

Formatif task (D): Show that $A \cup (A \cap B) = A$.

$$A \cup (A \cap B)$$

Restart

$$= (A \cap \mathcal{U}) \cup (A \cap B)$$

Identity of \cap

$$= A \cap (\mathcal{U} \cup B)$$

Distributivity of \cap over \cup

$$= A \cap ((B \cup B^c) \cup B)$$

Complement with \cup

$$= A \cap ((B^c \cup B) \cup B)$$

Commutativity of \cup

$$= A \cap (B^c \cup (B \cup B))$$

Associativity of \cup

$$= A \cap (B^c \cup B)$$

Idempotence of \cup

$$= A \cap (B \cup B^c)$$

Commutativity of \cup

$$= A \cap \mathcal{U}$$

Complement with \cup

$$= A$$

Identity of \cap

Edit