect them from the questions in the validation set, as shown in Table 13. The radius of the extracted ego-graph is no more than two. Four self-reflection iterations have been done. A batch contains five web pages.

C.1.2 Baseline Implementation

STARK We use "ada-002" as the embedding model for dense retrieval and ranking, as used in the paper. HYBGRAG uses Claude 3 Sonnet as the base model, while ReAct, Reflexion, AVATAR, and VSS with LLM reranker use Claude 3 Opus, which is designed to be more powerful than Claude 3 Sonnet⁵. For QAGNN and Dense Retriever, because of the need of training, RoBERTa is used as the base model. In experiments where the base LLM is not specified, we default to using Claude 3

⁵https://www.anthropic.com/news/claude-3-family

Table 11: The design choices in HyBGRAG are necessary in CRAG. denotes the settings of HyBGRAG, and _ denotes the baseline that use ground truth during inference.

Validator	Commentor	Accuracy ↑	Halluc.↓	Missing	Score _a ↑
w/o Context	ICL	0.5581	0.3461	0.0958	0.2120
w/ Context	0-Shot	0.6277	0.3004	0.0719	0.3273
w/ Context	ICL	0.6322	0.2959	0.0719	0.3363
Oracle	Oracle	0.7813	0.1640	0.0547	0.6173

Table 12: Design of critic module in HYBGRAG for CRAG.

Error Source	Error Type	Feedback		
Input	Incorrect Question Type	The predicted question type is wrong. Please answer again. Which type is this question?		
	Incorrect Question Dynamism	The predicted dynamism of the question is wrong. Please answer again. Which dynamism is this question?		
	Incorrect Question Domain	The predicted domain of the question is wrong. Please answer as Which domain is this question from?		
	Incorrect Entity and Relation	The topic entities and useful information extracted from the question are incorrect. Please extract them again.		
Selection	Incorrect Retrieval Module	The reference does not contain useful information for solving the question. Should we use knowledge graph as reference source based on newly extracted entity and relation, or use the next batch of text documents as reference source?		

Sonnet. We implement Think-on-Graph with their provided code⁶, using Claude 3 Sonnet as the base model. As running the full experiment takes more than a week, we evaluated it with only 10% of the testing data, as is done for the LLM reranker in the STARK paper.

CRAG We use Claude 3 Sonnet as the LLM evaluator, and CoT prompting (Wei et al., 2022) for all generator LLMs. We use "BAAI/bge-m3" (Chen et al., 2024) as the embedding model for dense retrieval and ranking. ReAct and Corrective RAG share the same backbone with HYBGRAG, while having different critics. ReAct has three actions, "search web", "search KG", and "extract entity relation domain", and is given some examples. The process iterates among action, observation, and thought for four iterations as HYBGRAG. While Corrective RAG requires a fine-tuned retrieval evaluator, we implement a version with only a pre-trained LLM. It starts with the text retrieval module and validates if the retrieved reference is correct, ambiguous, or incorrect. If incorrect, it uses the graph retrieval module instead. An final answer is generated based on the reference with CoT prompting.

C.2 Prompts

STARK The prompt of the router for the first decision making is:

You are a helpful, pattern-following assistant. Given the following question, extract the information from the question as requested. Rules: 1. The Relational information must come from the given relational types. 2. Each entity must exactly have one category in the parentheses.

<<<{10 examples for entity and relation extraction}>>>

Given the following question, based on the entity type and the relation type, extract the topic entities and useful relations from the question. **Entity Type:** <<<{entity types}>>>

Relation Type: <<<{relation types}>>>

Question: <<<{question}>>>

Documents are required to answer the given question, and the goal is to search the useful documents. Each entity in the knowledge graph is associated with a document. Based on the extracted entities and relations, is knowledge graph or text documents helpful to narrow down the search space? You must answer with either of them with no more than two words.

The prompt of the router for reflection is:

⁶https://github.com/GasolSun36/ToG

Table 13: Type of entity and relation in the CRAG benchmark.

Domain	Type	Content		
	Entity	company_name, ticker_symbol, market_capitalization, earnings_per_share, price_to_earnings_ratio, datetime		
Finance	Relation	get_company_ticker, get_ticker_dividends, get_ticker_market_capitalization, get_ticker_earnings_per_share, get_ticker_price_to_earnings_ratio, get_ticker_history_last_year_per_day, get_ticker_history_last_week_per_minute, get_ticker_open_price, get_ticker_close_price, get_ticker_high_price, get_ticker_low_price, get_ticker_volume, get_ticker_financial_information		
	Entity	nba_team_name, nba_player, soccer_team_name, datetime_day, datetime_month, datetime_year		
Sports	Relation	get_nba_game_on_date, get_soccer_previous_games_on_date, get_soccer_future_games_on_date, get_nba_team_win_by_year		
	Entity	artist, lifespan, song, release_date, release_country, birth_place, birth_date, grammy_award_count, grammy_year		
Music Relation		grammy_get_best_artist_by_year, grammy_get_award_count_by_artist, grammy_get_award_count_by_song, grammy_get_best_song_by_year, grammy_get_award_date_by_artist, grammy_get_best_album_by_year, get_artist_birth_place, get_artist_birth_date, get_members, get_lifespan, get_song_author, get_song_release_country, get_song_release_date, get_artist_all_works		
	Entity	actor, movie, release_date, original_title, original_language, revenue, award_category		
Movie	Relation	act_movie, has_birthday, has_character, has_release_date, has_original_title, has_original_language, has_revenue, has_orew, has_job, has_award_winner, has_award_category		
Encyclopedia	Entity	encyclopedia_entity		
Encyclopedia	Relation	get_entity_information		

The retrieved document is incorrect.

 $\textbf{Feedback: } <<<\{\textbf{feedback on extracted entity}$

and relation}>>>

Question: <<<{question}>>>

The retrieved document is incorrect. Answer again based on newly extracted topic entities and useful relations. Is knowledge graph or text documents helpful to narrow down the search space? You must answer with either of them with no more than two words.

The prompt of the validator is:

```
You are a helpful, pattern-following assistant. <<<{examples for retrieval validation, 2 for each type of entity}>>>
```

Question: <<<{question}>>>

Document: <<<{content of document and reasoning paths}>>>

Task: Is the document aligned with the requirements of the question? Reply with only yes or no.

The prompt of the commentor is:

You are a helpful, pattern-following assistant. $<<<\{30$ examples of action and feedback pair}>>>

Question: <<<{question}>>>

Topic Entities: <<<{extracted entities}>>> Useful Relations: <<<{extracted relations}>>> Please point out the wrong entity or relation extracted from the question, if there is any.

CRAG The prompt of the router for the first decision making is:

You are a helpful, pattern-following assistant. Given the following question, extract the information from the question as requested. Rules: 1. Each entity must exactly have one category in the parentheses. 2. Strictly follow the examples. <<<{examples of entity and relation extraction, 5 for each domain}>>>

Question Type: simple, simple_w_condition, set, comparison, aggregation, multi_hop, post_processing, false_premise.

Question: <<<{question}>>>

Task: Which type is this question? Answer must be one of them.

Dynamism: real-time, fast-changing, slow-changing, static.

Question: <<<{question}>>>

Task: Which category of dynamism is this question? Answer with one word and the answer must be one of them.

Domain: music, movie, finance, sports, encyclopedia.

Question: <<<{question}>>>

Task: Which domain is this question from? Answer with one word and the answer must be one of them.

Given the following question, based on the entity type and the relation type, extract the topic entities and useful relations from the question.

Entity Type: <<<{entity types}>>>
Relation Type: <<<{relation types}>>>

Question: <<<{question}>>>

Reference Source: knowledge graph, text documents.

Question: <<<{question}>>>

Task: Based on the extracted entity, which reference source is useful to answer the question? You must pick one of them and answer with no more than two words.

The prompt of the router for reflection is:

```
### Question Type: simple, simple_w_condition,
set, comparison, aggregation, multi_hop,
post_processing, false_premise.
### Question: <<<{question}>>>
### Task: The predicted question type is wrong.
Please answer again. Which type is this question?
Answer with one word and the answer must be
one of them.
### Dynamism:
                    real-time, fast-changing,
slow-changing, static.
### Question: <<<{question}>>>
### Task: The predicted dynamism of the
question is wrong. Please answer again. Which
dynamism is this question? Answer with one
word and the answer must be one of them.
### Domain: music, movie, finance, sports,
encyclopedia.
### Question: <<<{question}>>>
### Task: The predicted domain of the question
is wrong. Please answer again. Which domain is
this question from? Answer with one word and
the answer must be one of them.
The topic entities and useful information
extracted from the question are incorrect. Please
extract them again. Given the following question,
based on the entity type and the relation type,
extract the topic entities and useful relations from
the question.
Entity Type: <<<{entity types}>>>
Relation Type: <<<{relation types}>>>
Question: <<<{question}>>>
### Reference Source:
                          knowledge graph,
text documents.
### Question: <<<{question}>>>
### Task: The answer is incorrect. The reference
does not contain useful information for solving
the question. Please answer again, should we use
knowledge graph as reference source based on
newly extracted entity and relation, or use the
next batch of text documents as reference source?
You must pick one of them and answer with no
more than two words.
```

The prompt of the validator is:

```
### Reference: <<<{reference}>>>
### Prediction: <<<{output of generator}>>>
### Question: <<<{question}>>>
### Query Time: <<{question time}>>>
### Task: The prediction is generated based on
the reference. Does the prediction answer the ques-
tion? Answer with one word, yes or no.
```

The prompt of the commentor is:

```
You are a helpful, pattern-following assistant.

<<<{5 examples of action and feedback
pair}>>>

### Reference Source: <<{{source}>>>
### Question: <<{{question}>>>
### Query Time: <<{{question time}>>>
### Query Type: <<{{question type}>>>
### Query Dynamism: <<<{dynamism}>>>
### Query Domain: <<<{domain}>>>
### Task: Please point out the wrong information
about the question (Reference Source, Query
Type, Query Dynamism, Query Domain), if there
is any. The answer must be one of them.
```

The prompt of the generator is:

```
You are a helpful, pattern-following assistant.
<<<{1 chain-of-though prompt example}>>>
### Reference: <<<{reference}>>>
### Reference Source: <<<{source}>>>
### Question: <<<{question}>>>
### Query Time: <<<{question time}>>>
### Query Type: <<<{question type}>>>
### Query Dynamism: <<<{dynamism}>>>
### Query Domain: <<<{domain}>>>
### Task: You are given a Question, References
and the time when it was asked in the Pacific
Time Zone (PT), referred to as Query Time.
The query time is formatted as mm/dd/yyyy,
hh:mm:ss PT. The reference may help answer the
question. If the question contains a false premise
or assumption, answer "invalid question". First,
list systematically and in detail all the problems in
this problem that need to be solved before we can
arrive at the correct answer. Then, solve each sub
problem using the answers of previous problems
and reach a final solution.
What is the final answer?
```

The prompt of the evaluator is:

```
### Question: <<<{question}>>>
### True Answer: <<<{ground truth
answer}>>>
### Predicted Answer: <<<{output of
generator}>>>
### Task: Based on the question and the
true answer, is the predicted answer accurate,
incorrect, or missing? The answer must be one of
them and is in one word.
```